Package 'qgcomp'

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Title Quantile G-Computation

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Author Alexander Keil [aut, cre]

Maintainer Alexander Keil <akeil@unc.edu>

Description G-computation for a set of time-fixed exposures with quantile-based basis functions, possibly under linearity and homogeneity assumptions. This approach estimates a regression line corresponding to the expected change in the outcome (on the link basis) given a simultaneous increase in the quantile-based category for all exposures. Works with continuous, binary, and right-censored time-to-event outcomes. Reference: Alexander P. Keil, Jessie P. Buckley, Katie M. OBrien, Kelly K. Ferguson, Shanshan Zhao, and Alexandra J. White (2019) A quantile-based g-computation approach to addressing the effects of exposure mixtures; <doi:10.1289/EHP5838>.

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checknames

Check for valid model terms in a qgcomp fit

Description

This is an internal function called by qgcomp, qgcomp.boot, and qgcomp.noboot, but is documented here for clarity. Generally, users will not need to call this function directly. This function tries to determine whether there are non-linear terms in the underlying model, which helps infer whether the appropriate function is called, and whether more explicit function calls are needed.

coxmsm.fit

Usage

checknames(terms)

Arguments

terms

model terms from attr(terms(modelfunction, data), "term.labels")

coxmsm.fit	Marginal structura	l Cox	model	(MSM)	fitting	within	quantile	<i>g</i> -
	computation							

Description

this is an internal function called by qgcomp.cox.noboot, qgcomp.cox.boot, and qgcomp.cox.noboot, but is documented here for clarity. Generally, users will not need to call this function directly.

Usage

```
coxmsm.fit(
   f,
   qdata,
   intvals,
   expnms,
   main = TRUE,
   degree = 1,
   id = NULL,
   weights,
   cluster = NULL,
   MCsize = 10000,
   ...
)
```

Arguments

f	an R formula representing the conditional model for the outcome, given all exposures and covariates. Interaction terms that include exposure variables should be represented via the AsIs function. Offset terms can be included via Surv(time, event) ~ exposure + offset(z)
qdata	a data frame with quantized exposures (as well as outcome and other covariates)
intvals	sequence, the sequence of integer values that the joint exposure is 'set' to for estimating the msm. For quantile g-computation, this is just 0:(q-1), where q is the number of quantiles of exposure.
expnms	a character vector with the names of the columns in qdata that represent the exposures of interest (main terms only!)
main	logical, internal use: produce estimates of exposure effect (psi) and expected outcomes under g-computation and the MSM

degree	polynomial bases for marginal model (e.g. degree = 2 allows that the relationship between the whole exposure mixture and the outcome is quadratic. Default=1)
id	(optional) NULL, or variable name indexing individual units of observation (only needed if analyzing data with multiple observations per id/cluster)
weights	"case weights" - passed to the "weight" argument of coxph
cluster	not yet implemented
MCsize	integer: sample size for simulation to approximate marginal hazards ratios
	arguments to coxph (e.g. ties)

Details

This function first computes expected outcomes under hypothetical interventions to simultaneously set all exposures to a specific quantile. These predictions are based on g-computation, where the exposures are 'quantized', meaning that they take on ordered integer values according to their ranks, and the integer values are determined by the number of quantile cutpoints used. The function then takes these expected outcomes and fits an additional model (a marginal structural model) with the expected outcomes as the outcome and the intervention value of the exposures (the quantile integer) as the exposure. Under causal identification assumptions and correct model specification, the MSM yields a causal exposure-response representing the incremental change in the expected outcome given a joint intervention on all exposures.

See Also

qgcomp.cox.boot, and qgcomp.cox.noboot

Examples

```
set.seed(50)
dat <- data.frame(time=(tmg <- pmin(.1,rweibull(50, 10, 0.1))), d=1.0*(tmg<0.1),</pre>
                  x1=runif(50), x2=runif(50), z=runif(50))
expnms=paste0("x", 1:2)
qdata = qgcomp:::quantize(dat, expnms)$data
f = survival::Surv(time, d)~x1 + x2
fit <- survival::coxph(f, data = qdata, y=TRUE, x=TRUE)</pre>
r1 = qdata[1,,drop=FALSE]
times = survival::survfit(fit, newdata=r1, se.fit=FALSE)$time
(obj <- qgcomp:::coxmsm.fit(f, qdata, intvals=c(0,1,2,3), expnms, main=TRUE, degree=1,</pre>
   id=NULL, MCsize=100))
#dat2 <- data.frame(psi=seq(1,4, by=0.1))</pre>
#summary(predict(obj))
#summary(predict(obj, newdata=dat2))
```

glance.qgcompfit Glance at a qgcompfit object

Description

Glance accepts a model object and returns a tibble::tibble() with exactly one row of model summaries. The summaries are typically goodness of fit measures, p-values for hypothesis tests on residuals, or model convergence information.

Glance never returns information from the original call to the modelling function. This includes the name of the modelling function or any arguments passed to the modelling function.

Glance does not calculate summary measures. Rather, it farms out these computations to appropriate methods and gathers the results together. Sometimes a goodness of fit measure will be undefined. In these cases the measure will be reported as NA. (Description taken from broom::glance help file.)

Usage

```
## S3 method for class 'qgcompfit'
glance(x, ...)
```

Arguments

х	a qgcompfit object
	Not used

hurdlemsm.fit Secondary prediction method for the (hurdle) qgcomp MSM.

Description

this is an internal function called by qgcomp.hurdle.boot, but is documented here for clarity. Generally, users will not need to call this function directly.

Usage

```
hurdlemsm.fit(
   f,
   qdata,
   intvals,
   expnms,
   main = TRUE,
   degree = 1,
   id = NULL,
   weights,
```

```
MCsize = 10000,
containmix = list(count = TRUE, zero = TRUE),
bayes = FALSE,
x = FALSE,
msmcontrol = hurdlemsm.fit.control(),
...
```

Arguments

)

f	an r formula representing the conditional model for the outcome, given all exposures and covariates. Interaction terms that include exposure variables should be represented via the AsIs function
qdata	a data frame with quantized exposures (as well as outcome and other covariates)
intvals	sequence, the sequence of integer values that the joint exposure is 'set' to for estimating the msm. For quantile g-computation, this is just 0:(q-1), where q is the number of quantiles of exposure.
expnms	a character vector with the names of the columns in qdata that represent the exposures of interest (main terms only!)
main	logical, internal use: produce estimates of exposure effect (psi) and expected outcomes under g-computation and the MSM
degree	polynomial bases for marginal model (e.g. degree = 2 allows that the relation- ship between the whole exposure mixture and the outcome is quadratic. De- fault=1)
id	(optional) NULL, or variable name indexing individual units of observation (only needed if analyzing data with multiple observations per id/cluster)
weights	not yet implemented
MCsize	integer: sample size for simulation to approximate marginal hazards ratios
containmix	named list of logical scalars with names "count" and "zero"
bayes	not used
x	keep design matrix? (logical)
msmcontrol	named list from hurdlemsm.fit.control
	arguments to hurdle (e.g. dist)

Details

This function first computes expected outcomes under hypothetical interventions to simultaneously set all exposures to a specific quantile. These predictions are based on g-computation, where the exposures are 'quantized', meaning that they take on ordered integer values according to their ranks, and the integer values are determined by the number of quantile cutpoints used. The function then takes these expected outcomes and fits an additional model (a marginal structural model) with the expected outcomes as the outcome and the intervention value of the exposures (the quantile integer) as the exposure. Under causal identification assumptions and correct model specification, the MSM yields a causal exposure-response representing the incremental change in the expected outcome given a joint intervention on all exposures.

hurdlemsm.fit.control

See Also

qgcomp.cox.boot, and qgcomp.cox.noboot

Examples

```
set.seed(50)
n=100
## Not run:
dat <- data.frame(y=rbinom(n, 1, 0.5)*rpois(n, 1.2), x1=runif(n), x2=runif(n), z=runif(n))
expnms = c("x1", "x2")
q = 4
qdata = quantize(dat, q=q, expnms=expnms)$data
f = y ~ x1 + x2 + z | 1
msmfit <- qgcomp:::hurdlemsm.fit(f, qdata, intvals=(1:q)-1, expnms, main=TRUE,
    degree=1, id=NULL, MCsize=10000, containmix=list(count=TRUE, zero=FALSE),
    x=FALSE)
msmfit$
## End(Not run)</pre>
```

hurdlemsm.fit.control Control of fitting parameters for zero inflated MSMs

Description

this is an internal function called by qgcomp.hurdle.boot, but is documented here for clarity. Generally, users will not need to call this function directly.

Usage

```
hurdlemsm.fit.control(predmethod = c("components", "catprobs"))
```

Arguments

predmethod character in c("components", "catprobs"). "components" simulates from the model parameters directly while "catprobs" simulates outcomes from the category specific probabilities, which is output from predict.hurdle. The former is slightly more flexible and stable, but the latter is preferred in zero inflated negative bionomial models.

Details

Provides fine control over zero inflated MSM fitting

metals

Description

Simulated well water measurements in North Carolina: 16 metals, 6 water chemistry measures, and 2 health outcomes (y = continuous; disease_state = binary/time-to-event in combination with disease_time)

A dataset containing well water measurements and health outcomes for 253 individuals. All continuous variables are standardized to have mean 0, standard deviation 1.

Usage

metals

Format

A data frame with 253 rows and 24 variables:

y continuous birth outcome

disease_state binary outcome

disease_time time-to-disease_state: survival outcome censored at approximately the median

arsenic metal

barium metal

cadmium metal

calcium metal chloride metal

chromium metal

copper metal

iron metal

lead metal

magnesium metal

manganese metal

mercury metal

selenium metal

silver metal

sodium metal

zinc metal

mage35 Binary covariate: maternal age > 35

nitrate water chemistry measure

nitrite water chemistry measure

sulfate water chemistry measure
ph water chemistry measure
total_alkalinity water chemistry measure
total_hardness water chemistry measure

mice.impute.leftcenslognorm

Imputation for limits of detection problems

Description

This function integrates with mice to impute values below the LOD using a left censored log-normal distribution.

Usage

```
mice.impute.leftcenslognorm(
    y,
    ry,
    x,
    wy = NULL,
    lod = NULL,
    debug = FALSE,
    ...
)
```

Arguments

У	Vector to be imputed
ry	Logical vector of length length(y) indicating the the subset of elements in y to which the imputation model is fitted. The ry generally distinguishes the observed (TRUE) and missing values (FALSE) in y.
x	Numeric design matrix with length(y) rows with predictors for y. Matrix x may have no missing values.
wy	Logical vector of length length(y). A TRUE value indicates locations in y for which imputations are created.
lod	numeric vector of limits of detection (must correspond to index in original data)
debug	logical, print extra info
	arguments to survreg

Details

While this function has utility far beyond qgcomp, it is included in the qgcomp package because it will be useful for a variety of settings in which qgcomp is useful. Note that LOD problems where the LOD is small, and the q parameter from qgcomp.noboot or qgcomp.boot is not large, the LOD may be below the lowest quantile cutpoint which will yield identical datasets from the MICE procedure in terms of quantized exposure data. If only exposures are missing, and they have low LODs, then there will be no benefit in qgcomp from using MICE rather than imputing some small value below the LOD.

