# Package 'pcts'

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Type Package

Title Periodically Correlated and Periodically Integrated Time Series

Description Classes and methods for modelling and simulation of periodically correlated (PC) and periodically integrated time series. Compute theoretical periodic autocovariances and related properties of PC autoregressive moving average models. Some original methods including Boshnakov & Iqelan (2009) <doi:10.1111/j.1467-9892.2009.00617.x>, Boshnakov (1996) <doi:10.1111/j.1467-9892.1996.tb00281.x>.

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pcts-package

Periodically Correlated and Periodically Integrated Time Series

# Description

Classes and methods for modelling and simulation of periodically correlated (PC) and periodically integrated time series. Compute theoretical periodic autocovariances and related properties of PC autoregressive moving average models. Some original methods including Boshnakov & Iqelan (2009) <doi:10.1111/j.1467-9892.2009.00617.x>, Boshnakov (1996) <doi:10.1111/j.1467-9892.1996.tb00281.x>.

#### Details

Index of the main exported objects, classes and methods:

# Model fitting functions:

fitPM	Fit periodic time series models
mC.ss	Create environment for mc-fitting
num2pcpar	Fit PAR model using sample autocorrelations
pcAr.ss	Compute the sum of squares for a given PAR model
pcarma_acvf2model	Fit a PC-ARMA model to a periodic autocovariance function
pclsdf	Fit PAR models using least squares
pclspiar	Fit a periodically integrated autoregressive model

# Tests and statistics:

# pcts-package

parcovmatlist	Compute asymptotic covariance matrix for PAR model
pcTest-methods	Test for periodicity
<pre>periodic_acf1_test</pre>	McLeod's test for periodic autocorrelation
<pre>pwn_McLeodLjungBox_test</pre>	Nelsed Lines Dev test for periodic white raise
test_piar	McLeod-Ljung-Box test for periodic white noise Test for periodic integration
Generator functions for cla	sses::
pcts	Create objects from periodic time series classes
Simulation:	
sim_parAcvf	Create a random periodic autocovariance function
<pre>sim_parCoef</pre>	Generate a periodic autoregression model
sim_pc	Simulate Periodically Correlated ARMA Series
sim_pwn	Simulate periodic white noise
Periodic autoregression:	
alg1	Periodic Levinson-Durbin algorithm
alg1util	Give partial periodic autocorrelations or other
	partial prediction quantities for a pcAcvf object.
pc.sdfactor	Compute normalising factors
pcAR2acf	Compute periodic autocorrelations from PAR
<b>0</b>	coefficients
pcacfMat pdSafeParOrder	Compute PAR autocovariance matrix
pusarerarorder	Functions for some basic operations with seasons
permean2intercept	Convert between periodic centering and intercepts
permodelmf	Compute the multi-companion form of a per model
Integrated PAR:	
pi1ar2par	Convert PIAR coefficients to PAR coefficients
Other:	
dataFranses1996	Example data from Franses (1996)
ex1f	An example PAR autocorrelation function
nCycles	Basic time information about periodic time series
pc.filter	Applies a periodic ARMA filter to a time series
pc.filter.xarma	Filter time series with periodic arma filters
pcacf_pwn_var	Variances of sample periodic autocorrelations
pcarma_acvf_lazy	Functions to compute various characteristics of
	a PCARMA model

# pcts-package

pcarma_unvec pcts	Functions for work with a simple list specification of pcarma models Create objects from periodic time series
pcts-deprecated pcts-package	classes Deprecated Functions in Package 'pcts' Periodically Correlated and Periodically Integrated Time Series
toSeason	Functions for some basic operations with seasons
pc.arma:	
pc.hat.h	function to compute estimates of the h weights
Methods:	
\$-methods PeriodicArModel-methods	
[-methods	Create objects from class PeriodicArModel Indexing of objects from classes in package pcts
[ <methods< td=""><td>Index assignments for objects from classes in package pcts</td></methods<>	Index assignments for objects from classes in package pcts
[[-methods autocorrelations-method	Methods for function''[['' in package 'pcts'
	Compute autocorrelations and periodic autocorrelations
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	Compute autocovariances and periodic autocovariances
filterCoef-methods maxLag-methods nSeasons-methods pcCycle-methods	Get the coefficients of a periodic filter Methods for function maxLag() in package 'pcts' Number of seasons for a periodic object Create or extract Cycle objects
<pre>pcTest-methods seqSeasons-methods sigmaSq-methods unitCycle-methods unitCycle<methods pre="" unitseason-methods="" unitseason<methods<=""></methods></pre>	Test for periodicity Methods for seqSeasons() in package pcts Methods for 'sigmaSq' in package pcts Methods for unitCycle() in package pcts Methods for '"unitCycle<-"()' in package pcts Methods for unitSeason() in package pcts Methods for '"unitSeason<-"()' in package pcts

The naming conventions are as follows. Names of classes generally consists of one or more words. The first letter of each word, is capitalised. Only the first letter of abbreviations for models, such as ARMA, is capitalised. Similarly for generic functions but for them the first word is not capitalised. In a few names PM stands for 'periodic model' and TS for 'time series'.

Significant portion of the code was written in 2005–2007. Many of the functions and classes have been renamed under the above conventions and most of those that are not are not exported but a few still are and they should be considered subject to change.

#### pcts-package

autocovariances and autocorrelations are one-stop generic functions for computation of these second order properties. What to compute is deduced from the type of the object. For models they compute theoretical quantities — periodic or non-periodic, scalar or multivariate. For time series they compute the corresponding sample counterparts.

## Author(s)

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#### See Also

mcompanion

```
data(dataFranses1996)
class(dataFranses1996) # [1] "mts"
                                       "ts"
                                                "matrix"
pcfr <- pcts(dataFranses1996)</pre>
                   # "PeriodicMTS"
class(pcfr)
nSeasons(pcfr) # 4
allSeasons(pcfr)
allSeasons(pcfr, abb = TRUE)
## subsetting
## one index, x[i], is analogous to lists
pcfr2to4 <- pcfr[2:4]; class(pcfr2to4) # "PeriodicMTS"</pre>
pcfr2to2 <- pcfr[2]; class(pcfr2to2) # "PeriodicMTS"</pre>
         <- pcfr[[2]]; class(pcfr2)  # note '[[', "PeriodicTS"
pcfr2
## with empty index, returns the underlying data
dim(pcfr[]) # [1] 148 19
dim(pcfr2to2[]) # 148 1
length(pcfr2[]) # 148 (this is numeric)
summary(pcfr2)
summary(pcfr2to4)
## make the output width shorter
summary(pcfr2to4, row.names = FALSE)
summary(pcfr2to4, row.names = 5) # trim row names to 5 characters
```

## allSeasons

```
head(pcfr2to4) # starts with NA's
tail(pcfr2to4) # some NA's at the end too
## time of first and last data, may be NA's
start(pcfr2to4) # 1955 Q1
end(pcfr2to4) # 1991 Q4
## time of first nonNA:
availStart(pcfr2)
                   # 1955 Q1
availStart(pcfr2to4) # 1955 Q1
## time of last nonNA:
availEnd(pcfr[[2]])
                    # 1991 Q4
availEnd(pcfr[[3]])
                    # 1987 Q4
availEnd(pcfr[[4]]) # 1990 Q4
## but at least one of them is available for 1991 Q4, so:
availEnd(pcfr2to4) # 1991 Q4
## use window() to pick part of the ts by time:
window(pcfr2to4, start = c(1990, 1), end = c(1991, 4))
## drop NA's at the start and end:
window(pcfr2to4, start = availStart(pcfr2to4), end = availEnd(pcfr2to4))
plot(pcfr2) # the points mark the first season in each cycle
boxplot(pcfr2)
monthplot(pcfr2)
```

allSeasons Get names of seasons

#### Description

Functions and methods fo get names of seasons and related quantities for objects from the cycle, periodic time series classes and other objects for which the concepts are defined.

#### Usage

```
unitSeason(x)
unitCycle(x)
seqSeasons(x)
allSeasons(x, abb = FALSE, prefix = "S", ...)
unitSeason ( x, ... ) <- value
unitCycle ( x, ... ) <- value
allSeasons ( x, abb, ... ) <- value
## S4 replacement method for signature 'SimpleCycle'
allSeasons(x, abb, prefix, ...) <- value</pre>
```

```
## S4 replacement method for signature 'Cyclic'
allSeasons(x, abb = FALSE, ...) <- value</pre>
```

#### Arguments

х	a cycle, time series or other object for which the concept of seasons is defined.
abb	if TRUE give the abbreviated names of the seasons.
prefix	use this prefix for automatically generated names of seasons.
	further arguments for methods.
value	a character string

#### Details

The cycle classes, i.e. classes inheriting from class BasicCycle, provide common functionality. In particular, they guarantee that the functions described in this topic are available. These functions work also for the periodic time series classes and may be defined for other classes where they make sense.

#### Methods

Methods for allSeasons():

```
signature(x = "BasicCycle", abb = "ANY")
signature(x = "DayWeekCycle", abb = "logical")
signature(x = "DayWeekCycle", abb = "missing")
signature(x = "FiveDayWeekCycle", abb = "logical")
signature(x = "FiveDayWeekCycle", abb = "missing")
signature(x = "MonthYearCycle", abb = "logical")
signature(x = "MonthYearCycle", abb = "missing")
signature(x = "OpenCloseCycle", abb = "logical")
signature(x = "OpenCloseCycle", abb = "missing")
signature(x = "QuarterYearCycle", abb = "logical")
signature(x = "QuarterYearCycle", abb = "missing")
signature(x = "SimpleCycle", abb = "ANY")
signature(x = "Cyclic", abb = "ANY")
signature(x = "Every30MinutesCycle", abb = "logical")
signature(x = "Every30MinutesCycle", abb = "missing")
signature(x = "VirtualPeriodicModel", abb = "ANY")
```

## Author(s)

Georgi N. Boshnakov

#### allSeasons

```
opcycle <- new("OpenCloseCycle")</pre>
## convert to SimpleCycle to change some names
siopcycle <- as(opcycle, "SimpleCycle")</pre>
## siopcycle inherits names from opcycle
unitSeason(siopcycle) # "Season"
                                 # "Cycle"
unitCycle(siopcycle)
                                 # "Open" "Close"
allSeasons(siopcycle)
allSeasons(siopcycle, abb = TRUE) # "O" "C"
allSeasons(siopcycle) <- c("Day", "Night")</pre>
allSeasons(siopcycle) # now: "Day" "Night"
## change also abbreviations
allSeasons(siopcycle, abb = TRUE) <- c("D", "N")
allSeasons(siopcycle, abb = TRUE) # now: "D" "N"
seasons <- new("SimpleCycle", 4)</pre>
unitSeason(seasons)
                                 # "Season"
                                 # "Cycle"
unitCycle(seasons)
allSeasons(seasons)
allSeasons(seasons, abb = TRUE)
unitCycle(seasons) <- "Year"</pre>
unitCycle(seasons)
allSeasons(seasons) <- c("Winter", "Spring", "Summer", "Autumn")</pre>
allSeasons(seasons)
allSeasons(seasons, abb = TRUE) <- c("Win", "Spr", "Sum", "Aut")
allSeasons(seasons, abb = TRUE)
## change autumn to Fall
allSeasons(seasons)[4] <- "Fall"
allSeasons(seasons, abb = TRUE)[4] <- "Fal"
allSeasons(seasons)
allSeasons(seasons, abb = TRUE)
## indexing of cycle objects is equivalent to allSeasons.
seasons[]
seasons[ , abb = TRUE]
seasons[4] <- "Herbst"</pre>
seasons
unitCycle(seasons) <- "Jahre"</pre>
unitCycle(seasons)
unitSeason(seasons) <- "Jahreszeit"</pre>
seasons[] <- c("Winter", "Frueling", "Sommer", "Herbst")</pre>
seasons[ , abb = TRUE] <- c("W", "F", "S", "H")</pre>
seasons[]
seasons
```

```
autocorrelations-methods
```

Compute autocorrelations and periodic autocorrelations

# Description

Methods for computation of autocorrelations and periodic autocorrelations.

#### Methods

```
signature(x = "numeric", maxlag = "ANY", lag_0 = "missing")
signature(x = "PeriodicTimeSeries", maxlag = "ANY", lag_0 = "missing")
signature(x = "PeriodicAutocovariances", maxlag = "ANY", lag_0 = "missing")
signature(x = "SamplePeriodicAutocovariances", maxlag = "ANY", lag_0 = "missing")
signature(x = "VirtualPeriodicAutocovariances", maxlag = "ANY", lag_0 = "missing")
signature(x = "VirtualPeriodicAutocovarianceModel", maxlag = "ANY", lag_0 = "missing")
```

## See Also

autocovariances-methods for autocovariances; autocorrelations in package "sarima" for further details.

#### Examples

```
## periodic
autocorrelations(pcts(AirPassengers), maxlag = 10)
## for "ts" or "numeric" objects the default is non-periodic
## non-periodic acf
autocorrelations(AirPassengers, maxlag = 10)
autocorrelations(as.numeric(AirPassengers))
## argument 'nseasons' forces periodic acf
autocorrelations(AirPassengers, maxlag = 10, nseasons = 12)
```

autocorrelations(as.numeric(AirPassengers), maxlag = 10, nseasons = 12)

autocovariances-methods

Compute autocovariances and periodic autocovariances

#### Description

Methods for the generic function autocovariances(), which computes autocovariances meaningful for the first argument. For objects representing time series, it computes sample autocovariances (univariate, multivariate, periodic, as appropriate). For objects representing models, it computes the relevant theoretical autocovariances.

## availStart

# Methods

```
signature(x = "matrix", maxlag = "ANY")
signature(x = "numeric", maxlag = "ANY")
signature(x = "PeriodicArmaModel", maxlag = "ANY")
signature(x = "PeriodicArModel", maxlag = "ANY")
signature(x = "PeriodicAutocovarianceModel", maxlag = "ANY")
signature(x = "PeriodicTS", maxlag = "ANY")
signature(x = "VirtualPeriodicAutocovariances", maxlag = "ANY")
```

## See Also

autocorrelations-methods for autocorrelations; autocovariances in package "sarima" for further details.

availStart

Time of first or last non-NA value

## Description

Time of first or last non-NA value.

#### Usage

```
availStart(x)
availEnd(x)
```

#### Arguments

Х

a time series or similar object

# Details

The time is given as a cycle-season pair. The functions can be used to trim NA's from the beginning or end of the data.

# Value

numeric, length 2

#### See Also

window

## Examples

```
tipi <- pcts(dataFranses1996[ , "USTotalIPI"])</pre>
start(tipi)
end(tipi)
head(tipi)
tail(tipi)
tipi <- window(tipi, start = availStart(tipi), end = availEnd(tipi))</pre>
start(tipi)
end(tipi)
plot(tipi)
pcfr <- pcts(dataFranses1996)</pre>
pcfr2to4 <- pcfr[2:4]</pre>
head(pcfr2to4)
tail(pcfr2to4)
## time of first and last data, can be NA's
start(pcfr2to4) # 1955 Q1
end(pcfr2to4) # 1991 Q4
## time of first nonNA:
availStart(pcfr[[2]]) # 1960 Q1
availStart(pcfr2to4) # 1960 Q1
## time of last nonNA:
availEnd(pcfr[[2]]) # 1991 Q4
availEnd(pcfr[[3]]) # 1987 Q4
availEnd(pcfr[[4]]) # 1990 Q4
## but at least one of them is available for 1991 Q4, so:
availEnd(pcfr2to4) # 1991 Q4
pcfr2to4a <- window(pcfr2to4, start = availStart(pcfr2to4), end = availEnd(pcfr2to4))</pre>
head(pcfr2to4a)
```

```
tail(pcfr2to4a)
```

BareCycle-class Class BareCycle

#### Description

Class BareCycle.

#### **Objects from the Class**

Objects can be created by calls of the form pcCycle(nseasons) or new("BareCycle", nseasons). Class "BareCycle" represents the number of seasons and is sufficient for many computations.

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# BareCycle-class

# Slots

nseasons: Object of class "integer", the number of seasons.

### Extends

Class "BasicCycle", directly.

# Methods

```
coerce signature(from = "BuiltinCycle",to = "BareCycle"): ...
```

initialize signature(.Object = "BareCycle"): ...

**nSeasons** signature(object = "BareCycle"): ...

show signature(object = "BareCycle"): ...

#### Author(s)

Georgi N. Boshnakov

# See Also

pcCycle for creation of cycle objects and extraction of cycle part of time series,

BuiltinCycle-class, SimpleCycle-class,

DayWeekCycle-class, FiveDayWeekCycle-class, MonthYearCycle-class, OpenCloseCycle-class, QuarterYearCycle-class

BasicCycle-class (virtual, for use in signatures)

```
pcCycle(5)
cycle <- new("BareCycle", 5)
identical(new("BareCycle", 5), pcCycle(5)) # TRUE
unitSeason(cycle)
unitCycle(cycle)
allSeasons(cycle)
seqSeasons(cycle)
cycle[]
cycle[3]
## if cycle represents 5-days week one may prefer:
```

```
new("FiveDayWeekCycle")
```

BasicCycle-class Class BasicCycle

# Description

Class BasicCycle.

# **Objects from the Class**

A virtual Class: No objects may be created from it.

# Methods

[ signature(x = "BasicCycle", i = "ANY", j = "missing", drop = "ANY")
[ signature(x = "BasicCycle", i = "missing", j = "missing", drop = "ANY")
[<- signature(x = "BasicCycle", i = "ANY", j = "missing", value = "ANY")
[<- signature(x = "BasicCycle", i = "missing", j = "missing", value = "ANY")
allSeasons signature(x = "BasicCycle", abb = "ANY")
seqSeasons signature(x = "BasicCycle")</pre>

# Author(s)

Georgi N. Boshnakov

## See Also

BareCycle-class, SimpleCycle-class, BuiltinCycle-class

DayWeekCycle-class, FiveDayWeekCycle-class, MonthYearCycle-class, OpenCloseCycle-class, QuarterYearCycle-class

# Examples

showClass("BasicCycle")

BuiltinCycle

## Description

Create cycle objects from the builtin cycle classes.

#### Usage

BuiltinCycle(n, coerce = FALSE, first = 1)

#### Arguments

n	number of seasons, an integer.
coerce	if TRUE coerce the objects to a modifiable cycle class, currently "SimpleCycle".
first	which season is first for this object.

#### Details

BuiltinCycle is a convenience function to create objects from builtin cycle classes by specifying the number of seasons. The builtin cycle classes are esseintially fixed, except that which season is considered first can be changed using argument first. If other modifications are desired, convert the returned builtin cycle object to class "SimpleCycle". This can be done also in the call to BuiltinCycle() by specifying coerce = TRUE.

## Value

one of the builtin classes, coerced if requested.

# See Also

class BuiltinCycle for the available builtin classes, allSeasons for further examples,

```
BuiltinCycle(2) # "OpenCloseCycle"
BuiltinCycle(4) # "QuarterYearCycle"
BuiltinCycle(5) # "FiveDayWeekCycle"
BuiltinCycle(7) # "DayWeekCycle"
BuiltinCycle(12) # "MonthYearCycle"
BuiltinCycle(48) # "Every30MinutesCycle"
```

BuiltinCycle-class Class "BuiltinCycle" and its subclasses in package 'pcts'

#### Description

Class "BuiltinCycle" and its subclasses in package 'pcts'.

