## Package 'smog'

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Type Package

Title Structural Modeling by using Overlapped Group Penalty

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**Description** Fits a linear non-penalized phenotype (demographic) variables and penalized groups of prognostic effect and predictive effect, by satisfying such hierarchy structures that if a predictive effect exists, its prognostic effect must also exist. This package can deal with continuous, binomial or multinomial, and survival response variables, underlying the assumption of Gaussian, binomial (multinomial), and Cox proportional hazard models, respectively. It is implemented by combining the iterative shrinkage-thresholding algorithm and the alternating direction method of multipliers algorithms. The main method is built in C++, and the complementary methods are written in R.

**License** GPL ( $\geq 2$ )

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## **R** topics documented:

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cv.smog

#### Cross-valiation for smog

## Description

cv.smog conducts a greedy-search for optimal lambda's and yields a sparse model given a provided model selection criterion. When type is "nloglike", the method allows the nfolds to be processed in parallel for speeding up the cross-validation.

#### Usage

```
cv.smog(x, y, g, v, label, type, family = "gaussian", lambda.max = NULL,
nlambda.max = 20, delta = 0.9, nfolds = 5, parallel = FALSE,
ncores = NULL, ...)
```

## Arguments

| x      | a model matrix, or a data frame of dimensions n by p, in which the columns represents the predictor variables.  |
|--------|---|
| У      | response variable, corresponds to the family description. When family is "gaus-<br>sian" or "binomial", y ought to be a numeric vector of observations of length<br>n; when family is "coxph", y represents the survival objects, containing the sur-<br>vival time and the censoring status. See Surv. |
| g      | a vector of group labels for the predictor variables.   |
| v      | a vector of binary values, represents whether or not the predictor variables are penalized. Note that 1 indicates penalization and 0 for not penalization.  |
| label  | a character vector, represents the type of predictors in terms of treatment, prog-<br>nostic, and predictive effects by using "t", "prog", and "pred", respectively.  |
| type   | model selction criterion, should choose from "nloglike", "cAIC", "AIC", "BIC", and "GCV", respectively.   |
| family | a description of the distribution family for the response variable variable. For continuous response variable, family is "gaussian"; for multinomial or binary response variable, family is "binomial"; for survival response variable, family is "coxph", respectively.                                |

#### cv.smog

| lambda.max  | the maximum value for lambda's. If NULL, the default lambda . max is $1/\lambda_{min}(x'x)$ .   |
|-------------|---|
| nlambda.max | the maximum number of lambdas' shrunk down from the maximum lambda lambda.max. Default is 20.   |
| delta       | the damping rate for lambda's such that $\lambda_k = \delta^k \lambda_0$ . Default is 0.9.  |
| nfolds      | number of folds. One fold of the observations in the data are used as the testing, and the remaining are fitted for model training. Default is 5. |
| parallel    | Whether or not process the nfolds cross-validations in parallel. If TRUE, use foreach to do each cross-validation in parallel. Default is FALSE.  |
| ncores      | number of cpu's for parallel computing. See makeCluster and registerDoParallel. Default is NULL.  |
|             | other arguments that can be supplied to smog.   |

#### Details

When the type is "nloglike", it requires doing nfolds cross-validations. For each cross-validation, evenly split the whole data into nfolds, and one fold of the observations are used as the testing data, and the remaining are used for model training. After calculating the AIC for each fold of testing data, return the average of the AICs. Note that we keep lambda2=0 during the greedy search for lambda's.

#### Value

includes the profile containing a path of lambda's and the corresponding model selectio criterion value, the optimal lambda's, and the optimal model, respectively. The type comes from a list of model selection criteria values, includes the average of the negative log-likelihood values and the correction AIC for each fold of the data.

| cvfit   | the fitted model based on the optimal lambda's.  |
|---------|--|
| lhat    | the optimal lambda's which has the minimum model selection criterion.  |
| profile | a data frame contains the path of lambda's and the corresponding model selection criterion, which is determined by the type. |

## Author(s)

Chong Ma, <chongma8903@gmail.com>.

## References

Ma C, Deng W, Ma S, Liu R and Galinsky K (2019). "Structural modeling using overlapped group penalties for discovering predictive biomarkers for subgroup analysis." *arXiv preprint arXiv:1904.11648*.