Value

Vector with imputed data, same type as y, and of length sum(wy)

Examples

```
N = 100
set.seed(123)
dat <- data.frame(y=runif(N), x1=runif(N), x2=runif(N), z=runif(N))</pre>
true = qgcomp.noboot(f=y ~ z + x1 + x2, expnms = c('x1', 'x2'),
        data=dat, q=2, family=gaussian())
mdat <- dat
mdat$x1 = ifelse(mdat$x1>0.5, mdat$x1, NA)
mdat$x2 = ifelse(mdat$x2>0.75, mdat$x2, NA)
cc <- qgcomp.noboot(f=y \sim z + x1 + x2, expnms = c('x1', 'x2'),
       data=mdat[complete.cases(mdat),], q=2, family=gaussian())
## Not run:
# note the following example imputes from the wrong parametric model and is expected to be biased
# as a result (but it demonstrates how to use qgcomp and mice together)
library("mice")
library("survival")
impdat = mice(data = mdat,
  method = c("", "leftcenslognorm", "leftcenslognorm", ""),
  lod=c(NA, 0.5, 0.75, NA), debug=FALSE)
qc.fit.imp <- list(</pre>
  call = call("qgcomp.noboot(y~., expnms = c('x1', 'x2'), family=gaussian())"),
  call1 = impdat$call,
  nmis = impdat$nmis,
  analyses = lapply(1:5, function(x) qgcomp.noboot(y~., expnms = c("x1", "x2"),
    data=complete(impdat, x), family=gaussian(), bayes=TRUE))
)
obj = pool(as.mira(qc.fit.imp))
# true values
true
# complete case analysis
CC
# MI based analysis
summary(obj)
## End(Not run)
```

modelbound.boot

Description

Calculates: expected outcome (on the link scale), and upper and lower confidence intervals (both pointwise and simultaneous)

Usage

modelbound.boot(x, alpha = 0.05, pwonly = FALSE)

Arguments

Х	"qgcompfit" object from qgcomp.boot,
alpha	alpha level for confidence intervals
pwonly	logical: return only pointwise estimates (suppress simultaneous estimates)

Details

This method leverages the bootstrap distribution of qgcomp model coefficients to estimate pointwise regression line confidence bounds. These are defined as the bounds that, for each value of the independent variable X (here, X is the joint exposure quantiles) the 95% bounds (for example) for the model estimate of the regression line E(Y|X) are expected to include the true value of E(Y|X) in 95% of studies. The "simultaneous" bounds are also calculated, and the 95% simultaneous bounds contain the true value of E(Y|X) for all values of X in 95% of studies. The latter are more conservative and account for the multiple testing implied by the former. Pointwise bounds are estimated using the bootstrap method of Cheng (reference below). All bounds are large sample bounds that assume normality and thus will be underconservative in small samples. These bounds may also inclue illogical values (e.g. values less than 0 for a dichotomous outcome) and should be interpreted cautiously in small samples.

Reference:

Cheng, Russell CH. "Bootstrapping simultaneous confidence bands." Proceedings of the Winter Simulation Conference, 2005.. IEEE, 2005.

Value

A data frame containing expected values of the outcome at each quantized value of all exposures as well as "pointwise" (pw) and "simultaneous" (simul) confidence intervals at each each quantized value of all exposures.

See Also

qgcomp.boot

Examples

End(Not run)

msm.fit	Fitting	marginal	structural	model	(MSM)	within	quantile	<i>g</i> -
	comput	ation						

Description

This is an internal function called by qgcomp, qgcomp.boot, and qgcomp.noboot, but is documented here for clarity. Generally, users will not need to call this function directly.

Usage

```
msm.fit(
    f,
    qdata,
    intvals,
    expnms,
    rr = TRUE,
    main = TRUE,
    degree = 1,
    id = NULL,
    weights,
    bayes = FALSE,
    MCsize = nrow(qdata),
    ...
)
```

Arguments

f	an r formula representing the conditional model for the outcome, given all exposures and covariates. Interaction terms that include exposure variables should be represented via the AsIs function
qdata	a data frame with quantized exposures
intvals	sequence, the sequence of integer values that the joint exposure is 'set' to for estimating the msm. For quantile g-computation, this is just 0:(q-1), where q is the number of quantiles of exposure.
expnms	a character vector with the names of the columns in qdata that represent the exposures of interest (main terms only!)

rr	logical, estimate log(risk ratio) (family='binomial' only)
main	logical, internal use: produce estimates of exposure effect (psi) and expected outcomes under g-computation and the MSM
degree	polynomial bases for marginal model (e.g. degree = 2 allows that the relation- ship between the whole exposure mixture and the outcome is quadratic. De- fault=1)
id	(optional) NULL, or variable name indexing individual units of observation (only needed if analyzing data with multiple observations per id/cluster)
weights	"case weights" - passed to the "weight" argument of glm or bayesglm
bayes	use underlying Bayesian model (arm package defaults). Results in penalized parameter estimation that can help with very highly correlated exposures. Note: this does not lead to fully Bayesian inference in general, so results should be interpreted as frequentist.
MCsize	integer: sample size for simulation to approximate marginal zero inflated model parameters. This can be left small for testing, but should be as large as needed to reduce simulation error to an acceptable magnitude (can compare psi coeffi- cients for linear fits with qgcomp.zi.noboot to gain some intuition for the level of expected simulation error at a given value of MCsize)
	arguments to glm (e.g. family)

Details

This function first computes expected outcomes under hypothetical interventions to simultaneously set all exposures to a specific quantile. These predictions are based on g-computation, where the exposures are 'quantized', meaning that they take on ordered integer values according to their ranks, and the integer values are determined by the number of quantile cutpoints used. The function then takes these expected outcomes and fits an additional model (a marginal structural model) with the expected outcomes as the outcome and the intervention value of the exposures (the quantile integer) as the exposure. Under causal identification assumptions and correct model specification, the MSM yields a causal exposure-response representing the incremental change in the expected outcome given a joint intervention on all exposures.

See Also

qgcomp.boot, and qgcomp

Examples

```
msm.predict
```

Description

this is an internal function called by qgcomp.boot, but is documented here for clarity. Generally, users will not need to call this function directly.

Get predicted values from a qgcompfit object from qgcomp.boot.

Usage

```
msm.predict(object, newdata = NULL)
```

Arguments

object	"qgcompfit" object from qgcomp.boot function
newdata	(optional) new set of data (data frame) with a variable called psi representing the joint exposure level of all exposures under consideration

Details

(Not usually called by user) Makes predictions from the MSM (rather than the conditional gcomputation fit) from a "qgcompfit" object. Generally, this should not be used in favor of the default predict.qgcompfit function. This function can only be used following the qgcomp.boot function. For the qgcomp.noboot function, predict.qgcompfit gives identical inference to predicting from an MSM.

Examples

```
set.seed(50)
dat <- data.frame(y=runif(50), x1=runif(50), x2=runif(50), z=runif(50))
obj <- qgcomp.boot(y ~ z + x1 + x2 + I(z*x1), expnms = c('x1', 'x2'), data=dat, q=4, B=10, seed=125)
dat2 <- data.frame(psi=seq(1,4, by=0.1))
summary(msm.predict(obj))
summary(msm.predict(obj, newdata=dat2))
```

plot.qgcompfit Default plotting method for a qgcompfit object

Description

Plot a quantile g-computation object. For qgcomp.noboot, this function will create a butterfly plot of weights. For qgcomp.boot, this function will create a box plot with smoothed line overlaying that represents a non-parametric fit of a model to the expected outcomes in the population at each quantile of the joint exposures (e.g. '1' represents 'at the first quantile for every exposure')

plot.qgcompfit

Usage

```
## S3 method for class 'qgcompfit'
plot(
    x,
    suppressprint = FALSE,
    pointwisebars = TRUE,
    modelfitline = TRUE,
    modelband = TRUE,
    flexfit = TRUE,
    pointwiseref = ceiling(x$q/2),
    ...
)
```

Arguments

x	"qgcompfit" object from qgcomp.noboot, qgcomp.boot, qgcomp.cox.noboot, qgcomp.cox.boot, qgcomp.zi.boot functions
suppressprint	If TRUE, suppresses the plot, rather than printing it by default (it can be saved as a ggplot2 object (or list of ggplot2 objects if x is from a zero- inflated model) and used programmatically) (default = FALSE)
pointwisebars	(boot.gcomp only) If TRUE, adds 95% error bars for pointwise comparisons of $E(Y joint exposure)$ to the smooth regression line plot
modelfitline	(boot.gcomp only) If TRUE, adds fitted (MSM) regression line of E(Yljoint exposure) to the smooth regression line plot
modelband	If TRUE, adds 95% prediction bands for E(Yljoint exposure) (the MSM fit)
flexfit	(boot.gcomp only) if TRUE, adds flexible interpolation of predictions from un- derlying (conditional) model
pointwiseref	(boot.gcomp only) integer: which category of exposure (from 1 to q) should serve as the referent category for pointwise comparisons? (default=1)
	unused

See Also

qgcomp.noboot, qgcomp.boot, and qgcomp

Examples

```
# using non-linear outcome model
ft2 <- qgcomp.boot(y ~ z + x1 + x2 + x3 + I(x1*x1), expnms=c('x1','x2','x3'),
data=dat, q=4, B=10)
ft2
plot(ft2$fit, which=1) # much better looking fit diagnostics suggests
# it is better to include interaction term for x
plot(ft2) # the msm predictions don't match up with a smooth estimate
# of the expected outcome, so we should consider a non-linear MSM
# using non-linear marginal structural model
ft3 <- qgcomp.boot(y ~ z + x1 + x2 + x3 + I(x1*x1), expnms=c('x1','x2','x3'),
data=dat, q=4, B=10, degree=2)
# plot(ft3$fit, which=1) - not run - this is identical to ft2 fit
plot(ft3) # the MSM estimates look much closer to the smoothed estimates
# suggesting the non-linear MSM fits the data better and should be used
# for inference about the effect of the exposure
# Using survival data ()
set.seed(50)
N=200
dat <- data.frame(time=(tmg <- pmin(.1,rweibull(N, 10, 0.1))),</pre>
                d=1.0*(tmg<0.1), x1=runif(N), x2=runif(N), z=runif(N))</pre>
expnms=paste0("x", 1:2)
f = survival::Surv(time, d)~x1 + x2
(fit1 <- survival::coxph(f, data = dat))</pre>
# non-bootstrap method to get a plot of weights
(obj <- qgcomp.cox.noboot(f, expnms = expnms, data = dat))</pre>
plot(obj)
# bootstrap method to get a survival curve
# this plots the expected survival curve for the underlying (conditional) model
# as well as the expected survival curve for the MSM under the following scenarios:
# 1) highest joint exposure category
# 2) lowest joint exposure category
# 3) average across all exposure categories
# differences between the MSM and conditional fit suggest that the MSM is not flexible
# enough to accomodate non-linearities in the underlying fit (or they may simply signal that
# MCSize should be higher). Note that if linearity
# is assumed in the conditional model, the MSM will typically also appear linear and
# will certainly appear linear if no non-exposure covariates are included in the model
# not run (slow when using boot version to proper precision)
(obj2 <- qgcomp.cox.boot(f, expnms = expnms, data = dat, B=10, MCsize=2000))</pre>
plot(obj2)
## End(Not run)
```

pointwisebound.boot Estimating pointwise comparisons for qgcomp.boot objects

Description

Calculates: expected outcome (on the link scale), mean difference (link scale) and the standard error of the mean difference (link scale) for pointwise comparisons

Usage

```
pointwisebound.boot(x, alpha = 0.05, pointwiseref = 1)
```

Arguments

х	"qgcompfit" object from qgcomp.boot,
alpha	alpha level for confidence intervals
pointwiseref	referent quantile (e.g. 1 uses the lowest joint-exposure category as the referent category for calculating all mean differences/standard deviations)

Details

The comparison of interest following a qgcomp fit is often comparisons of model predictions at various values of the joint-exposures (e.g. expected outcome at all exposures at the 1st quartile vs. the 3rd quartile). The expected outcome at a given joint exposure, and marginalized over non-exposure covariates (W), is given as $E(Y^s|S) = sum_w E_w(Y|S,W)Pr(W) = sum_i E(Y_i|S)$ where Pr(W) is the emprical distribution of W and S takes on integer values 0 to q-1. Thus, comparisons are of the type $E_w(Y|S=s) - E_w(Y|S=s2)$ where s and s2 are two different values of the joint exposures (e.g. 0 and 2). This function yields $E_w(Y|S)$ as well as $E_w(Y|S=s) - E_w(Y|S=p)$ where s is any value of S and p is the value chosen via "pointwise ref" - e.g. for binomial variables this will equal the risk/ prevalence difference at all values of S, with the referent category S=p-1. The standard error of E(Y|S=s) - E(Y|S=p) is calculated from the bootstrap covariance matrix of $E_w(Y|S)$, such that the standard error for $E_w(Y|S=s) - E_w(Y|S=s)$.