#### **Objects from the Class**

Class "BuiltinCycle" is a virtual Class: no objects may be created from it. Class "BuiltinCycle" has several built-in cycle subclasses. Objects from the subclasses can be created by calls of the form new("className", first,...), where "className" is the name of the subclass. The optional argument first can be used to designate a season to be considered first in the cycle, by default the first.

The function BuiltinCycle provides a more convenient way to generate objects from subclasses of class "BuiltinCycle". Its argument is the number of seasons.

These classes are effectively unmodifiable, but the user can convert them to other cycle classes, e.g. class "SimpleCycle", and adapt as needed.

The subclasses of "BuiltinCycle" have definitions for all methods promised by its superclass "BasicCycle".

## Slots

The class "BuiltinCycle" and its subclasses have a single common slot:

first: Object of class "integer", the index of the season to be treated as the first in a cycle.

#### Extends

Class "BuiltinCycle" extends class "BasicCycle", directly.

Classes "DayWeekCycle", "Every30MinutesCycle", "FiveDayWeekCycle", "OpenCloseCycle" and "QuarterYearCycle" extend:

Class "BuiltinCycle", directly. Class "BasicCycle", by class "BuiltinCycle", distance 2.

# Methods

Functions with methods for this class:

coerce signature(from = "BuiltinCycle",to = "BareCycle"): ... coerce signature(from = "BuiltinCycle",to = "SimpleCycle"): ... initialize signature(.Object = "BuiltinCycle"): ... show signature(object = "BuiltinCycle"): ... allSeasons signature(x = "DayWeekCycle",abb = "logical") allSeasons signature(x = "DayWeekCycle",abb = "missing") nSeasons signature(object = "DayWeekCycle")

```
unitCycle signature(x = "DayWeekCycle")
unitSeason signature(x = "DayWeekCycle")
allSeasons signature(x = "Every30MinutesCycle", abb = "logical"): ...
allSeasons signature(x = "Every30MinutesCycle", abb = "missing"): ...
nSeasons signature(object = "Every30MinutesCycle"): ...
unitCycle signature(x = "Every30MinutesCycle"): ...
unitSeason signature(x = "Every30MinutesCycle"): ...
allSeasons signature(x = "FiveDayWeekCycle", abb = "logical"): ...
allSeasons signature(x = "FiveDayWeekCycle",abb = "missing"): ...
nSeasons signature(object = "FiveDayWeekCycle"): ...
unitCycle signature(x = "FiveDayWeekCycle"): ...
unitSeason signature(x = "FiveDayWeekCycle"): ...
allSeasons signature(x = "MonthYearCycle", abb = "logical"): ...
allSeasons signature(x = "MonthYearCycle",abb = "missing"): ...
nSeasons signature(object = "MonthYearCycle"): ...
unitCycle signature(x = "MonthYearCycle"): ...
unitSeason signature(x = "MonthYearCycle"): ...
allSeasons signature(x = "OpenCloseCycle",abb = "logical"): ...
allSeasons signature(x = "OpenCloseCycle", abb = "missing"): ...
nSeasons signature(object = "OpenCloseCycle"): ...
unitCycle signature(x = "OpenCloseCycle"): ...
unitSeason signature(x = "OpenCloseCycle"): ...
allSeasons signature(x = "QuarterYearCycle", abb = "logical"): ...
allSeasons signature(x = "QuarterYearCycle",abb = "missing"): ...
nSeasons signature(object = "QuarterYearCycle"): ...
unitCycle signature(x = "QuarterYearCycle"): ...
unitSeason signature(x = "QuarterYearCycle"): ...
```

# Author(s)

Georgi N. Boshnakov

#### See Also

BuiltinCycle, pcCycle for creation of cycle objects and extraction of cycle part of time series, BareCycle-class, SimpleCycle-class,

# Examples

```
showClass("BuiltinCycle")
## class "DayWeekCycle"
dwcycle <- new("DayWeekCycle")</pre>
identical(BuiltinCycle(7), dwcycle) # TRUE
unitSeason(dwcycle)
unitCycle(dwcycle)
allSeasons(dwcycle)
dwcycle[] # same
allSeasons(dwcycle, abb = TRUE)
dwcycle[ , abb = TRUE] # same
dwcycle[2]
dwcycle[2, abb = TRUE]
seqSeasons(dwcycle)
## start the week on Sunday
dws <- new("DayWeekCycle", first = 7)</pre>
dws[1] # "Sunday"
allSeasons(dws)
## class \code{"Every30MinutesCycle"}
cyc48 <- new("Every30MinutesCycle")</pre>
nSeasons(cyc48)
allSeasons(cyc48)
## class \code{"FiveDayWeekCycle"}
fdcycle <- new("FiveDayWeekCycle")</pre>
## identical(new("BareCycle", 5), pcCycle(5)) # TRUE
unitSeason(fdcycle)
unitCycle(fdcycle)
allSeasons(fdcycle)
fdcycle[] # same
allSeasons(fdcycle, abb = TRUE)
fdcycle[ , abb = TRUE] # same
fdcycle[2]
fdcycle[2, abb = TRUE]
seqSeasons(fdcycle)
## class \code{MonthYearCycle}
mycycle <- new("MonthYearCycle")</pre>
## identical(new("BareCycle", 5), pcCycle(5)) # TRUE
```

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```
unitSeason(mycycle)
unitCycle(mycycle)
allSeasons(mycycle)
mycycle[ ] # same
allSeasons(mycycle, , abb = TRUE)
mycycle[ , abb = TRUE] # same
mycycle[2]
mycycle[2, abb = TRUE]
seqSeasons(mycycle)
## class \code{"OpenCloseCycle"}
opcycle <- new("OpenCloseCycle")</pre>
## identical(new("BareCycle", 5), pcCycle(5)) # TRUE
unitSeason(opcycle)
unitCycle(opcycle)
allSeasons(opcycle)
opcycle[ , abb = FALSE] # same
allSeasons(opcycle, abb = FALSE)
opcycle[] # same
opcycle[2]
opcycle[2, abb = TRUE]
seqSeasons(opcycle)
## class \code{"QuarterYearCycle"}
qycycle <- new("QuarterYearCycle")</pre>
## identical(new("BareCycle", 5), pcCycle(5)) # TRUE
unitSeason(qycycle)
unitCycle(qycycle)
allSeasons(qycycle)
qycycle[] # same
allSeasons(qycycle, abb = TRUE)
qycycle[ , abb = TRUE] # same
qycycle[2]
qycycle[2, abb = TRUE]
seqSeasons(qycycle)
```

Cyclic-class

## Description

Class "Cyclic"

## **Objects from the Class**

Objects can be created by calls of the form new("Cyclic",...).

# Slots

cycle: Object of class "BasicCycle" ~~
pcstart: Object of class "ANY" ~~

## Methods

```
nSeasons signature(object = "Cyclic"): ...
pcCycle signature(x = "Cyclic", type = "ANY"): ...
allSeasons signature(x = "Cyclic", abb = "ANY"): ...
seqSeasons signature(x = "Cyclic"): ...
unitCycle signature(x = "Cyclic"): ...
unitCycle<- signature(x = "Cyclic"): ...
unitSeason signature(x = "Cyclic"): ...
unitSeason<- signature(x = "Cyclic"): ...</pre>
```

#### Examples

showClass("Cyclic")

dataFranses1996 Example data from Franses (1996)

## Description

A multivariate time series containing the data used in examples by Franses (1996).

### Usage

data("dataFranses1996")

## Format

A multivariate quarterly time series.

#### Details

Each column is a quarterly time series. The time series start and end at different times, so NA's are used to align them in a single multivariate time series. Detailed account of the sources of the data is given by Franses (1996; Data Appendix, p. 214).

```
year (column 1)
```

The time formatted as yyyy.Q, where yyyy is the year and Q is the quarter (one of 1, 2, 3 or 4.). This column was part of the original data but is not really needed here since the time series object contains the time information.

```
USTotalIPI (column 2)
```

Total Industrial Production Index for the United States (1985 = 100), 1960.1–1991.4.

```
CanadaUnemployment (column 3)
```

Unemployment in Canada, measured in 1000 persons, 1960.1 - 1987.4.

```
GermanyGNP (column 4)
```

Real GNP in Germany, 1960.1 - 1990.4.

UKTotalInvestment (column 5)

Real Total Investment in the United Kindom, 1955.1 - 1988.4.

SA\_USTotalIPI (column 6) Seasonally adjusted USTotalIPI.

SA\_CanadaUnemployment (column 7)

Seasonally adjusted CanadaUnemployment.

```
SA_GermanyGNP (column 8)
```

Seasonally adjusted GermanyGNP.

```
UKGDP (column 9)
```

United Kingdom gross domestic product (at 1985 prices), 1955.1-1988.4.

```
UKTotalConsumption (column 10)
```

United Kingdom total consumption (at 1985 prices), 1955.1-1988.4.

```
UKNondurablesConsumption (column 11)
```

United Kindom nondurables consumption (at 1985 prices), 1955.1–1988.4.

```
UKExport (column 12)
```

United Kindom exports of goods and services (at 1985 prices), 1955.1–1988.4.

```
UKImport (column 13)
```

```
United Kindom imports of goods and services (at 1985 prices), 1955.1–1988.4.
```

```
UKPublicInvestment (column 14)
```

United Kindom public investment (at 1985 prices), 1962.1–1988.4.

```
UKWorkforce (column 15)
```

United Kindom workforce (consisting of workforce in employment and unemployment), 1955.1–1988.4.

```
SwedenNondurablesConsumption (column 16)
```

Real per capita non-durables consumption in Sweden (measured in logs), 1963.1–1988.1.

SwedenDisposableIncome (column 17)

Real per capita disposable income in Sweden (measured in logs), 1963.1–1988.1.

SA\_SwedenNondurablesConsumption (column 18)

Seasonally adjusted SwedenNondurablesConsumption with Census X-11 method, 1964.1–1988.1. (Using the approximate linear Census X-11 filter given in Table 4.1, p. 52 in Franses (1996) and generating the forecasts and backcasts as described in Ooms (1994)).

```
SA_SwedenDisposableIncome (column 19)
```

Seasonally adjusted SwedenDisposableIncome with Census X-11 method, 1964.1–1988.1. (Using the same method as above.)

More details on the individual time series are given by Franses (1996).

#### Note

Most of the time series in dataFranses1996 are available as separate datasets in package 'partsm'. The numbers should be the same but note that, at the time of writing this, not all datasets there carry complete time information.

#### Source

The data were downloaded from http://people.few.eur.nl/franses/research/data/data1.txt, but this link is now broken.

## References

Franses PH (1996). *Periodicity and Stochastic Trends In Economic Time Series*. Oxford University Press Inc., New York.

```
data(dataFranses1996)
class(dataFranses1996)
dim(dataFranses1996) # c(148, 19)
plot(dataFranses1996[ , 2:11])
tipi <- dataFranses1996[ , "USTotalIPI"]
plot(tipi)
## convert to PeriodicTS and remove NA's at the start and end
pctipi <- pcts(tipi)
pctipi <- window(pctipi, start = availStart(pctipi), end = availEnd(pctipi))
plot(pctipi)
## convert the whole dataset to class "PeriodicMTS"
pcfr <- pcts(dataFranses1996)
colnames(pcfr)[2:3] # "USTotalIPI" "CanadaUnemployment"
```

```
## subset as "PeriodicMTS"
pcfr2to3 <- pcfr[2:3]
plot(pcfr2to3)
## "[" "PeriodicMTS" even with length one arg.
pcfr2to2 <- pcfr[2]
pcfr2to2a <- pcfr["USTotalIPI"] # same
## use "[[" or $ to get "PeriodicTS"
pcfr2 <- pcfr[[2]]
pcfr2a <- pcfr[["USTotalIPI"]] # same
pcfr2b <- pcfrsUSTotalIPI # same
identical(pcfr2, pcfr2a) # TRUE
identical(pcfr2, pcfr2b) # TRUE
cycle(pcfr)
frequency(pcfr)</pre>
```

ex1f

An example PAR autocorrelation function

## Description

ex1 is the autocorrelation function used in the reference as an example when the solution of the periodic Yule-Walker system gives an invalid PAR model. This can happen only if Lambert-Lacroix's condition on the PAR order is not satisfied, see pdSafeParOrder.

## Format

A function of two arguments

## Source

See pp. 429-430 of the reference.

## References

Lambert-Lacroix S (2005). "Extension of autocovariance coefficients sequence for periodically correlated processes." *Journal of Time Series Analysis*, **26**(6), pp. 423-435.

# See Also

pdSafeParOrder

## Examples

```
data(ex1f)
## compute the first few autocorrelations
pc3 <- slMatrix(period = 2, maxlag = 5, f = ex1f, type = "tt")
## Fir a PAR(0,2) model
res0p2 <- alg1(pc3[],c(0,2))
## model is invalid since a partial autocorrelation is larger than one:
res0p2$be
## Find a modified order:
pdSafeParOrder(c(0,2)) # PAR(1,2)
## now the parcor's are fine:
res1p2 <- alg1(pc3[],c(1,2))
res1p2$be</pre>
```

filterCoef-methods Get the coefficients of a periodic filter

#### Description

Get the coefficients of a periodic filter.

# Details

filterCoef is a generic function to extract the coefficients of periodic filters. Argument convention can be used to force a particular convention for the signs. The description here is for the methods defined in this package.

If convention is missing, the coefficient matrix is returned as stored in the object. Otherwise, if convention is one of the strings "BJ", "--" or "-", the coefficients returned have the opposite sign of those in the auxilliary polynomial (Box-Jenkins' convention). if convention is one of "SP", "++" or "+", the coefficients are as in the auxilliary polynomial (convention used in signal processing).

# Value

a matrix

#### Methods

```
signature(object = "PeriodicBJFilter", convention = "character")
signature(object = "PeriodicSPFilter", convention = "character")
```

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fitPM

#### Description

Generic function with methods for fitting periodic time series models.

#### Usage

fitPM( model, x, ...)

#### Arguments

х	the time series.
model	a periodic model, see Details.
	further arguments to be passed on to individual methods.

## Details

This is a generic function.

model provides the specification of the model. In particular, the class of model determines what model is fitted. Specific values of the parameters are generally ignored by non-iterative methods but some methods can handle more detailed specifications, see the individual methods.

#### Value

the fitted model, typically an object of class class(model)

#### Methods

- signature(model = "ANY", x = "ANY") This is the default method. It simply exits with an error message stating that fitPM does not have a method for the model specified by model.
- signature(model = "numeric", x = "ANY") Fits a PAR model to x. model should be a vector of non-negative integers giving the PAR order. The length of this vector is taken to be the number of seasons.

This is a convenience method. It constructs a PAR model and callls the method for model = "PeriodicArModel".

signature(model = "PeriodicArModel", x = "ANY") Fits a PAR model.

signature(model = "mcSpec", x = "ANY") Fits a periodic model according to the specification
given by model.

Currently this method uses mC.ss to set up the optimisation environment and then calls one of the optimisation functions in that environment as specified by argument optim.method, see below.

Additional arguments may be specified to control the optimisation.

Argument init can be used to give initial values. It is passed on to mC.ss (and so has the format required by it).

optim.method is the name of an optimisation function in the environment returned by mC.ss. The default is optim.method = "minim", which is based on the standard R function optim. Alternatives are "minimBB" or "minimBBLU". All this needs to be documented but see mC.ss and xx.ss for details.

Further arguments are passed on to the optimisation method. A typical argument supported by most optimisation functions is control.

signature(model = "PiPeriodicArModel", x = "ANY") Fits a periodically integrated PAR model
using the parameters of model as initial values. Calls pclspiar to do the actual work.

```
signature(model = "SiPeriodicArModel", x = "ANY") Fits a seasonally integrated PAR model.
```

```
signature(model = "PeriodicArModel", x = "PeriodicMTS")
```

```
signature(model = "PeriodicArModel", x = "PeriodicTS")
```

## Author(s)

Georgi N. Boshnakov

#### References

(todo: to be completed properly later)

Hipel KW and McLeod AI (1994). *Time series modelling of water resources and environmental systems*, series Developments in water science; 45. London; Amsterdam: Elsevier.

Boshnakov GN and Iqelan BM (2009). "Generation of time series models with given spectral properties." *J. Time Series Anal.*, **30**(3), pp. 349–368. ISSN 0143-9782, http://dx.doi.org/10. 1111/j.1467-9892.2009.00617.x.

```
## newm1 <- list(phi = matrix(1:12, nrow=4), p=rep(3,4), period=4, si2 = rep(1,4))
## new_pfm1 <- PeriodicFilterModel(newm1, intercept=0)</pre>
## generate some data;
set.seed(1234)
simts1 <- pcts(rnorm(1024), nseasons = 4)</pre>
fitPM(c(3,3,3,3), simts1)
fitPM(3, simts1)
## the fit on the underlying data is equivalent.
fitPM(c(3,3,3,3), as.numeric(simts1))
## equivalently, use a PAR(3,3,3,3) model for argument 'model'
## here the coefficients of pfm1 are ignored, since the estimation is linear.
pfm1 <- PeriodicArModel(matrix(1:12, nrow = 4), order = rep(3,4), sigma2 = 1)</pre>
pfm1
## these give same results as above
fitPM(pfm1, simts1)
fitPM(pfm1, as.numeric(simts1))
```

## fitPM

```
fitPM(c(1,1,1,1), simts1)
fitPM(c(3,2,2,1), simts1)
fitPM(c(3,2,2,2), simts1)
pdSafeParOrder(c(3,2,2,1))
pdSafeParOrder(rev(c(3,2,2,1)))
x <- arima.sim(list(ar = 0.9), n = 960)</pre>
pcx <- pcts(x, nseasons = 4)</pre>
mx <- matrix(x, nrow = 4)</pre>
##pc.acf(mx)
##pc.acf(mx, maxlag=10)
## TODO: avoid the warning when length ot the time series is not multiple
autocovariances(t(mx), maxlag = 6, nseasons = 4)
autocovariances(t(mx))
##It is an error to have more columns than rows.
## autocovariances(mx, maxlag = 6, nseasons = 4)
## autocovariances(mx)
num2pcpar(mx, c(1,1,1,1), period = 4)
num2pcpar(mx, c(3,3,3,3), period = 4)
sipfm1 <- new("SiPeriodicArModel", iorder = 1, siorder = 1, pcmodel = pfm1)</pre>
sipfm1
fitPM(sipfm1, mx)
pfm1
## experiments and testing
fit1
      <- fitPM(c(3,3,3,3), simts1)
fit1_mf <- new("MultiFilter", coef = fit1@ar@coef)</pre>
        <- mcompanion::mf_VSform(fit1_mf, form = "I")
vs
tmp <- mcompanion::VAR2pcfilter(vs$Phi[ , -4],</pre>
                                 Phi0inv = vs$Phi0inv, D = fit1@sigma2, what = "")
names(tmp) # "pcfilter" "var"
                                     "Uform"
tmp$var
zapsmall(tmp$pcfilter)
fit1@ar@coef
all.equal(tmp$pcfilter[, 1:3], fit1@ar@coef, check.attributes = FALSE) # TRUE
tmp$Uform
fit1@sigma2
## both give the matrix Sigma for the "I" form
identical(
    vs$Phi0inv
    tmp$Uform$U0inv
) # TRUE
## no, this is a different matrix
var1_mat <- cbind(vs$Phi0, # identity matrix</pre>
```

