

# Package ‘rstpm2’

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**Type** Package

**Title** Smooth Survival Models, Including Generalized Survival Models

**Version** 1.5.1

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**Depends** R (>= 3.0.2), methods, survival, splines

**Imports** graphics, Rcpp (>= 0.10.2), stats, mgcv, bbmle (>= 1.0.20), fastGHQuad, deSolve, utils, parallel

**Suggests** eha, testthat, ggplot2, lattice, readstata13, mstate

**LinkingTo** Rcpp, RcppArmadillo

**Maintainer** Mark Clements <mark.clements@ki.se>

**Description** R implementation of generalized survival models (GSMs), smooth accelerated failure time (AFT) models and Markov multi-state models. For the GSMs,  $g(S(t|x)) = \eta(t, x)$  for a link function  $g$ , survival  $S$  at time  $t$  with covariates  $x$  and a linear predictor  $\eta(t, x)$ . The main assumption is that the time effects are smooth <doi:10.1177/0962280216664760>. For fully parametric models with natural splines, this re-implements Stata's 'stpm2' function, which are flexible parametric survival models developed by Royston and colleagues. We have extended the parametric models to include any smooth parametric smoothers for time. We have also extended the model to include any smooth penalized smoothers from the 'mgcv' package, using penalized likelihood. These models include left truncation, right censoring, interval censoring, gamma frailties and normal random effects <doi:10.1002/sim.7451>. For the smooth AFTs,  $S(t|x) = S_0(t * \eta(t, x))$ , where the baseline survival function  $S_0(t) = \exp(-\exp(\eta_0(t)))$  is modelled for natural splines for  $\eta_0$ , and the time-dependent cumulative acceleration factor  $\eta(t, x) = \int_0^t \exp(\eta_1(u, x)) du$  for log acceleration factor  $\eta_1(u, x)$ . The Markov multi-state models allow for a range of models with smooth transitions to predict transition probabilities, length of stay, utilities and costs, with differences, ratios and standardisation.

**URL** <http://github.com/mclements/rstpm2>

**BugReports** <http://github.com/mclements/rstpm2/issues>

**License** GPL-2 | GPL-3

**LazyData** yes

**NeedsCompilation** yes

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Rstpm2-package      *Flexible parametric survival models.*

---

## Description

The package implements the stpm2 models from Stata. Such models use a flexible parametric formulation for survival models, using natural splines to model the log-cumulative hazard. Model predictions are rich, allowing for direct estimation of the hazard, survival, hazard ratios, hazard differences and survival differences. The models allow for time-varying effects, left truncation and relative survival.

The R implementation departs from the Stata implementation, using the ns() function, which is based on a projection of B-splines, rather than using truncated power splines as per Stata.

## Details

Package: Rstpm2  
Type: Package  
Version: 1.0  
Date: 2011-07-06  
License: GPL-2  
LazyLoad: yes  
Depends: methods, bbmle  
Imports: splines, survival, stats, graphics

The package exports the [stpm2](#) object, which inherits from the [mle2](#) object from the [bbmle](#) package. Methods are specified for the [stpm2](#) object, including predict and plot methods.

## Author(s)

Mark Clements and Paul Lambert.

Maintainer: <mark.clements@ki.se>

## See Also

[stpm2](#)

## Examples

```
data(brcancer)
summary(fit <- stpm2(Surv(rectime,censrec==1)~hormon,data=brcancer,df=3))
summary(fit.tvc <- stpm2(Surv(rectime,censrec==1)~hormon,data=brcancer,df=3,
                        tvc=list(hormon=3)))
anova(fit,fit.tvc)
plot(fit.tvc,newdata=data.frame(hormon=0),type="hr",var="hormon")
```

aft

*Parametric accelerated failure time model with smooth time functions***Description**

This implements the accelerated failure time models  $S_0(t \exp(\beta x))$  and  $S_0(\int_0^t \exp(\beta x(u)) du)$ . The baseline function  $S_0(t^*)$  is modelled as  $\exp(-\exp(\eta_0(\log(t^*))))$ , where  $\eta_0(\log(t^*))$  is a linear predictor using natural splines.

**Usage**

```
aft(formula, data, smooth.formula = NULL, df = 3,
    tvc = NULL, control = list(parscale = 1, maxit = 1000),
    init = NULL, weights = NULL, timeVar = "", time0Var = "",
    log.time.transform = TRUE,
    reltol = 1e-08, trace = 0, contrasts = NULL, subset = NULL,
    use.gr = TRUE, ...)
```

**Arguments**

formula	a formula object, with the response on the left of a ~ operator, and the regression terms (excluding time) on the right. The response should be a survival object as returned by the <a href="#">Surv</a> function. The terms can include linear effects for any time-varying coefficients. [required]
data	a data-frame in which to interpret the variables named in the formula argument. [at present: required]
smooth.formula	a formula for describing the time effects for the linear predictor, excluding the baseline $S_0(t^*)$ , but including time-dependent acceleration factors. The time-dependent acceleration factors can be modelled with any smooth functions.
df	an integer that describes the degrees of freedom for the ns function for modelling the baseline log-cumulative hazards function (default=3).
tvc	a list with the names of the time-varying coefficients. This uses natural splines (e.g. <code>tvc=list(hormon=3)</code> is equivalent to <code>smooth.formula=~...+hormon:nsx(log(time),df=3)</code> ), which by default does <i>not</i> include an intercept (or main effect) term.
control	control argument passed to <code>optim</code> .
init	init should either be FALSE, such that initial values will be determined using Cox regression, or a numeric vector of initial values.
weights	an optional vector of 'prior weights' to be used in the fitting process. Should be NULL or a numeric vector.
timeVar	string variable defining the time variable. By default, this is determined from the survival object, however this may be ambiguous if two variables define the time.
time0Var	string variable to determine the entry variable; useful for when more than one data variable is used in the entry time.

<code>log.time.transform</code>	logical for whether to log-transform time when calculating the design matrix for the derivative of <code>S_0</code> with respect to time.
<code>reltol</code>	relative tolerance for the model convergence
<code>trace</code>	integer for whether to provide trace information from the optim procedure
<code>contrasts</code>	an optional list. See the <code>contrasts.arg</code> of <code>model.matrix.default</code> .
<code>subset</code>	an optional vector specifying a subset of observations to be used in the fitting process.
<code>use.gr</code>	logical indicating whether to use gradients in the calculation
<code>...</code>	additional arguments to be passed to the <code>mle2</code> .

### Details

The implementation extends the `mle2` object from the `bbmle` package. The model inherits all of the methods from the `mle2` class.

### Value

An `stpm2`-class object that inherits from `mle2`-class.

### Author(s)

Mark Clements.

### See Also

[survreg](#), [coxph](#)

### Examples

```
summary(aft(Surv(rectime,censrec==1)~hormon,data=brcancer,df=4))
```

---

aft-class	<i>Class "stpm2" ~~~</i>
-----------	--------------------------

---

### Description

Regression object for aft.

### Objects from the Class

Objects can be created by calls of the form `new("aft", ...)` and `aft(...)`.

### Slots

`args`: Object of class "list" ~~

**Extends**

Class "mle2", directly.

**Methods**

**plot** signature(x = "aft", y = "missing"): ...

**predict** signature(object = "aft"): ...

**predictnl** signature(object = "aft", ...): ...

**Examples**

```
showClass("aft")
```

---

brcancer

*German breast cancer data from Stata.*

---

**Description**

See <http://www.stata-press.com/data/r11/brcancer.dta>.

**Usage**

```
data(brcancer)
```

**Format**

A data frame with 686 observations on the following 15 variables.

id a numeric vector

hormon hormonal therapy

x1 age, years

x2 menopausal status

x3 tumour size, mm

x4 tumour grade

x5 number of positive nodes

x6 progesterone receptor, fmol

x7 estrogen receptor, fmol

rectime recurrence free survival time, days

censrec censoring indicator

x4a tumour grade $\geq$ 2

x4b tumour grade $\leq$ 3

x5e  $\exp(-0.12 \cdot x5)$

**Examples**

```
data(brcancer)
## maybe str(brcancer) ; plot(brcancer) ...
```

---

coef<-                                    *Generic method to update the coef in an object.*

---

**Description**

Generic method to update the coef in an object.

**Usage**

```
coef(x) <- value
```

**Arguments**

x	object to be updated
value	value of the coefficient to be updated.

**Details**

This simple generic method is used for the numerical delta method.

**Value**

The updated object is returned.

**Examples**

```
##---- Should be DIRECTLY executable !! ----
##-- ==> Define data, use random,
##--or do help(data=index) for the standard data sets.

## The function is currently defined as
function (x, value)
UseMethod("coef<-")
```

---

colon	<i>Colon cancer.</i>
-------	----------------------

---

**Description**

Diagnoses of colon cancer.

**Usage**

```
data(colon)
```

**Format**

A data frame with 15564 observations on the following 13 variables.

sex Sex (1=male, 2=female))

age Age at diagnosis

stage Clinical stage at diagnosis (1=Unknown, 2=Localised, 3=Regional, 4=Distant)

mmdx Month of diagnosis

yydx Year of diagnosis

surv\_mm Survival time in months

surv\_yy Survival time in years

status Vital status at last contact (1=Alive, 2=Dead: cancer, 3=Dead; other, 4=Lost to follow-up)

subsite Anatomical subsite of tumour (1=Coecum and ascending, 2=Transverse, 3=Descending and sigmoid, 4=Other and NOS)

year8594 Year of diagnosis (1=Diagnosed 75-84, 2=Diagnosed 85-94)

agegrp Age in 4 categories (1=0-44, 2=45-59, 3=60-74, 4=75+)

dx Date of diagnosis

exit Date of exit

**Details**

Caution: there is a colon dataset in the survival package. We recommend using `data(colon, package="rstm2")` to ensure the correct dataset is used.