 $Var(E_w(Y|S=s)) + -Var(E_w(Y|S=p)) - 2*Cov(E_w(Y|S=p), -E_w(Y|S=s))$

This is used to create pointwise confidence intervals. Note that this differs slightly from the pointwisebound.noboot function, which estimates the variance of the conditional regression line given by E(YIS,W=w), where w is a vector of medians of W (i.e. predictions are made at the median value of all covariates).

Value

A data frame containing expected values of the outcome at each quantized value of all exposures as well as a mean difference contrasting the expected outcome at each quantized value of all exposures, and associated standard error and confidence intervals.

See Also

qgcomp.boot, pointwisebound.noboot

Examples

pointwisebound.noboot Estimating pointwise comparisons for ggcomp.noboot objects

Description

Calculates: expected outcome (on the link scale), mean difference (link scale) and the standard error of the mean difference (link scale) for pointwise comparisons

Usage

```
pointwisebound.noboot(x, alpha = 0.05, pointwiseref = 1)
```

Arguments

Х	"qgcompfit" object from qgcomp.noboot,
alpha	alpha level for confidence intervals
pointwiseref	referent quantile (e.g. 1 uses the lowest joint-exposure category as the referent category for calculating all mean differences/standard deviations)

Details

The comparison of interest following a qgcomp fit is often comparisons of model predictions at various values of the joint-exposures (e.g. expected outcome at all exposures at the 1st quartile vs. the 3rd quartile). The expected outcome at a given joint exposure and at a given level of non-exposure covariates (W) is given as E(Y|S,W=w), where S takes on integer values 0 to q-1. Thus, comparisons are of the type E(Y|S=s,W=w) - E(Y|S=s2,W=w) where s and s2 are two different values of the joint exposures (e.g. 0 and 2). This function yields E(Y|S,W=w) as well as E(Y|S=s,W=w) - E(Y|S=s,W=w) - E(Y|S=s,W=w) as well as E(Y|S=s,W=w) - E(Y|S=s,W=w) - E(Y|S=s,W=w) as well as E(Y|S=s,W=w) - E(Y|S=s,W=w) - E(Y|S=s,W=w). For the non-boostrapped version of quantile g-computation (under a linear model)

 $f(\beta) = \sum_{i}^{p} \beta_{i}$ given gradient vector

 $G = \left[\partial(f(\beta))/\partial\beta_1 = 1, \dots, \partial(f(\beta))/\partial\beta_3 k = 1\right]$

 $t(G)Cov(\beta)G$ = delta method variance, where t() is the transpose operator and $\partial y/\partial x$ denotes the partial derivative/gradient and G is the "gradient vector". The vector G takes on values that equal

predict.qgcompfit

the difference in quantiles of S for each pointwise comparison (e.g. for a comparison of the 3rd vs the 5th category, G is a vector of 2s)

This is used to create pointwise confidence intervals

Value

A data frame containing expected values of the outcome at each quantized value of all exposures as well as a mean difference contrasting the expected outcome at each quantized value of all exposures, and associated standard error and confidence intervals.

See Also

qgcomp.noboot, pointwisebound.boot

Examples

```
set.seed(12)
## Not run:
n = 100
dat <- data.frame(x1=(x1 <- runif(n)), x2=(x2 <- runif(n)), x3=(x3 <- runif(n)), z=(z <- runif(n)),</pre>
                  y=rnorm(n)+x1 + x2 - x3 +z)
ft <- qgcomp.noboot(y ~ z + x1 + x2 + x3, expnms=c('x1', 'x2', 'x3'), data=dat, q=10)</pre>
ft2 <- qgcomp.boot(y ~ z + x1 + x2 + x3, expnms=c('x1','x2','x3'), data=dat, q=10)
pointwisebound.noboot(ft, alpha=0.05, pointwiseref=3)
pointwisebound.boot(ft2, alpha=0.05, pointwiseref=3)
dat <- data.frame(x1=(x1 <- runif(n)), x2=(x2 <- runif(n)), x3=(x3 <- runif(n)), z=(z <- runif(n)),
                  y=rbinom(n, 1, 1/(1+exp(-(x1 + x2 - x3 +z))))
ft <- qgcomp.noboot(y ~ z + x1 + x2 + x3, expnms=c('x1','x2','x3'), data=dat, q=10)</pre>
ft2 <- qgcomp.boot(y ~ z + x1 + x2 + x3, expnms=c('x1','x2','x3'), data=dat, q=10)
pointwisebound.noboot(ft, alpha=0.05, pointwiseref=3)
pointwisebound.boot(ft2, alpha=0.05, pointwiseref=3)
dat$z = as.factor(sample(1:3, n, replace=TRUE))
ftf <- qgcomp.noboot(y ~ z + x1 + x2 + x3, expnms=c('x1','x2','x3'), data=dat, q=10)</pre>
pointwisebound.noboot(ftf, alpha=0.05, pointwiseref=3)
```

End(Not run)

predict.qgcompfit Default prediction method for a qgcompfit object (non-survival outcomes only)

Description

get predicted values from a qgcompfit object, or make predictions in a new set of data based on the qgcompfit object. Note that when making predictions from an object from qgcomp.boot, the predictions are made from the g-computation model rather than the marginal structural model. Predictions from the marginal structural model can be obtained via msm.predict

Usage

```
## S3 method for class 'qgcompfit'
predict(object, expnms = NULL, newdata = NULL, type = "response", ...)
```

Arguments

object	"qgcompfit" object from qgcomp.noboot, qgcomp.boot, qgcomp.zi.noboot, or qgcomp.zi.bootfunctions
expnms	character vector of exposures of interest
newdata	(optional) new set of data with all predictors from "qgcompfit" object
type	(from predict.glm) the type of prediction required. The default is on the scale of the linear predictors; the alternative "response" is on the scale of the response variable. Thus for a default binomial model the default predictions are of log- odds (probabilities on logit scale) and type = "response" gives the predicted probabilities. The "terms" option returns a matrix giving the fitted values of each term in the model formula on the linear predictor scale.
	arguments to predict.glm

Examples

```
set.seed(50)
dat <- data.frame(y=runif(50), x1=runif(50), x2=runif(50), z=runif(50))</pre>
obj1 <- qgcomp.noboot(y ~ z + x1 + x2, expnms = c('x1', 'x2'), data=dat, q=2)</pre>
obj2 <- qgcomp.boot(y ~ z + x1 + x2, expnms = c('x1', 'x2'), data=dat, q=2, B=10, seed=125)
set.seed(52)
dat2 <- data.frame(y=runif(50), x1=runif(50), x2=runif(50), z=runif(50))</pre>
summary(predict(obj1, expnms = c('x1', 'x2'), newdata=dat2))
summary(predict(obj2, expnms = c('x1', 'x2'), newdata=dat2))
```

Default printing method for a qgcompfit object print.qgcompfit

Description

Gives variable output depending on whether qgcomp.noboot or qgcomp.boot is called. For qgcomp.noboot will output final estimate of joint exposure effect (similar to the 'index' effect in weighted quantile sums), as well as estimates of the 'weights' (standardized coefficients). For qgcomp.boot, the marginal effect is given, but no weights are reported since this approach generally incorporates non-linear models with interaction terms among exposures, which preclude weights with any useful interpretation.

Usage

```
## S3 method for class 'qgcompfit'
print(x, showweights = TRUE, ...)
```

qgcomp

Arguments

Х	"qgcompfit" object from qgcomp, qgcomp.noboot or qgcomp.boot function
showweights	logical: should weights be printed, if estimated?
	unused

See Also

qgcomp.noboot, qgcomp.boot, and qgcomp

Examples

```
set.seed(50)
dat <- data.frame(y=runif(50), x1=runif(50), x2=runif(50), z=runif(50))
obj1 <- qgcomp.noboot(y ~ z + x1 + x2, expnms = c('x1', 'x2'), data=dat, q=2)
obj2 <- qgcomp.boot(y ~ z + x1 + x2, expnms = c('x1', 'x2'), data=dat, q=2, B=10, seed=125)
# does not need to be explicitly called, but included here for clarity
print(obj1)
print(obj2)
```

qgcomp	Quantile g-computation for continuous, binary, count, and censored
	survival outcomes

Description

This function automatically selects between qgcomp.noboot, qgcomp.boot, qgcomp.cox.noboot, and qgcomp.cox.boot for the most efficient approach to estimate the average expected change in the (log) outcome per quantile increase in the joint exposure to all exposures in expnms', given the underlying model. For example, if the underlying model (specified by the formula f) is a linear model with all linear terms for exposure, then qgcomp.noboot" will be called to fit the model. Non-linear terms or requesting the risk ratio for binomial outcomes will result in the qgcomp.boot function being called. For a given linear model, boot and noboot versions will give identical inference, though when using survival outcomes, the 'boot' version uses simulation based inference, which can vary from the 'noboot' version due to simulation error (which can be minimized via setting the MCsize parameter very large - see qgcomp.cox.boot for details).

Usage

qgcomp(f, data = data, family = gaussian(), rr = TRUE, ...)

Arguments

f	R style formula (may include survival outcome via Surv)
data	data frame
family	<pre>gaussian(), binomial(), cox(), poisson() (works as argument to 'family' parameter in glm' or 'dist' parameter in zeroinfl)</pre>

rr	logical: if using binary outcome and rr=TRUE, qgcomp.boot will estimate risk
	ratio rather than odds ratio. Note, to get population average effect estimates
	for a binary outcome, set rr=TRUE (default: ORs are generally not of interest
	as population average effects, so if rr=FALSE then a conditional OR will be estimated, which cannot be interpreted as a population average effect
	arguments to qgcomp.noboot or qgcomp.boot (e.g. q) or glm

Value

a qgcompfit object, which contains information about the effect measure of interest (psi) and associated variance (var.psi), as well as information on the model fit (fit) and possibly information on the marginal structural model (msmfit) used to estimate the final effect estimates (qgcomp.boot, qgcomp.cox.boot only). If appropriate, weights are also reported, which represent the proportion of a directional (positive/negative) effect that is accounted for by each exposure.

See Also

qgcomp.noboot, qgcomp.boot, qgcomp.cox.noboot, qgcomp.cox.boot qgcomp.zi.noboot and qgcomp.zi.boot (qgcomp is just a wrapper for these functions)

Examples

```
set.seed(50)
dat <- data.frame(y=runif(50), x1=runif(50), x2=runif(50), z=runif(50))</pre>
qgcomp.noboot(y \sim z + x1 + x2, expnms = c('x1', 'x2'), data=dat, q=2)
qgcomp.boot(y \sim z + x1 + x2, expnms = c('x1', 'x2'), data=dat, q=2, B=10, seed=125)
# automatically selects appropriate method
qgcomp(y \sim z + x1 + x2, expnms = c('x1', 'x2'), data=dat, q=2)
# note for binary outcome this will choose the risk ratio (and bootstrap methods) by default
dat <- data.frame(y=rbinom(100, 1, 0.5), x1=runif(100), x2=runif(100), z=runif(100))</pre>
## Not run:
qgcomp.noboot(y \sim z + x1 + x2, expnms = c('x1', 'x2'), data=dat, q=2, family=binomial())
set.seed(1231)
qgcomp.boot(y \sim z + x1 + x2, expnms = c('x1', 'x2'), data=dat, q=2, family=binomial())
set.seed(1231)
qgcomp(y \sim z + x1 + x2, expnms = c('x1', 'x2'), data=dat, q=2, family=binomial())
# automatically selects appropriate method when specifying rr or degree explicitly
qgcomp(y \sim z + x1 + x2, expnms = c('x1', 'x2'), data=dat, q=2, family=binomial(), rr=FALSE)
qgcomp(y \sim z + x1 + x2, expnms = c('x1', 'x2'), data=dat, q=2, family=binomial(), rr=TRUE)
qgcomp(y \sim z + factor(x1) + factor(x2), degree=2, expnms = c('x1', 'x2'), data=dat, q=4,
family=binomial())
#survival objects
set.seed(50)
N=200
dat <- data.frame(time=(tmg <- pmin(.1,rweibull(N, 10, 0.1))),</pre>
                d=1.0*(tmg<0.1), x1=runif(N), x2=runif(N), z=runif(N))</pre>
expnms=paste0("x", 1:2)
f = survival::Surv(time, d)~x1 + x2
qgcomp(f, expnms = expnms, data = dat)
```

qgcomp.boot

```
# note if B or MCsize are set but the model is linear, an error will result
try(qgcomp(f, expnms = expnms, data = dat, B1=, MCsize))
# note that in the survival models, MCsize should be set to a large number
# such that results are repeatable (within an error tolerance such as 2 significant digits)
# if you run them under different seed values
f = survival::Surv(time, d)~x1 + x2 + x1:x2
qgcomp(f, expnms = expnms, data = dat, B=10, MCsize=100)
## End(Not run)
```

```
qgcomp.boot
```

Quantile g-computation for continuous and binary outcomes

Description

This function estimates a linear dose-response parameter representing a one quantile increase in a set of exposures of interest. This model estimates the parameters of a marginal structural model (MSM) based on g-computation with quantized exposures. Note: this function allows linear and non-additive effects of individual components of the exposure, as well as non-linear joint effects of the mixture via polynomial basis functions, which increase the computational computational burden due to the need for non-parametric bootstrapping.

