Package 'saeME'

March 20, 2020

Title Small Area Estimation with Measurement Error

Type Package

Version 1.0.1

Author Muhammad Rifqi Mubarak [aut, cre], Azka Ubaidillah [aut]

Maintainer Muhammad Rifqi Mubarak <16.9304@stis.ac.id>

Description A set of functions and datasets implementation of small area estimation when auxiliary variable is measured with error. These functions provide a empirical best linear unbiased prediction (EBLUP) estimator and mean squared error (MSE) estimator of the EBLUP. These models were developed by Ybarra and Lohr (2008) <doi:10.1093/biomet/asn048>.

License GPL-2

Depends R (>= 3.1.0)

Encoding UTF-8

Imports expm, MASS, stats

LazyData true

RoxygenNote 6.1.1

NeedsCompilation no

Repository CRAN

Date/Publication 2020-03-20 10:10:05 UTC

R topics documented:

saeME-package	. 2
dataME	
datamix	3
FHme	. 4
mse_FHme	5
	7

Index

```
saeME-package
```

Description

The sae with measurement error provides function for small area estimation when auxiliary variable is measured with error, and function for mean squared error estimation using jackknife method. This package implement model of Fay Herriot with Measurement Error developed by Ybarra and Lohr (2008).

Authors

Muhammad Rifqi Mubarak, Azka Ubaidillah

Email

Muhammad Rifqi Mubarak <16.9304@stis.ac.id>

Functions

FHme Gives the EBLUP of SAE with Measurement Error

mse_FHme Gives the MSE of SAE with Measurement Error

References

Ybarra, L.M. and Lohr, S. L. (2008). Small area estimation when auxiliary information is measured with error. Biometrika 95, 919-931.

dataME

dataME

Description

This data generated by simulation based on Fay-Herriot with Measurement Error Model by following these steps:

- 1. Generate x_i from a UNIF(5, 10) distribution, $\psi_i = 3$, $c_i = 0.25$, and $\sigma_v^2 = 2$.
- 2. Generate u_i from a N(0, c_i) distribution, e_i from a N(0, ψ_i) distribution, and v_i from a N(0, σ_v^2) distribution.
- 3. Generate $\hat{x}_i = x_i + u_i$.
- 4. Then for each iteration, we generated $Y_i = 2 + 0.5\hat{x}_i + v_i$ and $y_i = Y_i + e_i$.

Direct estimator y, auxiliary variable \hat{x} , sampling variance ψ , and c are arranged in a dataframe called dataME.

datamix

Usage

data(dataME)

Format

A data frame with 100 observations on the following 4 variables.

y Direct estimator for each domain.

x.hat Auxiliary variable for each domain.

vardir Sampling variances for each domain.

var.x MSE of auxiliary variable and sorted as x.hat

datamix

datamix

Description

This data generated by simulation based on Fay-Herriot with Measurement Error Model by following these steps:

- 1. Generate x_{1i} from a UNIF(5, 10) distribution, x_{2i} from a UNIF(9, 11) distribution, $\psi_i = 3$, $c_{1i} = c_{2i} = 0.25$, and $\sigma_v^2 = 2$.
- 2. Generate u_{1i} from a N(0, c_{1i}) distribution, u_{2i} from a N(0, c_{2i}) distribution, e_i from a N(0, ψ_i) distribution, and v_i from a N(0, σ_v^2) distribution.
- 3. Generate x_{3i} from a UNIF(1, 5) distribution and x_{4i} from a UNIF(10, 14) distribution.
- 4. Generate $\hat{x}_{1i} = x_{1i} + u_{1i}$ and $\hat{x}_{2i} = x_{2i} + u_{2i}$.
- 5. Then for each iteration, we generated $Y_i = 2 + 0.5\hat{x}_{1i} + 0.5\hat{x}_{2i} + 2x_{3i} + 0.5x_{4i} + v_i$ and $y_i = Y_i + e_i$.