**Examples**

```
data(colon, package="rstm2") # avoids name conflict with survival::colon
## maybe str(colon) ; ...
```



---

`cox.tvc`*Test for a time-varying effect in the coxph model*

---

## Description

Test for a time-varying effect in the coxph model by re-fitting the partial likelihood including a time-varying effect, plot the effect size, and return the re-fitted model. The main advantage of this function over the `tt()` special is that it scales well for moderate sized datasets (cf. `tt` which expands the dataset and scales very poorly).

## Usage

```
cox.tvc(obj, var=NULL, method="logt")
```

## Arguments

<code>obj</code>	A coxph object. Currently restricted to right censoring with Breslow ties and without stratification, etc.
<code>var</code>	String for the effect name. Currently assumes simple continuous effects.
<code>method</code>	A string representing the possible time transformations. Currently only "logt".

## Value

Returns a `tvcCoxph` object (which inherits from the `mle2` class) of the re-fitted model.

## See Also

[coxph](#), [cox.zph](#)

## Examples

```
## As per the example for cox.zph:
fit <- coxph(Surv(futime, fustat) ~ age + ecog.ps,
             data=ovarian)
temp <- rstpm2::cox.tvc(fit, "age")
print(temp)           # display the results
plot(temp)           # plot curves
```

---

eform.stpm2	<i>S3 method for to provide exponentiated coefficients with confidence intervals.</i>
-------------	---

---

**Description**

S3 method for to provide exponentiated coefficients with confidence intervals.

**Usage**

```
eform(object, ...)
## S3 method for class 'stpm2'
eform(object, parm, level = 0.95, method = c("Profile"), name = "exp(beta)")
```

**Arguments**

object	regression object
parm	not currently used
level	significance level for the confidence interval
method	Currently only the profile method is available.
name	name for the fitted value
...	other arguments

---

grad	<i>gradient function (internal function)</i>
------	--

---

**Description**

Numerical gradient for a function at a given value (internal).

**Usage**

```
grad(func, x, ...)
```

**Arguments**

func	Function taking a vector argument x (returns a vector of length>=1)
x	vector of arguments for where the gradient is wanted.
...	other arguments to the function

**Details**

$(\text{func}(x+\text{delta}, \dots) - \text{func}(x-\text{delta}, \dots)) / (2 \text{ delta})$  where delta is the third root of the machine precision times  $\text{pmax}(1, \text{abs}(x))$ .

**Value**

A vector if `func(x)` has length 1, otherwise a matrix with rows for `x` and columns for `func(x)`.

**Author(s)**

Mark Clements.

**See Also**

`numDelta()`

---

gsm

*Parametric and penalised generalised survival models*

---

**Description**

This implements the generalised survival model  $g(S(t|x)) = \eta$ , where  $g$  is a link function,  $S$  is survival,  $t$  is time,  $x$  are covariates and  $\eta$  is a linear predictor. The linear predictor can include either parametric or penalised smoothers for the time effects, for time:covariate interactions and for covariate effects. The main model assumption is that the time effects in the linear predictor are smooth. This extends the class of flexible parametric survival models developed by Royston and colleagues. The model has been extended to include relative survival (excess hazards), Gamma frailties and normal random effects.

**Usage**

```
gsm(formula, data, smooth.formula = NULL, smooth.args = NULL,
     df = 3, cure = FALSE,
     tvc = NULL, tvc.formula = NULL,
     control = list(), init = NULL,
     weights = NULL, robust = FALSE, baseoff = FALSE,
     timeVar = "", time0Var = "", use.gr = NULL,
     optimiser=NULL, log.time.transform=TRUE,
     reltol=NULL, trace = NULL,
     link.type=c("PH","PO","probit","AH","AO"), theta.A0=0,
     contrasts = NULL, subset = NULL,
     robust_initial=NULL,
     coxph.strata = NULL, coxph.formula = NULL,
     logH.formula = NULL, logH.args = NULL,
     bhazard = NULL, bhazinit=NULL,
     frailty = !is.null(cluster) & !robust, cluster = NULL, logtheta=NULL,
     nodes=NULL, RandDist=c("Gamma","LogN"), recurrent = FALSE,
     adaptive = NULL, maxkappa = NULL,
     sp=NULL, criterion=NULL, penalty=NULL,
     smoother.parameters=NULL, Z=~1, outer_optim=NULL,
     alpha=1, sp.init=1,
     penalised=FALSE,
```

```

    ... )
  stpm2(formula, data, weights=NULL, subset=NULL, coxph.strata=NULL, ...)
  pstpm2(formula, data, weights=NULL, subset=NULL, coxph.strata=NULL, ...)

```

### Arguments

formula	a formula object, with the response on the left of a <code>~</code> operator, and the parametric terms on the right. The response must be a survival object as returned by the <a href="#">Surv</a> function. Specials include <code>cluster</code> and <code>bhazard</code> . [required]
data	a <code>data.frame</code> in which to interpret the variables named in the <code>formula</code> argument.
smooth.formula	either a parametric formula or a penalised <code>mgcv : : gam</code> formula for describing the time effects and time-dependent effects and smoothed covariate effects on the linear predictor scale (default=NULL). The default model is equal to <code>~s(log(time),k=-1)</code> where <code>time</code> is the time variable.
df	an integer that describes the degrees of freedom for the <code>ns</code> function for modelling the baseline log-cumulative hazard (default=3). Parametric model only.
smooth.args	a list describing the arguments for the <code>s</code> function for modelling the baseline time effect on the linear predictor scale (default=NULL).
tvc	a list with the names of the time-varying coefficients. For a parametric model, this uses natural splines (e.g. <code>tvc=list(hormon=3)</code> is equivalent to <code>smooth.formula=~...+hormon:nsx</code> which by default does <i>not</i> include an intercept (or main effect) term. For a penalised model, this uses cubic splines (e.g. <code>tvc=list(hormon=-1)</code> is equivalent to <code>smooth.formula=~...+s(log(time),by=hormon,k=-1)</code> ), which by default <i>does</i> include an intercept (or main effect) term (and this code will remove any main effect from formula).
tvc.formula	separate formula for the time-varying effects. This is combined with <code>smooth.formula</code> or the default <code>smooth.formula</code> .
baseoff	Boolean used to determine whether fully define the model using <code>tvc.formula</code> rather than combining <code>logH.formula</code> and <code>tvc.formula</code>
logH.args	as per <code>smooth.args</code> . Deprecated.
logH.formula	as per <code>smooth.formula</code> . Deprecated.
cure	logical for whether to estimate a cure model (parametric model only).
control	list of arguments passed to <code>gsm.control</code> .
init	<code>init</code> should either be NULL, such that initial values will be determined using Cox regression, or a numeric vector of initial values.
coxph.strata	variable in the <code>data</code> argument for stratification of the <code>coxph</code> model fit for estimating initial values.
weights	an optional vector of 'prior weights' to be used in the fitting process. Should be NULL or a numeric vector.
robust	Boolean used to determine whether to use a robust variance estimator.
bhazard	variable for the baseline hazard for relative survival
bhazinit	scalar used to adjust the background cumulative hazards for calculating initial values. Default=0.1. Deprecated argument: use of the <code>control</code> argument is preferred.

timeVar	variable defining the time variable. By default, this is determined from the survival object, however this may be ambiguous if two variables define the time
sp	fix the value of the smoothing parameters.
use.gr	in R, a Boolean to determine whether to use the gradient in the optimisation. Default=TRUE, Deprecated argument: use of the control argument is preferred.
criterion	in Rcpp, determine whether to use "GCV" or "BIC" for for the smoothing parameter selection.
penalty	use either the "logH" penalty, which is the default penalty from mgcv, or the "h" hazard penalty. Default="logH". Deprecated argument: use of the control argument is preferred.
smoother.parameters	for the hazard penalty, a list with components which are lists with components var, transform and inverse.
alpha	an ad hoc tuning parameter for the smoothing parameter.
sp.init	initial values for the smoothing parameters.
trace	integer for trace reporting; 0 represents no additional reporting. Default=0. Deprecated argument: use of the control argument is preferred.
contrasts	an optional list. See the contrasts.arg of <a href="#">model.matrix.default</a> .
subset	an optional vector specifying a subset of observations to be used in the fitting process.
coxph.formula	additional formula used to improve the fitting of initial values [optional and rarely used].
time0Var	string variable to determine the entry variable; useful for when more than one data variable is used in the entry time.
link.type	type of link function. For "PH" (generalised proportional hazards), $g(S)=\log(-\log(S))$ ; for "PO" (generalised proportional odds), $g(S)=-\text{logit}(S)$ ; for "probit" (generalised probit), $g(S)=-\text{probit}(S)$ ; for "AH" (generalised additive hazards), $g(S)=-\log(S)$ ; for "AO" (generalised Aranda-Ordaz), $g(S)=\log((S^{-(\text{theta.AO})}-1)/\text{theta.AO})$ .
theta.AO	theta parameter for the Aranda-Ordaz link type.
optimiser	select which optimiser is used. Default="BFGS". Deprecated argument: use of the control argument is preferred.
log.time.transform	should a log-transformation be used for calculating the derivative of the design matrix with respect to time? (default=TRUE)
recurrent	logical for whether clustered, left truncated data are recurrent or for first event (where the latter requires an adjustment for the frailties or random effects)
frailty	logical for whether to fit a shared frailty model
cluster	variable that determines the cluster for the frailty. This can be a vector, a string for the column, or a name. This can also be specified using a special.
logtheta	initial value for log-theta used in the gamma shared frailty model (defaults to value from a coxph model fit)

nodes	number of integration points for Gaussian quadrature. Default=9. Deprecated argument: use of the control argument is preferred.
RandDist	type of distribution for the random effect or frailty
adaptive	logical for whether to use adaptive or non-adaptive quadrature, Default=TRUE. Deprecated argument: use of the control argument is preferred.
maxkappa	double float value for the maximum value of the weight used in the constraint. Default=1000. Deprecated argument: use of the control argument is preferred.
Z	formula for the design matrix for the random effects
reltol	list with components for search and final relative tolerances. Default=list(search=1e-10, final=1e-10, outer=1e-5). Deprecated argument: use of the control argument with arguments reltol.search, reltol.final and reltol.outer is preferred.
outer_optim	Integer to indicate the algorithm for outer optimisation. If outer_optim=1 (default), then use Nelder-Mead, otherwise use Nlm.
robust_initial	logical for whether to use Nelder-Mead to find initial values (max 50 iterations). This is useful for ill-posed initial values. Default= FALSE. Deprecated argument: use of the control argument is preferred.
penalised	logical to show whether to use penalised models with pstpm (penalised=TRUE) or parametrics models with stpm2 (penalised=FALSE).
...	additional arguments to be passed to the <code>mle2</code> .