Usage

```
qgcomp.boot(
  f,
  data,
  expnms = NULL,
  q = 4,
 breaks = NULL,
  id = NULL,
 weights,
  alpha = 0.05,
 B = 200,
  rr = TRUE,
  degree = 1,
  seed = NULL,
 bayes = FALSE,
 MCsize = nrow(data),
  parallel = FALSE,
  . . .
)
```

Arguments

f	R style formula
data	data frame

expnms	character vector of exposures of interest
q	NULL or number of quantiles used to create quantile indicator variables representing the exposure variables. If NULL, then gcomp proceeds with untransformed version of exposures in the input datasets (useful if data are already transformed, or for performing standard g-computation)
breaks	(optional) NULL, or a list of (equal length) numeric vectors that characterize the minimum value of each category for which to break up the variables named in expnms. This is an alternative to using 'q' to define cutpoints.
id	(optional) NULL, or variable name indexing individual units of observation (only needed if analyzing data with multiple observations per id/cluster). Note that qgcomp.noboot will not produce cluster-appropriate standard errors. Qg- comp.boot can be used for this, which will use bootstrap sampling of clus- ters/individuals to estimate cluster-appropriate standard errors via bootstrap- ping.
weights	"case weights" - passed to the "weight" argument of glm or bayesglm
alpha	alpha level for confidence limit calculation
В	integer: number of bootstrap iterations (this should typically be >=200, though it is set lower in examples to improve run-time).
rr	logical: if using binary outcome and rr=TRUE, qgcomp.boot will estimate risk ratio rather than odds ratio
degree	polynomial bases for marginal model (e.g. degree = 2 allows that the relation- ship between the whole exposure mixture and the outcome is quadratic (default = 1).
seed	integer or NULL: random number seed for replicable bootstrap results
bayes	use underlying Bayesian model (arm package defaults). Results in penalized parameter estimation that can help with very highly correlated exposures. Note: this does not lead to fully Bayesian inference in general, so results should be interpreted as frequentist.
MCsize	integer: sample size for simulation to approximate marginal zero inflated model parameters. This can be left small for testing, but should be as large as needed to reduce simulation error to an acceptable magnitude (can compare psi coeffi- cients for linear fits with qgcomp.noboot to gain some intuition for the level of expected simulation error at a given value of MCsize). This likely won't matter much in linear models, but may be important with binary or count outcomes.
parallel	use (safe) parallel processing from the future and future.apply packages
	arguments to glm (e.g. family)

Details

Estimates correspond to the average expected change in the (log) outcome per quantile increase in the joint exposure to all exposures in 'expnms'. Test statistics and confidence intervals are based on a non-parametric bootstrap, using the standard deviation of the bootstrap estimates to estimate the standard error. The bootstrap standard error is then used to estimate Wald-type confidence intervals. Note that no bootstrapping is done on estimated quantiles of exposure, so these are treated as fixed quantities

qgcomp.boot

Value

a qgcompfit object, which contains information about the effect measure of interest (psi) and associated variance (var.psi), as well as information on the model fit (fit) and information on the marginal structural model (msmfit) used to estimate the final effect estimates.

See Also

qgcomp.noboot, and qgcomp

Examples

```
set.seed(30)
# continuous outcome
dat <- data.frame(y=rnorm(100), x1=runif(100), x2=runif(100), z=runif(100))</pre>
# Conditional linear slope
qgcomp.noboot(y \sim z + x1 + x2, expnms = c('x1', 'x2'), data=dat, q=4, family=gaussian())
# Marginal linear slope (population average slope, for a purely linear,
# additive model this will equal the conditional)
## Not run:
qgcomp.boot(f=y \sim z + x1 + x2, expnms = c('x1', 'x2'), data=dat, q=4,
 family=gaussian(), B=200) # B should be at least 200 in actual examples
# Population average mixture slope which accounts for non-linearity and interactions
qgcomp.boot(y \sim z + x1 + x2 + I(x1^2) + I(x2*x1), family="gaussian",
expnms = c('x1', 'x2'), data=dat, q=4, B=200)
# generally non-linear/non-addiive underlying models lead to non-linear mixture slopes
qgcomp.boot(y \sim z + x1 + x2 + I(x1^2) + I(x2*x1), family="gaussian",
expnms = c('x1', 'x2'), data=dat, q=4, B=200, deg=2)
# binary outcome
dat <- data.frame(y=rbinom(50,1,0.5), x1=runif(50), x2=runif(50), z=runif(50))
# Conditional mixture OR
qgcomp.noboot(y ~ z + x1 + x2, family="binomial", expnms = c('x1', 'x2'),
 data=dat, q=2)
#Marginal mixture OR (population average OR – in general, this will not equal the
# conditional mixture OR due to non-collapsibility of the OR)
qgcomp.boot(y \sim z + x1 + x2, family="binomial", expnms = c('x1', 'x2'),
 data=dat, q=2, B=3, rr=FALSE)
# Population average mixture RR
qgcomp.boot(y ~ z + x1 + x2, family="binomial", expnms = c('x1', 'x2'),
 data=dat, q=2, rr=TRUE, B=3)
# Population average mixture RR, indicator variable representation of x2
# note that I(x==...) operates on the quantile-based category of x,
# rather than the raw value
res = qgcomp.boot(y ~ z + x1 + I(x2==1) + I(x2==2) + I(x2==3),
 family="binomial", expnms = c('x1', 'x2'), data=dat, q=4, rr=TRUE, B=200)
res$fit
```

```
plot(res)
# now add in a non-linear MSM
res2 = qgcomp.boot(y ~ z + x1 + I(x2==1) + I(x2==2) + I(x2==3),
 family="binomial", expnms = c('x1', 'x2'), data=dat, q=4, rr=TRUE, B=200,
 degree=2)
res2$fit
res2$msmfit # correct point estimates, incorrect standard errors
res2 # correct point estimates, correct standard errors
plot(res2)
# Log risk ratio per one IQR change in all exposures (not on quantile basis)
dat$x1iqr <- dat$x1/with(dat, diff(quantile(x1, c(.25, .75))))</pre>
dat$x2iqr <- dat$x2/with(dat, diff(quantile(x2, c(.25, .75))))</pre>
# note that I(x>...) now operates on the untransformed value of x,
# rather than the quantized value
res2 = qgcomp.boot(y ~ z + x1iqr + I(x2iqr>0.1) + I(x2>0.4) + I(x2>0.9),
 family="binomial", expnms = c('x1iqr', 'x2iqr'), data=dat, q=NULL, rr=TRUE, B=200,
 degree=2)
res2
# using parallel processing
qgcomp.boot(y ~ z + x1iqr + I(x2iqr>0.1) + I(x2>0.4) + I(x2>0.9),
 family="binomial", expnms = c('x1iqr', 'x2iqr'), data=dat, q=NULL, rr=TRUE, B=200,
 degree=2, parallel=TRUE)
# weighted model
N=5000
dat4 <- data.frame(id=1:N, x1=runif(N), x2=runif(N), z=runif(N))</pre>
dat4$y <- with(dat4, rnorm(N, x1*z + z, 1))</pre>
dat4$w=runif(N) + dat4$z*5
qdata = quantize(dat4, expnms = c("x1", "x2"), q=4)$data
# first equivalent models with no covariates
qgcomp.noboot(f=y ~ x1 + x2, expnms = c('x1', 'x2'), data=dat4, q=4, family=gaussian())
qgcomp.noboot(f=y ~ x1 + x2, expnms = c('x1', 'x2'), data=dat4, q=4, family=gaussian(),
              weights=w)
set.seed(13)
qgcomp.boot(f=y ~ x1 + x2, expnms = c('x1', 'x2'), data=dat4, q=4, family=gaussian(),
            weights=w)
# using the correct model
set.seed(13)
qgcomp.boot(f=y ~ x1*z + x2, expnms = c('x1', 'x2'), data=dat4, q=4, family=gaussian(),
            weights=w, id="id")
(qgcfit <- qgcomp.boot(f=y ~ z + x1 + x2, expnms = c('x1', 'x2'), data=dat4, q=4,
                       family=gaussian(), weights=w))
qgcfit$fit
summary(glm(y ~ z + x1 + x2, data = qdata, weights=w))
## End(Not run)
```

qgcomp.cox.boot

Description

This function yields population average effect estimates for (possibly right censored) time-to event outcomes

Usage

```
qgcomp.cox.boot(
  f,
 data,
 expnms = NULL,
 q = 4,
 breaks = NULL,
 id = NULL,
 weights,
 cluster = NULL,
 alpha = 0.05,
 B = 200,
 MCsize = 10000,
 degree = 1,
 seed = NULL,
 parallel = FALSE,
  . . .
)
```

Arguments

f	R style survival formula, which includes Surv in the outcome definition. E.g. Surv(time, event) ~ exposure. Offset terms can be included via Surv(time, event) ~ exposure + offset(z)
data	data frame
expnms	character vector of exposures of interest
q	NULL or number of quantiles used to create quantile indicator variables representing the exposure variables. If NULL, then gcomp proceeds with untransformed version of exposures in the input datasets (useful if data are already transformed, or for performing standard g-computation)
breaks	(optional) NULL, or a list of (equal length) numeric vectors that characterize the minimum value of each category for which to break up the variables named in expnms. This is an alternative to using 'q' to define cutpoints.
id	(optional) NULL, or variable name indexing individual units of observation (only needed if analyzing data with multiple observations per id/cluster). Note

	that qgcomp.noboot will not produce cluster-appropriate standard errors. Qg- comp.boot can be used for this, which will use bootstrap sampling of clus- ters/individuals to estimate cluster-appropriate standard errors via bootstrap- ping.
weights	"case weights" - passed to the "weight" argument of coxph
cluster	not yet implemented
alpha	alpha level for confidence limit calculation
В	integer: number of bootstrap iterations (this should typically be >=200, though it is set lower in examples to improve run-time).
MCsize	integer: sample size for simulation to approximate marginal hazards ratios (if < sample size, then set to sample size). Note that large values will slow down the fitting, but will result in higher accuracy - if you run the function multiple times you will see that results vary due to simulation error. Ideally, MCsize would be set such that simulation error is negligible in the precision reported (e.g. if you report results to 2 decimal places, then MCsize should be set high enough that you consistenty get answers that are the same to 2 decimal places).
degree	polynomial bases for marginal model (e.g. degree = 2 allows that the relation- ship between the whole exposure mixture and the outcome is quadratic.
seed	integer or NULL: random number seed for replicable bootstrap results
parallel	logical (default FALSE): use future package to speed up bootstrapping
	arguments to glm (e.g. family)

Details

qgcomp.cox.boot' estimates the log(hazard ratio) per quantile increase in the joint exposure to all exposures in expnms'. This function uses g-computation to estimate the parameters of a marginal structural model for the population average effect of increasing all exposures in 'expnms' by a single quantile. This approach involves specifying an underlying conditional outcome model, given all exposures of interest (possibly with non-linear basis function representations such as splines or product terms) and confounders or covariates of interest. This model is fit first, which is used to generate expected outcomes at each quantile of all exposures, which is then used in a second model to estimate a population average dose-response curve that is linear or follows a simple polynomial function. See section on MCSize below

Test statistics and confidence intervals are based on a non-parametric bootstrap, using the standard deviation of the bootstrap estimates to estimate the standard error. The bootstrap standard error is then used to estimate Wald-type confidence intervals. Note that no bootstrapping is done on estimated quantiles of exposure, so these are treated as fixed quantiles

MCSize is crucial to get accurate point estimates. In order to get marginal estimates of the population hazard under different values of the joint exposure at a given quantile for all exposures in expnms, qgcomp.cox.boot uses Monte Carlo simulation to generate outcomes implied by the underlying conditional model and then fit a separate (marginal structural) model to those outcomes. In order to get accurate results that don't vary much from run-to-run of this approach, MCsize must be set large enough so that results are stable across runs according to a pre-determined precision (e.g. 2 significant digits).

qgcomp.cox.noboot

Value

a qgcompfit object, which contains information about the effect measure of interest (psi) and associated variance (var.psi), as well as information on the model fit (fit) and information on the marginal structural model (msmfit) used to estimate the final effect estimates.