```
- vs$Phi) # drop trailing zero columns?
var1_mat <- mcompanion(var1_mat)
var1_Sigma <- vs$Phi0inv
abs(eigen(diag(nrow(var1_mat)) - var1_mat)$values)
```

FittedPeriodicArModel-class Class FittedPeriodicArModel

#### Description

Class FittedPeriodicArModel.

## **Objects from the Class**

Objects can be created by calls of the form new("FittedPeriodicArModel", ar, ma, sigma2,...).

#### Slots

asyCov: Object of class "ANY" ~~ sigma2: Object of class "numeric" ~~ ar: Object of class "PeriodicArFilter" ~~ ma: Object of class "PeriodicMaFilter" ~~ center: Object of class "numeric" ~~ intercept: Object of class "numeric" ~~ theTS: Object of class "PeriodicTS" ~~ ns: Object of class "numeric" ~~

# Extends

Class "PeriodicArModel", directly. Class "PeriodicArmaModel", by class "PeriodicArModel", distance 2. Class "VirtualPeriodicArmaModel", by class "PeriodicArModel", distance 3. Class "PeriodicArmaSpec", by class "PeriodicArModel", distance 3. Class "VirtualPeriodicFilterModel", by class "PeriodicArModel", distance 4. Class "VirtualPeriodicStationaryModel", by class "PeriodicArModel", distance 4. Class "VirtualPeriodicAutocovarianceModel", by class "PeriodicArModel", distance 5. Class "VirtualPeriodicMeanModel", distance 5. Class "Virtu

# Methods

No methods defined with class "FittedPeriodicArModel" in the signature.

show signature(object = "FittedPeriodicArModel"): ...

summary signature(object = "FittedPeriodicArModel"): ...

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maxLag-methods

# Description

Methods for function maxLag() in package 'pcts'.

## Methods

signature(object = "PeriodicArmaFilter")

mC.ss

Create environment for mc-fitting

## Description

Creates an environment for mc-fitting. These functions are transitory, hence the strange names.

#### Usage

mC.ss(spec, ...)

## Arguments

spec	a model, an object of class mcSpec.
	further arguments to be passed on to xx.ss.
period	the number of seasons.
type.eigval	types of the eigenvalues, a character vector with elements "r" or "cp", see De- tails.
n.root	number of roots. Currently the dimension of the matrix is set to this.
eigabs	The absolute values/moduli of the eigenvalues, numeric vector.
eigsign	The signs/moduli of the eigenvalues.
co_r	similar to eigabs but for the co parameters.
co_arg	similar to eigsign but for the co parameters.
init	initial values, see Details.
len.block	lengths of Jordan blocks.
mo.col	last non-zero column in the top of the matrix.
generators	~~ TODO: describe this argument. ~~

#### Details

mC.ss takes the specification of the model as an object of class mcSpec and calls xx.ss.

Basically, the value returned by these functions is an extended model specification together with an environment which can be used for fitting the model, exploring the results and trying various things. This may be used for getting better understanding of the model and the optimisation routines.

The result of both function is a list, containing several functions and an environment. The environment (element env) is the most important element since it allows access to everything in the model environment. The function elements of the list are simply a convenience.

Several functions in env are available for fitting the model. Currently these are minim, minimBB and minimBBlu. The first argument of all these functions is a time series to which the model is to be fitted. By default, a conditional likelihood is being optimised. To base the optimisation on conditional sum of squares, set argument CONDLIK to FALSE. The remaining arguments in a call to any of the above functions are passed on to the corresponding optimisation routine (whose help page should be consulted for details).

minim uses the core R function optim. minimBB and minimBBlu use BBoptim from package BB. They result is a list, as returned by the corresponding optimisation function with the optimal parameters in element par. The elements of this vector are named to help somewhat in its interpretation but complete information about the fitted model can be obtained from the environment.

Firstly, at the end of the optimisation, the optimal parameters and other information are stored in env. If the same call (maybe with modified instructions for the optimisation) is repeated, these parameters will be used as initial values for a new optimisation run. This may be useful, for example, if the previous run didn't converge.

Secondly, properties of the fitted model and more useful representations can be obtained using functions in the environment or the convinience functions in the list returned by xx.ss.

optparam2mcparam converts a vector of parameters into the more familiar filter representation, where the i-th row contains the coefficients for the i-th season. This function takes one argument the vector of parameters, e.g. the one returned by the fitting functions. It updates a number of variables in env, computes the filter representation of the model and stores it in wrkmodel. It returns NULL. This function may be used for exploratory purposes or to set new values for the parameters, e.g. to be used as starting values for a new optimisation run.

mcparam2optparam does the opposite. It converts the current model in env to a vector of parameter. This function does not have arguments.

mclik computes the value of the conditional likelihood for given parameters. Its first argument is a time series, the second is a vector of parameters and the third is a vector of innovations. Only the first argument is compulsory. If param is not supplied, the current parameters in env are used. Otherwise, they are updated with the new parameters and then used. The innovations default to the zero vector. mcss is similar but computes the conditional sum of squares.

**Argument** init can be used to provide initial values. If it is missing or NULL, random initial values are generated for the free parameters. init may also be a numeric vector suitable for the call optparam2mcparam(init), see above. This vector would typically come from a previous optimisation run.

init may also be a list with elements "eigabs", "eigsign", "co\_r", "co\_abs". These components have the same meaning as the corresponding arguments of xx.ss.

#### **TODO: more is needed here!**

#### meanvarcheck

# Value

A list with the following components:

fmcss	a function to compute the sum of squares for a model.
fparamvec	a function to convert mc-parameters to optimisation parameters.
fmcparam	a function to convert optimisation parameters to mc-parameters.
env	an object of class environment

## Author(s)

Georgi N. Boshnakov

## References

Boshnakov GN and Iqelan BM (2009). "Generation of time series models with given spectral properties." *J. Time Series Anal.*, **30**(3), pp. 349–368. ISSN 0143-9782, http://dx.doi.org/10. 1111/j.1467-9892.2009.00617.x.

# See Also

xx.ss which is called by mC.ss

# Examples

```
# test0 roots
spec.coz2 <- mcompanion::mcSpec(dim = 5, mo = 4, root1 = c(1,1), order = rep(2,4))
spec.coz2
xxcoz2a <- mC.ss(spec.coz2)
## test0 roots
spec.coz4 <- mcompanion::mcSpec(dim = 5, mo = 4, root1 = c(1,1), order = rep(3,4))
xxcoz4a <- mC.ss(spec.coz4)</pre>
```

meanvarcheck Asymptotic covariance matrix of periodic mean

## Description

Asymptotic covariance matrix of periodic mean.

#### Usage

meanvarcheck(parmodel, n)

```
meancovmat(parmodel, n, cor = FALSE, result = "var")
```

#### Arguments

parmodel	a periodic model.
n	number of observations (TODO: need clarification here).
cor	if TRUE, return correlations
result	if "var", return the diagonal of the covariance matrix, otherwise return the matrix.

## Details

Computes asymptotic covariance or correlation matrix of the periodic means.

#### Value

if result = "var" a matrix, otherwise a vector

## Author(s)

Georgi N. Boshnakov

## See Also

parcovmatlist

#### Examples

```
x <- arima.sim(list(ar=0.9), n=1000)
proba1 <- fitPM(c(3,2,2,2), x)
meancovmat(proba1, 100)
meancovmat(proba1, 100, cor = TRUE)
meancovmat(proba1, 100, result = "")
meancovmat(proba1, 100, cor = TRUE, result = "")</pre>
```

meanvarcheck(proba1, 100)

modelCycle

Get the cycle of a periodic object

# Description

Get the cycle of a periodic object, ageneric function.

# Usage

modelCycle(object)

modelCycle ( object, ... ) <- value</pre>

#### Arguments

object	an object.
value	the new value for the cycle, an object inheriting from "BasicCycle".
	not used.

## Details

modelCycle() is essentially internal, for programming. The user level function to get the cycle of an object is pcCycle.

modelCycle() returns the Cycle object (in the sense of package **pcts**), associated with object. This is a generic function which makes it possible to associate a cycle with objects from a class, without inheriting from the cycle classes.

The default method returns NULL, unconditionally.

## Value

for modelCycle(), an object inheriting from class "BasicCycle" or NULL;

"modelCycle<-"() is used for the side effect of changing the cycle of object.

## Methods

```
signature(object = "ANY")
signature(object = "ModelCycleSpec")
```

## See Also

"modelCycle<-" for the replacement version.

ModelCycleSpec-class Class ModelCycleSpec

## Description

Class ModelCycleSpec.

#### **Objects from the Class**

Objects can be created by calls of the form new("ModelCycleSpec",...).

## Slots

```
modelCycle: Object of class "BasicCycle" ~~
```

#### Methods

```
modelCycle signature(object = "ModelCycleSpec"): ...
modelCycle<- signature(object = "ModelCycleSpec"): ...</pre>
```

nCycles

# Description

Basic information about periodic time series.

# Usage

```
nCycles(x, ...)
nTicks(x, ...)
nVariables(x, ...)
```

#### Arguments

х	an object from a periodic time series class.
	further arguments for methods.

## Details

These are generic functions. The default methods will work for any objects for which NROW and NCOL are defined and have the conventional case by variables interpretation.

nTicks gives the number of time points, i.e. number of rows in the matrix representation.

nVariables gives the nmber of variables in the time series.

nCycles gives the number of cycles available in the data, e.g. number of years for monthly data. It always gives an integer number. Cuttently, if the result is not an integer an error is raised. **TODO:** There is a case to round up or give the number of full cycles available but this seems somewhat dangerous if done quietly. A good alternative is to provide argument for control of this.

# Value

integer number

#### Author(s)

Georgi N. Boshnakov

```
ap <- pcts(AirPassengers)
nVariables(ap)
nTicks(ap)
nCycles(ap)
monthplot(ap)
boxplot(ap)</pre>
```

nSeasons-methods Number of seasons for a periodic object

## Description

Number of seasons for a periodic object.

## Arguments

object an object for which the notion of number of seasons makes sense.

## Details

nSeasons is a generic function. This page gives its methods for the periodic classes in package "pcts".

### Value

an integer number

### Methods

```
signature(object = "DayWeekCycle")
signature(object = "FiveDayWeekCycle")
signature(object = "MonthYearCycle")
signature(object = "PeriodicIntegratedArmaSpec")
signature(object = "QuarterYearCycle")
signature(object = "PeriodicInterceptSpec")
signature(object = "Cyclic")
signature(object = "BareCycle")
```

# Author(s)

Georgi N. Boshnakov

## Examples

```
ap <- pcts(AirPassengers)
nSeasons(ap) # 12
pcfr <- pcts(dataFranses1996)
nSeasons(pcfr) # 4</pre>
```

num2pcpar

#### Description

Fit PAR model using sample autocorrelations.

#### Usage

```
num2pcpar(x, order, result = NULL, ...)
```

### Arguments

х	time series, a numeric vector.
order	PAR order, a single number or a vector with one entry for each season.
result	what to return, the default is to return the full model, see Details.
	passed on to calc_peracf.

#### Details

Computes the periodic autocorrelations and fits a PAR model using the Periodic Levinson-Durbin algorithm.

The order is a vector of non-negative integers, specifying the autoregressive orders for each season. If order is a single number, then all seasons have that order.

mean controls centering in the computation of the autocorrelations. If mean is numeric, then subtract the supplied mean before computing the autocovariances. If mean is TRUE, the default, compute and subtract the sample periodic mean before computing the autocovariances. If mean is FALSE, do not centre the series, i.e. assume that the mean is zero.

If result is NULL, the default, returns the full model. If result = "coef", returns the PAR coefficients only (currently any value of result other than NULL has this effect).

### Value

The coefficients of the fitted model or a list with components:

mean	the mean, set as described in Details.
coef	forward prediction coefficients.
scale	standard deviations of the innovations.

## Author(s)

Georgi N. Boshnakov

#### See Also

fitPM which uses num2pcpar for calculations

### parcovmatlist

### Examples

```
## Not run:
simts1 <- matrix(rnorm(100), nrow = 4)
num2pcpar(simts1, order = c(3,2,2,2), period = 4 )
num2pcpar(simts1, order = c(3,2,1,2), period = 4 )
pdSafeParOrder(c(3,2,1,2))
pdSafeParOrder(c(3,2,2,1))
num2pcpar(simts1, order = c(3,2,2,1), period = 4 )
num2pcpar(simts1, order = pdSafeParOrder(c(3,2,2,1)), period = 4 )
num2pcpar(simts1, order = c(3,2,1,2), period = 4 )
num2pcpar(simts1, order = c(3,2,1,2), period = 4, mean = rep(0,4) )
num2pcpar(simts1, order = c(3,2,1,2), period = 4, mean = FALSE )
num2pcpar(simts1, order = c(3,2,1,2), period = 4, mean = FALSE )$coef@m -
num2pcpar(simts1, order = c(3,2,1,2), period = 4 )$coef@m
```

## End(Not run)

parcovmatlist Compute asymptotic covariance matrix for PAR model

#### Description

Compute asymptotic covariance matrix for PAR model

#### Usage

```
parcovmatlist(parmodel, n, cor = FALSE, result = "list")
```

## Arguments

parmodel	PAR model, object of class parModel
n	length of the series or a vector with one element for each season.
cor	If TRUE return correlation matrix.
result	if "list", the default, return a list, if "Matrix" return a Matrix object, otherwise return an ordinary matrix, see Details.

#### Details

Uses eq. (3.3) in the reference.

If result = "list", parcovmatlist returns a list whose s-th element is the covariance matrix of the PAR parameters for the s-th season. Otherwise, if result = "Matrix" it returns a block-diagonal matrix created by .bdiag() from package "Matrix". If result = "matrix" it returns an ordinary matrix (with the current implementation this is returned for any value other than "list" or "Matriix").

a list, matrix or block-diagonal matrix, as described in Details

#### Author(s)

Georgi N. Boshnakov

## References

McLeod A (1994). "Diagnostic checking of periodic autoregression models with application." *Journal of time series analysis*, **15**(2), pp. 221-233.

## See Also

pcacfMat, pc.acf.parModel

## Examples

```
x <- arima.sim(list(ar=0.9), n=1000)
proba1 <- fitPM(c(3,2,2,2), x)</pre>
```

```
parcovmatlist(proba1, 100)
parcovmatlist(proba1, 100, cor = TRUE)
sqrt(diag(parcovmatlist(proba1, 100, cor = TRUE)[[1]]))
```

```
meanvarcheck(proba1, 100)
```

PartialPeriodicAutocorrelations-class Class PartialPeriodicAutocorrelations

## Description

Class PartialPeriodicAutocorrelations.

### **Objects from the Class**

Objects can be created by calls of the form new("PartialPeriodicAutocorrelations",...,data).

# Slots