## Details

The implementation extends the `mle2` object from the `bbmle` package.

The default smoothers for time on the linear predictor scale are `nsxs(log(time),df=3)` for the parametric model and `s(log(time))` for the penalised model.

## Value

Either a `stpm2`-class or `pstpm2`-class object.

## Author(s)

Mark Clements, Xing-Rong Liu.

## Examples

```
## Not run:
data(brcancer)
summary(fit <- stpm2(Surv(rectime,censrec==1)~hormon,data=brcancer,df=3))

## some predictions
head(predict(fit,se.fit=TRUE,type="surv"))
head(predict(fit,se.fit=TRUE,type="hazard"))

## some plots
plot(fit,newdata=data.frame(hormon=0),type="hazard")
```

```

plot(fit,newdata=data.frame(hormon=0),type="surv")

## the same model using logH.formula
summary(stpm2(Surv(rectime,censrec==1)~hormon,
              data=brcancer,logH.formula=~ns(log(rectime),df=3)))

## time-varying coefficient
summary(fit.tvc <- stpm2(Surv(rectime,censrec==1)~hormon,data=brcancer,df=3,
                        tvc=list(hormon=3)))
anova(fit,fit.tvc) # compare with and without tvc

## some more plots
plot(fit.tvc,newdata=data.frame(hormon=0),type="hr",var="hormon", ylim=c(0,2))
# no lines method: use add=TRUE
plot(fit.tvc,newdata=data.frame(hormon=1),type="hr",var="hormon",
     add=TRUE,ci=FALSE,line.col=2)

plot(fit.tvc,newdata=data.frame(hormon=0),type="sdiff",var="hormon")

plot(fit.tvc,newdata=data.frame(hormon=0),type="hdiff",var="hormon")

plot(fit.tvc,newdata=data.frame(hormon=0),type="hazard")
plot(fit.tvc,newdata=data.frame(hormon=1),type="hazard",line.col=2,ci=FALSE,add=TRUE)

## compare number of knots
hormon0 <- data.frame(hormon=0)
plot(fit,type="hazard",newdata=hormon0)
AIC(fit)
for (df in 4:6) {
  fit.new <- stpm2(Surv(rectime,censrec==1)~hormon,data=brcancer,df=df)
  plot(fit.new,type="hazard",newdata=hormon0,add=TRUE,ci=FALSE,line.col=df)
  print(AIC(fit.new))
}

## End(Not run)

```

---

incrVar

*Utility that returns a function to increment a variable in a data-frame.*


---

## Description

A functional approach to defining an increment in one or more variables in a data-frame. Given a variable name and an increment value, return a function that takes any data-frame to return a data-frame with incremented values.

## Usage

```
incrVar(var, increment = 1)
```

**Arguments**

var                   String for the name(s) of the variable(s) to be incremented  
 increment            Value that the variable should be incremented.

**Details**

Useful for defining transformations for calculating rate ratios.

**Value**

A function with a single data argument that increments the variables in the data list/data-frame.

**Examples**

```
##---- Should be DIRECTLY executable !! ----
##-- ==> Define data, use random,
##--or do help(data=index) for the standard data sets.

## The function is currently defined as
function (var, increment = 1)
{
  n <- length(var)
  if (n > 1 && length(increment)==1)
    increment <- rep(increment, n)
  function(data) {
    for (i in 1:n) {
      data[[var[i]]] <- data[[var[i]]] + increment[i]
    }
    data
  }
}
```

---

legendre.quadrature.rule.200

*Legendre quadrature rule for n=200.*

---

**Description**

Legendre quadrature rule for n=200.

**Usage**

```
data(legendre.quadrature.rule.200)
```

**Format**

A data frame with 200 observations on the following 2 variables.

x x values between -1 and 1

w weights



**Examples**

```
data(legendre.quadrature.rule.200)
## maybe str(legendre.quadrature.rule.200) ; ...
```

---

lines.stpm2

*S3 methods for lines*


---

**Description**

S3 methods for lines

**Usage**

```
## S3 method for class 'stpm2'
lines(x, newdata = NULL, type = "surv", col = 1, ci.col= "grey",
lty = par("lty"), ci = FALSE, rug = FALSE, var = NULL,
exposed = incrVar(var), times = NULL,
type.relsurv = c("excess", "total", "other"),
ratetable = survival::survexp.us, rmap, scale = 365.24, ...)
## S3 method for class 'pstpm2'
lines(x, newdata = NULL, type = "surv", col = 1,
ci.col= "grey",
lty = par("lty"), ci = FALSE, rug = FALSE, var = NULL,
exposed = incrVar(var), times = NULL, ...)
```

**Arguments**

x	an stpm2 object
newdata	required list of new data. This defines the unexposed newdata ( <i>excluding</i> the event times).
type	specify the type of prediction
col	line colour
lty	line type
ci.col	confidence interval colour
ci	whether to plot the confidence interval band (default=TRUE)
rug	whether to add a rug plot of the event times to the current plot (default=TRUE)
var	specify the variable name or names for the exposed/unexposed (names are given as characters)
exposed	function that takes newdata and returns the exposed dataset. By default, this increments var
times	specifies the times. By default, this uses a span of the observed times.
type.relsurv	type of predictions for relative survival models: either "excess", "total" or "other"

scale	scale to go from the days in the ratetable object to the analysis time used in the analysis
rmap	an optional list that maps data set names to the ratetable names. See survexp
ratetable	a table of event rates used in relative survival when type.relsurv is "total" or "other"
...	additional arguments (add to the plot command)

---

markov_msm	<i>Predictions for continuous time, nonhomogeneous Markov multi-state models using parametric and penalised survival models.</i>
------------	--

---

### Description

A numerically efficient algorithm to calculate predictions from a continuous time, nonhomogeneous Markov multi-state model. The main inputs are the models for the transition intensities, the initial values, the transition matrix and the covariate patterns. The predictions include state occupancy probabilities (possibly with discounting and utilities), length of stay and costs. Standard errors are calculated using the delta method. Includes, differences, ratios and standardisation.

### Usage

```
markov_msm(x, trans, t = c(0,1), newdata = NULL, init=NULL,
           tmvar = NULL,
           sing.inf = 1e+10, method="adams", rtol=1e-10, atol=1e-10, slow=FALSE,
           min.tm=1e-8,
           utility=function(t) rep(1, nrow(trans)),
           utility.sd=rep(0,nrow(trans)),
           use.costs=FALSE,
           transition.costs=function(t) rep(0, sum(!is.na(trans))), # per transition
           transition.costs.sd=rep(0,sum(!is.na(trans))),
           state.costs=function(t) rep(0,nrow(trans)), # per unit time
           state.costs.sd=rep(0,nrow(trans)),
           discount.rate = 0,
           block.size=500,
           debug=FALSE,
           ...)
## S3 method for class 'markov_msm'
vcov(object, ...)
## S3 method for class 'markov_msm'
as.data.frame(x, row.names=NULL, optional=FALSE,
              ci=TRUE,
              P.conf.type="logit", L.conf.type="log",
              C.conf.type="log",
              P.range=c(0,1), L.range=c(0,Inf),
              C.range=c(0,Inf),
              ...)
```

```

## S3 method for class 'markov_msm_diff'
as.data.frame(x, row.names=NULL, optional=FALSE,
              P.conf.type="plain", L.conf.type="plain",
              C.conf.type="plain",
              P.range=c(-Inf,Inf), L.range=c(-Inf,Inf),
              C.range=c(-Inf,Inf),
              ...)
## S3 method for class 'markov_msm_ratio'
as.data.frame(x, row.names=NULL, optional=FALSE, ...)
standardise(x, ...)
## S3 method for class 'markov_msm'
standardise(x,
            weights = rep(1,nrow(x$newdata)),
            normalise = TRUE, ...)
## S3 method for class 'markov_msm'
plot(x, y, stacked=TRUE, which=c('P','L'),
     xlab="Time", ylab=NULL, col=2:6, border=col,
     ggplot2=FALSE, lattice=FALSE, alpha=0.2,
     strata=NULL,
     ...)
## S3 method for class 'markov_msm'
subset(x, subset, ...)
## S3 method for class 'markov_msm'
diff(x, y, ...)
ratio_markov_msm(x, y, ...)
## S3 method for class 'markov_msm'
rbind(..., deparse.level=1)
## S3 method for class 'markov_msm'
transform(`_data`, ...)
collapse_markov_msm(object, which=NULL, sep="; ")
zeroModel(object)
hrModel(object,hr=1,ci=NULL,seloghr=NULL)
aftModel(object,af=1,ci=NULL,selogaf=NULL)
addModel(...)
hazFun(f, tmvar="t", ...)
splineFun(time,rate,method="natural",scale=1,...)

```

## Arguments

For `markov_msm`:

list of functions or parametric or penalised survival models. Currently the models include combinations of `stpm2`, `pstpm2`, `glm`, `gam`, `survPen` or an object of class "zeroModel" from `zeroModel` based on one of the other classes. The order in the list matches the indexing in the `trans` argument. The functions can optionally use a `t` argument for time and/or a `newdata` argument. Uncertainty in the models are incorporated into the gradients, while uncertainty in the functions are currently not modelled.