See Also

qgcomp.cox.noboot, and qgcomp

Examples

```
set.seed(50)
N=200
dat <- data.frame(time=(tmg <- pmin(.1,rweibull(N, 10, 0.1))),</pre>
                d=1.0*(tmg<0.1), x1=runif(N), x2=runif(N), z=runif(N))</pre>
expnms=paste0("x", 1:2)
f = survival::Surv(time, d)~x1 + x2
(fit1 <- survival::coxph(f, data = dat))</pre>
(obj <- qgcomp.cox.noboot(f, expnms = expnms, data = dat))</pre>
## Not run:
# not run (slow when using boot version to proper precision)
(obj2 <- qgcomp.cox.boot(f, expnms = expnms, data = dat, B=10, MCsize=20000))
# weighted analysis
# using future package, marginalizing over confounder z
(obj3 <- qgcomp.cox.boot(survival::Surv(time, d)~x1 + x2 + z, expnms = expnms, data = dat,</pre>
                          B=1000, MCsize=20000, parallel=TRUE))
# non-constant hazard ratio, non-linear terms
(obj4 <- qgcomp.cox.boot(survival::Surv(time, d)~factor(x1) + splines::bs(x2) + z,</pre>
                          expnms = expnms, data = dat,
                          B=1000, MCsize=20000, parallel=FALSE, degree=1))
# weighted analysis
dat$w = runif(N)
(objw1 <- qgcomp.cox.noboot(f, expnms = expnms, data = dat, weights=w))</pre>
(objw2 <- qgcomp.cox.boot(f, expnms = expnms, data = dat, weights=w, B=5, MCsize=20000))
## End(Not run)
```

qgcomp.cox.noboot Quantile g-computation for survival outcomes under linearity/additivity

Description

This function performs quantile g-computation in a survival setting. The approach estimates the covariate-conditional hazard ratio for a joint change of 1 quantile in each exposure variable specified in expnms parameter

Usage

```
qgcomp.cox.noboot(
   f,
   data,
   expnms = NULL,
   q = 4,
   breaks = NULL,
   id = NULL,
   weights,
   cluster = NULL,
   alpha = 0.05,
   ...
)
```

Arguments

f	R style survival formula, which includes Surv in the outcome definition. E.g. Surv(time, event) ~ exposure. Offset terms can be included via Surv(time, event) ~ exposure + offset(z)
data	data frame
expnms	character vector of exposures of interest
q	NULL or number of quantiles used to create quantile indicator variables rep- resenting the exposure variables. If NULL, then gcomp proceeds with un- transformed version of exposures in the input datasets (useful if data are already transformed, or for performing standard g-computation)
breaks	(optional) NULL, or a list of (equal length) numeric vectors that characterize the minimum value of each category for which to break up the variables named in expnms. This is an alternative to using 'q' to define cutpoints.
id	(optional) NULL, or variable name indexing individual units of observation (only needed if analyzing data with multiple observations per id/cluster)
weights	"case weights" - passed to the "weight" argument of coxph
cluster	not yet implemented
alpha	alpha level for confidence limit calculation
	arguments to glm (e.g. family)

Details

For survival outcomes (as specified using methods from the survival package), this yields a conditional log hazard ratio representing a change in the expected conditional hazard (conditional on covariates) from increasing every exposure by 1 quantile. In general, this quantity quantity is not equivalent to g-computation estimates. Hypothesis test statistics and 95% confidence intervals are based on using the delta estimate variance of a linear combination of random variables.

Value

a qgcompfit object, which contains information about the effect measure of interest (psi) and associated variance (var.psi), as well as information on the model fit (fit) and information on the weights/standardized coefficients in the positive (pos.weights) and negative (neg.weights) directions.

See Also

gcomp.cox.boot, gcomp.boot, and gcomp

Examples

```
set.seed(50)
N=200
dat <- data.frame(time=(tmg <- pmin(.1,rweibull(N, 10, 0.1))),</pre>
                d=1.0*(tmg<0.1), x1=runif(N), x2=runif(N), z=runif(N))</pre>
expnms=paste0("x", 1:2)
f = survival::Surv(time, d)~x1 + x2
(fit1 <- survival::coxph(f, data = dat))</pre>
(obj <- qgcomp.cox.noboot(f, expnms = expnms, data = dat))</pre>
## Not run:
# weighted analysis
dat$w = runif(N)
qdata = quantize(dat, expnms=expnms)
(obj2 <- qgcomp.cox.noboot(f, expnms = expnms, data = dat, weight=w))</pre>
obj2$fit
survival::coxph(f, data = qdata$data, weight=w)
# not run: bootstrapped version is much slower
(obj2 <- qgcomp.cox.boot(f, expnms = expnms, data = dat, B=200, MCsize=20000))
## End(Not run)
```

gcomp.hurdle.boot *Quantile g-computation for hurdle count outcomes*

Description

This function estimates a linear dose-response parameter representing a one quantile increase in a set of exposures of interest for hurdle count outcomes. This function is limited to linear and additive effects of individual components of the exposure. This model estimates the parameters of a marginal structural hurdle count model (MSM) based on g-computation with quantized exposures. Note: this function allows linear and non-additive effects of individual components of the exposure, as well as non-linear joint effects of the mixture via polynomial basis functions, which increase the computational computational burden due to the need for non-parametric bootstrapping.

Usage

```
qgcomp.hurdle.boot(
 f,
 data,
 expnms = NULL,
 q = 4,
 breaks = NULL,
 id = NULL,
 weights,
 alpha = 0.05,
 B = 200,
 degree = 1,
  seed = NULL,
 bayes = FALSE,
 parallel = FALSE,
 MCsize = 10000,
 msmcontrol = hurdlemsm.fit.control(),
  . . .
)
```

Arguments

f	R style formula
data	data frame
expnms	character vector of exposures of interest
q	NULL or number of quantiles used to create quantile indicator variables rep- resenting the exposure variables. If NULL, then gcomp proceeds with un- transformed version of exposures in the input datasets (useful if data are already transformed, or for performing standard g-computation)
breaks	(optional) NULL, or a list of (equal length) numeric vectors that characterize the minimum value of each category for which to break up the variables named in expnms. This is an alternative to using 'q' to define cutpoints.
id	(optional) NULL, or variable name indexing individual units of observation (only needed if analyzing data with multiple observations per id/cluster)
weights	"case weights" - passed to the "weight" argument of hurdle. NOTE - this does not work with parallel=TRUE!
alpha	alpha level for confidence limit calculation
В	integer: number of bootstrap iterations (this should typically be >=200, though it is set lower in examples to improve run-time).
degree	polynomial basis function for marginal model (e.g. degree = 2 allows that the relationship between the whole exposure mixture and the outcome is quadratic.
seed	integer or NULL: random number seed for replicable bootstrap results
bayes	not currently implemented.
parallel	use (safe) parallel processing from the future and future.apply packages

MCsize	integer: sample size for simulation to approximate marginal zero inflated model
	parameters. This can be left small for testing, but should be as large as needed
	to reduce simulation error to an acceptable magnitude (can compare psi coeffi-
	cients for linear fits with qgcomp.hurdle.noboot to gain some intuition for the
	level of expected simulation error at a given value of MCsize)
msmcontrol	named list from hurdlemsm.fit.control
	arguments to glm (e.g. family)

Details

Hurdle count models allow excess zeros in standard count outcome (e.g. Poisson distributed outcomes). Such models have two components: 1) the probability of arising from a degenerate distribution at zero (versus arising from a count distribution) and 2) the rate parameter of a (possibly truncated > 0) count distribution. Thus, one has the option of allowing exposure and covariate effects on the zero distribution, the count distribution, or both. The zero distribution parameters correspond to log-odds ratios for the probability of arising from the zero distribution. Count distribution parameters. Test statistics and confidence intervals are based on a non-parametric bootstrap, using the standard deviation of the bootstrap estimates to estimate the standard error. The bootstrap standard error is then used to estimate Wald-type confidence intervals. Note that no bootstrapping is done on estimated quantiles of exposure, so these are treated as fixed quantities.

Of note, this function yields marginal estimates of the expected outcome under values of the joint exposure quantiles (e.g. the expected outcome if all exposures are below the 1st quartile). These outcomes can be used to derive estimates of the effect on the marginal expectation of the outcome, irrespective of zero/count portions of the statistical model.

Estimates correspond to the average expected change in the (log) outcome per quantile increase in the joint exposure to all exposures in 'expnms'. Test statistics and confidence intervals are based on a non-parametric bootstrap, using the standard deviation of the bootstrap estimates to estimate the standard error. The bootstrap standard error is then used to estimate Wald-type confidence intervals. Note that no bootstrapping is done on estimated quantiles of exposure, so these are treated as fixed quantities

Value

a qgcompfit object, which contains information about the effect measure of interest (psi) and associated variance (var.psi), as well as information on the model fit (fit) and information on the marginal structural model (msmfit) used to estimate the final effect estimates.

See Also

qgcomp.hurdle.noboot,qgcomp.boot,qgcomp.cox.boot, and hurdle

Examples

```
set.seed(50)
n=500
dat <- data.frame(y=rbinom(n, 1, 0.5)*rpois(n, 1.2), x1=runif(n), x2=runif(n), z=runif(n))
# poisson count model, mixture in both portions
## Not run:</pre>
```

```
# warning: the examples below can take a long time to run
res = qgcomp.hurdle.boot(f=y ~ x1 + x2 | x1 + x2, expnms = c('x1', 'x2'),
    data=dat, q=4, dist="poisson", B=1000, MCsize=10000, parallel=TRUE)
qgcomp.hurdle.noboot(f=y \sim x1 + x2 | x1 + x2, expnms = c('x1', 'x2'),
   data=dat, q=4, dist="poisson")
res
# accuracy for small MCsize is suspect (compare coefficients between boot/noboot versions),
# so re-check with MCsize set to larger value (this takes a long time to run)
res2 = qgcomp.hurdle.boot(f=y ~ x1 + x2 | x1 + x2, expnms = c('x1', 'x2'),
    data=dat, q=4, dist="poisson", B=1000, MCsize=50000, parallel=TRUE)
res2
plot(density(res2$bootsamps[4,]))
# negative binomial count model, mixture and covariate in both portions
qgcomp.hurdle.boot(f=y ~ z + x1 + x2 | z + x1 + x2, expnms = c('x1', 'x2'),
  data=dat, q=4, dist="negbin", B=10, MCsize=10000)
# weighted analysis (NOTE THIS DOES NOT WORK WITH parallel=TRUE!)
dat = runif(n) *5
qgcomp.hurdle.noboot(f=y \sim z + x1 + x2 | x1 + x2, expnms = c('x1', 'x2'),
    data=dat, q=4, dist="poisson", weights=w)
# You may see this:
# Warning message:
# In eval(family$initialize) : non-integer #successes in a binomial glm!
qgcomp.hurdle.boot(f=y ~ x1 + x2 | x1 + x2, expnms = c('x1', 'x2'),
    data=dat, q=4, dist="poisson", B=5, MCsize=50000, parallel=FALSE, weights=w)
# Log rr per one IQR change in all exposures (not on quantile basis)
dat$x1iqr <- dat$x1/with(dat, diff(quantile(x1, c(.25, .75))))</pre>
dat$x2iqr <- dat$x2/with(dat, diff(quantile(x2, c(.25, .75))))</pre>
# note that I(x>...) now operates on the untransformed value of x,
# rather than the quantized value
res2 = qgcomp.hurdle.boot(f=y ~ z + x1iqr + x2iqr + I(x2iqr>0.1) +
                             I(x2iqr>0.4) + I(x2iqr>0.9) | x1iqr + x2iqr,
                   expnms = c('x1iqr', 'x2iqr'),
                   data=dat, q=NULL, B=2, degree=2, MCsize=2000, dist="poisson")
res2
## End(Not run)
```

gcomp.hurdle.noboot Quantile g-computation for hurdle count outcomes under linearity/additivity

Description

This function estimates a linear dose-response parameter representing a one quantile increase in a set of exposures of interest for hurdle count outcomes. This function is limited to linear and additive effects of individual components of the exposure. This model estimates the parameters of a marginal structural hurdle model (MSM) based on g-computation with quantized exposures.

qgcomp.hurdle.noboot

Note: this function is valid only under linear and additive effects of individual components of the exposure, but when these hold the model can be fit with very little computational burden.