```
modelCycle: Object of class "BasicCycle" ~~
data: Object of class "Lagged" ~~
```

# Extends

Class "ModelCycleSpec", directly. Class "FlexibleLagged", directly. Class "VirtualPeriodicAutocorrelations", directly. Class "Lagged", by class "FlexibleLagged", distance 2. Class "VirtualPeriodicModel", by class "VirtualPeriodicAutocorrelations", distance 2.

40

# pc.filter

## Methods

show signature(object = "PartialPeriodicAutocorrelations"): ...

pc.filter

#### *Applies a periodic ARMA filter to a time series*

# Description

Filter time series with a periodic arma filter. If whiten is FALSE (default) the function applies the given ARMA filter to eps (eps is often periodic white noise). If whiten is TRUE the function applies the "inverse filter" to x, effectively computing residuals.

## Usage

### Arguments

x	the time series to be filtered, a vector.
eps	residuals, a vector or NULL.
model	the model parameters, a list with components "phi", "theta", "p", "q", "period", "mean" and "intercept", see Details.
seasonof1st	the season of the first observation (i.e., of $x[1]$ ).
from	the index from which to start filtering.
whiten	if TRUE use x as input and apply the inverse filter to produce eps ("whiten" x), if FALSE use eps as input and generate x ("colour" eps).
nmean	a vector of means having the length of the series, see Details.
nintercept	a vector of intercepts having the length of the series, see details.

#### Details

The model is specified by argument model, which is a list with the following components:

phi the autoregression parameters,

theta the moving average parameters,

p the autoregression orders, a single number or a vector with one element for each season,

q the moving average orders, a single number or a vector with one element for each season,

period number of seasons in a cycle,

mean means of the seasons,

intercept intercepts of the seasons.

The relation between x and eps is assumed to be the following. Let

$$y_t = x_t - mu_t$$

be the mean corrected series, where  $mu_t$  is the mean, see below. The equation relating the mean corrected series,  $y_t = x_t - \mu_t$ , and eps is the following:

$$y_t = c_t + \sum_{i=1}^{p_t} \phi_t(i) y_{t-i} + \sum_{i=1}^{q_t} \theta_t(i) \varepsilon_{t-i} + \varepsilon_t$$

where  $c_t$  is the intercept, nintercept. The inverse filter is obtained by writing this as an equation expressing  $\varepsilon_t$  through the remaining quantities.

If whiten = TRUE, pc.filter uses the above formula to compute the filtered values of x for t=from, ..., n, i.e. whitening the time series if eps is white noise. If whiten = FALSE, eps is computed, i.e. the inverse filter is applied x from eps, i.e. "colouring" x. In both cases the first few values in x and/or eps are used as initial values.

Essentially, the mean is subtracted from the series to obtain the mean-corrected series, say y. Then either y is filtered to obtain eps or the inverse filter is applied to obtain y from eps finally the mean is added back to y and the result returned.

The mean is formed by model\$mean and argument nmean. If model\$mean is supplied it is recycled periodically to the length of the series x and subtracted from x. If argument nmean is supplied, it is subtracted from x. If both model\$mean and nmean are supplied their sum is subtracted from x.

The above gives a vector y,  $y_t = x_t - \mu_t$ , which is then filtered. If the mean is zero,  $y_t = x_t$  in the formulas below.

Finally, the mean is added back,  $x_t = y_t + \mu_t$ , and the new x is returned.

The above gives a vector y which is used in the filtering. If the mean is zero,  $y_t = x_t$  in the formulae below.

pc.filter can be used to simulate pc-arma series with the default value of whiten=FALSE. In this case eps is the input series and y the output.

$$y_t = c_t + \sum_{i=1}^{p_t} \phi_t(i) y_{t-i} + \sum_{i=1}^{q_t} \theta_t(i) \varepsilon_{t-i} + \varepsilon_t$$

Then model\$mean or nmean are added to y to form the output vector x.

Residuals corresponding to a series y can be obtained by setting whiten=TRUE. In this case y is the input series. The elements of the output vector eps are calculated by the formula:

$$\varepsilon_t = -c_t - \sum_{i=1}^{q_t} \theta_t(i)\varepsilon_{t-i} - \sum_{i=1}^{p_t} \phi_t(i)y_{t-i} + y_t$$

There is no need in this case to restore x since eps is returned.

In both cases any necessary initial values are assumed to be already in the vectors. If from is not supplied it is chosen as the smallest i such that for all  $t \ge i$ , t-p[t]>0 and t-q[t]>0, i.e. the filter will not require negative indices for x or eps.

pc.filter calls the lower level function pc.filter.xarma to do the computation.

# pc.filter.xarma

# Value

The filtered series: the modified x if whiten=FALSE, the modified eps if whiten=TRUE.

### Level

1

# Author(s)

Georgi N. Boshnakov

## See Also

the lower level functions pc.filter.xarma which do the computations

pc. I II cel . Xal IIIa I I litter little series with periodic drind fillers	pc.filter.xarma	Filter time series with periodic arma filters
--	-----------------	---

# Description

Filter time series with periodic arma filters with or options for periodic and non-periodic intercepts.

## Usage

# Arguments

x	the time series to be filtered, a vector.
eps	the innovations, a vector.
phi	the autoregression parameters, a matrix.
theta	the moving average parameters, a matrix.
period	the period (number of seasons in a year).
р	the autoregression orders, recycled to period if length(p)=1.
q	the moving average orders, recycled to period if length(q)=1.
n	a positive integer, the time index of the last observation to be filtered.
from	a positive integer, the time index of the first observation to be filtered.
seasonof1st	a positive integer, the season of the time index of x[1], see Details.
intercept	the intercepts of the seasons, a vector of length period.
nintercept	intercepts, a vector of the same length as x.

#### **Details**

pc.filter.xarma is somewhat lower level. The user level function is pc.filter which uses pc.filter.xarma to do the computations.

pc.filter.xarma filters the time series x by the following formula (for t=from,...,n):

$$x_t = c_t + \sum_{i=1}^{p_t} \phi_t(i) x_{t-i} + \sum_{i=1}^{q_t} \theta_t(i) \varepsilon_{t-i} + \varepsilon_t,$$

where  $c_t$  is the overall intercept at time t, see below. Values of x[t] for t outside the range from, n, if any, are left unchanged. Values for t<from are used as initial values when needed.

Two intercepts are provided for convenience and some flexibility. The periodic intercept, intercept, is a vector of length period. It is replicated to length n, taking care to ensure that the first element of the resulting vector, say a, starts with intercept[seasonof1st]. nintercept can be an arbitrary vector of length n. It can be used to represent trend or contributions from covariates. nintercept is not necessarilly periodic and argument seasonof1st does not affect its use. The overall intercept is obtained as the sum c = a + nintercept.

Usually x is a numeric vector but it can also be a matrix in which each column represents the data for one "year". Also, the length of x is typically, but not necessarilly, equal to n. It is prudent to ensure that  $length(x) \ge n$  and this must be done if x is a matrix.

Argument phi is ignored if p==0, argument theta is ignored if q==0.

pc.filter.xarma is meant to be called by other functions whose task is to prepare the arguments with proper checks. It does not make much sense to repeat the checks in pc.filter.xarma. In particular, no check is made to ensure that from and n are correctly specified.

This is a low level function meant to be used with basic vectors and matrices. TODO: Implement in C/C++. In the current implementation. it accesses the elements of the arguments with straightforward indexing, so objects from classes may be used as well, provided that x[t], eps[t], phi[t,i], theta[t,i], as well as assignment to x[t], are defined for scalar indices.

## Value

Returns x with x[from] to x[n] filled with the filtered values and values outside the interval from, ..., n left unchanged.

The mode of x is left unchanged. In particular, x may be a matrix with each row representing the data for a season. This is convenient since periodic time series are often more easily processed in this form.

## Level

0 (base)

## Author(s)

Georgi N. Boshnakov

### See Also

pc.filter

pc.hat.h

# Description

The h coefficients are scaled cross-covariances between the time series and the innovations. This function computes estimates for h using as input the observed series, a series of estimated innovations, and an estimate of the variance of the innovations.

### Usage

pc.hat.h(x, eps, maxlag, si2hat)

## Arguments

х	the observed time series $x(t)$
eps	a series of esimated innovations
maxlag	maximum lag
si2hat	estimate of the variance of the innovations

## Details

If missing, the variance of the innovations is estimated from eps.

#### Value

A matrix of the coefficient up to lag maxlag with one row for each season.

## Author(s)

Georgi N. Boshnakov

# References

Boshnakov GN (1996). "Recursive computation of the parameters of periodic autoregressive movingaverage processes." *J. Time Ser. Anal.*, **17**(4), pp. 333–349. ISSN 0143-9782, http://dx.doi. org/10.1111/j.1467-9892.1996.tb00281.x. pc.sdfactor

# Description

This function computes a matrix of factors such that elementwise division of the periodic autocovariance matrix by it will give the periodic autocorrelations.

# Usage

pc.sdfactor(sd, maxlag)

## Arguments

sd	standard deviations of the seasons
maxlag	maximal lag

## Details

todo: describe!

## Value

a matrix of coefficients of size period x (maxlag+1). The length of sd is taken to be the period.

## Author(s)

Georgi N. Boshnakov

### See Also

autocorrelations

pcacfMat

Compute PAR autocovariance matrix

# Description

Compute PAR autocovariance matrix

# Usage

pc.acf.parModel(parmodel, maxlag = NULL)

pcacfMat(parmodel)

#### pcacfMat

#### Arguments

parmodel	PAR model, an object of class parModel.
maxlag	maximum lag

### Details

pc.acf.parModel returns the autocovariances of a PAR model in season-lag form with maximum lag equal to maxlag. If maxlag is larger than the available precomputed autocovariances, they missing ones are computed using the Yule-Walker relations. Note that pc.acf.parModel assumes that there are enough precomputed autocovariances to use the Yule-Walker recursions directly.

TODO: pc.acf.parModel is tied to the old classes since it accesses their slots. Could be used as a template to streamline the method for autocovariances for class "PeriodicAutocovariance".

The season-lag form can be easily converted to other forms with the powerful indexing operator, see the examples and slMatrix-class.

pcacfMat is a convenience function for statistical inference. It creates a covariance matrix with dimension chosen automatically. This covariance matrix is such that the asymptotic covariance matrix of the estimated parameters can be obtained by dividing sub-blocks by innovation variances and inverting them. See, eq. (3.3) in the reference.

#### Value

for pcacfMat, a matrix

for pc.acf.parModel, an slMatrix

### Author(s)

Georgi N. Boshnakov

## References

McLeod A (1994). "Diagnostic checking of periodic autoregression models with application." *Journal of time series analysis*, **15**(2), pp. 221-233.

## See Also

#### slMatrix-class

### Examples

```
x <- arima.sim(list(ar = 0.9), n = 1000)
proba1 <- fitPM(c(3,2,2,2), x)
acfb <- pc.acf.parModel(proba1, maxlag = 8)
acfb[4:(-2), 4:(-2), type = "tt"]</pre>
```

pcacfMat(proba1)

pcacf\_pwn\_var

## Description

Computes the variances of sample periodic autocorrelations from periodic white noise.

# Usage

```
pcacf_pwn_var(nepoch, period, lag, season)
```

# Arguments

lag	desired lags, a vector of positive integers.
season	desired seasons.
nepoch	number of epochs.
period	number of seasons.

## Details

These are given by McLeod (1994), see the reference, eq. (4.3).

## Value

A matrix whose (i,j)th entry contains the variance of the autocorrelation coefficient for season season[i] and lag lag[j].

## Author(s)

Georgi N. Boshnakov

#### References

McLeod A (1994). "Diagnostic checking of periodic autoregression models with application." *Journal of time series analysis*, **15**(2), pp. 221-233.

### Examples

pcacf\_pwn\_var(79, 12, 0:16, 1:12)

### Description

Calculate partial periodic autocorrelations, forward and backward prediction coefficients and error variances using the periodic Levinson-Durbin algorithm.

## Usage

alg1(r, p)

### Arguments

r	periodic autocovariances, a matrix, see 'Details'.
р	autoregressive orders, numeric vector.

## Details

alg1(r, p) calculates the partial periodic correlations from autocovariances r and autoregression orders p. The matrix r has the same format as that of the r slot of pcAcvf objects. The periodicity, d, is set equal to the number of rows in r. If the length of p is not equal to the periodicity, all autoregressive orders are set to the first element of p. This last feature is really meant to be used only with a scalar p.

The convention for the signs of the coefficients is the one from Boshnakov(1996) and is consistent with other R time series functions.

pmax below stands for the maximal element of p, i.e. the maximal AR order.

As in the non-periodic case, the periodic Levinson-Durbin algorithm fits recursively models of order 0, 1, ..., pmax. Namely, at step i the AR orders for all seasons are set to i. This is done in a way that correctly handles the case when not all elements of p are equal, see the references.

The essential quantities calculated by the periodic Levinson-Durbin algorithm are returned as matrices, whose ith rows contain values for season i. The complete details depend on the quantities, as described below.

The partial autocorrelations, the forward innovation variances and the backward innovation variances are returned as matrices with d rows and 1+pmax columns, whose j-th columns contain the quantities for order j-1 (partial autocorrelations, forward innovation variances and backward innovation variances, respectively). Note that the lag-0 partial autocorrelations are the autocovariances for lag 0, see the references for details.

The forward autoregression parameters are returned as a list whose jth element is a matrix containing the coefficients for order j. Similarly for the backward autoregression parameters.

One often is interested in the model of order p only. Its coefficients are given by af[[pmax]], while the innovation variances are in the last column of fv.

pcalg1

## Value

A list with the following elements.

orders	autoregression orders
be	partial autocorrelations, a matrix with d rows
fv	forward innovation variances, a matrix with d rows
bv	backward innovation variances, a matrix with d rows
af	forward autoregression parameters, a list with one element for the parameters for each order.
ab	backward autoregression parameters, a list with one element for the parameters for each order.

# Note

The autoregression orders of the output are not necessarilly the same as those specified in the call. There may be no PAR model with the requested orders, see the references.

## Author(s)

Georgi N. Boshnakov

# References

Boshnakov GN (1996). "Recursive computation of the parameters of periodic autoregressive movingaverage processes." *J. Time Ser. Anal.*, **17**(4), pp. 333–349. ISSN 0143-9782, http://dx.doi. org/10.1111/j.1467-9892.1996.tb00281.x.

Lambert-Lacroix S (2000). "On periodic autoregressive process estimation ." *IEEE Transactions on Signal Processing*, **48**(6), pp. 1800-1803.

Lambert-Lacroix S (2005). "Extension of autocovariance coefficients sequence for periodically correlated processes." *Journal of Time Series Analysis*, **26**(6), pp. 423-435.

#### See Also

pdSafeParOrder

# Examples

```
r1 <- rbind(c(1,0.81,0.729),c(1,0.90,0.900))
alg1(r1,2)
## pc2 <- pcAcvf(init=r1)
## pc2a <- pcAcvf(init=r1,seasonnames=c("am","pm"), periodunit="day")
# example of Lambert-Lacroix
data(ex1f)
pc3 <- slMatrix(period=2,maxlag=5,f=ex1f,type="tt")
res0p2 <- alg1(pc3[],c(0,2))
res1p2 <- alg1(pc3[],c(1,2))</pre>
```

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# pcalg1util

```
res3p3 <- alg1(pc3[],c(3,3))</pre>
paramsys1 <- pcarma_param_system(pc3, NULL, NULL, 2, 0, 2)</pre>
t1 <- solve(paramsys1$A,paramsys1$b)</pre>
# this is from tests.r but I have lost t1
# set it to pc3 below
# note: t1 is not the t1 computed above and in other examples!
t1 <- pc3
t1
t1[]
alg1(t1[],c(1,1))
alg1(t1[],c(1,0))
alg1(t1[],c(0,1))
alg1(t1[],c(5,5))
alg1(t1[],c(2,2))
alg1(t1[],c(2,3))
alg1(t1[],c(3,3))
alg1(t1[],c(4,4))
alg1(t1[],c(5,5))
```

pcalg1util	Give partial periodic autocorrelations or other partial prediction
	quantities for a pcAcvf object.

### Description

Give partial periodic autocorrelations or other partial prediction quantities for a pcAcvf object.

## Usage

alg1util(x, s, at0 = 1)

# Arguments

x	an object of a class inheriting from pc.Model.WeaklyStat
S	the required quantity, the name of one of the elements of the list returned by alg1.
at0	if not identical to "var", replace the elements of the result at lag zero with 1, see 'Details'.

## Details

This function is a wrapper for alg1(). It calls alg1, to do the computations and returns the requested element as an object from class slMatrix. The model order is set to the maximal lag avialable in x,

If at0 is the character string "var", then the lag zero values in the result are set to the lag zero autocovariances, otherwise they are set to 1. This is mainly relevant for the periodic partial autocorrelations (s="be"), since the setting at0="var" ensures that they are in one to one correspondence with the autocovariances.

## Value

the requested quantity as an object of type slMatrix

## Author(s)

Georgi N. Boshnakov

## References

Lambert-Lacroix S (2000). "On periodic autoregressive process estimation ." *IEEE Transactions* on Signal Processing, **48**(6), pp. 1800-1803.

Lambert-Lacroix S (2005). "Extension of autocovariance coefficients sequence for periodically correlated processes." *Journal of Time Series Analysis*, **26**(6), pp. 423-435.

#### See Also

pdSafeParOrder, alg1

#### Examples

```
r1 <- rbind(c(1,0.81,0.729),c(1,0.90,0.900))
```

```
# example of Lambert-Lacroix
data(ex1f)
pc3 <- slMatrix(period=2,maxlag=5,f=ex1f,type="tt")
res0p2 <- alg1(pc3[],c(0,2))
res1p2 <- alg1(pc3[],c(1,2))
res3p3 <- alg1(pc3[],c(3,3))</pre>
```

pcAr.ss

Compute the sum of squares for a given PAR model

#### Description

Compute the sum of squares for a given PAR model.

#### Usage

pcAr.ss(x, model, eps = numeric(length(x)))

# pcAR2acf

#### Arguments

х	time series, a numeric vector.
model	a model.
eps	residuals, defaults to a vector of zeroes. This may be used for models with moving average terms, for example.

## Details

todo:

## Value

a number

### Author(s)

Georgi N. Boshnakov

pcAR2acf	Compute periodic autocorrelations from PAR coefficients	
	J	

# Description

Compute periodic autocorrelations from PAR coefficients. This effectively solves the inverse problem to that solved by the periodic Levinson-Durbin algorithm but does not use a recursion.

## Usage

```
pcAR2acf(coef, sigma2, p, maxlag = 10)
```

### Arguments

coef	PAR coefficients, a matrix, see Details.
sigma2	innovations variances.
р	PAR order.
maxlag	How many lags to compute.

#### Details

coef is a matrix with the coefficients for season i in the i-th row. The coefficients start from lag 1.

The first few autocorrelations are computed by solving a linear system, see the references. The rest, are generated using the periodic Yule-Walker equations.

## Value

a matrix, in which row s contains the acf's for season s for lags 0, 1, ..., maxlag (in this order).

#### Author(s)

Georgi N. Boshnakov

### References

Boshnakov GN (1996). "Recursive computation of the parameters of periodic autoregressive movingaverage processes." *J. Time Ser. Anal.*, **17**(4), pp. 333–349. ISSN 0143-9782, http://dx.doi. org/10.1111/j.1467-9892.1996.tb00281.x.

Boshnakov GN and Boteva A (1992). "An algorithm for the computation of the theoretical autocovariances of a periodic autoregression process." Varna.

## See Also

pcarma\_acvf\_lazy, which does the main computation, but note that the coefficients for it start from lag zero

## Examples

```
m <- rbind( c(0.81,0), c(0.4972376, 0.4972376) )
si2 <- PeriodicVector(c(0.3439000,0.1049724))
pcAR2acf(m, si2, 2)
pcAR2acf(m, si2, 2, maxlag=10)
# same using pcarma_acvf_lazy directly
m1 <- rbind( c(1, 0.81, 0), c(1, 0.4972376, 0.4972376) )
testphi <- slMatrix( init=m1 )
myf <- pcarma_acvf_lazy(testphi, testtheta, si2, 2, 0, 2, maxlag=10)
myf(1:2,0:9)  # get a matrix of values
all(myf(1:2,0:9) == pcAR2acf(m, si2, 2, maxlag = 9)) # TRUE</pre>
```

pcarma\_acvf2model Fit a PC-ARMA model to a periodic autocovariance function

#### Description

Fit a PC-ARMA model to a periodic autocovariance function.

#### Usage

pcarma\_acvf2model(acf, model, maxlag)

### pcarma\_solve

### Arguments

acf	a periodic autocovariance function, an object of class pcAcvf.
model	a pc- arma model, an object of class pcARMApq. (todo: check!)
maxlag	not used. (todo: check!)

# Value

~Describe the value returned If it is a LIST, use

comp1	Description of 'comp1'
comp2	Description of 'comp2'

•••

## Author(s)

Georgi N. Boshnakov

## References

Boshnakov GN (1996). "Recursive computation of the parameters of periodic autoregressive movingaverage processes." *J. Time Ser. Anal.*, **17**(4), pp. 333–349. ISSN 0143-9782, http://dx.doi. org/10.1111/j.1467-9892.1996.tb00281.x.

## Examples

```
data(ex1f)
pc3 <- slMatrix(period=2,maxlag=5,f=ex1f,type="tt")
# pcarma_param_system(pc3, NULL, NULL, 2, 0, 2)
parsys <- pcarma_param_system(pc3, NULL, NULL, c(2,2), 0, 2)
param <- solve(parsys$A,parsys$b)
# res <- pcarma_acvf2model(pc3, list(p=c(1,2),q=0,period=2))
# res <- pcarma_acvf2model(pc3, list(p=c(1,2),q=0))
# res <- pcarma_acvf2model(pc3, list(p=c(1,2),period=2))
res <- pcarma_acvf2model(pc3, list(p=c(1,2)))
print(param)
print(res)</pre>
```

pcarma\_solve

Functions to compute various characteristics of a PCARMA model

## Description

Given a PCARMA model, create a function for computing autocovariances or coefficients of the corresponding infinite moving average representation or prepare the linear system whose solution provides the first few autocovariances of the model.

## Usage