**xtrans** Transition matrix describing the states and transitions in the multi-state model.

If  $S$  is the number of states in the multi-state model, `trans` should be an  $S \times S$  matrix, with (i,j)-element a positive integer if a transition from  $i$  to  $j$  is possible in the multi-state model, NA otherwise. In particular, all diagonal elements should be NA. The integers indicating the possible transitions in the multi-state model should be sequentially numbered,  $1, \dots, K$ , with  $K$  the number of transitions. See [msprep](#)

<code>t</code>	numerical vector for the times to evaluation the predictions. Includes the start time
<code>newdata</code>	<a href="#">data.frame</a> of the covariates to use in the predictions
<code>init</code>	vector of the initial values with the same length as the number of states. Defaults to the first state having an initial value of 1 (i.e. " <code>[&lt;-</code> "( <code>rep(0, nrow(trans))</code> ), 1, 1)).
<code>tmvar</code>	specifies the name of the time variable. This should be set for regression models that do not specify this (e.g. <a href="#">glm</a> ) or where the time variable is ambiguous
<code>sing.inf</code>	If there is a singularity in the observed hazard, for example a Weibull distribution with $\text{shape} < 1$ has infinite hazard at $t=0$ , then as a workaround, the hazard is assumed to be a large finite number, <code>sing.inf</code> , at this time. The results should not be sensitive to the exact value assumed, but users should make sure by adjusting this parameter in these cases.
<code>method</code>	For <code>markov_msm</code> , the method used by the ordinary differential equation solver. Defaults to Adams method (" <code>adams</code> ") for non-stiff differential equations. For <code>splineFun</code> , the method used for spline interpolation; see <code>splinefun</code> .
<code>rtol</code>	relative error tolerance, either a scalar or an array as long as the number of states. Passed to <a href="#">lsode</a>
<code>atol</code>	absolute error tolerance, either a scalar or an array as long as the number of states. Passed to <a href="#">lsode</a>
<code>slow</code>	logical to show whether to use the slow R-only implementation. Useful for debugging. Currently needed for costs.
<code>min.tm</code>	Minimum time used for evaluations. Avoids <code>log(0)</code> for some models.
<code>utility</code>	a function of the form <code>function(t)</code> that returns a utility for each state at time $t$ for the length of stay values
<code>utility.sd</code>	a function of the form <code>function(t)</code> that returns the standard deviation for the utility for each state at time $t$ for the length of stay values
<code>use.costs</code>	logical for whether to use costs. Default: FALSE
<code>transition.costs</code>	a function of the form <code>function(t)</code> that returns the cost for each transition
<code>transition.costs.sd</code>	a function of the form <code>function(t)</code> that returns the standard deviation for the cost for each transition
<code>state.costs</code>	a function of the form <code>function(t)</code> that returns the cost per unit time for each state
<code>state.costs.sd</code>	a function of the form <code>function(t)</code> that returns the standard deviation for the cost per unit time for each state
<code>discount.rate</code>	numerical value for the proportional reduction (per unit time) in the length of stay and costs

block.size	divide newdata into blocks. Uses less memory but is slower. Reduce this number if the function call runs out of memory.
debug	logical flag for whether to keep the full output from the ordinary differential equation in the res component (default=FALSE).
...	other arguments. For markov_msm, these are passed to the <code>ode</code> solver from the <code>deSolve</code> package. For <code>plot.markov_msm</code> , these arguments are passed to <code>plot.default</code> For <code>as.data.frame.markov_msm</code> :
row.names	add in row names to the output data-frame
optional	(not currently used)
ci	logical for whether to include confidence intervals. Default: TRUE
P.conf.type	type of transformation for the confidence interval calculation for the state occupancy probabilities. Default: log-log transformation. This is changed for <code>diff</code> and <code>ratio_markov_msm</code> objects
L.conf.type	type of transformation for the confidence interval calculation for the length of stay calculation. Default: log transformation. This is changed for <code>diff</code> and <code>ratio_markov_msm</code> objects
C.conf.type	type of transformation for the confidence interval calculation for the length of stay calculation. Default: log transformation. This is changed for <code>diff</code> and <code>ratio_markov_msm</code> objects
P.range	valid values for the state occupancy probabilities. Default: (0,1). This is changed for <code>diff</code> and <code>ratio_markov_msm</code> objects
L.range	valid values for the state occupancy probabilities. Default: (0,Inf). This is changed for <code>diff</code> and <code>ratio_markov_msm</code> objects
C.range	valid values for the state occupancy probabilities. Default: (0,Inf). This is changed for <code>diff</code> and <code>ratio_markov_msm</code> objects For <code>standardise.markov_msm</code> :
weights	numerical vector to use in standardising the state occupancy probabilities, length of stay and costs. Default: 1 for each observation.
normalise	logical for whether to normalise the weights to 1. Default: TRUE For <code>plot.markov_msm</code> :
y	(currently ignored)
stacked	logical for whether to stack the plots. Default: TRUE
xlab	x-axis label
ylab	x-axis label
col	colours (ignored if <code>ggplot2=TRUE</code> )
border	border colours for the <code>polygon</code> (ignored if <code>ggplot=TRUE</code> )
ggplot2	use <code>ggplot2</code>
alpha	alpha value for confidence bands ( <code>ggplot</code> )
lattice	use <code>lattice</code>

<code>strata</code>	formula for the stratification factors for the plot For <code>subset.markov_msm</code> :
<code>subset</code>	expression that is evaluated on the <code>newdata</code> component of the object to filter (or restrict) for the covariates used for predictions For <code>transform.markov_msm</code> :
<code>_data</code>	an object of class "markov_msm" For <code>rbind.markov_msm</code> :
<code>deparse.level</code>	not currently used For <code>collapse.states</code> :
<code>which</code>	either an index of the states to collapse or a character vector of the state names to collapse
<code>sep</code>	separator to use for the collapsed state names For <code>zeroModel</code> to predict zero rates:
<code>object</code>	survival regression object to be wrapped For <code>hrModel</code> to predict rates times a hazard ratio:
<code>hr</code>	hazard ratio
<code>seloghr</code>	alternative specification for the se of the log(hazard ratio); see also <code>ci</code> argument For <code>aftModel</code> to predict accelerated rates:
<code>af</code>	acceleration factor
<code>selogaf</code>	alternative specification for the se of the log(acceleration factor); see also <code>ci</code> argument <code>addModel</code> predict rates based on adding rates from different models <code>hazFun</code> provides a rate function without uncertainty:
<code>f</code>	rate function, possibly with <code>tmvar</code> and/or <code>newdata</code> as arguments <code>splineFun</code> predicts rates using spline interpolation:
<code>time</code>	exact times
<code>rate</code>	rates as per time
<code>scale</code>	rate multiplier (e.g. <code>scale=365.25</code> for converting from daily rates to yearly rates)

## Details

The predictions are calculated using an ordinary differential equation solver. The algorithm uses a single run of the solver to calculate the state occupancy probabilities, length of stay, costs and their partial derivatives with respect to the model parameters. The predictions can also be combined to calculate differences, ratios and standardised.

The current implementation supports a list of models for each transition.

The current implementation also only allows for a vector of initial values rather than a matrix. The predictions will need to be re-run for different vectors of initial values.

For `as.data.frame.markov_msm_ratio`, the data are provided in log form, hence the default transformations and bounds are as per `as.data.frame.markov_msm_diff`, with untransformed data on the real line.

TODO: allow for one model to predict for the different transitions.

**Value**

markov\_msm returns an object of class "markov\_msm".

The function summary is used to obtain and print a summary and analysis of variance table of the results. The generic accessor functions coef and vcov extract various useful features of the value returned by markov\_msm.

An object of class "markov\_msm" is a list containing at least the following components:

time	a numeric vector with the times for the predictions
P	an <a href="#">array</a> for the predicted state occupancy probabilities. The array has three dimensions: time, state, and observations.
L	an <a href="#">array</a> for the predicted sojourn times (or length of stay). The array has three dimensions: time, state, and observations.
Pu	an <a href="#">array</a> for the partial derivatives of the predicted state occupancy probabilities with respect to the model coefficients. The array has four dimensions: time, state, coefficients, and observations.
Lu	an <a href="#">array</a> for the partial derivatives of the predicted sojourn times (or length of stay) with respect to the model coefficients. The array has four dimensions: time, state, coefficients, and observations.
newdata	a <a href="#">data.frame</a> with the covariates used for the predictions
vcov	the variance-covariance matrix for the models of the transition intensities
trans	copy of the trans input argument
call	the call to the function
For debugging:	
res	data returned from the ordinary differential equation solver. This may include more information on the predictions

**Author(s)**

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**See Also**

[pmatrix.fs](#), [probtrans](#)

