

# Package ‘semPower’

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**Type** Package

**Title** Power Analyses for SEM

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**Description** Provides a-priori, post-hoc, and compromise power-analyses for structural equation models (SEM). Moshagen & Erdfelder (2016) <[doi:10.1080/10705511.2014.950896](https://doi.org/10.1080/10705511.2014.950896)>.

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checkBounded	<i>checkBounded</i>
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---

**Description**

checks whether x is defined and lies within the specified bound

**Usage**

```
checkBounded(x, message, bound = c(0, 1))
```

**Arguments**

x	x
message	identifier for x
bound	the boundaries, array of size two

---

`checkPositive`*checkPositive*

---

**Description**

checks whether x is defined and a positive number, stop otherwise

**Usage**

```
checkPositive(x, message)
```

**Arguments**

x

x

message

identifier for x

---

---

`checkPositiveDefinite` *checkPositiveDefinite*

---

**Description**

checks whether x is positive definite

**Usage**

```
checkPositiveDefinite(x, message)
```

**Arguments**

x

x

message

identifier for x

getAGFI.F

*getAGFI.F***Description**

calculates AGFI from minimum of the ML-fit-function

**Usage**

```
getAGFI.F(Fmin, df, p)
```

**Arguments**

Fmin	minimum of the ML-fit-function
df	model degrees of freedom
p	number of observed variables

**Value**

AGFI

getBetadiff

*getBetadiff***Description**

get squared difference between requested and achieved beta on a logscale

**Usage**

```
getBetadiff(cN, critChi, logBetaTarget, fmin, df)
```

**Arguments**

cN	current N
critChi	critical chi-square associated with chosen alpha error
logBetaTarget	log(desired beta)
fmin	minimum of the ML fit function
df	the model degrees of freedom

**Value**

squared difference requested and achieved beta on a log scale

getCFI.Sigma	<i>getCFI.Sigma</i>
--------------	---------------------

### Description

calculates CFI given model-implied and observed covariance matrix.

### Usage

```
getCFI.Sigma(SigmaHat, S)
```

### Arguments

SigmaHat	model implied covariance matrix
S	observed (or population) covariance matrix

### Details

$\text{cfi} = (\text{f\_null} - \text{f\_hyp}) / \text{f\_null}$

### Value

CFI

getChiSquare.F	<i>getChiSquare.F</i>
----------------	-----------------------

### Description

calculates chis-square from the population minimum of the fit-function

### Usage

```
getChiSquare.F(Fmin, n, df)
```

### Arguments

Fmin	population minimum of the fit-function
n	number of observations
df	model degrees of freedom

### Details

$\text{chi} = (n-1)*F + df = ncp + df$

note that F is the population minimum; using F\_hat would give chi = (n-1)\*F\_hat

**Value**

NCP

---

getChiSquare.NCP	<i>getChiSquare.NCP</i>
------------------	-------------------------

---

**Description**

calculates chi-square from NCP

**Usage**

```
getChiSquare.NCP(NCP, df)
```

**Arguments**

NCP	non-centrality parameter
df	model degrees of freedom

**Details**

$\text{chi} = \text{ncp} + \text{df}$

**Value**

chiSquare

---

getErrorDiff	<i>getErrorDiff</i>
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---

**Description**

determine the squared log-difference between alpha and beta error given a certain chi-square value from central chi-square(df) and a non-central chi-square(df, ncp) distribution.

**Usage**

```
getErrorDiff(critChiSquare, df, ncp, log.abratio)
```

**Arguments**

critChiSquare	evaluated chi-squared value
df	the model degrees of freedom
ncp	the non-centrality parameter
log.abratio	$\log(\alpha/\beta)$

**Value**

squared difference between alpha and beta on a log scale

---

**getF**

*getF calculates minimum of the ML-fit-function from known fit indices*

---

**Description**

getF calculates minimum of the ML-fit-function from known fit indices

**Usage**

```
getF(  
  effect,  
  effect.measure,  
  df = NULL,  
  p = NULL,  
  SigmaHat = NULL,  
  Sigma = NULL  
)
```

**Arguments**

effect	magnitude of effect
effect.measure	measure of effect, one of 'fmin','rmsea','agfi','gfi','mc'
df	model degrees of freedom
p	number of observed variables
SigmaHat	model implied covariance matrix
Sigma	population covariance matrix