#### See Also

smog.default, smog.formula, predict.smog, plot.smog.

#### Examples

```
# generate design matrix x
set.seed(2018)
n=50;p=100
s=10
x=matrix(0,n,1+2*p)
x[,1]=sample(c(0,1),n,replace = TRUE)
x[,seq(2,1+2*p,2)]=matrix(rnorm(n*p),n,p)
x[,seq(3,1+2*p,2)]=x[,seq(2,1+2*p,2)]*x[,1]
g=c(p+1,rep(1:p,rep(2,p))) # groups
v=c(0,rep(1,2*p))
                            # penalization status
label=c("t",rep(c("prog","pred"),p)) # type of predictor variables
# generate beta
beta=c(rnorm(13,0,2),rep(0,ncol(x)-13))
beta[c(2,4,7,9)]=0
# generate y
data=x%*%beta
noise=rnorm(n)
snr=as.numeric(sqrt(var(data)/(s*var(noise))))
y=data+snr*noise
cvfit=cv.smog(x,y,g,v,label,type="GCV",family="gaussian")
```

glog

*Generalized linear model constraint on hierarchical structure by using overlapped group penalty* 

#### Description

Generalized linear model constraint on hierarchical structure by using overlapped group penalty

## Usage

```
glog(y, x, g, v, lambda, hierarchy, family = "gaussian", rho = 10,
scale = TRUE, eabs = 0.001, erel = 0.001, LL = 1, eta = 1.25,
maxitr = 1000L)
```

#### Arguments

у

response variable, in the format of matrix. When family is "gaussian" or "binomial", y ought to be a matrix of n by 1 for the observations; when family is "coxph", y represents the survival objects, that is, a matrix of n by 2, containing the survival time and the censoring status. See Surv.

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| х         | a model matrix of dimensions n by p,in which the column represents the predic-<br>tor variables.   |
|-----------|--|
| g         | a numeric vector of group labels for the predictor variables.  |
| v         | a numeric vector of binary values, represents whether or not the predictor vari-<br>ables are penalized. Note that 1 indicates penalization and 0 for not penalization.  |
| lambda    | a numeric vector of three penalty parameters corresponding to L2 norm, squared L2 norm, and L1 norm, respectively.   |
| hierarchy | a factor value in levels 0, 1, 2, which represent different hierarchical structure within groups, respectively. When hierarchy=0, $\lambda_2$ and $\lambda_3$ are forced to be zeroes; when hierarchy=1, $\lambda_2$ is forced to be zero; when hierarchy=2, there is no constraint on $\lambda$ 's. See smog. |
| family    | a description of the distribution family for the response variable variable. For<br>continuous response variable, family is "gaussian"; for multinomial or binary<br>response variable, family is "binomial"; for survival response variable, family is<br>"coxph", respectively.                              |
| rho       | the penalty parameter used in the alternating direction method of multipliers algorithm (ADMM). Default is 10.   |
| scale     | whether or not scale the design matrix. Default is true.   |
| eabs      | the absolute tolerance used in the ADMM algorithm. Default is 1e-3.  |
| erel      | the reletive tolerance used in the ADMM algorithm. Default is 1e-3.  |
| LL        | initial value for the Lipschitz continuous constant for approximation to the objective function in the Majorization- Minimization (MM) (or iterative shrinkage-thresholding algorithm (ISTA)). Default is 1.   |
| eta       | gradient stepsize for the backtrack line search for the Lipschitz continuous con-<br>stant. Default is 1.25.   |
| maxitr    | the maximum iterations for convergence in the ADMM algorithm. Default is 500.  |

## Value

A list of

| coefficients | A data frame of the variable name and the estimated coefficients      |
|--------------|---|
| llikelihood  | The log likelihood value based on the ultimate estimated coefficients |
| loglike      | The sequence of log likelihood values since the algorithm starts      |
| PrimalError  | The sequence of primal errors in the ADMM algorithm                   |
| DualError    | The sequence of dual errors in the ADMM algorithm                     |
| converge     | The integer of the iteration when the convergence occurs              |

## Author(s)

Chong Ma, <chongma8903@gmail.com>.