Usage

```
qgcomp.hurdle.noboot(
   f,
   data,
   expnms = NULL,
   q = 4,
   breaks = NULL,
   id = NULL,
   weights,
   alpha = 0.05,
   bayes = FALSE,
   ...
)
```

Arguments

f	R style formula using syntax from 'pscl' package: depvar ~ indvars_count indvars_zero
data	data frame
expnms	character vector of exposures of interest
q	NULL or number of quantiles used to create quantile indicator variables representing the exposure variables. If NULL, then gcomp proceeds with untransformed version of exposures in the input datasets (useful if data are already transformed, or for performing standard g-computation)
breaks	(optional) NULL, or a list of (equal length) numeric vectors that characterize the minimum value of each category for which to break up the variables named in expnms. This is an alternative to using 'q' to define cutpoints.
id	(optional) NULL, or variable name indexing individual units of observation (only needed if analyzing data with multiple observations per id/cluster)
weights	"case weights" - passed to the "weight" argument of hurdle.
alpha	alpha level for confidence limit calculation
bayes	not yet implemented
	arguments to hurdle (e.g. dist)

Details

A hurdle version of quantile g-computation based on the implementation in the 'pscl' package. A hurdle distribution is a mixture distribution in which one of the distributions is a point mass at zero (with probability given by a logistic model), and the other distribution is a discrete or continuous distribution. This estimates the effect of a joint increase in all exposures on 1) the odds of belonging to the "zero" vs. "count" portions of the distribution and/or 2) the rate parameter for the "count" portion of the distribution.

Value

a qgcompfit object, which contains information about the effect measure of interest (psi) and associated variance (var.psi), as well as information on the model fit (fit) and information on the weights/standardized coefficients in the positive (pos.weights) and negative (neg.weights) directions.

See Also

qgcomp.hurdle.boot,qgcomp.noboot, qgcomp.cox.noboot, and hurdle

Examples

```
set.seed(50)
n=100
dat <- data.frame(y=rbinom(n, 1, 0.5)*rpois(n, 1.2), x1=runif(n), x2=runif(n), z=runif(n))</pre>
# poisson count model, mixture in both portions
qgcomp.hurdle.noboot(f=y ~ z + x1 + x2 | x1 + x2, expnms = c('x1', 'x2'),
    data=dat, q=2, dist="poisson")
# negative binomial count model, mixture and covariate in both portions
qgcomp.hurdle.noboot(f=y ~ z + x1 + x2 | z + x1 + x2, expnms = c('x1', 'x2'),
   data=dat, q=2, dist="negbin")
qgcomp.hurdle.noboot(f=y \sim z + x1 + x2, expnms = c('x1', 'x2'),
   data=dat, q=2, dist="negbin") # equivalent
# negative binomial count model, mixture only in the 'count' portion of the model
qgcomp.hurdle.noboot(f=y ~ z + x1 + x2 | z, expnms = c('x1', 'x2'), data=dat, q=2, dist="negbin")
# weighted analysis
dat$w = runif(n)*5
qgcomp.hurdle.noboot(f=y \sim z + x1 + x2 | x1 + x2, expnms = c('x1', 'x2'),
    data=dat, q=2, dist="poisson", weights=w)
# Expect this:
# Warning message:
# In eval(family$initialize) : non-integer #successes in a binomial glm!
```

qgcomp.noboot

Quantile g-computation for continuous, binary, and count outcomes under linearity/additivity

Description

This function estimates a linear dose-response parameter representing a one quantile increase in a set of exposures of interest. This function is limited to linear and additive effects of individual components of the exposure. This model estimates the parameters of a marginal structural model (MSM) based on g-computation with quantized exposures. Note: this function is valid only under linear and additive effects of individual components of the exposure, but when these hold the model can be fit with very little computational burden.

qgcomp.noboot

Usage

```
qgcomp.noboot(
   f,
   data,
   expnms = NULL,
   q = 4,
   breaks = NULL,
   id = NULL,
   weights,
   alpha = 0.05,
   bayes = FALSE,
   ...
)
```

Arguments

f	R style formula
data	data frame
expnms	character vector of exposures of interest
q	NULL or number of quantiles used to create quantile indicator variables representing the exposure variables. If NULL, then gcomp proceeds with untransformed version of exposures in the input datasets (useful if data are already transformed, or for performing standard g-computation)
breaks	(optional) NULL, or a list of (equal length) numeric vectors that characterize the minimum value of each category for which to break up the variables named in expnms. This is an alternative to using 'q' to define cutpoints.
id	(optional) NULL, or variable name indexing individual units of observation (only needed if analyzing data with multiple observations per id/cluster). Note that qgcomp.noboot will not produce cluster-appropriate standard errors (this parameter is essentially ignored in qgcomp.noboot). Qgcomp.boot can be used for this, which will use bootstrap sampling of clusters/individuals to estimate cluster-appropriate standard errors via bootstrapping.
weights	"case weights" - passed to the "weight" argument of glm or bayesglm
alpha	alpha level for confidence limit calculation
bayes	use underlying Bayesian model (arm package defaults). Results in penalized parameter estimation that can help with very highly correlated exposures. Note: this does not lead to fully Bayesian inference in general, so results should be interpreted as frequentist.
•••	arguments to glm (e.g. family)

Details

For continuous outcomes, under a linear model with no interaction terms, this is equivalent to gcomputation of the effect of increasing every exposure by 1 quantile. For binary/count outcomes outcomes, this yields a conditional log odds/rate ratio(s) representing the change in the expected conditional odds/rate (conditional on covariates) from increasing every exposure by 1 quantile. In general, the latter quantity is not equivalent to g-computation estimates. Hypothesis test statistics and confidence intervals are based on using the delta estimate variance of a linear combination of random variables.

Value

a qgcompfit object, which contains information about the effect measure of interest (psi) and associated variance (var.psi), as well as information on the model fit (fit) and information on the weights/standardized coefficients in the positive (pos.weights) and negative (neg.weights) directions.

See Also

qgcomp.boot, and qgcomp

Examples

```
set.seed(50)
# linear model
dat <- data.frame(y=runif(50), x1=runif(50), x2=runif(50), z=runif(50))</pre>
qgcomp.noboot(f=y ~ z + x1 + x2, expnms = c('x1', 'x2'), data=dat, q=2, family=gaussian())
# logistic model
dat2 <- data.frame(y=rbinom(50, 1,0.5), x1=runif(50), x2=runif(50), z=runif(50))
qgcomp.noboot(f=y ~ z + x1 + x2, expnms = c('x1', 'x2'), data=dat2, q=2, family=binomial())
# poisson model
dat3 <- data.frame(y=rpois(50, .5), x1=runif(50), x2=runif(50), z=runif(50))</pre>
qgcomp.noboot(f=y ~ z + x1 + x2, expnms = c('x1', 'x2'), data=dat3, q=2, family=poisson())
# weighted model
N=5000
dat4 <- data.frame(y=runif(N), x1=runif(N), x2=runif(N), z=runif(N))</pre>
dat4$w=runif(N)*2
qdata = quantize(dat4, expnms = c("x1", "x2"))$data
(qgcfit <- qgcomp.noboot(f=y ~ z + x1 + x2, expnms = c('x1', 'x2'), data=dat4, q=4,
                         family=gaussian(), weights=w))
qgcfit$fit
glm(y \sim z + x1 + x2, data = qdata, weights=w)
```

qgcomp.partials Partial effect sizes, confidence intervals, hypothesis tests

Description

Obtain effect estimates for "partial positive" and "partial negative" effects using quantile g-computation. This approach uses sample splitting to evaluate the overall impact of a set of variables with effects in a single direction, where, using training data, all variables with effects in the same direction are grouped.

qgcomp.partials

Usage

```
qgcomp.partials(
  fun = c("qgcomp.noboot", "qgcomp.cox.noboot", "qgcomp.zi.noboot"),
  traindata = NULL,
  validdata = NULL,
  expnms = NULL,
  ...
)
```

Arguments

fun	character variable in the set "qgcomp.noboot" (binary, count, continuous out- comes), "qgcomp.cox.noboot" (survival outcomes), "qgcomp.zi.noboot" (zero inflated outcomes). This describes which qgcomp package function is used to fit the model. (default = "qgcomp.noboot")
traindata	Data frame with training data
validdata	Data frame with validation data
expnms	Exposure mixture of interest
	Arguments to qgcomp.noboot, qgcomp.cox.noboot, or qgcomp.zi.noboot

Details

In the basic (non bootstrapped) qgcomp functions, the positive and negative "sums of coefficients" or "partial effect sizes" are given, which equal the sum of the negative and positive coefficients in the underlying model. Unfortunately, these partial effects don't constitute variables for which we can derive confidence intervals or hypothesis tests, so they are mainly for exploratory purposes. By employing sample splitting, however, we can obtain better estimates of these partial effects.

Sample splitting proceeds by partitioning the data into two samples (40/60 training/validtion split seems acceptable in many circumstances). The "overall mixture effect" is then estimated in the training data, and the mixture variables with positive and negative coefficients are split into separate groups. These two different groups are then used as "the mixture of interest" in two additional qgcomp fits, where the mixture of interest is adjusted for the other exposure variables. For example, if the "positive partial effect" is of interest, then this effect is equal to the sum of the coefficients in the qgcomp model fit to the validation data, with the mixture of interest selected by the original fit to the training data (note that some of these coefficients may be negative in the fit to the validation data - this is expected and necessary for valid hypothesis tests).