**Value**

Fmin

getF.AGFI

*getFAGFI***Description**

calculates minimum of the ML-fit-function from AGFI

**Usage**

```
getF.AGFI(AGFI, df, p)
```

**Arguments**

AGFI	AGFI
df	model degrees of freedom
p	number of observed variables

**Details**

$$F_{\min} = rmsea^2 * df$$
**Value**

Fmin

getF.GFI

*getFGFI***Description**

calculates minimum of the ML-fit-function from AGFI

**Usage**

```
getF.GFI(GFI, p)
```

**Arguments**

GFI	GFI
p	number of observed variables

**Value**

Fmin

---

`getF.Mc`*getF.Mc*

---

**Description**

calculates minimum of the ML-fit-function from Mc

**Usage**`getF.Mc(Mc)`**Arguments**

Mc                    Mc

**Value**

Fmin

---

`getF.RMSEA`*getF.RMSEA*

---

**Description**

calculates minimum of the ML-fit-function from RMSEA

**Usage**`getF.RMSEA(RMSEA, df)`**Arguments**

RMSEA                RMSEA  
df                    model degrees of freedom

**Details**

$F_{\text{min}} = \text{rmsea}^2 * df$

**Value**

Fmin

getF.Sigma	<i>getF.Sigma</i>
------------	-------------------

### Description

calculates minimum of the ML-fit-function given model-implied and observed covariance matrix.

### Usage

```
getF.Sigma(SigmaHat, S)
```

### Arguments

SigmaHat	model implied covariance matrix
S	observed (or population) covariance matrix

### Details

$F_{min} = \text{tr}(S$

### Value

$F_{min}$

getFormattedResults	<i>getFormattedResults</i>
---------------------	----------------------------

### Description

returned dataframe containing formatted results

### Usage

```
getFormattedResults(type, result, digits = 6)
```

### Arguments

type	type of power analysis
result	result object (list)
digits	number of significant digits

### Value

`data.frame`

---

`getGFI.F``getGFI.F`

---

**Description**

calculates GFI from minimum of the ML-fit-function

**Usage**`getGFI.F(Fmin, p)`**Arguments**

<code>Fmin</code>	minimum of the ML-fit-function
<code>p</code>	number of observed variables

**Value**`GFI`

---

`getIndices.F``getIndices.F`

---

**Description**

calculates known indices from minimum of the ML-fit-function

**Usage**`getIndices.F(fmin, df, p = NULL, SigmaHat = NULL, Sigma = NULL)`**Arguments**

<code>fmin</code>	minimum of the ML-fit-function
<code>df</code>	model degrees of freedom
<code>p</code>	number of observed variables
<code>SigmaHat</code>	model implied covariance matrix
<code>Sigma</code>	population covariance matrix

**Value**

list of indices

getMc.F

*getMc.F***Description**

calculates Mc from minimum of the ML-fit-function

**Usage**

```
getMc.F(Fmin)
```

**Arguments**

Fmin                minimum of the ML-fit-function

**Value**

Mc

getNCP

*getNCP***Description**

calculates non-centrality parameter from the population minimum of the fit-function

**Usage**

```
getNCP(Fmin, n)
```

**Arguments**

Fmin                population minimum of the fit-function  
 n                    number of observations

**Details**

$$\text{ncp} = (n-1) * F$$

**Value**

NCP

---

`getRMSEA.F`*getRMSEA.F*

---

**Description**

calculates RMSEA from minimum of the ML-fit-function

**Usage**

```
getRMSEA.F(Fmin, df)
```

**Arguments**

Fmin	minimum of the ML-fit-function
df	model degrees of freedom

**Details**

$F_{\text{min}} = \text{rmsea}^2 * df$

**Value**

RMSEA

---

`getSRMR.Sigma`*getSRMR.Sigma*

---

**Description**

calculates SRMR given model-implied and observed covariance matrix.

**Usage**

```
getSRMR.Sigma(SigmaHat, S)
```

**Arguments**

SigmaHat	model implied covariance matrix
S	observed (or population) covariance matrix

**Value**

SRMR

---

semPower*semPower: Power analyses for structural equation models (SEM).*

---

**Description**

semPower allows for performing a-priori, post-hoc, and compromise power-analyses for structural equation models (SEM).

**Details**

- A-priori power analysis `semPower.aPriori` computes the required N, given an effect, alpha, power, and the model df
- Post-hoc power analysis `semPower.postHoc` computes the achieved power, given an effect, alpha, N, and the model df
- Compromise power analysis `semPower.compromise` computes the implied alpha and power, given an effect, the alpha/beta ratio, N, and the model df

In SEM, the discrepancy between H0 and H1 (the magnitude of effect) refers to the difference in fit between two models. If only one model is defined (which is the default), power refers to the global chi-square test. If both models are explicitly defined, power is computed for nested model tests. semPower allows for expressing the magnitude of effect by one of the following measures: F0, RMSEA, Mc, GFI, or AGFI.

Alternatively, the implied effect can also be computed from the discrepancy between the population (or a certain model-implied) covariance matrix defining H0 and the hypothesized (model-implied) covariance matrix from a nested model defining H1. See the examples below how to use this feature in conjunction with lavaan.