This data contain combination between auxiliary variable measured with error and without error. Direct estimator y, auxiliary variable $\hat{x}_1 \hat{x}_2 x_3 x_4$, sampling variance ψ , and $c_1 c_2$ are arranged in a dataframe called datamix.

Usage

```
data(datamix)
```

Format

A data frame with 100 observations on the following 8 variables.

y Direct estimator for each domain.

x.hat1 Auxiliary variable (measured with error) for each domain.

x.hat2 Auxiliary variable (measured with error) for each domain.

x3 Auxiliary Variable (measured without error) for each domain.

x4 Auxiliary Variable (measured without error) for each domain.
vardir Sampling variances for each domain.
var.x1 MSE of auxiliary variable and sorted as x.hat1
var.x2 MSE of auxiliary variable and sorted as x.hat2

FHme

Fay-Herriot Model with Measurement Error

Description

This function gives the EBLUP estimator based on Fay-Herriot model with measurement error.

Usage

```
FHme(formula, vardir, var.x, type.x = "witherror", data)
```

Arguments

formula	an object of class formula (or one that can be coerced to that class): a symbolic description of the model to be fitted. The variables included formula must have a length equal to the number of domains m. This formula can provide auxiliary variable either measured with error or without error or combination between them. If the auxiliary variable are combination between noerror and witherror variable, input all witherror variable first then noerror variable.
vardir	vector containing the m sampling variances of direct estimators for each domain. The values must be sorted as the Y.
var.x	vector containing mean squared error of X. The values must be sorted as the X. if you use optional data, input this parameter use $c("")$, example: var.x = $c("c1")$ or var.x = $c("c1", "c2")$.
type.x	type of auxiliary variable used in the model. Either source measured with noerror, witherror and mix. Default value is witherror.
data	optional data frame containing the variables named in formula, vardir, and var.x.

Details

A formula has an implied intercept term. To remove this use either $y \sim x - 1$ or $y \sim 0 + x$. See formula for more details of allowed formulae.

Value

The function returns a list with the following objects:

eblup vector with the values of the estimators for the domains.

fit a list containing the following objects:

• method : type of fitting method.

- convergence : a logical value of convergence when calculating estimated beta and estimated random effects.
- iterations : number of iterations when calculating estimated beta and estimated random effects.
- estcoef : a dataframe with the estimated model coefficient (beta) in the first column, their standard error in the second column, the t statistics in the third column, and the p-values of the significance of each coefficient in the last column.
- refvar : a value of estimated random effects.

Examples

mse_FHme	Mean Squared Error Estimator of the EBLUP under a Fay-Herriot
	Model with Measurement Error

Description

This function gives the mean squared error estimator of the EBLUP based on Fay-Herriot model with measurement error using jackknife method.

Usage

```
mse_FHme(formula, vardir, var.x, type.x = "witherror", data)
```

Arguments

formula	an object of class formula (or one that can be coerced to that class): a symbolic description of the model to be fitted. The variables included formula must have a length equal to the number of domains m. This formula can provide auxiliary variable either measured with error or without error or combination between them. If the auxiliary variable are combination between noerror and witherror variable, input all witherror variable first then noerror variable.
vardir	vector containing the m sampling variances of direct estimators for each domain. The values must be sorted as the Y.
var.x	vector containing mean squared error of X. The values must be sorted as the X. if you use optional data, input this parameter use $c("")$, example: var.x = $c("c1")$ or var.x = $c("c1", "c2")$.
type.x	type of auxiliary variable used in the model. Either source measured with noerror, witherror and mix. Default value is witherror.
data	optional data frame containing the variables named in formula, vardir, and var.x.

Details

A formula has an implied intercept term. To remove this use either $y \sim x - 1$ or $y \sim 0 + x$. See formula for more details of allowed formulae.

Value

The function returns a list with the following objects:

mse vector with the values of the mean squared error for each domain.

Examples

```
data(dataME)
data(datamix)
```

Index

 $\begin{array}{c} \text{dataME, 2} \\ \text{datamix, 3} \end{array}$

FHme, 2, 4 formula, *4*--6

mse_FHme, 2, 5

saeME-package, 2