#### References

Ma C, Deng W, Ma S, Liu R and Galinsky K (2019). "Structural modeling using overlapped group penalties for discovering predictive biomarkers for subgroup analysis." *arXiv preprint arXiv:1904.11648*.

#### See Also

cv.smog,smog.default,smog.formula,predict.smog,plot.smog.

## Examples

```
set.seed(2018)
# generate design matrix x
n=50;p=100
s=10
x=matrix(0,n,1+2*p)
x[,1]=sample(c(0,1),n,replace = TRUE)
x[,seq(2,1+2*p,2)]=matrix(rnorm(n*p),n,p)
x[,seq(3,1+2*p,2)]=x[,seq(2,1+2*p,2)]*x[,1]
g=c(p+1,rep(1:p,rep(2,p))) # groups
                            # penalization status
v=c(0,rep(1,2*p))
# generate beta
beta=c(rnorm(13,0,2),rep(0,ncol(x)-13))
beta[c(2,4,7,9)]=0
# generate y
data1=x%*%beta
noise1=rnorm(n)
snr1=as.numeric(sqrt(var(data1)/(s*var(noise1))))
y1=data1+snr1*noise1
lambda = c(8, 0, 8)
hierarchy = 1
gfit1 = glog(y1,x,g,v,lambda,hierarchy,family = "gaussian")
```

penalty

Penalty function on the composite L2, L2-Square, and L1 penalties

#### Description

Penalty function on the composite L2, L2-Square, and L1 penalties

#### Usage

penalty(x, lambda, hierarchy, d)

#### plot.smog

#### Arguments

| x         | A vector of two numeric values, in which $x_1$ represents the prognostic effect, and $x_2$ for the predictive effect, respectively.   |
|-----------|---|
| lambda    | a vector of three penalty parameters. $\lambda_1$ and $\lambda_2$ are L2 and L2-Square (ridge) penalties for x in a group level, and $\lambda_3$ is the L1 penalty for $x_2$ , respectively.  |
| hierarchy | a factor value in levels 0, 1, 2, which represent different hierarchical structure in x, respectively. When hierarchy=0, $\lambda_2$ and $\lambda_3$ are forced to be zeroes; when hierarchy=1, $\lambda_2$ is forced to be zero; when hierarchy=2, there is no constraint on $\lambda$ 's. See smog. |
| d         | indices for overlapped variables in x.  |

#### Value

A numeric value of the penalty function based on the composition of L2, L2-Square, and L2 penalties.

#### Author(s)

Chong Ma, <chongma8903@gmail.com>.

#### References

Ma C, Deng W, Ma S, Liu R and Galinsky K (2019). "Structural modeling using overlapped group penalties for discovering predictive biomarkers for subgroup analysis." *arXiv preprint arXiv:1904.11648*.

#### See Also

cv.smog, smog.default, smog.formula, predict.smog, plot.smog.

#### Examples

penalty(x = rnorm(6,2,1), lambda = c(0.5,0.3,0.1), hierarchy = 0, d = c(1,1,2,2,3,3))

plot.smog

plot method for objects of the class smog

#### Description

plot.smog can produce a panel of plots for the primal errors, dual errors, and the penalized loglikelihood values, based on the provided fitted model (x) in the S3method of smog.

#### Usage

```
## S3 method for class 'smog'
plot(x, type = "l", xlab = "iteration",
    caption = list("primal error", "dual error", "log-likelihood"), ...)
```

#### Arguments

| a fitted object of class inheriting from smog.               |
|--|
| default line types and x axis labels for the panel of plots. |
| a list of y axes labels for the panel of plots.              |
| additional arguments that could be supplied to plot and par. |
|  |

## Details

For the panel of three plots, the xlab is "iterations" and the type is "l", by default. The ylab are "primal error", "dual error", "log-likelihood", respectively. This panel of plots can reflect the convergence performance for the algorithm used in smog.

## Author(s)

Chong Ma, <chongma8903@gmail.com>.

#### References

Ma C, Deng W, Ma S, Liu R and Galinsky K (2019). "Structural modeling using overlapped group penalties for discovering predictive biomarkers for subgroup analysis." *arXiv preprint arXiv:1904.11648*.