**Author(s)**

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---

semPower.aPriori

*semPower.aPriori*

---

**Description**

Determine required sample size given alpha, beta/power, df, and effect

**Usage**

```
semPower.aPriori(
  effect = NULL,
  effect.measure = NULL,
  alpha,
  beta = NULL,
```

```

power = NULL,
df,
p = NULL,
SigmaHat = NULL,
Sigma = NULL
)

```

**Arguments**

effect	effect size specifying the discrepancy between H0 and H1
effect.measure	type of effect, one of "F0", "RMSEA", "Mc", "GFI", AGFI"
alpha	alpha error
beta	beta error; set either beta or power
power	power (1-beta); set either beta or power
df	the model degrees of freedom
p	the number of observed variables, required for effect.measure = "GFI" and "AGFI"
SigmaHat	model implied covariance matrix. Use in conjunction with Sigma to define effect and effect.measure.
Sigma	population covariance matrix. Use in conjunction with SigmaHat to define effect and effect.measure.

**Value**

list

**Examples**

```

## Not run:
power <- semPower.aPriori(effect = .05, effect.measure = "RMSEA", alpha = .05, beta = .05, df = 200)
power
power <- semPower.aPriori(effect = .15, effect.measure = "F0", alpha = .05, power = .80, df = 100)
power
power <- semPower.aPriori(alpha = .01, beta = .05, df = 5,
                           SigmaHat = diag(4), Sigma = cov(matrix(rnorm(4*1000), ncol=4)))
power

## End(Not run)

```

semPower.compromise    *semPower.compromise*

**Description**

Performs a compromise power analysis, i.e. determines the critical chi-square along with the implied alpha and beta, given a specified alpha/beta ratio, effect, N, and df

**Usage**

```
semPower.compromise(
  effect = NULL,
  effect.measure = NULL,
  abratio = 1,
  N,
  df,
  p = NULL,
  SigmaHat = NULL,
  Sigma = NULL
)
```

**Arguments**

effect	effect size specifying the discrepancy between H0 and H1
effect.measure	type of effect, one of "F0", "RMSEA", "Mc", "GFI", AGFI"
abratio	the ratio of alpha to beta
N	the number of observations
df	the model degrees of freedom
p	the number of observed variables, required for effect.measure = "GammaHat", "GFI", and "AGFI"
SigmaHat	model implied covariance matrix. Use in conjunction with Sigma to define effect and effect.measure.
Sigma	population covariance matrix. Use in conjunction with SigmaHat to define effect and effect.measure.

**Value**

list

**Examples**

```
## Not run:
cp.ph <- semPower.compromise(effect = .08, effect.measure = "RMSEA", abratio = 1, N = 250, df = 200)
summary(cp.ph)

## End(Not run)
```

**Description**

Determine power (1-beta) given alpha, df, and effect

**Usage**

```
semPower.postHoc(
  effect = NULL,
  effect.measure = NULL,
  alpha,
  N,
  df,
  p = NULL,
  SigmaHat = NULL,
  Sigma = NULL
)
```

**Arguments**

<code>effect</code>	effect size specifying the discrepancy between H0 and H1
<code>effect.measure</code>	type of effect, one of "F0", "RMSEA", "Mc", "GFI", AGFI"
<code>alpha</code>	alpha error
<code>N</code>	the number of observations
<code>df</code>	the model degrees of freedom
<code>p</code>	the number of observed variables, required for effect.measure = "GammaHat", "GFI", and "AGFI"
<code>SigmaHat</code>	model implied covariance matrix. Use in conjunction with Sigma to define effect and effect.measure.
<code>Sigma</code>	population covariance matrix. Use in conjunction with SigmaHat to define effect and effect.measure.

**Value**

list

**Examples**

```
## Not run:
power <- semPower.postHoc(effect = .05, effect.measure = "RMSEA", alpha = .05, N = 250, df = 200)
power
power <- semPower.postHoc(N = 1000, df = 5, alpha = .05,
                           SigmaHat = diag(4), Sigma = cov(matrix(rnorm(4*1000), ncol=4)))
power

## End(Not run)
```

---

```
semPower.powerPlot.byEffect
    semPower.powerPlot.byEffect
```

---

## Description

show a plot showing power as function of N for a given effect and alpha

## Usage

```
semPower.powerPlot.byEffect(
  effect.measure = NULL,
  alpha,
  N,
  df,
  p = NULL,
  effect.min = NULL,
  effect.max = NULL,
  steps = 50,
  linewidth = 1
)
```

## Arguments

<code>effect.measure</code>	type of effect, one of "F0", "RMSEA", "Mc", "GFI", AGFI"
<code>alpha</code>	alpha error
<code>N</code>	the number of observations
<code>df</code>	the model degrees of freedom
<code>p</code>	the number of observed variables, required for <code>effect.measure = "GFI"</code> and <code>"AGFI"</code>
<code>effect.min</code>	minimum effect
<code>effect.max</code>	maximum effect
<code>steps</code>	number of steps
<code>linewidth</code>	linewidth