**Examples**

```
## Not run:
## Crowther and Lambert (2019)
library(readstata13)
library(mstate)
library(ggplot2)
mex.1 <- read.dta13("http://fmwww.bc.edu/repec/bocode/m/multistate_example.dta")
transmat <- rbind("Post-surgery"=c(NA,1,2),
                 "Relapsed"=c(NA,NA,3),
                 "Died"=c(NA,NA,NA))
```

```

colnames(transmat) <- rownames(transmat)
mex.2 <- transform(mex.1,osi=(osi=="deceased")+0)
levels(mex.2$size)[2] <- ">20-50 mm" # fix typo
mex <- mstate::msprep(time=c(NA,"rf","os"),status=c(NA,"rfi","osi"),
                      data=mex.2,trans=transmat,id="pid",
                      keep=c("age","size","nodes","pr_1","hormon"))
mex <- transform(mex,
                 size2=(unclass(size)==2)+0, # avoids issues with TRUE/FALSE
                 size3=(unclass(size)==3)+0,
                 hormon=(hormon=="yes")+0,
                 Tstart=Tstart/12,
                 Tstop=Tstop/12)

##
c.ar <- stpm2(Surv(Tstart,Tstop,status) ~ age + size2 + size3 + nodes + pr_1 + hormon,
              data = mex, subset=trans==1, df=3, tvc=list(size2=1,size3=1,pr_1=1))
c.ad <- stpm2(Surv(Tstart, Tstop, status) ~ age + size + nodes + pr_1 + hormon,
              data = mex, subset=trans==2, df=1)
c.rd <- stpm2( Surv(Tstart,Tstop,status) ~ age + size + nodes + pr_1 + hormon,
              data=mex, subset=trans==3, df=3, tvc=list(pr_1=1))

##
nd <- expand.grid(nodes=seq(0,20,10), size=levels(mex$size))
nd <- transform(nd, age=54, pr_1=3, hormon=0,
                size2=(unclass(size)==2)+0,
                size3=(unclass(size)==3)+0)

## Predictions
system.time(pred1 <- rstpm2::markov_msm(list(c.ar,c.ad,c.rd), t = seq(0,15,length=301),
                                          newdata=nd, trans = transmat)) # ~15 seconds
pred1 <- transform(pred1, Nodes=paste("Nodes =",nodes), Size=paste("Size",size))
## Figure 3
plot(pred1, ggplot=TRUE) + facet_grid(Nodes ~ Size) + xlab("Years since surgery")
plot(pred1, strata=~nodes+size, xlab="Years since surgery", lattice=TRUE)
## Figure 4
plot(subset(pred1, nodes==0 & size=="<=20 mm"), stacked=FALSE, ggplot=TRUE) +
  facet_grid(. ~ state) +
  xlab("Years since surgery")
## Figure 5
a <- diff(subset(pred1,nodes==0 & size=="<=20 mm"),
          subset(pred1,nodes==0 & size==">20-50 mm"))
a <- transform(a, label = "Prob(Size<=20 mm)-Prob(20mm<Size<50mm)")
b <- ratio_markov_msm(subset(pred1,nodes==0 & size=="<=20 mm"),
                      subset(pred1,nodes==0 & size==">20-50 mm"))
b <- transform(b,label="Prob(Size<=20 mm)-Prob(20mm<Size<50mm)")
##
c <- diff(subset(pred1,nodes==0 & size=="<=20 mm"),
          subset(pred1,nodes==0 & size==">50 mm"))
c <- transform(c, label = "Prob(Size<=20 mm)-Prob(Size>=50mm)")
d <- ratio_markov_msm(subset(pred1,nodes==0 & size=="<=20 mm"),
                      subset(pred1,nodes==0 & size==">50 mm"))
d <- transform(d,label= "Prob(Size<=20 mm)-Prob(Size>=50mm)")
##
e <- diff(subset(pred1,nodes==0 & size==">20-50 mm"),
          subset(pred1,nodes==0 & size==">50 mm"))
e <- transform(e,label="Prob(20mm<Size<50 mm)-Prob(Size>=50mm)")

```



```
f <- ratio_markov_msm(subset(pred1,nodes==0 & size==">20-50 mm"),
                      subset(pred1,nodes==0 & size==">50 mm"))
f <- transform(f, label = "Prob(20mm<Size<50 mm)-Prob(Size>=50mm)")
## combine
diffs <- rbind(a,c,e)
ratios <- rbind(b,d,f)
## Figure 5
plot(diffs, stacked=FALSE, ggplot2=TRUE) + xlab("Years since surgery") +
  ylim(c(-0.4, 0.4)) + facet_grid(label ~ state)
##
plot(ratios, stacked=FALSE, ggplot2=TRUE) + xlab("Years since surgery") +
  ylim(c(0, 3)) + facet_grid(label ~ state)
## Figure 6
plot(subset(pred1, nodes==0 & size=="<=20 mm"), stacked=FALSE, which="L", ggplot2=TRUE) +
  facet_grid(. ~ state) + xlab("Years since surgery")
## Figure 7
plot(diffs, stacked=FALSE, which="L", ggplot2=TRUE) + xlab("Years since surgery") +
  ylim(c(-4, 4)) + facet_grid(label ~ state)
plot(ratios, stacked=FALSE, which="L", ggplot2=TRUE) + xlab("Years since surgery") +
  ylim(c(0.1, 10)) + coord_trans(y="log10") + facet_grid(label ~ state)

## End(Not run)
```

---

 nsx

*Generate a Basis Matrix for Natural Cubic Splines (with eXtensions)*


---

## Description

Generate the B-spline basis matrix for a natural cubic spline (with eXtensions).

## Usage

```
nsx(x, df = NULL, knots = NULL, intercept = FALSE,
    Boundary.knots = range(x), derivs = if (cure) c(2, 1) else c(2, 2),
    log = FALSE, centre = FALSE,
    cure = FALSE, stata.stpm2.compatible = FALSE)
```

## Arguments

x	the predictor variable. Missing values are allowed.
df	degrees of freedom. One can supply df rather than knots; ns() then chooses $df - 1 - intercept + 4 - sum(derivs)$ knots at suitably chosen quantiles of x (which will ignore missing values).
knots	breakpoints that define the spline. The default is no knots; together with the natural boundary conditions this results in a basis for linear regression on x. Typical values are the mean or median for one knot, quantiles for more knots. See also Boundary.knots.
intercept	if TRUE, an intercept is included in the basis; default is FALSE.

<code>Boundary.knots</code>	boundary points at which to impose the natural boundary conditions and anchor the B-spline basis (default the range of the data). If both <code>knots</code> and <code>Boundary.knots</code> are supplied, the basis parameters do not depend on <code>x</code> . Data can extend beyond <code>Boundary.knots</code>
<code>derivs</code>	an integer vector of length 2 with values between 0 and 2 giving the derivative constraint order at the left and right boundary knots; an order of 2 constrains the second derivative to zero ( $f''(x)=0$ ); an order of 1 constrains the first and second derivatives to zero ( $f'(x)=f''(x)=0$ ); an order of 0 constrains the zero, first and second derivatives to zero ( $f(x)=f'(x)=f''(x)=0$ )
<code>log</code>	a Boolean indicating whether the underlying values have been log transformed; (deprecated: only used to calculate derivatives in <code>rstpm2:::stpm2Old</code> )
<code>centre</code>	if specified, then centre the splines at this value (i.e. $f(\text{centre})=0$ ) (default=FALSE)
<code>cure</code>	a Boolean indicated whether to estimate cure; changes the default <code>derivs</code> argument, such that the right boundary has the first and second derivatives constrained to zero; defaults to FALSE
<code>stata.stpm2.compatible</code>	a Boolean to determine whether to use Stata <code>stpm</code> 's default knot placement; defaults to FALSE

## Value

A matrix of dimension  $\text{length}(x) * df$  where either `df` was supplied or if `knots` were supplied,  $df = \text{length}(\text{knots}) + 1 + \text{intercept}$ . Attributes are returned that correspond to the arguments to `ns`, and explicitly give the `knots`, `Boundary.knots` etc for use by `predict.nsx()`.

`nsx()` is based on the functions `ns` and `spline.des`. It generates a basis matrix for representing the family of piecewise-cubic splines with the specified sequence of interior knots, and the natural boundary conditions. These enforce the constraint that the function is linear beyond the boundary knots, which can either be supplied, else default to the extremes of the data. A primary use is in modeling formula to directly specify a natural spline term in a model.

The extensions from `ns` are: specification of the derivative constraints at the boundary knots; whether to centre the knots; incorporation of cure using derivatives; compatible knots with Stata's `stpm2`; and an indicator for a log-transformation of `x` for calculating derivatives.

## References

Hastie, T. J. (1992) Generalized additive models. Chapter 7 of *Statistical Models in S* eds J. M. Chambers and T. J. Hastie, Wadsworth & Brooks/Cole.

## See Also

`ns`, `bs`, `predict.nsx`, `SafePrediction`

## Examples

```
require(stats); require(graphics); require(splines)
nsx(women$height, df = 5)
summary(fm1 <- lm(weight ~ ns(height, df = 5), data = women))
```

```
## example of safe prediction
plot(women, xlab = "Height (in)", ylab = "Weight (lb)")
ht <- seq(57, 73, length.out = 200)
lines(ht, predict(fm1, data.frame(height=ht)))
```

---

nsxD	<i>Generate a Basis Matrix for the first derivative of Natural Cubic Splines (with eXtensions)</i>
------	--

---

### Description

Generate the B-spline basis matrix for the first derivative of a natural cubic spline (with eXtensions).

### Usage

```
nsxD(x, df = NULL, knots = NULL, intercept = FALSE,
     Boundary.knots = range(x), derivs = if (cure) c(2, 1) else c(2, 2),
     log = FALSE, centre = FALSE,
     cure = FALSE, stata.stpm2.compatible = FALSE)
```

### Arguments

x	the predictor variable. Missing values are allowed.
df	degrees of freedom. One can supply df rather than knots; ns() then chooses $df - 1 - intercept + 4 - sum(derivs)$ knots at suitably chosen quantiles of x (which will ignore missing values).
knots	breakpoints that define the spline. The default is no knots; together with the natural boundary conditions this results in a basis for linear regression on x. Typical values are the mean or median for one knot, quantiles for more knots. See also Boundary.knots.

<code>intercept</code>	if TRUE, an intercept is included in the basis; default is FALSE.
<code>Boundary.knots</code>	boundary points at which to impose the natural boundary conditions and anchor the B-spline basis (default the range of the data). If both <code>knots</code> and <code>Boundary.knots</code> are supplied, the basis parameters do not depend on <code>x</code> . Data can extend beyond <code>Boundary.knots</code>
<code>derivs</code>	an integer vector of length 2 with values between 0 and 2 giving the derivative constraint order at the left and right boundary knots; an order of 2 constrains the second derivative to zero ( $f''(x)=0$ ); an order of 1 constrains the first and second derivatives to zero ( $f'(x)=f''(x)=0$ ); an order of 0 constrains the zero, first and second derivatives to zero ( $f(x)=f'(x)=f''(x)=0$ )
<code>log</code>	a Boolean indicating whether the underlying values have been log transformed; (deprecated: only used to calculate derivatives in <code>rstpm2:::stpm2Old</code> )
<code>centre</code>	if specified, then centre the splines at this value (i.e. $f(\text{centre})=0$ ) (default=FALSE)
<code>cure</code>	a Boolean indicated whether to estimate cure; changes the default <code>derivs</code> argument, such that the right boundary has the first and second derivatives constrained to zero; defaults to FALSE
<code>stata.stpm2.compatible</code>	a Boolean to determine whether to use Stata <code>stpm</code> 's default knot placement; defaults to FALSE

### Value

A matrix of dimension  $\text{length}(x) * df$  where either `df` was supplied or if `knots` were supplied,  $df = \text{length}(\text{knots}) + 1 + \text{intercept}$ . Attributes are returned that correspond to the arguments to `ns`, and explicitly give the `knots`, `Boundary.knots` etc for use by `predict.nsxD()`.