### See Also

par, plot.default, predict.smog, smog.default, smog.formula, cv.smog.

| predict.smog | predict method for objects of the class smog |
|--------------|--|
|              |  |

#### Description

predict.smog can produce the prediction for user-given new data, based on the provided fitted model (object) in the S3method of smog. If the newdata omitted, it would output the prediction for the fitted model itself. The yielded result should match with the family in the provided model. See smog.

#### Usage

```
## S3 method for class 'smog'
predict(object, newdata = NULL, family = "gaussian", ...)
```

#### Arguments

| object  | a fitted object of class inheriting from smog.   |
|---------|--|
| newdata | a data frame containing the predictor variables, which are used to predict. If omitted, the fitted linear predictors are used. |
| family  | a description of distribution family for which the response variable is to be pre-<br>dicted.                                  |
|         | additional arguments affecting the predictions produced.   |

#### prox

### Details

If newdata = NULL, the fitted.value based on the object is used for the prediction.

#### Value

If family = "gaussian", a vector of prediction for the response is returned. For family = "coxph", a vector of predicted survival probability is returned. When family = "binomial", it outputs a data frame containing the predicted group labels and the corresponding probabilies.

#### Author(s)

Chong Ma, <chongma8903@gmail.com>.

## References

Ma C, Deng W, Ma S, Liu R and Galinsky K (2019). "Structural modeling using overlapped group penalties for discovering predictive biomarkers for subgroup analysis." *arXiv preprint arXiv:1904.11648*.

#### See Also

smog.default, smog.formula, cv.smog, plot.smog.

| prox | Composite proximal operator based on L2, L2-Square, and L1 penal- |
|------|---|
|      | ties  |

#### Description

Composite proximal operator based on L2, L2-Square, and L1 penalties

#### Usage

prox(x, lambda, hierarchy, d)

#### Arguments

| х         | A numeric vector of two.  |
|-----------|---|
| lambda    | a vector of three penalty parameters. $\lambda_1$ and $\lambda_2$ are L2 and L2-Square (ridge) penalties for x in a group level, and $\lambda_3$ is the L1 penalty for $x_2$ , respectively.  |
| hierarchy | a factor value in levels 0, 1, 2, which represent different hierarchical structure in x, respectively. When hierarchy=0, $\lambda_2$ and $\lambda_3$ are forced to be zeroes; when hierarchy=1, $\lambda_2$ is forced to be zero; when hierarchy=2, there is no constraint on $\lambda$ 's. See smog. |
| d         | indices for overlapped variables in x.  |

#### Value

A two-dimensional numerical vector, soft-thresholded based on a composition of  $\lambda_1$ ,  $\lambda_2$ , and  $\lambda_3$ .

## Author(s)

Chong Ma, <chongma8903@gmail.com>.

## References

Ma C, Deng W, Ma S, Liu R and Galinsky K (2019). "Structural modeling using overlapped group penalties for discovering predictive biomarkers for subgroup analysis." *arXiv preprint arXiv:1904.11648*.

#### See Also

cv.smog, smog.default, smog.formula, predict.smog, plot.smog.

#### Examples

```
prox(x = rnorm(6,2,1), lambda = c(0.5,0.3,0.1), hierarchy = 0, d = c(1,1,2,2,3,3))
```

proxL1

L1 proximal operator

#### Description

L1 proximal operator

#### Usage

proxL1(x, lambda)

#### Arguments

| Х      | numeric value.                              |  |  |  |
|--------|---|--|--|--|
| lambda | numeric value for the L1 penalty parameter. |  |  |  |

#### Value

A numeric value soft-thresholded by  $\lambda$ , which is  $sign(x)(|x| - \lambda)_+$ .

#### Author(s)

Chong Ma, <chongma8903@gmail.com>.

## References

Ma C, Deng W, Ma S, Liu R and Galinsky K (2019). "Structural modeling using overlapped group penalties for discovering predictive biomarkers for subgroup analysis." *arXiv preprint arXiv:1904.11648*.

## Examples

proxL1(2.0,0.5)

proxL2

#### Description

L2 proximal operator

### Usage

proxL2(x, lambda)

#### Arguments

| х      | A vector of p numerical values.             |
|--------|---|
| lambda | numeric value for the L2 penalty parameter. |

#### Value

A numeric vector soft-thresholded by  $\lambda$  as a group, which is  $(1 - \frac{\lambda\sqrt{p}}{\sqrt{x_1^2 + \dots + x_p^2}})_+ x$ .