```
pcarma_acvf_lazy(phi, theta, sigma2, p, q, period, maxlag = 100)
pcarma_h_lazy(phi, theta, p, q, period, maxlag = 200)
pcarma_acvf_system(phi, theta, sigma2, p, q, period)
pcarma_param_system(acf, h, sigma2, p, q, period)
pcarma_h(h, na = NA)
```

# Arguments

phi	the autoregression parameters, an object of class "slMatrix"
theta	the moving average parameters, an object of class "slMatrix"
sigma2	the innovation variances, an object of class "PeriodicVector" or a vector of size period, Details.
р	the (maximal) autoregression order or the autoregression orders.
q	the (maximal) moving average order or the moving average orders.
period	number of seasons in an epoch
maxlag	maximal lag for which the result is stored internally.
acf	the autocovariance function, an object of class pcAcvf, slMatrix, or similar
h	pcarma_param_system, h(t,k) is expected to return the coefficient $h_{t,k}$ . h is usually created by pcarma_h_lazy. For pcarma_h, a matrix of h(t,i) coefficients.
na	not used currently, controls what to do for large lags.

## Details

#### **Compute acvf from parameters:**

pcarma\_acvf\_lazy creates a function that will compute (on demand) values of the acf by a recursive formula. Computed values are stored internally for lags up to maxlag.

#### System for acvf from parameters:

pcarma\_acvf\_system forms a linear system for the calculation of autocovariances from the parameters of a pc-arma model. The argument theta is not used if q = 0 and phi is not used if p = 0.

**System for parameters from acvf:** pcarma\_param\_system takes the periodic autocovariances of a pc-arma model and computes a matrix and a vector representing the linear system whose solution provides the parameters of the model.

Scalar p specifies the same autoregression order for each season, similarly for q. p and q may be vectors of length period specifying the order for each season individually. In the latter case the solution of the system may not be a proper model or, if it is, its autocovariances may not be the ones used here! See the references for details.

The class of acf is not required to be one of those explicitly listed above, but it should understand their indexing conventions, similarly for sigma2.

For pure autoregression, q = 0, the arguments h and sigma2 are ignored. TODO: add sigma2 (if supplied) to the returned list?

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#### **Compute h from parameters:**

pcarma\_h\_lazy: h(t,i) are the coefficients in infinite the moving average representation of the pc.arma model. The calculations use formula (4.4) from my paper (or elsewhere) with internal storage (in an slMatrix) of calculated results (for i<maxlag) and recursive calls to itself. So, it is not necessary to compute h(t,i) in any particular order.

#### Infinite MA coefficients(h):

pcarma\_h Function to create a function for lazy computation of h(t,i) in pc.arma models Takes a matrix of h(t,i) coefficients and returns a function that calculates h(t,i) from my paper xxx. The returned value can be used in the same way as that of pcarma\_h\_lazy.

#### Value

## for pcarma\_acvf\_lazy:

a function taking two arguments t and k such that for scalar t and k the call f(t,k) will return EX(t)X(t-k). If either of the arguments is a vector, then f(t,k) returns a matrix of size (length(t), length(k)) containing the respective autocovariances.

#### for pcarma\_h\_lazy:

a function, say h. In calls to h, if both arguments are scalars h(t, i) returns  $h_{t,i}$ . If at least one of the arguments is a vector a matrix of values of h is returned.

#### for pcarma\_acvf\_system:

a list with two components representing the linear system:

A The (p+1) period  $\times$  (p+1) period matrix of the system, an object of class "matrix".

**b** The right-hand side of the system, a vector of length (p+1) period, an object of class "vector".

 $A^{-1}b$  can be used to get a vector of the autocovariances in the following order (d is the period, p is the maximal AR order):

K(1,0), ..., K(d,0), K(1,1), ..., K(d,1), ..., K(1,p), ..., K(d,p).

#### for pcarma\_param\_system:

A list with components representing the linear system and the AR and MA orders:

- **A** The matrix of the system
- **b** The right-hand side of the system
- **p** The AR order
- q The MA order

 $A^{-1}b$  will return a vector of the parameters of the pc-arma model: all parameters for the first season, followed by all parameters for the second seasons and so on. For each season the parameters are in the following order (s is the current season, d is the period, p[s] and q[s] are the corresponding AR and MA orders):

$$\sigma^2(s), \phi(s, 1), ..., \phi(s, p[s]), \theta(s, 1), ..., \theta(s, q[s]).$$

#### for pcarma\_h:

a function, say h. In calls to h, if both arguments are scalars h(t, i) returns  $h_{t,i}$ . If at least one of the arguments is a vector a matrix of values of h is returned. Analogous to pcarma\_h\_lazy.

for pcarma\_acvf\_lazy: The recursion may become extremely slow for lags greater than maxlag. If large lags are likely to be needed the argument maxlag should be used to increase the internal storage. The default for maxlag currently is 100.

### Author(s)

Georgi N. Boshnakov

### References

Boshnakov GN (1996). "Recursive computation of the parameters of periodic autoregressive movingaverage processes." *J. Time Ser. Anal.*, **17**(4), pp. 333–349. ISSN 0143-9782, http://doi.org/ 10.1111/j.1467-9892.1996.tb00281.x.

### See Also

pcarma\_h, pcarma\_param\_system

#### Examples

```
## periodic acf of Lambert-Lacroix
data(ex1f)
(pc3 <- slMatrix(period = 2, maxlag = 5, f = ex1f, type = "tt"))</pre>
## find the parameters
s3 <- pcarma_param_system(pc3, NULL, NULL, 2, 0, 2)
coef3 <- solve(s3$A, s3$b)</pre>
pcarma_unvec(list(p = 2, q = 0, period = 2, param = coef3))
## actually, the model is PAR(1,2):
s3a <- pcarma_param_system(pc3, NULL, NULL, c(1, 2), 0, 2)
coef3a <- solve(s3a$A, s3a$b)</pre>
pcarma_unvec(list(p = c(1,2), q = 0, period = 2, param = coef3a))
## prepare test parameters for a PAR(2) model with period=2.
## (rounded to 6 digits from the above example.
m1 <- rbind(c(1, 0.81, 0), c(1, 0.4972376, 0.4972376) )
m2 <- rbind(c(1, 0, 0), c(1, 0, 0))
testphi <- slMatrix(init = m1)</pre>
testtheta <- slMatrix(init = m2)</pre>
si2 <- PeriodicVector(c(0.3439000, 0.1049724)) # # or si2 <- c(1,1)
## acf from parameters
myf <- pcarma_acvf_lazy(testphi, testtheta, si2, 2, 0, 2, maxlag = 110)</pre>
              # compute a value
myf(1,4)
a1 <- myf(1:2,0:9) # get a matrix of values
## h from parameters
h <- pcarma_h_lazy(testphi, testtheta, 2, 2, 2)</pre>
h(3, 2)
               # a scalar
```

#### pcarma\_unvec

```
h1 <- h(1:2, 1:4) # a matrix
## compute acvf from parameters
( acfsys <- pcarma_acvf_system(testphi, testtheta, si2, 2, 0, 2) )
acfvec <- solve(acfsys$A, acfsys$b)
acf1 <- slMatrix(acfvec, period = 2)
## TODO: examples wirh q != 0</pre>
```

```
pcarma_unvec
```

Functions for work with a simple list specification of pcarma models

## Description

Handle a simple list specification of pcarma models. Functions to convert to and from a representation appropriate for handing on to optimisation functions.

### Usage

```
pcarma_prepare(model, type)
pcarma_unvec(model)
pcarma_tovec(model)
```

#### Arguments

model	specification of a pcarma model, a list, see Details.
type	not used.

## Details

These functions work with a specification of a pcarma model as a list with components period, p, q, param, phi, theta and si2, see also section 'Values'. The functions do not necessarily need or examine all these components.

Argument model is a list with components as accepted by pcarma\_prepare. Details are below but the guiding rule is that there are sensible defaults for absent components.

pcarma\_prepare gives a standard representation of model, in the sense that it ensures that the model has components period, p and q, such that p and q are vectors of length period. pcarma\_prepare does not examine any other components of the model. (**TODO:** do the same for the innovation variance?)

If model\$period is NULL, pcarma\_prepare sets it to the length of the longer of model\$p and model\$q. If model\$p is a scalar it is extended with rep(model\$p,period). Missing or NULL model\$p is equivalent to model\$p = 0. model\$q is processed analogously.

The net effect is that period, p and q will be set as expected as long as period is given or at least one of the other two is of length equal to the period. A warning is issued if period <= 1 (it is all too easy to give scalar values for p and q and forget to set the period, in which case period will be deduced to be one).

A number of functions (including pcarma\_tovec and pcarma\_unvec) dealing with the list representation of pcarma models start by calling pcarma\_prepare to avoid the need for handling all possible cases.

pcarma\_tovec returns a list with components p, q and param, where param is a numeric vector containing the pcarma parameters and the innovations variances and thus is suitable for optimisation functions. Notice that it is component param that is a vector. The reason that pcarma\_tovec returns a list, is that the caller may need to do further work before calling a generic optimisation function. For exampe, it may wish to dop the variances from the vector.

pcarma\_unvec(model) performs the inverse operation. It takes a list like that produced by pcarma\_tovec and converts it to a detailed list containing the components of the model.

#### Value

for pcarma\_unvec, a list with components:

р	autoregressive orders, numeric vector
q	moving average orders, numeric vector
si2	innovation variances
phi	autoregressive parameters
theta	moving average parameters

for pcarma\_tovec, a list with components:

р	autoregressive order
q	moving average order
param	parameters of the model, a numeric vector. TODO: give the order of the parameters in the vector!

for pcarma\_prepare, a list as pcarma\_unvec, see also Details.

# Note

The specification and the functions were created ad hoc to get the computations going and are not always consistent with other parts of the package.

## Author(s)

Georgi N. Boshnakov

pcCycle-methods

#### Description

Generic function with methods for creating or extracting cycle objects. The type of the cycle object to return is inferred from the arguments.

## Usage

pcCycle(x, type, ...)

#### Arguments

х	an object, methods include numeric, character and cyclic objects, see Details.
type	class of the result. If equal to "auto", the default, the class is determined by the argument(s), otherwise should be the name of a cycle class.
	further arguments for methods.

#### Details

pcCycle serves as both a constructor and extractor of cycle objects. It is meant to just do the right thing, relieving the user from the burden of specifying a particular cycle class.

If x inherits from "Cyclic", pcCycle returns its cycle component. If x is numeric it constructs a cycle object with period x and additional properties as specified by the other arguments. If x is a character string, it is taken to be the name of one of the builtin cycles.

Argument type should be rarely needed, except maybe to conveniently force conversion of the builtin type to an ordinary type.

# Value

an object from one of the cycle classes

## Methods

- signature(x = "Cyclic", type = "ANY") Returns x@cycle. Currently ignores the remaining arguments.
- signature(x = "numeric", type = "character") x is the period in this case. If x is the only
  argument (not counting type), a "BareCycle" object is created, otherwise the constructor of
  "SimpleCycle" is invoked with all arguments except type passed on to it.
- signature(x = "numeric", type = "missing") x is the period in this case. If x is the only argument (not counting type), a "BareCycle" object is created, otherwise the constructor of "SimpleCycle" is invoked with all arguments except type passed on to it.

```
signature(x = "PeriodicTimeSeries", type = "ANY")
```

signature(x = "ts", type = "ANY")

```
signature(x = "BasicCycle", type = "character")
signature(x = "BasicCycle", type = "missing")
signature(x = "character", type = "character")
signature(x = "character", type = "missing")
```

## Author(s)

Georgi N. Boshnakov

### Examples

```
pcCycle(4)
pcCycle(4, seasons = c("Spring", "Summer", "Autumn", "Winter"))
pcCycle("QuarterYearCycle")
pcCycle("QuarterYearCycle", type = "BareCycle")
pcCycle("QuarterYearCycle", type = "SimpleCycle")
```

```
pclsdf
```

Fit PAR models using least squares

## Description

Fit PAR models using least squares. The model may contain intercepts and linear trends, seasonal or non-seasonal.

#### Usage

### Arguments

х	time series, a numeric vector
d	period, an integer
lags	an integer vector, typically 1:p, where p is the order of the autoregression. The same lags are used for all seasons.
sintercept	if TRUE include seasonal intercepts.
sslope	if TRUE include seasonal linear trend.
intercept	if TRUE include non-seasonal intercept.
slope	if TRUE include non-seasonal linear trend.
xreg	additional regressors, not used currently.
contrasts	contrasts to use for the seasons factor variable.
seasonof1st	season of the first observation in the time series, see Details.
coefonly	if TRUE, return only the parameters of the fitted model, otherwise include also the object returned by 1m.

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#### pclsdf

## Details

This function fits PAR models by the method of least squares. Seasonal intercepts are included by default. Non-seasonal intercepts are available, as well as seasonal and non-seasonal linear trend. Separate arguments are provided, so that any combination of seasonal and non-seasonal intercepts and slopes can be specified.

If coefonly is TRUE, pclsdf returns only the estimated parameters, otherwise it includes additional statistical information, see section Note for the current details.

# Value

A list with the components listed below. Some components are present only if included in the model specification.

par	the PAR coefficients, a matrix with a row for each season.
sintercept	(if specified) seasonal intercepts, a numeric vector.
sigma2hat	innovation variances.
formula.char	the formula used in the call of 1m, a character string.
fit	(if coefonly = FALSE) the fitted object obtained from lm.

#### Note

Currently, pclsdf prepares a model formula according to the specification and calls lm to do the fitting. Component "fit" in the result (available when coefonly = FALSE) contains the raw fitted object returned by lm. Statistical inference based on this object would, in general, not be justified for correlated data.

todo: currently some of the parameters are returned only via the fitted object from 1m.

## Author(s)

Georgi N. Boshnakov

### See Also

pclspiar,

# Examples

```
## data(dataFranses1996)
cu <- pcts(dataFranses1996[ , "CanadaUnemployment"])
cu <- window(cu, start = availStart(cu), end = availEnd(cu))
pclsdf(cu, 4, 1:2, sintercept = TRUE)
pclsdf(austres, 4, lags = 1:3)
pclsdf(austres, 4, lags = 1:3, sintercept = TRUE)
pclsdf(austres, 4, lags = 1:3, sintercept = TRUE)
pclsdf(austres, 4, lags = 1:3, sintercept = TRUE, sslope = TRUE)
x <- rep(1:4,10)</pre>
```

```
pclsdf(x, 4, lags = 1:3, sintercept = TRUE, sslope = TRUE)
## this is for the version when contrasts arg. was passed on directly to lm.
## tmp1 <- pclsdf(austres, 4, lags = 1, sintercept = FALSE, sslope = TRUE,
## contrasts = list(Season = "contr.sum" ))</pre>
```

```
pclspiar
```

Fit a periodically integrated autoregressive model

### Description

Fit a periodically integrated autoregressive model.

# Usage

## Arguments

x	time series.
d	period.
р	order of the model, a positive integer, see Details.
icoef	initial values for the periodic integration coefficients.
parcoef	not used currently.
sintercept	if TRUE include seasonal intercepts.
seasonof1st	season of the first observation.
weights	if TRUE, use periodic weights in the nonlinear least squares, see Details.
itol	threshold value for the stopping criterion.
maxniter	maximum number of iterations.

### Details

This function fits a periodically integrated autoregressive model using non-linear least squares. The order of integration is one and the order of the periodically correlated part is p -1. So, p must be greater than or equal to one.

If weights = TRUE the non-linear optimisation is done with weights inversely proportional to the innovation variances for the seasons, otherwise the unweighted sum of squared residuals is minimised.

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# pcPlot

### Value

a list currently containing the following elements:

icoef	coefficients of the periodic integration filter.
parcoef	coefficients of the PAR filter.
sintercept	seasonal intercepts.
sigma2hat	innovation variances.

## Author(s)

Georgi N. Boshnakov

## References

Franses PH (1996). *Periodicity and Stochastic Trends In Economic Time Series*. Oxford University Press Inc., New York.

Franses PH and Paap R (2004). *Periodic Time Series Models*. Oxford University Press Inc., New York.

Boshnakov GN and Iqelan BM (2009). "Generation of time series models with given spectral properties." *J. Time Series Anal.*, **30**(3), pp. 349–368. ISSN 0143-9782, http://dx.doi.org/10. 1111/j.1467-9892.2009.00617.x.

## See Also

pclsdf, test\_piar, fitPM

## Examples

pcPlot

Plot periodic time series

# Description

Plot periodic time series.

## Usage

```
## S3 method for class 'PeriodicTimeSeries'
boxplot(x, ...)
## S3 method for class 'PeriodicTimeSeries'
monthplot(x, ylab = deparse(substitute(x)), base, ...)
```

# Arguments

х	a periodic time series object.
	further arguments to be passed to the plotting function.
ylab	label for the y-axis, only used for univariate time series.
base	a function for use for computing reference lines.

# Details

Functions for periodic/seasonal plots and boxplots.

The S3 method for monthplot() just calls pcPlot().

# Author(s)

Georgi N. Boshnakov

# Examples

```
ap <- pcts(AirPassengers)
monthplot(ap)
boxplot(ap)
fr23 <- pcts(dataFranses1996[ , 2:3])
monthplot(fr23)
boxplot(fr23)</pre>
```

pcTest-methods Test for periodicity

# Description

Test for periodicity

# Usage

```
pcTest(x, nullmodel, nseasons, ...)
```

# Arguments

х	the object to be tested, e.g. a time series or a periodic acf
nullmodel	specification of the test to be performed
nseasons	number of seasons
	additional arguments to be passed on to methods

#### pcTest-methods

#### Details

This is a generic function which acts as a despatcher for various tests for periodicity and periodic correlation.

x is typically a time series but conceptually it is an object containing the statistics needed for carrying out the requested test. For example, x may be the periodic autocovariance function for tests based on sample autocorrelations and autocovariances.

The method with signature (x = "ANY", nullmodel = "character") may be considered as default for pcTest. The "real" default method simply prints an error message.

#### Value

a list containing the results of the requested test, see the individual methods for details

### Methods

signature(x = "ANY", nullmodel = "character") Argument nullmodel specifies the test to be
performed. It should be a single character string. If it is one of the strings recognised by this
method, the test specified below is carried out. Otherwise nullmodel is taken to be the name
of a function which is called with arguments (x,...).

Currently, the following character strings are recognised:

"wn" Box test for (non-periodic) white noise, simply calls Box.test.

"piar" Franses (1996) test for periodic integration.

signature(x = "slMatrix", nullmodel = "character") x here is the periodic autocovariance function. This method works similarly to the method for signature (x = "ANY", nullmodel = "character"), see its description.

Currently, the following character strings are recognised:

"pwn" Ljung-Box test for periodic white noise,

"periodicity" McLeod test for periodic correlation.

signature(x = "numeric", nullmodel = "character")

signature(x = "PeriodicTimeSeries", nullmodel = "character")

#### Note

TODO: critical values

## Author(s)

Georgi N. Boshnakov

#### See Also

test\_piar, pwn\_McLeodLjungBox\_test periodic\_acf1\_test

# Examples

```
cu <- pcts(dataFranses1996[, "CanadaUnemployment"])
cu <- window(cu, start = availStart(cu), end = availEnd(cu))
test_piar(cu, 4, 1, sintercept = TRUE)
pcTest(cu, "piar", 4, 1, sintercept = TRUE)
if(require(partsm)){
    # same with LRurpar.test from partsm
LRurpar.test(cu, list(regular = c(0,0,0), seasonal = c(1,0), regvar = 0), p = 1)
}</pre>
```

pctime

Functions for some basic operations with seasons

# Description

Functions for some basic operations with seasons.

# Usage

```
toSeason(t, period, t1 = 1, from = 1)
toSeasonPair(t, s, period, ...)
ttTosl(r, period)
ttmatToslPairs(i, j, period)
```

## Arguments

r	covariance matrix, see 'Details'.
t	a vector of integers, representing times.
S	a vector of integers, representing times.
period	the number of seasons.
t1	time corresponding to the first season, an integer number.
from	1 or 0, depending on whether the season numbers start from 1 or 0.
i	a vector of integers.
j	a vector of integers.
	todo: describe!

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### pctime

#### Details

ttmatToslPairs(i, j, period) transforms time-time pairs to season-lag pairs. The time pairs are obtained by pairing each element of i with each element of j. A four column matrix is created with one row for each pair (t,s), such that t=i[m] and s=j[n] for some m and n. The row is m,n,s,l, where (s,l) is the season-lag pair corresponding to (t,s).

ttTosl(r, period) converts autocovariances given in a covariance matrix (i.e. in "tt" form) to the "sl" form. The result is a period x (maxlag+1) matrix, where maxlag is the maximal lag available in r. Entries for which no values are available are filled with NA's. Warning is given if contradictory entries are found (i.e. if r is not from a periodically correlated process with the given period).

toSeason(t,period, t1=1, from=1) returns the season corresponding to t. t1 is a time (integer) whose season is the first season, from is 1 if the numbering of seasons is 1,2,...,period, or 0 if the numbering of seasons is 0,1,...,period-1. Other values for from are not admissible (but not checked). **Note:** some of the functions in this package implicitly assume that t1=1 and from=1.

toSeasonPair(t,s,period) converts the "tt" pair t,s to "sl" pair and returns the result in the form of a list with elements season and lag. Currently t and s must be scalars.

pc.omitneg helps to implement dropping of negative indices in season-lag objects. It returns its first argument, lags, if all of its elements are non-negative. Otherwise, all elements of lags must be non-positive. In this case the function creates the vector 0:maxlag and drops the elements specified by lags. Note that the default indexing will not work properly since zero elements in an index are omitted (and there are such indices in season-lag objects).

## Value

for ttmatToslPairs, a matrix with four columns;

for ttTosl, a matrix with period rows;

for toSeason(t,period,t1=1,from=1), a vector of integers;

for toSeasonPair(t,s,period), a list with elements season and lag;

for pc.omitneg, a vector of lags (non-negative integers).

### Note

2013-10-24 - Corrected the description of the return value of ttmatToslPairs. It incorrectly stated that the first two columns are "tt" pair (they are actually indices in i and j).

## Author(s)

Georgi N. Boshnakov

## References

Boshnakov GN and Iqelan BM (2009). "Generation of time series models with given spectral properties." *J. Time Series Anal.*, **30**(3), pp. 349–368. ISSN 0143-9782, http://dx.doi.org/10. 1111/j.1467-9892.2009.00617.x.

## Examples