The positive/negative partial effects are necessarily exploratory, but sample splitting preserves the statistical properties at the expense of wider confidence intervals and larger variances. The two resulting mixture groups groups should be inspected for

Value

A 'qgcompmultifit' object, which inherits from list, which contains

posmix character vector of variable names with positive coefficients in the qgcomp model fit to the training data

- **negmix** character vector of variable names with negative coefficients in the qgcomp model fit to the training data
- **pos.fit** a qgcompfit object fit to the validation data, in which the exposures of interest are contained in 'posmix'
- **neg.fit** a qgcompfit object fit to the validation data, in which the exposures of interest are contained in 'negmix'

```
set.seed(123223)
dat = qgcomp:::.dgm_quantized(N=1000, coef=c(0.25,-0.25,0,0), ncor=1)
cor(dat)
# overall fit (more or less null due to counteracting exposures)
(overall <- qgcomp.noboot(f=y~., q=NULL, expnms=c("x1", "x2", "x3", "x4"), data=dat))</pre>
# partial effects using 40% training/60% validation split
trainidx <- sample(1:nrow(dat), round(nrow(dat)*0.4))</pre>
valididx <- setdiff(1:nrow(dat),trainidx)</pre>
traindata = dat[trainidx,]
validdata = dat[valididx,]
splitres <- qgcomp:::qgcomp.partials(fun="qgcomp.noboot", f=y~., q=NULL,</pre>
    traindata=traindata,validdata=validdata, expnms=c("x1", "x2", "x3", "x4"))
splitres
## Not run:
# under the null, both should give null results
set.seed(123223)
dat <- ggcomp:::.dgm_quantized(N=1000, coef=c(0,0,0,0), ncor=1)</pre>
# 40% training/60% validation
trainidx2 <- sample(1:nrow(dat), round(nrow(dat)*0.4))</pre>
valididx2 <- setdiff(1:nrow(dat),trainidx2)</pre>
traindata2 <- dat[trainidx2,]</pre>
validdata2 <- dat[valididx2,]</pre>
splitres2 <- qgcomp:::gcomp.partials(fun="qgcomp.noboot", f=y~.,</pre>
   q=NULL, traindata=traindata2,validdata=validdata2, expnms=c("x1", "x2", "x3", "x4"))
splitres2
# 60% training/40% validation
trainidx3 <- sample(1:nrow(dat), round(nrow(dat)*0.6))</pre>
valididx3 <- setdiff(1:nrow(dat),trainidx3)</pre>
traindata3 <- dat[trainidx3,]</pre>
validdata3 <- dat[valididx3,]</pre>
splitres3 <- ggcomp:::ggcomp.partials(fun="ggcomp.noboot", f=y~., g=NULL,</pre>
    traindata=traindata3,validdata=validdata3, expnms=c("x1", "x2", "x3", "x4"))
splitres3
# survival outcome
set.seed(50)
N=1000
dat <- data.frame(time=(tmg <- pmin(.1,rweibull(N, 10, 0.1))),</pre>
     d=1.0*(tmg<0.1), x1=runif(N)+(tmg<0.1)*0.1, x2=runif(N)-(tmg<0.1)*0.1, x3=runif(N),
                       x4=runif(N), x5=runif(N), z=runif(N))
trainidx4 <- sample(1:nrow(dat), round(nrow(dat)*0.6))</pre>
```

```
valididx4 <- setdiff(1:nrow(dat),trainidx4)</pre>
traindata4 <- dat[trainidx4,]</pre>
validdata4 <- dat[valididx4,]</pre>
expnms=paste0("x", 1:5)
f = survival::Surv(time, d)~x1 + x2 + x3 + x4 + x5 + z
(fit1 <- survival::coxph(f, data = dat))</pre>
(overall <- qgcomp.cox.noboot(f, expnms = expnms, data = dat))</pre>
(splitres4 <- qgcomp:::qgcomp.partials(fun="qgcomp.cox.noboot", f=f, q=4,</pre>
                traindata=traindata4,validdata=validdata4,
                 expnms=expnms))
 # zero inflated count outcome
 set.seed(50)
 n=1000
dat <- data.frame(y= (yany <- rbinom(n, 1, 0.5))*(ycnt <- rpois(n, 1.2)), x1=runif(n)+ycnt*0.2,</pre>
                        x2=runif(n)-ycnt*0.2, x3=runif(n),
                       x4=runif(n) , z=runif(n))
 # poisson count model, mixture in both portions, but note that the qgcomp.partials
 # function defines the "positive" variables only by the count portion of the model
 (overall5 <- qgcomp.zi.noboot(f=y ~ z + x1 + x2 + x3 + x4 | x1 + x2 + x3 + x4 + z,
                  expnms = c("x1", "x2", "x3", "x4"),
                   data=dat, q=4, dist="poisson"))
trainidx5 <- sample(1:nrow(dat), round(nrow(dat)*0.6))</pre>
valididx5 <- setdiff(1:nrow(dat),trainidx5)</pre>
traindata5 <- dat[trainidx5,]</pre>
validdata5 <- dat[valididx5,]</pre>
splitres5 <- qgcomp.partials(fun="qgcomp.zi.noboot",</pre>
    f=y ~ x1 + x2 + x3 + x4 + z | x1 + x2 + x3 + x4 + z, q=4,
    traindata=traindata5, validdata=validdata5,
    expnms=c("x1", "x2", "x3", "x4"))
splitres5
## End(Not run)
```

gcomp.zi.boot Quantile g-computation for zero-inflated count outcomes

Description

This function estimates a linear dose-response parameter representing a one quantile increase in a set of exposures of interest for zero-inflated count outcomes. This function is limited to linear and additive effects of individual components of the exposure. This model estimates the parameters of a marginal structural zero-inflated count model (MSM) based on g-computation with quantized exposures. Note: this function allows linear and non-additive effects of individual components of the exposure, as well as non-linear joint effects of the mixture via polynomial basis functions, which increase the computational computational burden due to the need for non-parametric bootstrapping.

Usage

```
qgcomp.zi.boot(
 f,
  data,
  expnms = NULL,
  q = 4,
  breaks = NULL,
  id = NULL,
  weights,
  alpha = 0.05,
  B = 200,
  degree = 1,
  seed = NULL,
  bayes = FALSE,
  parallel = FALSE,
  MCsize = 10000,
  msmcontrol = zimsm.fit.control(),
  . . .
)
```

Arguments

f	R style formula
data	data frame
expnms	character vector of exposures of interest
q	NULL or number of quantiles used to create quantile indicator variables rep- resenting the exposure variables. If NULL, then gcomp proceeds with un- transformed version of exposures in the input datasets (useful if data are already transformed, or for performing standard g-computation)
breaks	(optional) NULL, or a list of (equal length) numeric vectors that characterize the minimum value of each category for which to break up the variables named in expnms. This is an alternative to using 'q' to define cutpoints.
id	(optional) NULL, or variable name indexing individual units of observation (only needed if analyzing data with multiple observations per id/cluster)
weights	"case weights" - passed to the "weight" argument of zeroinfl. NOTE - this does not work with parallel=TRUE!
alpha	alpha level for confidence limit calculation
В	integer: number of bootstrap iterations (this should typically be >=200, though it is set lower in examples to improve run-time).
degree	polynomial basis function for marginal model (e.g. degree = 2 allows that the relationship between the whole exposure mixture and the outcome is quadratic.
seed	integer or NULL: random number seed for replicable bootstrap results
bayes	not currently implemented.
parallel	use (safe) parallel processing from the future and future.apply packages

qgcomp.zi.boot

MCsize	integer: sample size for simulation to approximate marginal zero inflated model
	parameters. This can be left small for testing, but should be as large as needed
	to reduce simulation error to an acceptable magnitude (can compare psi coeffi-
	cients for linear fits with qgcomp.zi.noboot to gain some intuition for the level
	of expected simulation error at a given value of MCsize)
msmcontrol	named list from zimsm.fit.control
	arguments to glm (e.g. family)

Details

Zero-inflated count models allow excess zeros in standard count outcome (e.g. Poisson distributed outcomes). Such models have two components: 1) the probability of arising from a degenerate distribution at zero (versus arising from a count distribution) and 2) the rate parameter of a count distribution. Thus, one has the option of allowing exposure and covariate effects on the zero distribution, the count distribution, or both. The zero distribution parameters correspond to log-odds ratios for the probability of arising from the zero distribution. Count distribution parameters correspond to log-rate-ratio parameters. Test statistics and confidence intervals are based on a non-parametric bootstrap, using the standard deviation of the bootstrap estimates to estimate the standard error. The bootstrap standard error is then used to estimate Wald-type confidence intervals. Note that no bootstrapping is done on estimated quantiles of exposure, so these are treated as fixed quantities.

Of note, this function yields marginal estimates of the expected outcome under values of the joint exposure quantiles (e.g. the expected outcome if all exposures are below the 1st quartile). These outcomes can be used to derive estimates of the effect on the marginal expectation of the outcome, irrespective of zero-inflated/count portions of the statistical model.

Estimates correspond to the average expected change in the (log) outcome per quantile increase in the joint exposure to all exposures in 'expnms'. Test statistics and confidence intervals are based on a non-parametric bootstrap, using the standard deviation of the bootstrap estimates to estimate the standard error. The bootstrap standard error is then used to estimate Wald-type confidence intervals. Note that no bootstrapping is done on estimated quantiles of exposure, so these are treated as fixed quantities

Value

a qgcompfit object, which contains information about the effect measure of interest (psi) and associated variance (var.psi), as well as information on the model fit (fit) and information on the marginal structural model (msmfit) used to estimate the final effect estimates.

See Also

qgcomp.zi.noboot,qgcomp.boot,qgcomp.cox.boot, and zeroinfl

```
set.seed(50)
n=100
dat <- data.frame(y=rbinom(n, 1, 0.5)*rpois(n, 1.2), x1=runif(n), x2=runif(n), z=runif(n))
# poisson count model, mixture in both portions
## Not run:
# warning: the examples below can take a long time to run</pre>
```

```
res = qgcomp.zi.boot(f=y ~ x1 + x2 | x1 + x2, expnms = c('x1', 'x2'),
     data=dat, q=4, dist="poisson", B=1000, MCsize=10000, parallel=TRUE)
 qgcomp.zi.noboot(f=y ~ x1 + x2 | x1 + x2, expnms = c('x1', 'x2'),
     data=dat, q=4, dist="poisson")
 res
 # accuracy for small MCsize is suspect (compare coefficients between boot/noboot versions),
 # so re-check with MCsize set to larger value (this takes a long time to run)
 res2 = qgcomp.zi.boot(f=y ~ x1 + x2 | x1 + x2, expnms = c('x1', 'x2'),
     data=dat, q=4, dist="poisson", B=1000, MCsize=50000, parallel=TRUE)
  res2
 plot(density(res2$bootsamps[4,]))
 # negative binomial count model, mixture and covariate in both portions
 qgcomp.zi.boot(f=y ~ z + x1 + x2 | z + x1 + x2, expnms = c('x1', 'x2'),
    data=dat, q=4, dist="negbin", B=10, MCsize=10000)
 # weighted analysis (NOTE THIS DOES NOT WORK WITH parallel=TRUE!)
 dat$w = runif(n)*5
 qgcomp.zi.noboot(f=y \sim z + x1 + x2 | x1 + x2, expnms = c('x1', 'x2'),
     data=dat, q=4, dist="poisson", weights=w)
 # Expect this:
 # Warning message:
 # In eval(family$initialize) : non-integer #successes in a binomial glm!
 qgcomp.zi.boot(f=y ~ x1 + x2 | x1 + x2, expnms = c('x1', 'x2'),
     data=dat, q=4, dist="poisson", B=5, MCsize=50000, parallel=FALSE, weights=w)
 # Log rr per one IQR change in all exposures (not on quantile basis)
 dat$x1iqr <- dat$x1/with(dat, diff(quantile(x1, c(.25, .75))))</pre>
 dat$x2iqr <- dat$x2/with(dat, diff(quantile(x2, c(.25, .75))))</pre>
 # note that I(x>...) now operates on the untransformed value of x,
 # rather than the quantized value
 res2 = qgcomp.zi.boot(y ~ z + x1iqr + x2iqr + I(x2iqr>0.1) + I(x2>0.4) + I(x2>0.9) | x1iqr + x2iqr,
                   family="binomial", expnms = c('x1iqr', 'x2iqr'), data=dat, q=NULL, B=2,
                     degree=2, MCsize=200, dist="poisson")
 res2
 ## End(Not run)
                          Quantile g-computation for zero-inflated count outcomes under linear-
qgcomp.zi.noboot
```

Description

This function estimates a linear dose-response parameter representing a one quantile increase in a set of exposures of interest for zero-inflated count outcomes. This function is limited to linear and additive effects of individual components of the exposure. This model estimates the parameters of a marginal structural zero-inflated model (MSM) based on g-computation with quantized exposures. Note: this function is valid only under linear and additive effects of individual components of the exposure, but when these hold the model can be fit with very little computational burden.

ity/additivity

qgcomp.zi.noboot

Usage

```
qgcomp.zi.noboot(
   f,
   data,
   expnms = NULL,
   q = 4,
   breaks = NULL,
   id = NULL,
   weights,
   alpha = 0.05,
   bayes = FALSE,
   ...
)
```

Arguments

f	R style formula using syntax from 'pscl' package: depvar ~ indvars_count indvars_zero
data	data frame
expnms	character vector of exposures of interest
q	NULL or number of quantiles used to create quantile indicator variables representing the exposure variables. If NULL, then gcomp proceeds with untransformed version of exposures in the input datasets (useful if data are already transformed, or for performing standard g-computation)
breaks	(optional) NULL, or a list of (equal length) numeric vectors that characterize the minimum value of each category for which to break up the variables named in expnms. This is an alternative to using 'q' to define cutpoints.
id	(optional) NULL, or variable name indexing individual units of observation (only needed if analyzing data with multiple observations per id/cluster)
weights	"case weights" - passed to the "weight" argument of zeroinfl.
alpha	alpha level for confidence limit calculation
bayes	not yet implemented
	arguments to zeroinfl (e.g. dist)

Details

A zero-inflated version of quantile g-computation based on the implementation in the 'pscl' package. A zero-inflated distribution is a mixture distribution in which one of the distributions is a point mass at zero (with probability given by a logistic model), and the other distribution is a discrete or continuous distribution. This estimates the effect of a joint increase in all exposures on 1) the odds of belonging to the "zero" vs. "count" portions of the distribution and/or 2) the rate parameter for the "count" portion of the distribution.