## Author(s)

Chong Ma, <chongma8903@gmail.com>.

### References

Ma C, Deng W, Ma S, Liu R and Galinsky K (2019). "Structural modeling using overlapped group penalties for discovering predictive biomarkers for subgroup analysis." *arXiv preprint arXiv:1904.11648*.

#### Examples

proxL2(rnorm(6,2,1),0.5)

sim\_rct\_biomarker Simulate a randomized clinical trial with biomarkers

## Description

sim\_rct\_biomarker is used to simulate clinical trial data with specified treatment, prognostic, and predictive effect sizes.

#### Usage

```
sim_rct_biomarker(n = 50, p = 100, p_prog = 5, p_pred = 5, p_both = 5,
v_trt = 0.4, v_prog = 0.2, v_pred = 0.2, v_err = 0.2, corr = NULL,
family = "gaussian", ...)
```

## Arguments

| n      | Number of subjects.  |
|--------|--|
| р      | Number of biomarkers.  |
| p_prog | Number of biomarkers with prognostic effects only.                               |
| p_pred | Number of biomarkers with predictive effects only.                               |
| p_both | Number of biomarkers with both prognostic and predictive effects                 |
| v_trt  | Variance of response due to treatment.   |
| v_prog | Variance of response due to prognostic effects.                                  |
| v_pred | Variance of response due to predictive effects.                                  |
| v_err  | Variance of response due to random noise.  |
| corr   | Autocorrelation parameter between biomarkers, default is NULL.                   |
| family | The distribution family for response variable, can be "gaussian", or "binomial". |
|        | Default is "gaussian".   |
|        | further arguments passed to or from other methods.                               |

## Value

A list containing several variables.

| Т     | Treatment status in 1 or -1 values.           |
|-------|---|
| Х     | Biomarkers.                                   |
| W     | Hadamard product of treatment and biomarkers. |
| Μ     | Model matrix - binding of T, X, and W.        |
| Υ     | Response.                                     |
| Y0    | Response without error.                       |
| tau   | Treatment effect.                             |
| beta  | Prognostic effects.                           |
| gamma | Predictive effects.                           |
| theta | All effects corresponding to M.               |

#### Author(s)

Chong Ma <chong.ma@yale.edu>, Kevin Galinsky <Kevin.Galinsky@takeda.com>.

## References

Ma C, Deng W, Ma S, Liu R and Galinsky K (2019). "Structural modeling using overlapped group penalties for discovering predictive biomarkers for subgroup analysis." *arXiv preprint arXiv:1904.11648*.

## Examples

```
sim <- sim_rct_biomarker(n = 1e5)
var(sim$T * sim$tau)
var(sim$X %*% sim$beta)
var(sim$W %*% sim$gamma)</pre>
```

smog.default

*Generalized linear model constraint on hierarchical structure by using overlapped group penalty* 

#### Description

smog fits a linear non-penalized phynotype (demographic) variables such as age, gender, treatment, etc, and penalized groups of prognostic effect (main effect) and predictive effect (interaction effect), by satisfying the hierarchy structure: if a predictive effect exists, its prognostic effect must be in the model. It can deal with continuous, binomial or multinomial, and survival response variables, underlying the assumption of Gaussian, binomial (multinomial), and Cox proportional hazard models, respectively. It can accept formula, and output coefficients table, fitted.values, and convergence information produced in the algorithm iterations.