```
# ttmatToslPairs
ttmatToslPairs(3, 3, 4) # 1, 1, 3, 0
ttmatToslPairs(3, 2, 4) # 1, 1, 3, 1
ttmatToslPairs(1:4, 1:4, 4)
ttmatToslPairs(3:4, 3:4, 4)
# ttTosl - :todo:
# toSeason
toSeason(1:10, 4)
                         #1234 1234 12
toSeason(1:10, 4, from = 0) # 0 1 2 3 0 1 2 3 0 1
## first data is for 3rd quarter
toSeason(1:10, 4, t1 = 3) # 3 4 1 2 3 4 1 2 3 4
# toSeasonPair
toSeasonPair(3, 3, period=4) # season=3, lag = 0
toSeasonPair(8, 8, period=4) # season=4, lag = 0
toSeasonPair(3, 2, period=4) # season=3, lag = 1
toSeasonPair(7, 6, period=4) # same
#### # pc.omitneg
##### pc.omitneg(0:5,10) # 0:5, unchaged since all values >= 0
####
#### pc.omitneg(-(0:5),10) # 6:10, works like
#### (0:10)[-(0:5 +1)]
                          # same
####
##### # don't mix positive and negative numbers in pc.omitneg
#### \dontrun{pc.omitneg(c(0,2,3,-4,5), 10)}
```

```
pcts
```

Create objects from periodic time series classes

#### Description

Create objects from periodic time series classes.

## Usage

pcts(x, nseasons, keep, ...)

## Arguments

xa time series.nseasonsnumber of seasons. This argument is ignored by some methods.

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if TRUE and x is from class "ts", "mts", "zoo", or "zooreg", create a periodic
object inheriting from that class.
 further arguments to be passed on to methods.

#### Details

pcts creates periodic time series objects inheriting from "PeriodicTimeSeries". The particular class depends on arguments x and, in some cases, keep. The idea is that in normal use the user does not care about the particular class.

There are also methods for as for conversion to and from the time series classes defined in package **pcts**.

TODO: more methods are needed.

## Value

an object inheriting from "PeriodicTimeSeries"

#### Methods

TODO: need methods for zoo and zooreg

- signature(x = "numeric") Creates an object of class "PeriodicTS", the native class for univariate periodic time series in package "pcts".
- signature(x = "matrix") Creates an object of class "PeriodicMTS", the native class for multivariate periodic time series in package "pcts".
- signature(x = "ts") If keep = TRUE creates an object of class "PeriodicTS\_ts", otherwise the result is from "PeriodicTS".
- signature(x = "mts") If keep = TRUE creates an object of class "PeriodicMTS\_ts", otherwise the result is from "PeriodicMTS".

# Author(s)

Georgi N. Boshnakov

## See Also

PeriodicTS

### Examples

pcts(AirPassengers,12)

pcts-deprecated

### Description

These functions are marked for removal and are provided temporarily for compatibility with older versions of package **pcts** only. Use the recommended renamed or new functions instead.

# Usage

ptildeorders(...)

### Arguments

. . .

arguments pass on to the new function.

# Details

**mCpar** has been renamed to sim\_parCoef **sim\_arAcf** has been renamed to sim\_parAcvf

pdSafeParOrder Functions for some basic operations with seasons

# Description

Functions for some basic operations with seasons.

#### Usage

pdSafeParOrder(p)

### Arguments

р

autoregression order, a vector of integers.

# Details

pdSafeParOrder(p) modifies the periodic AR order specified by vector p. The modified order is such that the correspondence between autocovariances and partial autocorrelations is one-to-one, see the references for details.

## Value

a vector of integers

## Author(s)

Georgi N. Boshnakov

## References

Lambert-Lacroix S (2000). "On periodic autoregressive process estimation ." *IEEE Transactions* on Signal Processing, **48**(6), pp. 1800-1803.

Lambert-Lacroix S (2005). "Extension of autocovariance coefficients sequence for periodically correlated processes." *Journal of Time Series Analysis*, **26**(6), pp. 423-435.

### Examples

pdSafeParOrder(c(0,2))
pdSafeParOrder(c(2,3))

PeriodicArmaFilter-class

Class "PeriodicArmaFilter"

# Description

Class PeriodicArmaFilter.

#### **Objects from the Class**

Objects can be created by calls of the form new("PeriodicArmaFilter",...,ar,ma,nseasons).

#### Slots

ar: Object of class "PeriodicBJFilter" ~~

ma: Object of class "PeriodicSPFilter" ~~

## Extends

Class "VirtualArmaFilter", directly. Class "VirtualMonicFilter", by class "VirtualArmaFilter", distance 2.

#### Methods

No methods defined with class "PeriodicArmaFilter" in the signature.

PeriodicArmaModel-class

Class PeriodicArmaModel

## Description

Class PeriodicArmaModel.

#### **Objects from the Class**

Objects can be created by calls of the form new("PeriodicArmaModel", ar, ma, sigma2,...).

#### Slots

sigma2: Object of class "numeric" ~~

ar: Object of class "PeriodicArFilter" ~~

ma: Object of class "PeriodicMaFilter" ~~

center: Object of class "numeric" ~~

intercept: Object of class "numeric" ~~

## Extends

Class "VirtualPeriodicArmaModel", directly. Class "PeriodicArmaSpec", directly. Class "VirtualPeriodicFilterMod by class "VirtualPeriodicArmaModel", distance 2. Class "VirtualPeriodicStationaryModel", by class "VirtualPeriodicArmaModel", distance 2. Class "PeriodicArmaFilter", by class "PeriodicArmaSpec", distance 2. Class "VirtualPeriodicAutocovarianceModel", by class "VirtualPeriodicArmaModel", distance 3. Class "VirtualPeriodicMeanModel", by class "VirtualPeriodicArmaModel", distance 3.

## Methods

autocovariances signature(x = "PeriodicArmaModel"): ...

PeriodicArmaSpec-class

Class PeriodicArmaSpec

#### Description

Class PeriodicArmaSpec.

#### **Objects from the Class**

Objects can be created by calls of the form new("PeriodicArmaSpec", pcmean, pcintercept, ...).

## PeriodicArModel-class

# Slots

sigma2: Object of class "numeric" ~~
ar: Object of class "PeriodicArFilter" ~~
ma: Object of class "PeriodicMaFilter" ~~
center: Object of class "numeric" ~~
intercept: Object of class "numeric" ~~

## Extends

Class "PeriodicArmaFilter", directly.

PeriodicArModel-class Class PeriodicArModel

#### Description

Class PeriodicArModel.

# **Objects from the Class**

Objects can be created by calls of the form new("PeriodicArModel", ar, ma, sigma2, ...).

#### Slots

sigma2: Object of class "numeric" ~~
ar: Object of class "PeriodicArFilter" ~~
ma: Object of class "PeriodicMaFilter" ~~
center: Object of class "numeric" ~~
intercept: Object of class "numeric" ~~

#### Extends

Class "PeriodicArmaModel", directly. Class "VirtualPeriodicArmaModel", by class "PeriodicArmaModel", distance 2. Class "PeriodicArmaSpec", by class "PeriodicArmaModel", distance 2. Class "VirtualPeriodicFilterModel", by class "PeriodicArmaModel", distance 3. Class "VirtualPeriodicStationaryModel", by class "PeriodicArmaModel", distance 3. Class "PeriodicArmaFilter", by class "PeriodicArmaModel", distance 3. Class "VirtualPeriodicAutocovarianceModel", by class "PeriodicArmaModel", distance 4. Class "VirtualPeriodicMeanModel", by class "PeriodicArmaModel", distance 4.

### Methods

autocovariances signature(x = "PeriodicArModel"): ...
fitPM signature(x = "ANY",model = "PeriodicArModel"): ...

PeriodicArModel-methods

Create objects from class PeriodicArModel

# Description

Create objects from class PeriodicArModel

### Usage

PeriodicArModel(object, ...)

## Arguments

object	an object, can have one of a number of classes.
	further arguments for methods.

## Details

PeriodicArModel creates objects from class PeriodicArModel. This is a generic function with despatch methods on the first argument.

## Value

an object from class "PeriodicArModel"

## Methods

```
signature(object = "matrix") "object" gives the coefficients, one row per season.
```

signature(object = "numeric") "object" gives the model order. Its length is taken to be the number of seasons. The coefficients are set to NA.

```
signature(object = "PeriodicMonicFilterSpec")
```

signature(object = "VirtualPeriodicArmaModel")

signature(object = "PeriodicMonicFilterSpec")

```
signature(object = "VirtualPeriodicArmaModel")
```

PeriodicAutocorrelations-class

Class PeriodicAutocorrelations

## Description

Class PeriodicAutocorrelations.

# **Objects from the Class**

Objects can be created by calls of the form new("PeriodicAutocorrelations",...,data).

# Slots

modelCycle: Object of class "BasicCycle" ~~

data: Object of class "Lagged" ~~

## Extends

Class "ModelCycleSpec", directly. Class "FlexibleLagged", directly. Class "VirtualPeriodicAutocorrelations", directly. Class "Lagged", by class "FlexibleLagged", distance 2. Class "VirtualPeriodicModel", by class "VirtualPeriodicAutocorrelations", distance 2.

#### Methods

```
plot signature(x = "PeriodicAutocorrelations",y = "missing"): ...
```

PeriodicAutocovarianceModel-class Class PeriodicAutocovarianceModel

# Description

Class PeriodicAutocovarianceModel.

### **Objects from the Class**

Objects can be created by calls of the form new("PeriodicAutocovarianceModel",...).

## Slots

```
pcmatrix: Object of class "ANY" ~~
```

#### Extends

Class "VirtualPeriodicAutocovarianceModel", directly. Class "PeriodicAutocovarianceSpec", directly.

#### Methods

```
autocovariances signature(x = "PeriodicAutocovarianceModel"): ...
[ signature(x = "PeriodicAutocovarianceModel",i = "missing",j = "missing",drop = "ANY"):
[ signature(x = "PeriodicAutocovarianceModel",i = "missing",j = "numeric",drop = "ANY"):
[ signature(x = "PeriodicAutocovarianceModel", i = "numeric", j = "missing", drop = "ANY"):
[ signature(x = "PeriodicAutocovarianceModel",i = "numeric",j = "numeric",drop = "ANY"):
     ...
[<- signature(x = "PeriodicAutocovarianceModel",i = "ANY",j = "ANY",value = "ANY"): ...</pre>
autocovariances signature(x = "PeriodicAutocovarianceModel",maxlag = "ANY"): ...
backwardPartialCoefficients signature(x = "PeriodicAutocovarianceModel"): ...
backwardPartialVariances signature(x = "PeriodicAutocovarianceModel"): ...
maxLag signature(object = "PeriodicAutocovarianceModel"): ...
partialAutocorrelations signature(x = "PeriodicAutocovarianceModel", maxlag = "ANY", lag_0
    = "ANY"): ...
partialAutocovariances signature(x = "PeriodicAutocovarianceModel"): ...
partialCoefficients signature(x = "PeriodicAutocovarianceModel"): ...
partialVariances signature(x = "PeriodicAutocovarianceModel"): ...
pc.bU signature(x = "PeriodicAutocovarianceModel"): ...
pc.fL signature(x = "PeriodicAutocovarianceModel"): ...
pc.phis2 signature(x = "PeriodicAutocovarianceModel"): ...
[[ signature(x = "PeriodicAutocovarianceModel", i = "numeric"): ...
```

PeriodicAutocovariances-class

Class PeriodicAutocovariances

## Description

Class PeriodicAutocovariances.

## **Objects from the Class**

Objects can be created by calls of the form new("PeriodicAutocovariances",...,data).

## Slots

```
modelCycle: Object of class "BasicCycle" ~~
data: Object of class "Lagged" ~~
```

### Extends

Class "ModelCycleSpec", directly. Class "FlexibleLagged", directly. Class "VirtualPeriodicAutocovariances", directly. Class "Lagged", by class "FlexibleLagged", distance 2. Class "VirtualPeriodicModel", by class "VirtualPeriodicAutocovariances", distance 2.

## Methods

autocorrelations signature(x = "PeriodicAutocovariances",maxlag = "ANY",lag\_0 = "missing"):

PeriodicAutocovarianceSpec-class Class PeriodicAutocovarianceSpec

# Description

Class PeriodicAutocovarianceSpec.

#### **Objects from the Class**

Objects can be created by calls of the form new("PeriodicAutocovarianceSpec", ...).

#### Slots

```
pcmatrix: Object of class "ANY" ~~
```

### Methods

No methods defined with class "PeriodicAutocovarianceSpec" in the signature.

PeriodicBJFilter-class

Class PeriodicBJFilter

## Description

A class for filters following the Box-Jenkins sign convention

## **Objects from the Class**

Objects can be created by calls of the form new("PeriodicBJFilter", coef, order, ...).

## Slots

coef: Object of class "matrix" ~~
order: Object of class "numeric" ~~

## Extends

Class "PeriodicMonicFilterSpec", directly. Class "VirtualBJFilter", directly. Class "VirtualMonicFilterSpec", by class "PeriodicMonicFilterSpec", distance 2. Class "VirtualMonicFilter", by class "Virtual-BJFilter", distance 2.

### Methods

filterCoef signature(object = "PeriodicBJFilter", convention = "character"): ...
coerce signature(from = "matrix", to = "PeriodicBJFilter"): ...
coerce signature(from = "PeriodicBJFilter", to = "PeriodicSPFilter"): ...
filterPoly signature(object = "PeriodicBJFilter"): ...
filterPolyCoef signature(object = "PeriodicBJFilter"): ...
show signature(object = "PeriodicBJFilter"): ...

### Author(s)

Georgi N. Boshnakov

## See Also

PeriodicSPFilter

### Examples

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```
show( as(co, "PeriodicBJFilter") )
show( as(co, "PeriodicSPFilter") )
## change the sign convention:
sp1 <- as(bj1, "PeriodicSPFilter")
## bj1 and sp1 represent the same filter
filterPolyCoef(bj1)
filterPolyCoef(bj1)
identical(filterPolyCoef(bj1), filterPolyCoef(sp1)) # TRUE
filterOrder(bj1)
nSeasons(bj1)
## filterPoly(bj1)
## filterPoly(sp1)</pre>
```

PeriodicFilterModel-class

Class PeriodicFilterModel

### Description

Class PeriodicFilterModel.

### **Objects from the Class**

Objects can be created by calls of the form new("PeriodicFilterModel", pcmean, pcintercept, ...).

## Slots

center: Object of class "numeric" ~~

intercept: Object of class "numeric" ~~

sigma2: Object of class "numeric" ~~

ar: Object of class "PeriodicArFilter" ~~

ma: Object of class "PeriodicMaFilter" ~~

# Extends

Class "VirtualPeriodicFilterModel", directly. Class "PeriodicArmaSpec", directly. Class "PeriodicArmaFilter", by class "PeriodicArmaSpec", distance 2.

PeriodicIntegratedArmaSpec-class

Class PeriodicIntegratedArmaSpec

## Description

Class PeriodicIntegratedArmaSpec.

#### **Objects from the Class**

Objects can be created by calls of the form new("PeriodicIntegratedArmaSpec",...).

#### Slots

pcmodel: Object of class "PeriodicArmaModel" ~~

### Methods

sigmaSq signature(object = "PeriodicIntegratedArmaSpec"): ...

PeriodicInterceptSpec-class

Class PeriodicInterceptSpec

## Description

Class PeriodicInterceptSpec.

## **Objects from the Class**

Objects can be created by calls of the form new("PeriodicInterceptSpec",...).

## Slots

center: Object of class "numeric" ~~

intercept: Object of class "numeric" ~~

sigma2: Object of class "numeric" ~~

modelCycle: Object of class "BasicCycle" ~~

# Extends

Class "numeric", from data part. Class "vector", by class "numeric", distance 2. Class "index", by class "numeric", distance 2. Class "replValue", by class "numeric", distance 2.

Class "numLike", by class "numeric", distance 2. Class "number", by class "numeric", distance 2. Class "atomicVector", by class "numeric", distance 2.

#### Methods

No methods defined with class "PeriodicInterceptSpec" in the signature.

sigmaSq signature(object = "PeriodicInterceptSpec"): ...
allSeasons signature(x = "PeriodicInterceptSpec", abb = "ANY"): ...
initialize signature(.Object = "PeriodicInterceptSpec"): ...
nSeasons signature(object = "PeriodicInterceptSpec"): ...
show signature(object = "PeriodicInterceptSpec"): ...

PeriodicMaModel-class Class PeriodicMaModel

# Description

Class PeriodicMaModel.

#### **Objects from the Class**

Objects can be created by calls of the form new("PeriodicMaModel", ar, ma, sigma2,...).

#### Slots

sigma2: Object of class "numeric" ~~
ar: Object of class "PeriodicArFilter" ~~
ma: Object of class "PeriodicMaFilter" ~~
center: Object of class "numeric" ~~
intercept: Object of class "numeric" ~~

#### Extends

Class "PeriodicArmaModel", directly. Class "VirtualPeriodicArmaModel", by class "PeriodicArmaModel", distance 2. Class "PeriodicArmaSpec", by class "PeriodicArmaModel", distance 2. Class "VirtualPeriodicFilterModel", by class "PeriodicArmaModel", distance 3. Class "VirtualPeriodicStationaryModel", by class "PeriodicArmaModel", distance 3. Class "PeriodicArmaFilter", by class "PeriodicArmaModel", distance 3. Class "VirtualPeriodicAutocovarianceModel", by class "PeriodicArmaModel", distance 4. Class "VirtualPeriodicMeanModel", by class "PeriodicArmaModel", by class "Per

#### Methods

No methods defined with class "PeriodicMaModel" in the signature.

PeriodicMTS-class Class "PeriodicMTS"

#### Description

Class "PeriodicMTS" is the main class for multivariate periodic time series in package "pcts".

#### **Objects from the Class**

Objects can be created by calls of the form new("PeriodicMTS",...) but it is recommended to use the function pcts in most cases.

### Slots

.Data: Object of class "matrix" ~~ cycle: Object of class "BasicCycle" ~~ pcstart: Object of class "ANY" ~~

## Extends

Class "PeriodicTimeSeries", directly. Class "matrix", from data part. Class "Cyclic", by class "PeriodicTimeSeries", distance 2. Class "array", by class "matrix", distance 2.

