

Package ‘sSDR’

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Type Package

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Description Performs structured OLS (sOLS) and structured SIR (sSIR).

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LazyData TRUE

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center *Center a vector*

Description

Center a vector

Usage

```
center(v)
```

Arguments

v A vector.

Details

This function centers any vector and returns a vector with mean zero.

Value

A vector with mean zero.

Examples

```
data <- gen.data(n=100)
y.centered <- center(data$y)
```

cov.x *Covariance matrix*

Description

Covariance matrix

Usage

```
cov.x(X)
```

Arguments

X a n x p matrix of n observations and p predictors.

Details

This function returns A p x p covariance matrix for any n x p matrix.

Value

A $p \times p$ covariance matrix.

Examples

```
data <- gen.data(n=100)
x.cov <- cov.x(data$X)
```

disvm	<i>Subspace distance</i>
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Description

Subspace distance

Usage

```
disvm(v1, v2)
```

Arguments

v1	A matrix, each column consists of a p-dimensional vector.
v2	A matrix, each column consists of a p-dimensional vector.

Details

This function computes the distances between two spaces using the formulation in Li, Zha, Chiaromonte (2005), which is the Frobenius norm of the difference between the two orthogonal projection matrices defined by v1 and v2.

Value

A scalar represents the distance between the two spaces spanned by v1 and v2 respectively.

References

Li, B., Zha, H., and Chiaromonte, F. (2005). Contour regression: a general approach to dimension reduction. *Annals of Statistics*, 33(4):1580-1616.

Examples

```
v1 <- c(1, 0, 0)
v2 <- c(0, 1, 0)
disvm(v1, v1)
disvm(v1, v2)
```

`gen.data`*Simulate data*

Description

Simulate data

Usage

```
gen.data(n, rho = 0.5, theta = 1, binary = FALSE)
```

Arguments

<code>n</code>	Sample size.
<code>rho</code>	Pairwise correlation between covariates.
<code>theta</code>	Standard deviation of the random error.
<code>binary</code>	If TRUE, generate binary responses; otherwise, by default, create continuous responses.

Details

This function simulates data as presented in Liu (2015).

Value

`gen.data` returns a list containing at least the following components: "X", a covariate matrix of n observations and p predictors; "y", a univariate response; "b.true", the actual coefficients for each predictor group.

References

Liu, Y. (2015). Approaches to reduce and integrate data in structured and high-dimensional regression problems in Genomics. Ph.D. Dissertation, The Pennsylvania State University, University Park, Department of Statistics.

Examples

```
data <- gen.data(n=100)
names(data)
```

gOLS	<i>Groupwise OLS (gOLS)</i>
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Description

Groupwise OLS (gOLS)

Usage

```
gOLS(X, Y, groups, dims)
```

Arguments

X	A covariate matrix of n observations and p predictors.
Y	A univariate response.
groups	A vector with the number of predictors in each group.
dims	A vector with the dimension (at most 1) for each predictor group.

Details

This function estimates directions for each predictor group using gOLS. Predictors need to be organized in groups within the "X" matrix, as the same order saved in "groups". We only allow continuous covariates in the "X" matrix; while categorical covariates can be handled outside of gOLS, e.g. structured OLS.

Value

gOLS returns a list containing at least the following components: "b_est", the estimated directions for each group with its own dimension using gOLS AFTER normalization; "B", the estimated directions for each group using gOLS BEFORE normalization.

References

Liu, Y., Chiaromonte, F., and Li, B. (2015). Structured Ordinary Least Squares: a sufficient dimension reduction approach for regressions with partitioned predictors and heterogeneous units. Submitted.