`nsxD()` is based on the functions `ns` and `spline.des`. It generates a basis matrix for representing the family of piecewise-cubic splines with the specified sequence of interior knots, and the natural boundary conditions. These enforce the constraint that the function is linear beyond the boundary knots, which can either be supplied, else default to the extremes of the data. A primary use is in modeling formula to directly specify a natural spline term in a model.

The extensions from `ns` are: specification of the derivative constraints at the boundary knots; whether to centre the knots; incorporation of cure using derivatives; compatible knots with Stata's `stpm2`; and an indicator for a log-transformation of `x` for calculating derivatives.

### References

Hastie, T. J. (1992) Generalized additive models. Chapter 7 of *Statistical Models in S* eds J. M. Chambers and T. J. Hastie, Wadsworth & Brooks/Cole.

### See Also

`ns`, `bs`, `predict.nsx`, `SafePrediction`

### Examples

```
require(stats); require(graphics); require(splines)
nsx(women$height, df = 5)
```

```
summary(fm1 <- lm(weight ~ ns(height, df = 5), data = women))

## example of safe prediction
plot(women, xlab = "Height (in)", ylab = "Weight (lb)")
ht <- seq(57, 73, length.out = 200)
lines(ht, predict(fm1, data.frame(height=ht)))
```

---

numDeltaMethod                      *Calculate numerical delta method for non-linear predictions.*

---

### Description

Given a regression object and an independent prediction function (as a function of the coefficients), calculate the point estimate and standard errors

### Usage

```
numDeltaMethod(object, fun, gd=NULL, ...)
```

### Arguments

object	A regression object with methods coef and vcov.
fun	An independent prediction function with signature function(coef, ...).
gd	Specified gradients
...	Other arguments passed to fun.

### Details

A more user-friendly interface is provided by predictnl.

**Value**

Estimate	Point estimates
SE	Standard errors

**See Also**

See Also [predictnl](#).

**Examples**

```
##---- Should be DIRECTLY executable !! ----
##-- ==> Define data, use random,
##--or do help(data=index) for the standard data sets.

## The function is currently defined as
function (object, fun, ...)
{
  coef <- coef(object)
  est <- fun(coef, ...)
  Sigma <- vcov(object)
  gd <- grad(fun, coef, ...)
  se.est <- as.vector(sqrt(colSums(gd * (Sigma %*% gd))))
  data.frame(Estimate = est, SE = se.est)
}
```

---

plot-methods

*plots for an stpm2 fit*

---

**Description**

Given an stpm2 fit, return a plot

**Usage**

```
## S4 method for signature 'stpm2'
plot(x,y,newdata,type="surv",
      xlab="Time",line.col=1,ci.col="grey",
      add=FALSE,ci=TRUE,rug=TRUE,
      var=NULL,exposed=incrVar(var),times=NULL,...)
## S4 method for signature 'pstpm2'
plot(x,y,newdata,type="surv",
      xlab="Time",line.col=1,ci.col="grey",
      add=FALSE,ci=TRUE,rug=TRUE,
      var=NULL,exposed=incrVar(var),times=NULL,...)
```

**Arguments**

x	an stpm2 object
y	not used (for generic compatibility)
newdata	required list of new data. This defines the unexposed newdata ( <i>excluding</i> the event times).
type	specify the type of prediction
xlab	x-axis label
line.col	line colour
ci.col	confidence interval colour
ci	whether to plot the confidence interval band (default=TRUE)
add	whether to add to the current plot (add=TRUE) or make a new plot (add=FALSE) (default=FALSE)
rug	whether to add a rug plot of the event times to the current plot (default=TRUE)
var	specify the variable name or names for the exposed/unexposed (names are given as characters)
exposed	function that takes newdata and returns the exposed dataset. By default, this increments var
times	specifies the times. By default, this uses a span of the observed times.
...	additional arguments (add to the plot command)

**Methods**

x = "stpm2", y = "missing" an stpm2 fit

**See Also**

[stpm2](#)

---

popmort

*Background mortality rates for the colon dataset.*

---

**Description**

Background mortality rates for the colon dataset.

**Usage**

data(popmort)

**Format**

A data frame with 10600 observations on the following 5 variables.

sex Sex (1=male, 2=female)  
 prob One year probability of survival  
 rate All cause mortality rate  
 age Age by single year of age through to age 105 years  
 year Calendar period

**Examples**

```
data(popmort)
## maybe str(popmort) ; ...
```

---

predict-methods	<i>Predicted values for an stpm2 or pstpm2 fit</i>
-----------------	--

---

**Description**

Given an stpm2 fit and an optional list of new data, return predictions

**Usage**

```
## S4 method for signature 'stpm2'
predict(object, newdata=NULL,
        type=c("surv", "cumhaz", "hazard", "density", "hr", "sdiff",
              "hdiff", "loghazard", "link", "meansurv", "meansurvdiff", "meanhr",
              "odds", "or", "margsurv", "marghaz", "marghr", "meanhaz", "af",
              "fail", "margfail", "meanmargsurv", "uncured", "rmst", "probcure",
              "lpmatrix", "gradh", "gradH"),
        grid=FALSE, seqLength=300,
        type.relsurv=c("excess", "total", "other"), scale=365.24,
        rmap, ratetable=survival::survexp.us,
        se.fit=FALSE, link=NULL, exposed=incrVar(var), var=NULL,
        keep.attributes=FALSE, use.gr=TRUE, level=0.95,
        n.gauss.quad=100, full=FALSE, ...)

## S4 method for signature 'pstpm2'
predict(object, newdata=NULL,
        type=c("surv", "cumhaz", "hazard", "density", "hr", "sdiff",
              "hdiff", "loghazard", "link", "meansurv", "meansurvdiff", "meanhr",
              "odds", "or", "margsurv", "marghaz", "marghr", "meanhaz", "af",
              "fail", "margfail", "meanmargsurv", "rmst", "lpmatrix",
              "gradh", "gradH"),
        grid=FALSE, seqLength=300,
        se.fit=FALSE, link=NULL, exposed=incrVar(var), var=NULL,
        keep.attributes=FALSE, use.gr=TRUE, level=0.95,
        n.gauss.quad=100, full=FALSE, ...)
```



**Arguments**

object	an stpm2 or pstpm2 object
newdata	optional list of new data (required if type in ("hr","sdiff","hdiff","meansurvdiff","or","uncured")). For type in ("hr","sdiff","hdiff","meansurvdiff","or","af","uncured"), this defines the unexposed newdata. This can be combined with grid to get a regular set of event times (i.e. newdata would <i>not</i> include the event times).
type	specify the type of prediction: <ul style="list-style-type: none"> <li>• "surv"survival probabilities</li> <li>• "cumhaz"cumulative hazard</li> <li>• "hazard"hazard</li> <li>• "density"density</li> <li>• "hr"hazard ratio</li> <li>• "sdiff"survival difference</li> <li>• "hdiff"hazard difference</li> <li>• "loghazard"log hazards</li> <li>• "meansurv"mean survival</li> <li>• "meansurvdiff"mean survival difference</li> <li>• "odds"odds</li> <li>• "or"odds ratio</li> <li>• "margsurv"marginal (population) survival</li> <li>• "marghaz"marginal (population) hazard</li> <li>• "marghr"marginal (population) hazard ratio</li> <li>• "meanhaz"mean hazard</li> <li>• "meanhr"mean hazard ratio</li> <li>• "af"attributable fraction</li> <li>• "fail"failure (=1-survival)</li> <li>• "margfail"marginal failure (=1-marginal survival)</li> <li>• "meanmargsurv"mean marginal survival, averaged over the frailty distribution</li> <li>• "uncured"distribution for the uncured</li> <li>• "rmst"restricted mean survival time</li> <li>• "probcure"probability of cure</li> <li>• "lpmatrix"design matrix</li> </ul>
grid	whether to merge newdata with a regular sequence of event times (default=FALSE)
seqLength	length of the sequence used when grid=TRUE
type.relsurv	type of predictions for relative survival models: either "excess", "total" or "other"
scale	scale to go from the days in the ratetable object to the analysis time used in the analysis
rmap	an optional list that maps data set names to the ratetable names. See survexp
ratetable	a table of event rates used in relative survival when type.relsurv is "total" or "other"

<code>se.fit</code>	whether to calculate confidence intervals (default=FALSE)
<code>link</code>	allows a different link for the confidence interval calculation (default=NULL, such that <code>switch(type,surv="cloglog",cumhaz="log",hazard="log",hr="log",sdiff="I",hdiff="I",loghazard="I",link="I",odds="log",or="log",margSurv="cloglog",marghaz="log",marghr="log")</code> )
<code>exposed</code>	a function that takes <code>newdata</code> and returns a transformed data-frame for those exposed or the counterfactual (defaults to incrementing "var")
<code>var</code>	specify the variable name or names for the exposed/unexposed (names are given as characters)
<code>keep.attributes</code>	Boolean to determine whether the output should include the <code>newdata</code> as an attribute (default=TRUE)
<code>use.gr</code>	Boolean to determine whether to use gradients in the variance calculations when they are available (default=TRUE)
<code>level</code>	confidence level for the confidence intervals (default=0.95)
<code>n.gauss.quad</code>	number of Gauassian quadrature points used for integrations (default=100)
<code>full</code>	logical for whether to return a full data-frame with predictions and <code>newdata</code> combined. Useful for <code>lattice</code> and <code>ggplot2</code> plots. (default=FALSE)
<code>...</code>	additional arguments (for generic compatibility)

## Details

The confidence interval estimation is based on the delta method using numerical differentiation.