## Value

powerplot

## Examples

```
## Not run:
semPower.powerPlot.byEffect(effect.measure = "RMSEA", alpha = .05,
                             N = 500, effect.min = .01, effect.max = .15, df = 200)

## End(Not run)
```

---

```
semPower.powerPlot.byN
  sempower:powerPlot.byN
```

---

**Description**

show a plot showing power as function of N for a given effect and alpha

**Usage**

```
semPower.powerPlot.byN(
  effect = NULL,
  effect.measure = NULL,
  alpha,
  df,
  p = NULL,
  SigmaHat = NULL,
  Sigma = NULL,
  power.min = alpha,
  power.max = 0.999,
  steps = 50,
  linewidth = 1
)
```

**Arguments**

<code>effect</code>	effect size specifying the discrepancy between H0 and H1
<code>effect.measure</code>	type of effect, one of "F0", "RMSEA", "Mc", "GFI", AGFI"
<code>alpha</code>	alpha error
<code>df</code>	the model degrees of freedom
<code>p</code>	the number of observed variables, required for effect.measure = "GFI" and "AGFI"
<code>SigmaHat</code>	model implied covariance matrix. Use in conjunction with Sigma to define effect and effect.measure.
<code>Sigma</code>	population covariance matrix. Use in conjunction with SigmaHat to define effect and effect.measure.
<code>power.min</code>	minimum power, must not be smaller than alpha
<code>power.max</code>	maximum power
<code>steps</code>	number of steps
<code>linewidth</code>	linewidth

**Value**

powerplot

## Examples

```
## Not run:
semPower.powerPlot.byN(effect = .05, effect.measure = "RMSEA",
                        alpha = .05, power.min = .05, power.max = .999, df = 200)

## End(Not run)
```

**semPower.showPlot**      *semPower.showPlot*

## Description

show a plot showing central and non-central chi-square distribution

## Usage

```
semPower.showPlot(chiCrit, ncp, df, linewidth = 1)
```

## Arguments

chiCrit	critical chi-square, e.g. qchisq(alpha, df, ncp=0, lower.tail = F)
ncp	non-centrality parameter under H1
df	degrees of freedom
linewidth	linewidth

**summary.semPower.aPriori**      *summary.semPower.aPriori*

## Description

provide summary of a-priori power analyses

## Usage

```
## S3 method for class 'semPower.aPriori'
summary(object, ...)
```

## Arguments

object	result object from semPower.aPriori
...	other

---

```
summary.semPower.compromise  
summary.semPower.compromise
```

---

**Description**

provide summary of compromise post-hoc power analyses

**Usage**

```
## S3 method for class 'semPower.compromise'  
summary(object, ...)
```

**Arguments**

object	result object from semPower.compromise
...	other

---

```
summary.semPower.postHoc  
summary.semPower.postHoc
```

---

**Description**

provide summary of post-hoc power analyses

**Usage**

```
## S3 method for class 'semPower.postHoc'  
summary(object, ...)
```

**Arguments**

object	result object from semPower.posthoc
...	other

---

validateInput	<i>validateInput</i>	
---------------	----------------------	--

---

### Description

Validates input for power calcuation function

### Usage

```
validateInput(
  power.type = NULL,
  effect = NULL,
  effect.measure = NULL,
  alpha = NULL,
  beta = NULL,
  power = NULL,
  abratio = NULL,
  N = NULL,
  df = NULL,
  p = NULL,
  SigmaHat = NULL,
  Sigma = NULL,
  power.min = alpha,
  power.max = 0.999,
  effect.min = NULL,
  effect.max = NULL,
  steps = 50,
  linewidth = 1
)
```

### Arguments

<code>power.type</code>	type of power analyses, one of "a-priori", post-hoc", "compromise", "power-plot.byN", "powerplot.byEffect"
<code>effect</code>	effect size specifying the discrepancy between H0 and H1
<code>effect.measure</code>	type of effect, one of "F0", "RMSEA", "Mc", "GFI", AGFI"
<code>alpha</code>	alpha error
<code>beta</code>	beta error
<code>power</code>	power (1-beta)
<code>abratio</code>	ratio alpha/beta
<code>N</code>	the number of observations
<code>df</code>	the model degrees of freedom
<code>p</code>	the number of observed variables, required for effect.measure = "GFI" and "AGFI"
<code>SigmaHat</code>	model implied covariance matrix

Sigma	population covariance matrix
power.min	for plotting: minimum power
power.max	for plotting: maximum power
effect.min	for plotting: minimum effect
effect.max	for plotting: maximum effect
steps	for plotting: number of sampled points
linewidth	for plotting: linewidth

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