Examples

```
data <- gen.data(n=1000, binary=FALSE) # generate data
dim(data$X) # covariate matrix of 1000 observations and 15 predictors
dim(data$y) # univariate response
groups <- c(5, 10) # two predictor groups and their numbers of predictors
dims <- c(1,1) # dimension of each predictor group
est_gOLS <- gOLS(data$X,data$y,groups,dims)
names(est_gOLS)
```

gOLS.comp.d	<i>Groupwise OLS (gOLS) BIC criterion to estimate dimensions with eigen-decomposition</i>
-------------	---

Description

Groupwise OLS (gOLS) BIC criterion to estimate dimensions with eigen-decomposition

Usage

```
gOLS.comp.d(X, y, groups)
```

Arguments

<code>X</code>	A covariate matrix of n observations and p predictors.
<code>y</code>	A univariate response.
<code>groups</code>	A vector with the number of predictors in each group.

Details

This function estimates dimension for each predictor group using eigen-decomposition. Predictors need to be organized in groups within the "X" matrix, as the same order saved in "groups". We only allow continuous covariates in the "X" matrix; while categorical covariates can be handled outside of gOLS, e.g. structured OLS.

Value

gOLS.comp.d returns a list containing at least the following components: "d", the estimated dimension (at most 1) for each predictor group; "crit", the BIC criterion from each iteration.

References

Liu, Y., Chiaromonte, F., and Li, B. (2015). Structured Ordinary Least Squares: a sufficient dimension reduction approach for regressions with partitioned predictors and heterogeneous units. Submitted.

Examples

```
data <- gen.data(n=1000, binary=FALSE) # generate data
dim(data$X) # covariate matrix of 1000 observations and 15 predictors
dim(data$y) # univariate response
groups <- c(5, 10) # two predictor groups and their numbers of predictors
dim_gOLS<-gOLS.comp.d(data$X,data$y,groups)
names(dim_gOLS)
```

gSIR *Groupwise SIR (gSIR) for binary response*

Description

Groupwise SIR (gSIR) for binary response

Usage

```
gSIR(X, Y, groups, dims)
```

Arguments

X	A covariate matrix of n observations and p predictors.
Y	A binary response.
groups	A vector with the number of predictors in each group.
dims	A vector with the dimension (at most 1) for each predictor group.

Details

This function estimates directions for each predictor group using gSIR. Predictors need to be organized in groups within the "X" matrix, as the same order saved in "groups". We only allow continuous covariates in the "X" matrix; while categorical covariates can be handled outside of gSIR, e.g. structured SIR.

Value

gSIR returns a list containing at least the following components: "b_est", the estimated directions for each group with its own dimension using gSIR AFTER normalization; "B", the estimated directions for each group using gSIR BEFORE normalization.

References

Guo, Z., Li, L., Lu, W., and Li, B. (2014). Groupwise dimension reduction via envelope method. Journal of the American Statistical Association, accepted.

Examples

```
data <- gen.data(n=1000, binary=TRUE) # generate data
dim(data$X) # covariate matrix of 1000 observations and 15 predictors
length(data$y) # binary response
groups <- c(5, 10) # two predictor groups and their numbers of predictors
dims <- c(1,1) # dimension of each predictor group
est_gSIR<-gSIR(data$X,data$y,groups,dims)
names(est_gSIR)
```

`gSIR.comp.d`*Groupwise SIR (gSIR) BIC criterion to estimate dimensions with eigen-decomposition (binary response)*

Description

Groupwise SIR (gSIR) BIC criterion to estimate dimensions with eigen-decomposition (binary response)

Usage

```
gSIR.comp.d(X, y, groups)
```

Arguments

<code>X</code>	A covariate matrix of n observations and p predictors.
<code>y</code>	A binary response.
<code>groups</code>	A vector with the number of predictors in each group.

Details

This function estimates dimension for each predictor group using eigen-decomposition. Predictors need to be organized in groups within the "X" matrix, as the same order saved in "groups". We only allow continuous covariates in the "X" matrix; while categorical covariates can be handled outside of gSIR, e.g. structured SIR.

Value

`gSIR.comp.d` returns a list containing at least the following components: "d", the estimated dimension (at most 1) for each predictor group; "crit", the BIC criterion from each iteration.