Class "mMatrix", by class "matrix", distance 2. Class "optionalMatrix", by class "matrix", distance 2. Class "structure", by class "matrix", distance 3. Class "vector", by class "matrix", distance 4, with explicit coerce.

### Methods

\$ signature(x = "PeriodicMTS"): ...
[ signature(x = "PeriodicMTS", i = "ANY", j = "missing", drop = "ANY"): ...
[ signature(x = "PeriodicMTS", i = "missing", j = "missing", drop = "ANY"): ...
[[ signature(x = "PeriodicMTS", i = "ANY"): ...
coerce signature(from = "mts", to = "PeriodicMTS"): ...
coerce signature(from = "PeriodicMTS", to = "ts"): ...
plot signature(x = "PeriodicMTS", y = "missing"): ...
show signature(object = "PeriodicMTS"): ...

# See Also

pcts which is the recommended way to create periodic time series,

class PeriodicTS for the univariate case,

dataFranses1996 and pcts-package for examples

#### PeriodicMTS\_ts-class

## Examples

```
pcfr <- pcts(dataFranses1996)</pre>
colnames(pcfr)[4] # "GermanyGNP"
## extracting single time series as univariate
class(pcfr[[4]]) # "PeriodicTS"
identical(pcfr[[4]], pcfr$GermanyGNP )
                                             # TRUE
identical(pcfr[[4]], pcfr[["GermanyGNP"]]) # TRUE
plot(pcfr[[4]])
## ... and as multivariate
pcfr[4] # "PeriodicMTS"
plot(pcfr[4])
## extracting more than one time series
plot(pcfr[2:4])
summary(pcfr[2:4])
pcfr2 <- pcfr[[2]]</pre>
plot(pcfr2)
```

PeriodicMTS\_ts-class Class "PeriodicMTS\_ts"

## Description

Class "PeriodicMTS\_ts" is a periodic class holding multivariate "ts" objects.

#### **Objects from the Class**

Objects can be created by calls of the form new("PeriodicMTS\_ts", x, ...).

### Slots

.Data: Object of class "vector" ~~

cycle: Object of class "BasicCycle" ~~

tsp: Object of class "numeric" ~~

.S3Class: Object of class "character" ~~

pcstart: Object of class "ANY" ~~

# Extends

Class "PeriodicTimeSeries", directly. Class "ts", directly. Class "Cyclic", by class "Periodic-TimeSeries", distance 2. Class "structure", by class "ts", distance 2. Class "oldClass", by class "ts", distance 2. Class "AnyTimeSeries", by class "ts", distance 2. Class "vector", by class "ts", distance 3, with explicit coerce.

### Methods

```
coerce signature(from = "ts",to = "PeriodicMTS_ts"): ...
initialize signature(.Object = "PeriodicMTS_ts"): ...
```

PeriodicMTS\_zooreg-class

Class "PeriodicMTS\_zooreg"

## Description

Class "PeriodicMTS\_zooreg" is a periodic class holding multivariate "zooreg" objects.

## **Objects from the Class**

Objects can be created by calls of the form new("PeriodicMTS\_zooreg",...).

## Slots

cycle: Object of class "BasicCycle" ~~

.S3Class: Object of class "character" ~~

pcstart: Object of class "ANY" ~~

#### Extends

Class "PeriodicTimeSeries", directly. Class "ts", directly. Class "Cyclic", by class "Periodic-TimeSeries", distance 2. Class "structure", by class "ts", distance 2. Class "oldClass", by class "ts", distance 2. Class "AnyTimeSeries", by class "ts", distance 2. Class "vector", by class "ts", distance 3, with explicit coerce.

### Methods

No methods defined with class "PeriodicMTS\_zooreg" in the signature.

PeriodicSPFilter-class

Class PeriodicSPFilter

## Description

A class for filters following the signal processing sign convention.

#### **Objects from the Class**

Objects can be created by calls of the form new("PeriodicSPFilter", coef, order, ...).

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## PeriodicTimeSeries-class

# Slots

coef: Object of class "matrix" ~~
order: Object of class "numeric" ~~

# Extends

Class "PeriodicMonicFilterSpec", directly. Class "VirtualSPFilter", directly. Class "VirtualMonicFilterSpec", by class "PeriodicMonicFilterSpec", distance 2. Class "VirtualMonicFilter", by class "Virtual-SPFilter", distance 2.

# Methods

filterCoef signature(object = "PeriodicSPFilter", convention = "character"): ...

## Author(s)

Georgi N. Boshnakov

## See Also

PeriodicBJFilter

# Examples

## see "PeriodicBJFilter-class" for examples

PeriodicTimeSeries-class

Class PeriodicTimeSeries

## Description

Class PeriodicTimeSeries.

## **Objects from the Class**

A virtual Class: No objects may be created from it.

# Slots

```
cycle: Object of class "BasicCycle".
pcstart: Object of class "ANY".
```

## Extends

Class "Cyclic", directly.

### Methods

```
pcTest signature(x = "PeriodicTimeSeries",nullmodel = "character"): ...
head signature(x = "PeriodicTimeSeries"): ...
pcCycle signature(x = "PeriodicTimeSeries",type = "ANY"): ...
tail signature(x = "PeriodicTimeSeries"): ...
```

PeriodicTS-class Class "PeriodicTS"

### Description

Class "PeriodicTS" is the main class for univariate periodic time series in package "pcts".

#### **Objects from the Class**

Objects can be created by calls of the form new("PeriodicTS",...).

## Slots

.Data: Object of class "numeric" ~~

cycle: Object of class "BasicCycle" ~~

pcstart: Object of class "ANY" ~~

### Extends

Class "PeriodicTimeSeries", directly. Class "numeric", from data part. Class "Cyclic", by class "PeriodicTimeSeries", distance 2. Class "vector", by class "numeric", distance 2. Class "index", by class "numeric", distance 2. Class "replValue", by class "numeric", distance 2.

Class "numLike", by class "numeric", distance 2. Class "number", by class "numeric", distance 2. Class "atomicVector", by class "numeric", distance 2. Class "numeric", by class "numeric", distance 2. Class "replValueSp", by class "numeric", distance 3. Class "Mnumeric", by class "numeric", distance 3.

## Methods

```
coerce signature(from = "mts",to = "PeriodicTS"): ...
coerce signature(from = "PeriodicTS",to = "ts"): ...
coerce signature(from = "ts",to = "PeriodicTS"): ...
plot signature(x = "PeriodicTS", y = "missing"): ...
show signature(object = "PeriodicTS"): ...
summary signature(object = "PeriodicTS"): ...
```

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#### Description

Class "PeriodicTS\_ts" is a periodic class holding "ts" objects.

## **Objects from the Class**

Objects can be created by calls of the form new("PeriodicTS\_zooreg",...).

# **Objects from the Class**

Objects can be created by calls of the form new("PeriodicTS\_ts", x, ...).

# Slots

.Data: Object of class "vector" ~~

cycle: Object of class "BasicCycle" ~~

tsp: Object of class "numeric" ~~

.S3Class: Object of class "character" ~~

pcstart: Object of class "ANY" ~~

## Extends

Class "PeriodicTimeSeries", directly. Class "ts", directly. Class "Cyclic", by class "Periodic-TimeSeries", distance 2. Class "structure", by class "ts", distance 2. Class "oldClass", by class "ts", distance 2. Class "AnyTimeSeries", by class "ts", distance 2. Class "vector", by class "ts", distance 3, with explicit coerce.

#### Methods

coerce signature(from = "ts", to = "PeriodicTS\_ts"): ...

initialize signature(.Object = "PeriodicTS\_ts"): ...

```
PeriodicTS_zooreg-class
```

Class "PeriodicTS\_zooreg"

### Description

Class "PeriodicTS\_zooreg" is a periodic class holding "zooreg" objects.

# **Objects from the Class**

Objects can be created by calls of the form new("PeriodicTS\_zooreg",...).

# Slots

cycle: Object of class "BasicCycle" ~~

.S3Class: Object of class "character" ~~

pcstart: Object of class "ANY" ~~

#### Extends

Class "PeriodicTimeSeries", directly. Class "ts", directly. Class "Cyclic", by class "Periodic-TimeSeries", distance 2. Class "structure", by class "ts", distance 2. Class "oldClass", by class "ts", distance 2. Class "AnyTimeSeries", by class "ts", distance 2. Class "vector", by class "ts", distance 3, with explicit coerce.

## Methods

No methods defined with class "PeriodicTS\_zooreg" in the signature.

### See Also

classes PeriodicTS and PeriodicMTS

PeriodicVector-class Class PeriodicVector

## Description

Objects and methods for class PeriodicVector.

### Usage

PeriodicVector(x, period = length(x))

### Arguments

х	the values for inidices from 1 to period, numeric.
period	the period, defaults to length(x).

### Details

A *p*-periodic vector, X, is such that  $X_{i+pk} = X_i$  for any integers i, k.

Class PeriodicVector stores the values of  $X_1, \ldots, X_p$  and provides indexing methods for extracting and setting its elements.

## Value

an object from class "PeriodicVector"

#### **Objects from the Class**

Objects can be created by calls of the form new("PeriodicVector",...) or more conveniently by using "PeriodicVector()".

## Slots

.Data: Object of class "numeric" ~~ period: Object of class "numeric" ~~

## Extends

Class "numeric", from data part. Class "vector", by class "numeric", distance 2. Class "atomicVector", by class "numeric", distance 2. Class "index", by class "numeric", distance 2.

Class "numLike", by class "numeric", distance 2.

Class "number", by class "numeric", distance 2. Class "replValue", by class "numeric", distance 2.

## Methods

"PeriodicVector" methods are defined for "[" and "[<-". Arithmetic operations just inherit the recycling rules from "numeric".

[ signature(x = "PeriodicVector",i = "ANY",j = "ANY",drop = "ANY"): ...

[ signature(x = "PeriodicVector", i = "ANY", j = "missing", drop = "ANY"): ...

```
[ signature(x = "PeriodicVector", i = "missing", j = "ANY", drop = "ANY"): ...
```

[ signature(x = "PeriodicVector", i = "missing", j = "missing", drop = "ANY"): ...

```
[<- signature(x = "PeriodicVector",i = "ANY",j = "ANY",value = "ANY"): ...</pre>
```

```
[<- signature(x = "PeriodicVector",i = "missing",j = "ANY",value = "ANY"): ...</pre>
```

### Author(s)

Georgi N. Boshnakov

## See Also

PeriodicVector

#### Examples

```
PeriodicVector(1:4, period = 4)
PeriodicVector(1:4) ## same
new("PeriodicVector", 1:4, period = 4)
## if period is given but x is missing, the vector is filled with NA's
PeriodicVector(period = 4)
## this throws error, since length(x) != period:
##
      PeriodicVector(1:3, period = 4)
## extract
x <- PeriodicVector(1:4)</pre>
x[3:12]
x[c(3, 7, 11, 15)]
# any indices in (-Inf, Inf) work
x[0]
x[-3:0]
## "[<-" works on the underling vector</pre>
x[1] <- 11; x
## modulo indexing works also in assignments:
x[5] <- 21; x
## empty index returns the underlying vector
x[]
## the recycling rule applies on assignment
x[] <- 9; x
x[] <- 1:2; x
## this gives warning, as for numeric vectors
##
      x[] <- 8:1
## compare:
##
      x <- 1:4
       x[] <- 8:1
##
## arithmetic works as usual:
2 * x
x + 1:4
## x + 1:3 # warning - '... a multiple ...'
```

periodic\_acf1\_test McLeod's test for periodic autocorrelation

#### permean2intercept

### Description

Performs McLeod's test for periodic autocorrelation.

#### Usage

```
periodic_acf1_test(acf, nepochs)
```

### Arguments

acf	sample periodic autocorrelation function
nepochs	the number of epochs used to get the acf

## Details

The test statistic is a scaled sum of squares of lag 1 sample periodic autocorrelation coefficients, see McLeod (1993), eq. (5). The distribution is approximately chi-square under the null hypothesis of no periodic autocorrelation.

## Value

A list containing the following components:

statistic	the value of the test statistic.
pvalue	the p-value associated with the test statistic.

#### Author(s)

Georgi N. Boshnakov

#### References

McLeod A (1993). "Parsimony, model adequacy and periodic correlation in time series forecasting." *Internat. Statist. Rev.*, **61**(3), pp. 387-393.

McLeod A (1994). "Diagnostic checking of periodic autoregression models with application." *Journal of time series analysis*, **15**(2), pp. 221-233.

permean2intercept Convert between periodic centering and intercepts

#### Description

Convert a periodic mean to periodic intercept and vice versa.

#### Usage

```
permean2intercept(mean, coef, order, nseasons = nrow(coef))
```

intercept2permean(intercept, coef, order, nseasons = nrow(coef))

### Arguments

mean	periodic mean, numeric.
coef	PAR coefficients, matrix.
order	PAR order, vector of positive integers.
nseasons	number of seasons, a.k.a. period.
intercept	periodic intercepts, numeric.

# Details

A PAR model can be written in mean corrected or intercept form. permean2intercept calculates the intercepts from the means, while intercept2permean does the inverse (means from intercepts).

No check is made for periodic stationarity of the model. Converting from mean corrected to intercept form allways succeeds and in fact the means do not need to be means. In the opposite direction there may be problems due to unit roots and similar features.

# Value

a numeric vector

#### Author(s)

Georgi N. Boshnakov

#### Examples

```
mu <- c(1, 2)
pm1 <- PeriodicArModel(matrix(c(0.5, 0.5), nrow = 2), order = rep(1, 2), sigma2 = 1, mean = mu)
cc <- permean2intercept(mu, pm1@ar@coef, c(1,1))
cc
intercept2permean(cc, pm1@ar@coef, c(1,1))
d <- 4
mu <- 1:d
co <- rep(0.5, d)
pm1 <- PeriodicArModel(matrix(co, nrow = d), order = rep(1, d), sigma2 = 1, mean = mu)
cc <- permean2intercept(mu, pm1@ar@coef, order = rep(1, d))
cc
intercept2permean(cc, pm1@ar@coef, order = rep(1, d) )</pre>
```

permodelmf

## Description

Compute the multi-companion form of a per model.

## Usage

```
permodelmf(permodel, update = TRUE)
```

# Arguments

permodel	a model.
update	If TRUE store the multi-companion form in permodel and return the whole
	model, otherwise simply return the multi-companion form.

# Details

todo:

### Value

the multi-companion form of the model or the updated model, as described in Details.

## Author(s)

Georgi N. Boshnakov

### References

Boshnakov GN and Iqelan BM (2009). "Generation of time series models with given spectral properties." *J. Time Series Anal.*, **30**(3), pp. 349–368. ISSN 0143-9782, http://dx.doi.org/10. 1111/j.1467-9892.2009.00617.x.

pi1ar2par

Convert PIAR coefficients to PAR coefficients

## Description

Convert PIAR coefficients to PAR coefficients

### Usage

```
pilar2par(picoef, parcoef)
piar2par(picoef, parcoef)
```

#### Arguments

picoef	coefficients of the periodic integration filter, a numeric vector or matrix, see Details.
parcoef	coefficients of the periodically correlated part of the model.

### Details

pilar2par converts PIAR(1) model coefficients specified as a set of coefficients corresponding to a periodic unit root and PAR coefficients to coefficients for a single filter.

piar2par does the same but admits higher order periodic integration.

picoef is a matrix, specifying one or more first order periodic unit root filters. Each column contains the coefficients of one filter. If there is only one filter, its coefficients can be given as a numeric vector.

The filters are applied from right to left, in the sense that first the PAR filter is applied to the time series, then the filter specified by the last column and so on.

Note that unlike the stationary case, in general, this is not equivalent to multiplication of the corresponding polynomials. This is rather different from the stationary case, where the analogous operation boils down just to multiplying the corresponding polynomials.

#### Value

a matrix, whose i-th row contains the coefficients for the i-th season.

### Author(s)

Georgi N. Boshnakov

#### Examples

PiPeriodicArmaModel-class

Class PiPeriodicArmaModel

### Description

Class PiPeriodicArmaModel.

## **Objects from the Class**

Objects can be created by calls of the form new("PiPeriodicArmaModel",...).

#### Slots

piorder: Object of class "numeric" ~~
picoef: Object of class "matrix" ~~
pcmodel: Object of class "PeriodicArmaModel" ~~

## Extends

Class "VirtualPeriodicFilterModel", directly. Class "PeriodicIntegratedArmaSpec", directly.

## Methods

No methods defined with class "PiPeriodicArmaModel" in the signature.

PiPeriodicArModel-class

Class PiPeriodicArModel

#### Description

Class PiPeriodicArModel.

#### **Objects from the Class**

Objects can be created by calls of the form new("PiPeriodicArModel",...).

# Slots

piorder: Object of class "numeric" ~~

picoef: Object of class "matrix" ~~

pcmodel: Object of class "PeriodicArmaModel" ~~

### Extends

Class "PiPeriodicArmaModel", directly. Class "VirtualPeriodicFilterModel", by class "PiPeriodicArmaModel", distance 2. Class "PeriodicIntegratedArmaSpec", by class "PiPeriodicArmaModel", distance 2.

#### Methods

fitPM signature(x = "ANY",model = "PiPeriodicArModel"): ...

PiPeriodicMaModel-class

Class PiPeriodicMaModel

## Description

Class PiPeriodicMaModel.

# **Objects from the Class**

Objects can be created by calls of the form new("PiPeriodicMaModel",...).

## Slots

piorder: Object of class "numeric" ~~

picoef: Object of class "matrix" ~~

pcmodel: Object of class "PeriodicArmaModel" ~~

### Extends

Class "PiPeriodicArmaModel", directly. Class "VirtualPeriodicFilterModel", by class "PiPeriodicArmaModel", distance 2. Class "PeriodicIntegratedArmaSpec", by class "PiPeriodicArmaModel", distance 2.

# Methods

No methods defined with class "PiPeriodicMaModel" in the signature.

pwn\_McLeodLjungBox\_test

McLeod-Ljung-Box test for periodic white noise

## Description

Compute the McLeod-Ljung-Box test statistic for examining the null hypothesis of periodic white noise.

#### Usage

#### Arguments

acf	the sample periodic autocorrelation function of the time series.
nepoch	number of cycles used in computing the acf.
use	number of lags to use, may be a vector.
maxlag	maximal lag.
period	number of seasons in a cycle.
fitdf	degrees of freedom corrections for the number of estimated parameters, see De- tails.

## Details

The McLeod-Ljung-Box test can be used to test the null hypothesis of periodic white noise.

If acf contains sample autocorrelations of residuals from a fitted model, a correction of the degrees of freedom is strongly recommended.

Argument fitdf is a vector specifying how may degrees of freedom to subtract for each season. In the case of PAR models fitdf can be set to the PAR orders.

The value of the statistic is set to NA where the correction for degrees of freedom results in negative numbers.

# Value

A list containing the following components:

statistic	the value of the test statistic for each lag specified by use.
df	the corresponding degrees of freedom

#### Note

TODO: Consolidate this and similar tests!

## Author(s)

Georgi N. Boshnakov

#### References

McLeod A (1994). "Diagnostic checking of periodic autoregression models with application." *Journal of time series analysis*, **15**(2), pp. 221-233.

### See Also

Box.test for the non-periodic case

SamplePeriodicAutocorrelations-class Class SamplePeriodicAutocorrelations

## Description

Class SamplePeriodicAutocorrelations.

## **Objects from the Class**

Objects can be created by calls of the form new("SamplePeriodicAutocorrelations",...,data).