Value

a qgcompfit object, which contains information about the effect measure of interest (psi) and associated variance (var.psi), as well as information on the model fit (fit) and information on the weights/standardized coefficients in the positive (pos.weights) and negative (neg.weights) directions.

See Also

qgcomp.zi.boot,qgcomp.noboot,qgcomp.cox.noboot, and zeroinfl

Examples

```
set.seed(50)
n=100
dat <- data.frame(y=rbinom(n, 1, 0.5)*rpois(n, 1.2), x1=runif(n), x2=runif(n), z=runif(n))</pre>
# poisson count model, mixture in both portions
qgcomp.zi.noboot(f=y ~ z + x1 + x2 | x1 + x2, expnms = c('x1', 'x2'),
   data=dat, q=2, dist="poisson")
# negative binomial count model, mixture and covariate in both portions
qgcomp.zi.noboot(f=y ~ z + x1 + x2 | z + x1 + x2, expnms = c('x1', 'x2'),
  data=dat, q=2, dist="negbin")
qgcomp.zi.noboot(f=y \sim z + x1 + x2, expnms = c('x1', 'x2'),
  data=dat, q=2, dist="negbin") # equivalent
# negative binomial count model, mixture only in the 'count' portion of the model
qgcomp.zi.noboot(f=y ~ z + x1 + x2 | z, expnms = c('x1', 'x2'), data=dat, q=2, dist="negbin")
# weighted analysis
dat = runif(n) *5
qgcomp.zi.noboot(f=y ~ z + x1 + x2 | x1 + x2, expnms = c('x1', 'x2'),
   data=dat, q=2, dist="poisson", weights=w)
# Expect this:
# Warning message:
# In eval(family$initialize) : non-integer #successes in a binomial glm!
```

quantize

Quantizing exposure data

Description

Create variables representing indicator functions with cutpoints defined by quantiles. Output a list that includes: 1) a dataset that is a copy of data, except that the variables whose names are included in the expnms variable are transformed to their quantized version and 2) an unnamed list of the quantile cutpoints that are used for each of the variables that were quantized

quantize

Usage

quantize(data, expnms, q = 4, breaks = NULL)

Arguments

data	a data frame
expnms	a character vector with the names of the columns to be quantized
q	integer, number of quantiles used in creating quantized variables
breaks	(optional) list of (equal length) numeric vectors that characterize the minimum value of each category for which to break up the variables named in expnms. This is an alternative to using 'q' to define cutpoints.

Details

This function creates categorical variables in place of the exposure variables named in 'expnms.' For example, a continuous exposure 'x1' will be replaced in the output data by another 'x1' that takes on values 0:(q-1), where, for example, the value 1 indicates that the original x1 value falls between the first and the second quantile.

Value

A list containing the following fields

data a quantized version of the original dataframe

breaks a list of the quantile cutpoints used to create the quantized variables which includes a very small number for the minimum and a very large number for the maximum to avoid causing issues when using these breaks to quantize new data.

se_comb

Description

This function uses the Delta method to calculate standard errors of linear functions of variables (similar to lincom in Stata). Generally, users will not need to call this function directly.

Usage

se_comb(expnms, covmat, grad = NULL)

Arguments

expnms	a character vector with the names of the columns to be of interest in the covari- ance matrix for a which a standard error will be calculated (e.g. same as expnms in qgcomp fit)
covmat	covariance matrix for parameters, e.g. from a model or bootstrap procedure
grad	the "weight" vector for calculating the contribution of each variable in expnms to the final standard error. For a linear combination, this is equal to a vector of ones (and is set automatically). Or can be calculated via the grad.poly procedure, in the case of coming up with proper weights when the combination of expnms derives from a polynomial function (as in qgcomp.boot with degree>1).

Details

This function takes inputs of a set of exposure names (character vector) and a covariance matrix (with colnames/rownames that contain the full set of exposure names), as well as a possible grad parameter to calculate the variance of a weighted combination of the exposures in expnms, where the weights are based off of grad (which defaults to 1, so that this function yields the variance of a sum of all variables in expnms)

Here is simple version of the delta method for a linear combination of three model coefficients:

 $f(\beta) = \beta_1 + \beta_2 + \beta_3$ given gradient vector

 $G = [d(f(\beta))/d\beta_1 = 1, d(f(\beta))/d\beta_2 = 1, d(f(\beta))/d\beta_3 = 1]$

 $t(G)Cov(\beta)G$ = delta method variance, where t() is the transpose operator

```
vcov = rbind(c(1.2, .9),c(.9, 2.0))
colnames(vcov) <- rownames(vcov) <- expnms <- c("x1", "x2")
qgcomp:::se_comb(expnms, vcov, c(1, 0))^2 # returns the given variance
qgcomp:::se_comb(expnms, vcov, c(1, 1)) # default linear MSM fit: all exposures
# have equal weight
qgcomp:::se_comb(expnms, vcov, c(.3, .1)) # used when one exposure contributes
# to the overall fit more than others = d(msmeffect)/dx</pre>
```

tidy.qgcompfit

Description

Tidy summarizes information about the components of a model. A model component might be a single term in a regression, a single hypothesis, a cluster, or a class. Exactly what tidy considers to be a model component varies cross models but is usually self-evident. If a model has several distinct types of components, you will need to specify which components to return. (Description taken from tidyr::tidy help file.)

Usage

```
## S3 method for class 'qgcompfit'
tidy(x, conf.level = 1 - x$alpha, exponentiate = FALSE, quick = FALSE, ...)
```

Arguments

x	a agcompfit object created by qgcomp().
conf.level	Real number between 0 and 1 corresponding to nominal percentage/100 of con- fidence limit (e.g. conf.level=0.95 means 95 per cent confidence intervals). De- faults to 1-alpha level of qgcompfit.
exponentiate	Logical indicating whether or not to exponentiate the the coefficient estimates. This is typical for logistic and multinomial regressions, but a bad idea if there is no log or logit link. Defaults to FALSE.
quick	Logical indiciating if the only the term and estimate columns should be returned. Often useful to avoid time consuming covariance and standard error calcula- tions. Defaults to FALSE.
	Additional arguments. Not used. Needed to match generic signature only. Cautionary note: Misspelled arguments will be absorbed in, where they will be ignored. If the misspelled argument has a default value, the default value will be used. For example, if you pass conf.lvel = 0.9 , all computation will proceed using conf.level = 0.95 . Additionally, if you pass newdata = my_tibble to an augment() method that does not accept a newdata argument, it will use the default value for the data argument.

 vc_comb

Calculate covariance matrix between one random variable and a linear combination of random variables

Description

This function uses the Delta method to calculate a covariance matrix of linear functions of variables and is used internally in qgcomp. Generally, users will not need to call this function directly.

Usage

```
vc_comb(aname = "(Intercept)", expnms, covmat, grad = NULL)
```

Arguments

aname	character scalar with the name of the first column of interest (e.g. variable A in the examples given in the details section)
expnms	a character vector with the names of the columns to be of interest in the covari- ance matrix for a which a standard error will be calculated (e.g. same as expnms in qgcomp fit)
covmat	covariance matrix for parameters, e.g. from a model or bootstrap procedure
grad	not yet used

Details

This function takes inputs of a name of random variable (character), as set of exposure names (character vector) and a covariance matrix (with colnames/rownames that contain the indepdendent variable and the full set of exposure names). See se_comb for details on variances of sums of random variables. Briefly, for variables A, B and C with covariance matrix Cov(A,B,C), we can calculate the covariance Cov(A,B+C) with the formula Cov(A,B) + Cov(A,C), and Cov(A,B+C+D) = Cov(A,B) + Cov(A,C) + Cov(A,D), and so on.

Value

A covariance matrix

Examples

zimsm.fit

Secondary prediction method for the (zero-inflated) qgcomp MSM.

Description

this is an internal function called by qgcomp.zi.boot, but is documented here for clarity. Generally, users will not need to call this function directly.

zimsm.fit

Usage

```
zimsm.fit(
 f,
 qdata,
 intvals,
 expnms,
 main = TRUE,
 degree = 1,
 id = NULL,
 weights,
 MCsize = 10000,
 containmix = list(count = TRUE, zero = TRUE),
 bayes = FALSE,
 x = FALSE,
 msmcontrol = zimsm.fit.control(),
  • • •
)
```

Arguments

f	an r formula representing the conditional model for the outcome, given all exposures and covariates. Interaction terms that include exposure variables should be represented via the AsIs function
qdata	a data frame with quantized exposures (as well as outcome and other covariates)
intvals	sequence, the sequence of integer values that the joint exposure is 'set' to for estimating the msm. For quantile g-computation, this is just 0:(q-1), where q is the number of quantiles of exposure.
expnms	a character vector with the names of the columns in qdata that represent the exposures of interest (main terms only!)
main	logical, internal use: produce estimates of exposure effect (psi) and expected outcomes under g-computation and the MSM
degree	polynomial bases for marginal model (e.g. degree = 2 allows that the relationship between the whole exposure mixture and the outcome is quadratic. Default=1)
id	(optional) NULL, or variable name indexing individual units of observation (only needed if analyzing data with multiple observations per id/cluster)
weights	not yet implemented
MCsize	integer: sample size for simulation to approximate marginal hazards ratios
containmix	named list of logical scalars with names "count" and "zero"
bayes	not used
x	keep design matrix? (logical)
msmcontrol	named list from zimsm.fit.control
	arguments to zeroinfl (e.g. dist)

Details

This function first computes expected outcomes under hypothetical interventions to simultaneously set all exposures to a specific quantile. These predictions are based on g-computation, where the exposures are 'quantized', meaning that they take on ordered integer values according to their ranks, and the integer values are determined by the number of quantile cutpoints used. The function then takes these expected outcomes and fits an additional model (a marginal structural model) with the expected outcomes as the outcome and the intervention value of the exposures (the quantile integer) as the exposure. Under causal identification assumptions and correct model specification, the MSM yields a causal exposure-response representing the incremental change in the expected outcome given a joint intervention on all exposures.

See Also

qgcomp.cox.boot, and qgcomp.cox.noboot

Examples

```
set.seed(50)
n=100
## Not run:
dat <- data.frame(y=rbinom(n, 1, 0.5)*rpois(n, 1.2), x1=runif(n), x2=runif(n), z=runif(n))
expnms = c("x1", "x2")
q = 4
qdata = quantize(dat, q=q, expnms=expnms)$data
f = y ~ x1 + x2 + z | 1
msmfit <- qgcomp:::zimsm.fit(f, qdata, intvals=(1:q)-1, expnms, main=TRUE,
    degree=1, id=NULL, MCsize=10000, containmix=list(count=TRUE, zero=FALSE),
    x=FALSE)
msmfit$#smfit
## End(Not run)</pre>
```

zimsm.fit.control Control of fitting parameters for zero inflated MSMs

Description

this is an internal function called by qgcomp.zi.boot, but is documented here for clarity. Generally, users will not need to call this function directly.

Usage

```
zimsm.fit.control(predmethod = c("components", "catprobs"))
```

Arguments

predmethod character in c("components", "catprobs"). "components" simulates from the model parameters directly while "catprobs" simulates outcomes from the category specific probabilities, which is output from predict.zeroinfl. The former is slightly more flexible and stable, but the latter is preferred in zero inflated negative bionomial models.

Details

Provides fine control over zero inflated MSM fitting

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