#### Usage

```
## Default S3 method:
smog(x, y, g, v, label, lambda1, lambda2, lambda3,
family = "gaussian", subset = NULL, rho = 10, scale = TRUE,
eabs = 0.001, erel = 0.001, LL = 1, eta = 1.25, maxitr = 1000, ...)
## S3 method for class 'formula'
smog(formula, data = list(), g, v, label, lambda1, lambda2,
lambda3, ...)
```

#### Arguments

| x       | a model matrix, or a data frame of dimensions n by p, in which the columns represents the predictor variables.  |
|---------|---|
| у       | response variable, corresponds to the family description. When family is "gaus-<br>sian" or "binomial", y ought to be a numeric vector of observations of length<br>n; when family is "coxph", y represents the survival objects, containing the sur-<br>vival time and the censoring status. See Surv. |
| g       | a vector of group labels for the predictor variables.   |
| v       | a vector of binary values, represents whether or not the predictor variables are penalized. Note that 1 indicates penalization and 0 for not penalization.  |
| label   | a character vector, represents the type of predictors in terms of treatment, prog-<br>nostic, and predictive effects by using "t", "prog", and "pred", respectively.  |
| lambda1 | penalty parameter for the L2 norm of each group of prognostic and predictive effects.   |
| lambda2 | ridge penalty parameter for the squared L2 norm of each group of prognostic and predictive effects.   |
| lambda3 | penalty parameter for the L1 norm of predictive effects.  |

| family  | a description of the distribution family for the response variable variable. For continuous response variable, family is "gaussian"; for multinomial or binary response variable, family is "binomial"; for survival response variable, family is |  |
|---------|---|--|
|         | "coxph", respectively.  |  |
| subset  | an optional vector specifying a subset of observations to be used in the model fitting. Default is NULL.  |  |
| rho     | the penalty parameter used in the alternating direction method of multipliers (ADMM) algorithm. Default is 10.  |  |
| scale   | whether or not scale the design matrix. Default is TRUE.  |  |
| eabs    | the absolute tolerance used in the ADMM algorithm. Default is 1e-3.   |  |
| erel    | the reletive tolerance used in the ADMM algorithm. Default is 1e-3.   |  |
| LL      | initial value for the Lipschitz continuous constant for approximation to the objective function in the Majorization-Minimization (MM) (or iterative shrinkage-thresholding algorithm (ISTA)). Default is 1.                                       |  |
| eta     | gradient stepsize for the backtrack line search for the Lipschitz continuous con-<br>stant. Default is 1.25.  |  |
| maxitr  | the maximum iterations for convergence in the ADMM algorithm. Default is 1000.  |  |
|         | other relevant arguments that can be supplied to smog.  |  |
| formula | an object of class "formula": a symbolic description of the model to be fitted.<br>Should not include the intercept.  |  |
| data    | an optional data frame, containing the variables in the model.  |  |

#### Details

The formula has the form response  $\sim 0 + \text{terms}$  where terms is a series of predictor variables to be fitted for response. For gaussian family, the response is a continuous vector. For binomial family, the response is a factor vector, in which the last level denotes the "pivot". For coxph family, the response is a Surv object, containing the survival time and censoring status.

The terms contains the non-penalized predictor variables, and many groups of prognostic and predictive terms, where in each group the prognostic term comes first, followed by the predictive term.

Different hierachical structures within groups can result from adjusting the penalty parameters in the penalty function:

$$\Omega(\boldsymbol{\beta}) = \lambda_1 ||\boldsymbol{\beta}|| + \lambda_2 ||\boldsymbol{\beta}||^2 + \lambda_3 |\beta_2|$$

Where  $\beta = (\beta_1, \beta_2)$ . Note that  $\beta_1$  denotes the prognostic effect (main effect), and  $\beta_2$  for the predictive effect (interactive effect), respectively. When  $\lambda_2 = 0$  and  $\lambda_3 = 0$ , it indicates no structure within groups. When  $\lambda_2 \neq 0$ , the penalty function honors the structure within groups such that: predictive effect  $\neq 0 \implies$  prognostic effect  $\neq 0$ .

rho, eabs, erel, LL, eta are the corresponding parameters used in the itervative shrinkage-thresholding algorithm (ISTA) and the alternating direction method of multipliers algorithm (ADMM).

Note that the missing values in the data are supposed to be dealt with in the data preprocessing, before applying the method.

#### Value

smog returns an object of class inhering from "smog". The generic accessor functions coef, coefficients, fitted.value, and predict can be used to extract various useful features of the value returned by smog.