## Value

A data-frame with components `Estimate`, `lower` and `upper`, with an attribute `"newdata"` for the `newdata` data-frame.

## Methods

**object= "stpm2"** an `stpm2` fit

## See Also

[stpm2](#)

---

 predict.nsx

*Evaluate a Spline Basis*


---

### Description

Evaluate a predefined spline basis at given values.

### Usage

```
## S3 method for class 'nsx'
predict(object, newx, ...)
```

### Arguments

object	the result of a call to <code>nsx</code> having attributes describing knots, degree, etc.
newx	the x values at which evaluations are required.
...	Optional additional arguments. At present no additional arguments are used.

### Value

An object just like `object`, except evaluated at the new values of `x`.

These are methods for the generic function `predict` for objects inheriting from classes "nsx". See `predict` for the general behavior of this function.

### See Also

`nsx`.

### Examples

```
basis <- nsx(women$height, df = 5)
newX <- seq(58, 72, length.out = 51)
# evaluate the basis at the new data
predict(basis, newX)
```

---

 predictnl

*Estimation of standard errors using the numerical delta method.*


---

### Description

A simple, yet exceedingly useful, approach to estimate the variance of a function using the numerical delta method. A number of packages provide functions that analytically calculate the gradients; we use numerical derivatives, which generalises to models that do not offer analytical derivatives (e.g. ordinary differential equations, integration), or to examples that are tedious or error-prone to calculate (e.g. sums of predictions from GLMs).

**Usage**

```
## Default S3 method:
predictnl(object, fun, newdata=NULL, gd=NULL, ...)
## S3 method for class 'lm'
predictnl(object, fun, newdata=NULL, ...)
## S3 method for class 'predictnl'
print(x, ...)
## S3 method for class 'formula'
predict(object,data,newdata,na.action,type="model.matrix",...)
## S3 method for class 'predictnl'
confint(object, parm, level=0.95, ...)
```

**Arguments**

object	An object with coef, vcov and <code>`coef&lt;-`</code> methods (required).
fun	A function that takes object as the first argument, possibly with newdata and other arguments (required). See notes for why it is often useful to include newdata as an argument to the function.
newdata	An optional argument that defines newdata to be passed to fun.
gd	An optional matrix of gradients. If this is not specified, then the gradients are calculated using finite differences.
parm	currently ignored
level	significance level for 2-sided confidence intervals
x	a predictnl object to be printed.
data	object used to define the model frame
na.action	passed to model.frame
type	currently restricted to "model.matrix"
...	Other arguments that are passed to fun.

**Details**

The signature for fun is either `fun(object, ...)` or `fun(object, newdata=NULL, ...)`.

The different predictnl methods call the utility function numDeltaMethod, which in turn calls the grad function for numerical differentiation. The numDeltaMethod function calls the standard coef and vcov methods, and the non-standard ``coef<-`` method for changing the coefficients in a regression object. This non-standard method has been provided for several regression objects and essentially mirrors the coef method.

One potential issue is that some predict methods do not re-calculate their predictions for the fitted dataset (i.e. when newdata=NULL). As the predictnl function changes the fitted coefficients, it is required that the predictions are re-calculated. One solution is to pass newdata as an argument to both predictnl and fun; alternatively, newdata can be specified in fun. These approaches are described in the examples below. The numDeltaMethod method called by predictnl provides a warning when the variance estimates are zero, which may be due to this cause.

For completeness, it is worth discussing why the example `predictnl(fit,predict)` does not work for when fit is a glm object. First, `predict.glm` does not update the predictions for the

fitted data. Second, the default predict method has a signature `predict(object, ...)`, which does not include a `newdata` argument. We could then either (i) require that a `newdata` argument be passed to the fun function for all examples, which would make this corner case work, or (ii) only pass the `newdata` argument if it is non-null or in the formals for the fun function, which would fail for this corner case. The current API defaults to the latter case (ii). To support this approach, the `predictnl.lm` method replaces a null `newdata` with `object$data`. We also provide a revised `numdelta::predict.lm` method that performs the same operation, although its use is not encouraged due to its clumsiness.

### Value

Returns an object of class an object with class `c("predictnl", "data.frame")` elements `c("fit", "se.fit", "Estimate", "Estimate.se")`, and with methods `print` and `confint`. Note that the `Estimate` and `SE` fields are deprecated and their use is discouraged, as we would like to remove them from future releases.

### Author(s)

Mark Clements

### Examples

```
df <- data.frame(x=0:1, y=c(10, 20))
fit <- glm(y ~ x, df, family=poisson)

predictnl(fit,
          function(obj,newdata)
            diff(predict(obj,newdata,type="response")))
```

---

predictnl-methods      *~~ Methods for Function predictnl ~~*

---

### Description

*~~ Methods for function predictnl ~~*

### Methods

**predictnl** `signature(object = "mle2", ...)`: Similar to `predictnl.default`, using S4 methods.

---

pstpm2-class                    *Class "pstpm2"*

---

### Description

Regression object for pstpm2.

### Objects from the Class

Objects can be created by calls of the form `new("pstpm2", ...)` and `pstpm2(...)`.

### Slots

xlevels: Object of class "list" ~~  
contrasts: Object of class "listOrNULL" ~~  
terms: Object of class "terms" ~~  
gam: Object of class "gam" ~~  
logli: Object of class "function" ~~  
timeVar: Object of class "character" ~~  
time0Var: Object of class "character" ~~  
time0Expr: Object of class "nameOrcall" ~~  
timeExpr: Object of class "nameOrcall" ~~  
like: Object of class "function" ~~  
model.frame: Object of class "list" ~~  
delayed: Object of class "logical" ~~  
frailty: Object of class "logical" ~~  
x: Object of class "matrix" ~~  
xd: Object of class "matrix" ~~  
termsd: Object of class "terms" ~~  
Call: Object of class "character" ~~  
y: Object of class "Surv" ~~  
sp: Object of class "numeric" ~~  
nevent: Object of class "numeric" ~~  
link: Object of class "list" ~~  
edf: Object of class "numeric" ~~  
edf\_var: Object of class "numeric" ~~  
df: Object of class "numeric" ~~  
call: Object of class "language" ~~  
call.orig: Object of class "language" ~~

coef: Object of class "numeric" ~~  
 fullcoef: Object of class "numeric" ~~  
 vcov: Object of class "matrix" ~~  
 min: Object of class "numeric" ~~  
 details: Object of class "list" ~~  
 minuslogl: Object of class "function" ~~  
 method: Object of class "character" ~~  
 data: Object of class "list" ~~  
 formula: Object of class "character" ~~  
 optimizer: Object of class "character" ~~  
 args: Object of class "list" ~~

### Extends

Class "[mle2](#)", directly.

### Methods

**plot** signature(x = "pstpm2", y = "missing"): ...  
**lines** signature(x = "pstpm2", ...): ...  
**anova** signature(object = "pstpm2", ...): ...  
**AIC** signature(object = "pstpm2", ..., k=2): ...  
**AICc** signature(object = "pstpm2", ..., nobs=NULL, k=2): ...  
**BIC** signature(object = "pstpm2", ..., nobs = NULL): ...  
**qAICc** signature(object = "pstpm2", ..., nobs = NULL, dispersion = 1, k = 2): ...  
**qAIC** signature(object = "pstpm2", ..., dispersion = 1, k = 2): ...  
**summary** signature(object = "pstpm2", ...): ...  
**eform** signature(object = "pstpm2", ...): ...  
**predictnl** signature(object = "pstpm2", ...): ...

### Examples

```
showClass("pstpm2")
```

---

residuals-methods      *Residual values for an stpm2 or pstpm2 fit*

---

### Description

Given an stpm2 or pstpm2 fit, return residuals

### Usage

```
## S4 method for signature 'stpm2'  
residuals(object, type=c("li","gradli"))  
## S4 method for signature 'pstpm2'  
residuals(object, type=c("li","gradli"))
```

### Arguments

object            an stpm2 or pstpm2 object

type             specify the type of residuals:

- "li" log-likelihood components (not strictly residuals)
- "gradli" gradient of the log-likelihood components (not strictly residuals)

### Details

The gradients are analytical.

### Value

A vector or matrix.

### Methods

**object= "stpm2"** an stpm2 fit

### See Also

[stpm2](#)



---

rstpm2-internal	<i>Internal functions for the rstpm2 package.</i>
-----------------	---

---

**Description**

Various utility functions used internally to the rstpm2 package.

**Usage**

```
lhs(formula)
rhs(formula)
lhs(formula) <- value
rhs(formula) <- value
```

**Arguments**

formula	A formula
value	A symbolic value to replace the current value.

---

stpm2-class	<i>Class "stpm2" ~~~</i>
-------------	--------------------------

---

**Description**

Regression object for stpm2.

**Objects from the Class**

Objects can be created by calls of the form `new("stpm2", ...)` and `stpm2( ...)`.

**Slots**

```
xlevels: Object of class "list" ~~
contrasts: Object of class "listOrNULL" ~~
terms: Object of class "terms" ~~
logli: Object of class "function" ~~
lm: Object of class "lm" ~~
timeVar: Object of class "character" ~~
time0Var: Object of class "character" ~~
timeExpr: Object of class "nameOrcall" ~~
time0Expr: Object of class "nameOrcall" ~~
delayed: Object of class "logical" ~~
```

```

frailty: Object of class "logical" ~~
interval: Object of class "logical" ~~
model.frame: Object of class "list" ~~
call.formula: Object of class "formula" ~~
x: Object of class "matrix" ~~
xd: Object of class "matrix" ~~
termsd: Object of class "terms" ~~
Call: Object of class "character" ~~
y: Object of class "Surv" ~~
link: Object of class "list" ~~
call: Object of class "language" ~~
call.orig: Object of class "language" ~~
coef: Object of class "numeric" ~~
fullcoef: Object of class "numeric" ~~
vcov: Object of class "matrix" ~~
min: Object of class "numeric" ~~
details: Object of class "list" ~~
minuslogl: Object of class "function" ~~
method: Object of class "character" ~~
data: Object of class "list" ~~
formula: Object of class "character" ~~
optimizer: Object of class "character" ~~
args: Object of class "list" ~~

```

### Extends

Class "[mle2](#)", directly.