References

Liu, Y. (2015). Approaches to reduce and integrate data in structured and high-dimensional regression problems in Genomics. Ph.D. Dissertation, The Pennsylvania State University, University Park, Department of Statistics.

Examples

```
data <- gen.data(n=1000, binary=TRUE) # generate data
dim(data$X) # covariate matrix of 1000 observations and 15 predictors
length(data$y) # univariate response
groups <- c(5, 10) # two predictor groups and their numbers of predictors
dim_gSIR<-gSIR.comp.d(data$X,data$y,groups)
names(dim_gSIR)
```

matpower	<i>Power of a matrix</i>
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Description

Power of a matrix

Usage

```
matpower(X, alpha)
```

Arguments

X	A p x p square matrix.
alpha	A scalar determining the order of the power.

Details

This function calculates the power of a square matrix.

Value

A p x p square matrix.

Examples

```
data <- gen.data(n=100)
cov.squared <- matpower(cov.x(data$X), 2)
```

norm1	<i>Normalize a vector</i>
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Description

Normalize a vector

Usage

```
norm1(v)
```

Arguments

v	A vector.
---	-----------

Details

This function normalizes any non-zero vector and returns a vector with the norm equal to 1.

Value

A vector with norm 1.

Examples

```
data <- gen.data(n=100)
y.norm1 <- norm1(data$y)
```

orthnormal

Gram-Schmidt orthonormalization

Description

Gram-Schmidt orthonormalization

Usage

```
orthnormal(X)
```

Arguments

X a n x p matrix of n observations and p predictors.

Details

This function orthonormalizes any n x p matrix.

Value

A n x p matrix of n observations and p predictors.

Examples

```
data <- gen.data(n=100)
x.orth <- orthnormal(data$X)
```

sOLS.comp.d	<i>Structured OLS (sOLS) outer level BIC criterion to estimate dimension with eigen-decomposition</i>
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Description

Structured OLS (sOLS) outer level BIC criterion to estimate dimension with eigen-decomposition

Usage

```
sOLS.comp.d(X, sizes)
```

Arguments

X	A matrix containing directions estimated from all subpopulations.
sizes	A vector with the sample sizes of all subpopulation.

Details

This function estimates dimension across the subpopulations using eigen-decomposition. The order of the subpopulations in the "sizes" vector should match the one in the "X" matrix. Also, this function returns the linearly independent directions among all subpopulations.

Value

sOLS.comp.d returns a list containing at least the following components: "d", the dimension estimated across subpopulations; "u", the "d" linearly independent directions among the matrix X.

References

Liu, Y., Chiaromonte, F., and Li, B. (2015). Structured Ordinary Least Squares: a sufficient dimension reduction approach for regressions with partitioned predictors and heterogeneous units. Submitted.

Examples

```
v1 <- c(1, 1, 0, 0)
v2 <- c(0, 1, 1, 0)
v3 <- c(0, 0, 1, 1)
v4 <- c(1, 1, 1, 1)
m1 <- cbind(v1, v2)
sizes1 <- c(100, 200)
sOLS.comp.d(m1, sizes1)
m2 <- cbind(v1, v2, v3)
sizes2 <- c(100, 200, 500)
sOLS.comp.d(m2, sizes2)
m3 <- cbind(v1, v3, v4)
sizes3 <- c(100, 500, 1000)
sOLS.comp.d(m3, sizes3)
```

`standmat`*Matrix standardization*

Description

Matrix standardization

Usage

```
standmat(x)
```

Arguments

`x` A $n \times p$ matrix of n observations and p predictors.

Details

This function standardizes a matrix treating each row as a random vector in an iid sample. It returns a $n \times p$ matrix with column-mean zero and identity-covariance matrix.

Value

A $n \times p$ matrix of n observations and p predictors.

Examples

```
data <- gen.data(n=100)
x.std <- standmat(data$X)
```

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