An object of "smog" is a list containing at least the following components:

- coefficients a data frame containing the nonzero predictor variables' indexes, names, and estimates. When family is "binomial", the estimates have K-1 columns, each column representing the weights for the corresponding group. The last group behaves the "pivot".
- fitted.values the fitted mean values for the response variable, for family is "gaussian". When family is "binomial", the fitted.values are the probabilies for each class; when family is "coxph", the fitted.values are survival probabilities.
- model a list of estimates for the intercept, treatment effect, and prognostic and predictive effects for the selectd biomarkers.
- weight the weight of predictors resulted from the penalty funciton, is used to calculate the degrees of freedom.
- DF the degrees of freedom. When family = "gaussian",  $DF = tr(x'_{\lambda}(x'_{\lambda}x_{\lambda} + W)x_{\lambda})$ . For other families, DF is approximated by diag(1/(1+W)).
- criteria model selection criteria, including the correction Akaike's Information Criterion (AIC), AIC, Bayesian Information Criterion (BIC), and the generalized cross-validation score (GCV), respectively. See also cv. smog.

**cAIC**  $\frac{n}{2}\log(|2*\log-likelihood|) + \frac{n}{2}\left(\frac{1+k/n}{1-k+2/n}\right).$ 

AIC log( $|2*\log-likelihood|/n$ ) +  $2\frac{k}{n}$ .

**BIC**  $\log(|2*\log-likelihood|/n) + 2\frac{k}{n}\log(n)$ .

**GCV** |2\*log-likelihood| /  $(n(1 - k/n)^2)$ .

Where k is the degrees of freedom DF, which is related to the penalty parameters  $\lambda$ 's.

- 11ikelihood the log-likelihood value for the converged model.
- loglike the penalized log-likelihood values for each iteration in the algorithm.
- PrimalError the averged norms  $||\beta Z||/\sqrt{p}$  for each iteration, in the ADMM algorithm.

| DualError | the averaged norms $  Z^{t+1} -$ | $Z^t    / \sqrt{p}$ for each | iteration, in the | ADMM algo- |
|-----------|----------------------------------|------------------------------|-------------------|------------|
|           | rithm.                           |                              |                   |            |

| converge | the number of iteration | s processed in the | e ADMM algorithm. |
|----------|-------------------------|--------------------|-------------------|
|----------|-------------------------|--------------------|-------------------|

- call the matched call.
- formula the formula supplied.

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#### References

Ma C, Deng W, Ma S, Liu R and Galinsky K (2019). "Structural modeling using overlapped group penalties for discovering predictive biomarkers for subgroup analysis." *arXiv preprint arXiv:1904.11648*.

#### See Also

cv.smog, predict.smog, plot.smog.

#### Examples

```
require(coxed)
n=50;p=100
set.seed(2018)
# generate design matrix x
s=10
x=matrix(0,n,1+2*p)
x[,1]=sample(c(0,1),n,replace = TRUE)
x[,seq(2,1+2*p,2)]=matrix(rnorm(n*p),n,p)
x[,seq(3,1+2*p,2)]=x[,seq(2,1+2*p,2)]*x[,1]
g=c(p+1,rep(1:p,rep(2,p))) # groups
                            # penalization status
v=c(0,rep(1,2*p))
label=c("t",rep(c("prog","pred"),p)) # type of predictor variables
# generate beta
beta=c(rnorm(13,0,2),rep(0,ncol(x)-13))
beta[c(2,4,7,9)]=0
# generate y
data1=x%*%beta
noise1=rnorm(n)
snr1=as.numeric(sqrt(var(data1)/(s*var(noise1))))
y1=data1+snr1*noise1
lfit1=smog(x,y1,g,v,label,lambda1=8,lambda2=0,lambda3=8,family = "gaussian")
## generate binomial data
prob=exp(as.matrix(x)%*%as.matrix(beta))/(1+exp(as.matrix(x)%*%as.matrix(beta)))
y2=ifelse(prob<0.5,0,1)</pre>
lfit2=smog(x,y2,g,v,label,lambda1=0.03,lambda2=0,lambda3=0.03,family = "binomial")
## generate survival data
data3=sim.survdata(N=n,T=100,X=x,beta=beta)
y3=data3$data[,c("y","failed")]
y3$failed=ifelse(y3$failed,1,0)
colnames(y3)=c("time","status")
lfit3=smog(x,y3,g,v,label,lambda1=0.2,lambda2=0,lambda3=0.2,family = "coxph")
```

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