### Methods

```

plot signature(x = "stpm2", y = "missing"): ...
lines signature(x = "stpm2", ...): ...
predictnl signature(object = "stpm2", ...): ...
summary signature(object = "stpm2", ...): ...
eform signature(object = "stpm2", ...): ...

```

### Examples

```
showClass("stpm2")
```

---

tvcCoxph-class	Class "tvcCoxph"
----------------	------------------

---

### Description

Experimental approach to modelling time-dependent effects in Cox regression.

### Objects from the Class

Objects can be created by calls of the form `new("tvcCoxph", ...)` or `cox.tvc(...)`. See the "[mle2](#)" documentation.

### Slots

call: Object of class "language" ~~  
call.orig: Object of class "language" ~~  
coef: Object of class "numeric" ~~  
fullcoef: Object of class "numeric" ~~  
vcov: Object of class "matrix" ~~  
min: Object of class "numeric" ~~  
details: Object of class "list" ~~  
minuslogl: Object of class "function" ~~  
method: Object of class "character" ~~  
data: Object of class "list" ~~  
formula: Object of class "character" ~~  
optimizer: Object of class "character" ~~

### Extends

Class "[mle2](#)", directly.

### Methods

**plot** signature(x = "tvcCoxph", y = "missing"): ...

### Examples

```
showClass("tvcCoxph")
```

vuniroot

*Vectorised One Dimensional Root (Zero) Finding***Description**

The function `vuniroot` searches the interval from `lower` to `upper` for a root (i.e., zero) of the vectorised function `f` with respect to its first argument.

Setting `extendInt` to a non-"no" string, means searching for the correct interval = `c(lower, upper)` if `sign(f(x))` does not satisfy the requirements at the interval end points; see the 'Details' section.

**Usage**

```
vuniroot(f, interval, ...,
         lower, upper,
         f.lower = f(lower, ...), f.upper = f(upper, ...),
         extendInt = c("no", "yes", "downX", "upX"), check.conv = FALSE,
         tol = .Machine$double.eps^0.25, maxiter = 1000, trace = 0)
```

**Arguments**

<code>f</code>	the function for which the root is sought.
<code>interval</code>	a matrix with two columns containing the end-points of the interval to be searched for the root.
<code>...</code>	additional named or unnamed arguments to be passed to <code>f</code>
<code>lower, upper</code>	the lower and upper end points of the interval to be searched.
<code>f.lower, f.upper</code>	the same as <code>f(upper)</code> and <code>f(lower)</code> , respectively. Passing these values from the caller where they are often known is more economical as soon as <code>f()</code> contains non-trivial computations.
<code>extendInt</code>	character string specifying if the interval <code>c(lower, upper)</code> should be extended or directly produce an error when <code>f()</code> does not have differing signs at the end-points. The default, "no", keeps the search interval and hence produces an error. Can be abbreviated.
<code>check.conv</code>	logical indicating whether a convergence warning of the underlying <code>vuniroot</code> should be caught as an error and if non-convergence in <code>maxiter</code> iterations should be an error instead of a warning.
<code>tol</code>	the desired accuracy (convergence tolerance).
<code>maxiter</code>	the maximum number of iterations.
<code>trace</code>	integer number; if positive, tracing information is produced. Higher values giving more details.

## Details

Note that arguments after `...` must be matched exactly.

Either `interval` or both `lower` and `upper` must be specified: the upper endpoint must be strictly larger than the lower endpoint.

The function values at the endpoints must be of opposite signs (or zero), for `extendInt="no"`, the default. Otherwise, if `extendInt="yes"`, the interval is extended on both sides, in search of a sign change, i.e., until the search interval  $[l, u]$  satisfies  $f(l) \cdot f(u) \leq 0$ .

If it is *known how*  $f$  changes sign at the root  $x_0$ , that is, if the function is increasing or decreasing there, `extendInt` can (and typically should) be specified as `"upX"` (for “upward crossing”) or `"downX"`, respectively. Equivalently, define  $S := \pm 1$ , to require  $S = \text{sign}(f(x_0 + \epsilon))$  at the solution. In that case, the search interval  $[l, u]$  possibly is extended to be such that  $S \cdot f(l) \leq 0$  and  $S \cdot f(u) \geq 0$ .

`vuniroot()` uses a C++ subroutine based on “`zeroIn`” (from Netlib) and algorithms given in the reference below. They assume a continuous function (which then is known to have at least one root in the interval).

Convergence is declared either if  $f(x) == 0$  or the change in  $x$  for one step of the algorithm is less than `tol` (plus an allowance for representation error in  $x$ ).

If the algorithm does not converge in `maxIter` steps, a warning is printed and the current approximation is returned.

$f$  will be called as  $f(x, \dots)$  for a numeric value of  $x$ .

The argument passed to  $f$  has special semantics and used to be shared between calls. The function should not copy it.

## Value

A list with at least three components: `root` and `f.root` give the location of the root and the value of the function evaluated at that point. `iter` gives the number of iterations used.

Further components may be added in future: component `init.it` was added in R 3.1.0.

## Source

Based on ‘`zeroIn.c`’ in <http://www.netlib.org/c/brent.shar>.

## References

Brent, R. (1973) *Algorithms for Minimization without Derivatives*. Englewood Cliffs, NJ: Prentice-Hall.

## See Also

`uniroot` for the standard single root solver `polyroot` for all complex roots of a polynomial; `optimize`, `nlm`.

## Examples

```

require(utils) # for str

## some platforms hit zero exactly on the first step:
## if so the estimated precision is 2/3.
f <- function(x, a) x - a
str(xmin <- vuniroot(f, lower=c(0, 0), upper=c(1,1), tol = 0.0001, a = c(1/3,2/3)))

## handheld calculator example: fixed point of cos(.):
vuniroot(function(x) cos(x) - x, lower = -pi, upper = pi, tol = 1e-9)$root

str(vuniroot(function(x) x*(x^2-1) + .5, lower = -2, upper = 2,
              tol = 0.0001))
str(vuniroot(function(x) x*(x^2-1) + .5, lower = -2, upper = 2,
              tol = 1e-10))

## Find the smallest value x for which exp(x) > 0 (numerically):
r <- vuniroot(function(x) 1e80*exp(x) - 1e-300, cbind(-1000, 0), tol = 1e-15)
str(r, digits.d = 15) # around -745, depending on the platform.

exp(r$root)      # = 0, but not for r$root * 0.999...
minexp <- r$root * (1 - 10*.Machine$double.eps)
exp(minexp)      # typically denormalized

##--- vuniroot() with new interval extension + checking features: -----

f1 <- function(x) (121 - x^2)/(x^2+1)
f2 <- function(x) exp(-x)*(x - 12)

tools::assertCondition(vuniroot(f1, cbind(0,10)),
                       "error", verbose=TRUE)
tools::assertCondition(vuniroot(f2, cbind(0, 2)),
                       "error", verbose=TRUE)
##--> error: f() .. end points not of opposite sign

## where as 'extendInt="yes"' simply first enlarges the search interval:
u1 <- vuniroot(f1, cbind(0,10),extendInt="yes", trace=1)
u2 <- vuniroot(f2, cbind(0,2), extendInt="yes", trace=2)
stopifnot(all.equal(u1$root, 11, tolerance = 1e-5),
          all.equal(u2$root, 12, tolerance = 6e-6))

## The *danger* of interval extension:
## No way to find a zero of a positive function, but
## numerically, f(-|M|) becomes zero :
tools::assertCondition(u3 <- vuniroot(exp, cbind(0,2), extendInt="yes", trace=TRUE),
                       "error", verbose=TRUE)

## Nonsense example (must give an error):
tools::assertCondition( vuniroot(function(x) 1, cbind(0,1), extendInt="yes"),
                       "error", verbose=TRUE)

```

```

## Convergence checking :
sinc_ <- function(x) ifelse(x == 0, 1, sin(x)/x)
curve(sinc_, -6,18); abline(h=0,v=0, lty=3, col=adjustcolor("gray", 0.8))

vuniroot(sinc_, cbind(0,5), extendInt="yes", maxiter=4) #-> "just" a warning

## now with check.conv=TRUE, must signal a convergence error :

vuniroot(sinc_, cbind(0,5), extendInt="yes", maxiter=4, check.conv=TRUE)

### Weibull cumulative hazard (example origin, Ravi Varadhan):
cumhaz <- function(t, a, b) b * (t/b)^a
froot <- function(x, u, a, b) cumhaz(x, a, b) - u

n <- 10
u <- -log(runif(n))
a <- 1/2
b <- 1
## Find failure times
ru <- vuniroot(froot, u=u, a=a, b=b, interval= cbind(rep(1.e-14,n), rep(1e4,n)),
              extendInt="yes")$root
ru2 <- vuniroot(froot, u=u, a=a, b=b, interval= cbind(rep(0.01,n), rep(10,n)),
              extendInt="yes")$root
stopifnot(all.equal(ru, ru2, tolerance = 6e-6))

r1 <- vuniroot(froot, u= 0.99, a=a, b=b, interval= cbind(0.01, 10),
              extendInt="up")
stopifnot(all.equal(0.99, cumhaz(r1$root, a=a, b=b)))

## An error if 'extendInt' assumes "wrong zero-crossing direction":

vuniroot(froot, u= 0.99, a=a, b=b, interval= cbind(0.1, 10), extendInt="down")

```

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