## Slots

modelCycle: Object of class "BasicCycle" ~~
data: Object of class "Lagged" ~~
n: Object of class "numeric" ~~
varnames: Object of class "character" ~~
objectname: Object of class "character" ~~

## Extends

Class "PeriodicAutocorrelations", directly. Class "Fitted", directly. Class "ModelCycleSpec", by class "PeriodicAutocorrelations", distance 2. Class "FlexibleLagged", by class "PeriodicAutocorrelations", distance 2. Class "VirtualPeriodicAutocorrelations", by class "PeriodicAutocorrelations", distance 2. Class "Lagged", by class "PeriodicAutocorrelations", distance 3. Class "VirtualPeriodicAutocorrelations", distance 3. Class "VirtualPeriodicAutocorrelations", distance 3.

## Methods

No methods defined with class "SamplePeriodicAutocorrelations" in the signature.

SamplePeriodicAutocovariances-class Class SamplePeriodicAutocovariances

## Description

Class SamplePeriodicAutocovariances.

### **Objects from the Class**

Objects can be created by calls of the form new("SamplePeriodicAutocovariances",...,data).

# Slots

modelCycle: Object of class "BasicCycle" ~~

data: Object of class "Lagged" ~~

n: Object of class "numeric" ~~

varnames: Object of class "character" ~~

objectname: Object of class "character" ~~

## Extends

Class "PeriodicAutocovariances", directly. Class "Fitted", directly. Class "ModelCycleSpec", by class "PeriodicAutocovariances", distance 2. Class "FlexibleLagged", by class "PeriodicAutocovariances", distance 2. Class "VirtualPeriodicAutocovariances", by class "PeriodicAutocovariances", distance 2. Class "Lagged", by class "PeriodicAutocovariances", distance 3. Class "VirtualPeriodicAutocovariances", distance 3. Class "VirtualPeriodicAutocovariances", distance 3.

### Methods

autocorrelations signature(x = "SamplePeriodicAutocovariances",maxlag = "ANY",lag\_0 =
 "missing"): ...

seqSeasons-methods *Methods for seqSeasons() in package pcts* 

### Description

Methods for seqSeasons() in package pcts.

#### Methods

```
signature(x = "BasicCycle")
```

```
signature(x = "Cyclic")
```

signature(x = "VirtualPeriodicModel")

#### See Also

allSeasons for related functions and examples

sigmaSq-methods

### Description

Methods for sigmaSq in package pcts.

### Methods

```
signature(object = "PeriodicIntegratedArmaSpec")
signature(object = "PeriodicInterceptSpec")
```

SimpleCycle-class Class SimpleCycle

#### Description

Class SimpleCycle.

## **Objects from the Class**

Objects can be created by calls of the form new("SimpleCycle", nseasons, seasons, first).

In addition to number of seasons, class "SimpleCycle" holds also seasons' names and the index of the season to be treated as the first in a cycle.

### Slots

seasons: Object of class "character", the names of the seasons.

nseasons: Object of class "integer", number of seasons.

cycle: Object of class "character" ~~

season: Object of class "character" ~~

abbreviated: Object of class "character" ~~

### Extends

Class "BareCycle", directly. Class "BasicCycle", directly.

## Methods

No methods defined with class "SimpleCycle" in the signature.

### Author(s)

Georgi N. Boshnakov

## sim\_parAcvf

### See Also

pcCycle for creation of cycle objects and extraction of cycle part of time series,

BuiltinCycle-class, SimpleCycle-class,

DayWeekCycle-class, FiveDayWeekCycle-class, MonthYearCycle-class, OpenCloseCycle-class, QuarterYearCycle-class

BasicCycle-class (virtual, for use in signatures)

# Examples

showClass("SimpleCycle")

sim\_parAcvf Create a random periodic autocovariance function

## Description

Select randomly a periodic autoregression model and return the periodic autocovariances associated with it.

## Usage

sim\_parAcvf(period, order, sigma2)

#### Arguments

period	the period, a positive integer.
order	the AR order, a vector of non-negative integers.
sigma2	the variances of the innovations, a numeric vector of length period (todo: or one?).

### Details

Uses sim\_parCoef() to generate a random PAR model.

# Value

an object of class "matrix". In addition, the specification of the model is in attribute "model" which is a list with the following components:

ar	a matrix, the coefficients of the PAR model,
sigma2	numeric, the innovation variances,
order	the PAR order.

### Author(s)

Georgi N. Boshnakov

### References

Boshnakov GN and Iqelan BM (2009). "Generation of time series models with given spectral properties." *J. Time Series Anal.*, **30**(3), pp. 349–368. ISSN 0143-9782, http://dx.doi.org/10. 1111/j.1467-9892.2009.00617.x.

### Examples

```
sim_parAcvf(2, 5)
sim_parAcvf(3, 5)
res <- sim_parAcvf(2, 6)</pre>
res
slMatrix(res)[3, 4, type = "tt"]
res <- sim_parAcvf(2, 4)</pre>
attr(res, "model")
acv <- res[ , ] # drop attributes</pre>
acv[2, 1 + 0]
acv[2, 1 + 1]
slMatrix(acv)[2, 0]
slMatrix(acv)[2, 1]
slMatrix(acv)[3, 4, type = "tt"]
slMatrix(acv)[1:2, 1:2, type = "tt"]
slMatrix(acv)[1:4, 1:4, type = "tt"]
## TODO: need method for autocorrelation()
## pc.acrf(acv)
## TODO: these need changing, after the change of the return values of sim_parAcvf
## pc.fcoeffs(acv, 2)
## pc.fcoeffs(acv, 3)
## pc.fcoeffs(acv, 4)
pcts:::calc_predictionCoefficients(acv, c(2, 2))
pcts:::calc_predictionCoefficients(acv, c(3, 3))
pcts:::calc_predictionCoefficients(acv, c(4, 4))
```

sim\_parCoef

Generate a periodic autoregression model

### Description

Generate a periodic autoregression model, possibly integrated.

### Usage

```
sim_parCoef(period, n.root, sigma2 = rep(1, period), ...)
```

#### sim\_parCoef

#### Arguments

period	number of seasons in a cycle.
n.root	number of non-zero roots, see details.
sigma2	variances of the innovations.
	additional arguments to be passed down to sim_pcfilter

# Details

sim\_parCoef uses the multi-companion method to generate the model. The function is essentially a wrapper for sim\_pcfilter.

The order of the filter is set to n.root for each season. Part of the spectral information may be specified with the "..." arguments, see sim\_pcfilter and sim\_mc for a discussion of this.

### Value

a periodic autoregression model as a list with elements:

ar	a matrix whose <i>i</i> th row contains the coefficients for the <i>i</i> season,
sigma2	the innovation variances, a numeric vector.

#### Author(s)

Georgi N. Boshnakov

## References

Boshnakov GN and Iqelan BM (2009). "Generation of time series models with given spectral properties." *J. Time Series Anal.*, **30**(3), pp. 349–368. ISSN 0143-9782, http://dx.doi.org/10. 1111/j.1467-9892.2009.00617.x.

## See Also

sim\_pcfilter

#### Examples

sim\_pc

### Description

Simulate a realization of a periodically correlated arma model or a continuation of an existing series. Initial values may be given too.

#### Usage

## Arguments

model	a list with elements phi, theta, p, q, period, mean, intercept, specifying the model.
n	length of the series.
randgen	random number generator as required by sim_pwn.
seasonof1st	season of the first value.
nepochs	number of epochs; if nepochs is given, then n is computed as $nepochs*period$ .
n.start	burn-in number; generate $n.start + n$ observations and discard the first $n.start$ of them, see Details.
х	initial or before values, see Details.
eps	innovations, see Details.
nmean	a vector of length n of means, see Details.
nintercept	a vector of length n of intercepts, see Details.
	any additional arguments to be passed on to sim_pwn.

#### **Details**

Argument x can be used to specify two types of initialisation values - 'before' and 'init'. They are used similarly in computations but 'before' values are not included in the result, while 'init' values are (unless dropped due to n.start). 'Before' values provide a convenient way to simulate continuation trajectories for a time series, for example for simulation based prediction intervals.

If x is "numeric", it represents 'before' values. Alternatively, x can be a list with components "before" and "init".

Innovations are usually generated with the random number generator specified by randgen (with default rnorm) and the ... parameters by a call to the function sim\_pwn, see the documentation for sim\_pwn for various ways to control the distribution of the generated sequence.

The innovations can also be generated in advance and supplied using argument eps. If eps is numeric, it is taken to represent the innovations. Alternatively, eps can be a list with the innovations

#### sim\_pc

in component "main". This list may also contain components "before" and/or "init" specifying 'before' or 'initial' values, with interpretation as for x.

nintercept can be used to specify trend representing the effect of time and/or covariates. As for eps, if it is numeric it is taken to represent the main values. It can also be a list with components before, init, and main.

To avoid ambiguity, let's reiterate that *before* values are past values of the corresponding quantity (before the start of the simulated series), while *init* values are "initial" values. In particular, if initial values are specified for x, these will form the start of the generated series (unless n.start leads to them being discarded).

If *before* values are specified for the series and the innovations, then they play a role analogous to that of initial values, so it does not make much sense to supply also *initial* values.

The function effectively does the following. innov is generated if not supplied, a vector of innovations is created eps <-c(innovbefore,innovinit,innov), a vector x is created of the same length as eps, and initialised with xbefore and xinit. If there are no initial or before values, these are assumed to be 0. The remaining values of x are filled using the pc-arma equations. Finally, the xbefore values are discarded as well as the first n.start values.

n.start should usually be a multiple of the period since otherwise the first observation in the returned vector will not correspond to seasonof1st.

sim\_pc deals mainly with the interpretation of the parameters. The actual computations are done by pc.filter. Moreover, sim\_pc does not look at the model. It knows only about model\$period and uses it to compute n if n is not specified. (It probably should not care even about this.)

## Value

numeric, the simulated time series

#### To do

option to return the innovation sequence; option to include the before values.

option to return the season of the first value in the returned series (it may be different from seasonof1st due to n.start).

#### Author(s)

Georgi N. Boshnakov

#### See Also

sim\_pwn, pc.filter

#### Examples

```
m1 <- rbind( c(1, 0.81, 0), c(1, 0.4972376, 0.4972376) )
testphi <- slMatrix( init = m1 )
m2 <- rbind( c(1, 0, 0), c(1, 0, 0) )
testtheta <- slMatrix( init = m2 )</pre>
```

```
## phi and theta are slMatrix here.
mo1 <- list(phi = testphi, theta = testtheta, p = 2, q = 2, period = 2)</pre>
set.seed(1234)
a1 <- sim_pc(mo1, 100)
## phi and theta are ordinary matrices here.
mo2 <- list(phi = m1[, 2:ncol(m1)], theta = m2[, 2:ncol(m2)], p = 2, q = 2, period = 2)</pre>
set.seed(1234)
a2 <- sim_pc(mo2, 100)
identical(a1, a2)
## Lina's PAR model
           <- rbind(c(0.5, -0.06), c(0.6, -0.08),
parcoef
                    c(0.7, -0.1), c(0.2, 0.15))
           <- c(0.8, 1.25, 2, 0.5)
picoef1
parcoef2 <- pilar2par(picoef1, parcoef)</pre>
picoef2
           <- c(4, 0.25, 5, 0.2)
coefper2I2 <- pi1ar2par(picoef2, parcoef2)</pre>
#### specify the model using multi-companion approach
            <- mcompanion::mc_from_filter(coefper2I2)
mc2I2
co2I2
            <- eigen(mc2I2)$vectors
co2I2
m2I2 <- mcompanion::sim_pcfilter(period = 4, n.root = 4,</pre>
                 eigabs = c(1, 0.036568887, 0.001968887),
                 eigsign = c(1, 1, -1),
                 len.block = c(2, 1, 1),
                 type.eigval = c("r", "r", "r"),
                 co = cbind(co2I2[ ,1], rep(NA, 4), co2I2[,3:4]))
m2I2$pcfilter
perunit2mc <- sim_pc(list(phi = m2I2$pcfilter, p = 4, q = 0, period = 4), 500)</pre>
plot(perunit2mc)
plot(perunit2mc, type = "p")
# todo: give example with sigmat^2 !!!
```

sim\_pwn

Simulate periodic white noise

## Description

Generates a sample from periodic white noise.

## Usage

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#### sim\_pwn

#### Arguments

n	length of the generated sample.
period	number of seasons in an epoch.
seasonof1st	season of the first observation in the result.
scale	scale the series by this amount, a vector of length period or 1.
shift	shift the series by this amount, a vector of length period or 1.
f	a function or list of functions to generate random numbers.
	arguments for the random number generator(s) specified by f.

#### Details

First a series, say x, of random numbers is generated as requested by the argument f. Then, if shift and/or scale are supplied, the values are modified as follows:

$$y_t = shift_k + scale_k x_t$$

where k is the season corresponding to time t. The vector y is returned.

If f is a single a function (or name of a function), then the series is generated (effectively) by the call f(n, ...).

The argument f may also be a list whose kth element is itself a list specifying the random number generator for the kth season. The first element being the function (such as rnorm) and the remaining elements being parameters for that function. Parameters common to all seasons may be supplied through the ... argument.

The argument period may be omitted. In that case it is inferred from f and/or the lengths of shift and scale. Currently there is no check for consistency here.

The arguments shift and scale may be used to specify simple linear transformations of the generated values, possibly different for the different seasons. Each of them should be a vector of length period or one.

seasonof1st can be used to request the simulated time series to start from a season other than the first one. Note that whatever the value of seasonof1st, the first elements of scale, shift and f (if a list) are taken to refer to season one.

## Value

A vector of length n representing a realization of a periodic white noise series. The season of the first observation is seasonof1st.

# Level

0 (base)

# Author(s)

Georgi N. Boshnakov

#### Examples

```
## three equivalent ways to specify periodic white noise with
## normal innovatios, 2 seasons, s.d. = 0.5 for season 1, and 2 for season 2
sim_pwn(100, f = rnorm, scale = c(0.5, 2))
sim_pwn(n = 100, scale = c(0.5, 2)) # rnorm is the default generator
sim_pwn(100, f = list(c(rnorm, 0, 0.5), c(rnorm, 0, 2)))
```

SiPeriodicArmaModel-class

Class SiPeriodicArmaModel

# Description

Class SiPeriodicArmaModel.

# **Objects from the Class**

Objects can be created by calls of the form new("SiPeriodicArmaModel",...).

# Slots

iorder: Object of class "numeric" ~~

siorder: Object of class "numeric" ~~

pcmodel: Object of class "PeriodicArmaModel" ~~

#### Extends

Class "VirtualPeriodicFilterModel", directly. Class "PeriodicIntegratedArmaSpec", directly.

#### Methods

No methods defined with class "SiPeriodicArmaModel" in the signature.

SiPeriodicArModel-class

Class SiPeriodicArModel

### Description

Class SiPeriodicArModel.

#### **Objects from the Class**

Objects can be created by calls of the form new("SiPeriodicArModel",...).

# Slots

iorder: Object of class "numeric" ~~

siorder: Object of class "numeric" ~~

pcmodel: Object of class "PeriodicArmaModel" ~~

# Extends

Class "SiPeriodicArmaModel", directly. Class "VirtualPeriodicFilterModel", by class "SiPeriodicArmaModel", distance 2. Class "PeriodicIntegratedArmaSpec", by class "SiPeriodicArmaModel", distance 2.

# Methods

```
fitPM signature(model = "SiPeriodicArModel",x = "ANY"): ...
```

SiPeriodicMaModel-class

Class SiPeriodicMaModel

# Description

Class SiPeriodicMaModel.

#### **Objects from the Class**

Objects can be created by calls of the form new("SiPeriodicMaModel",...).

#### Slots

iorder: Object of class "numeric" ~~

siorder: Object of class "numeric" ~~

pcmodel: Object of class "PeriodicArmaModel" ~~

#### Extends

Class "SiPeriodicArmaModel", directly. Class "VirtualPeriodicFilterModel", by class "SiPeriodicArmaModel", distance 2. Class "PeriodicIntegratedArmaSpec", by class "SiPeriodicArmaModel", distance 2.

#### Methods

No methods defined with class "SiPeriodicMaModel" in the signature.

test\_piar

#### Description

Test if a time series is periodically integrated.

#### Usage

test\_piar(x, d, p, sintercept = FALSE, sslope = FALSE, homoschedastic = FALSE)

#### Arguments

х	time series
d	period
р	autoregressive order, a positive integer
sintercept	if TRUE, include seasonal intercept
sslope	if TRUE, include seasonal slope
homoschedastic	if TRUE, assume the innovations variance is the same for all seasons

#### Details

Computes test statistics for Franses (1996) test for periodic integration of order 1. The test is based on periodic autoregression of order p, where p can be any positive integer.

#### Value

a list with the following components:

р	autoregressive order.
spec	values of sintercept, sslope, and homoschedastic, a named logical vector.
statistics	a matrix containing the the test statistics (first row) and the corresponding p-values (second row). "LR" is not normalised, so its p-value is NA.

#### Note

Currently only the case p = 1 is handled, for p > 1 the statistics are set to NA. **:TODO: handle this.** All statistics are computed but some p-values are not computed yet.

# Author(s)

Georgi N. Boshnakov

#### References

Boswijk HP and Franses PH (1996). "Unit roots in periodic autoregressions." *Journal of Time Series Analysis*, **17**(3), pp. 221–245.

# unitCycle-methods

#### See Also

pclspiar, pclsdf

# Examples

unitCycle-methods *Methods for unitCycle() in package pcts* 

# Description

Methods for unitCycle() in package pcts.

#### Methods

```
signature(x = "ANY")
signature(x = "DayWeekCycle")
signature(x = "FiveDayWeekCycle")
signature(x = "MonthYearCycle")
signature(x = "OpenCloseCycle")
signature(x = "QuarterYearCycle")
signature(x = "SimpleCycle")
signature(x = "Cyclic")
signature(x = "Every30MinutesCycle")
signature(x = "VirtualPeriodicModel")
```

#### See Also

allSeasons for related functions and examples.

unitCycle<--methods Methods for "unitCycle<-"() in package pcts</pre>

#### Description

Methods for "unitCycle<-"() in package pcts.

# Methods

```
signature(x = "Cyclic")
signature(x = "SimpleCycle")
```

unitSeason-methods *Methods for unitSeason() in package pcts* 

# Description

Methods for unitSeason() in package pcts.

#### Methods

```
signature(x = "ANY")
signature(x = "DayWeekCycle")
signature(x = "FiveDayWeekCycle")
signature(x = "MonthYearCycle")
signature(x = "OpenCloseCycle")
signature(x = "QuarterYearCycle")
signature(x = "SimpleCycle")
signature(x = "Cyclic")
signature(x = "Every30MinutesCycle")
signature(x = "VirtualPeriodicModel")
```

# See Also

allSeasons for related functions and examples

unitSeason<--methods Methods for "unitSeason<-"() in package pcts</pre>

# Description

Methods for "unitSeason<-"() in package pcts.

# Methods

```
signature(x = "Cyclic")
signature(x = "SimpleCycle")
```

Vec

# Core data of periodic time series

# Description

Core data of periodic time series.

# Usage

```
Vec(x, ...)
tsMatrix(x, ...)
tsVector(x, ...)
tsVec(x, ...)
pcMatrix(x, ...)
pcArray(x, ndim = 3, ...)
pctsArray(x, ndim = 3, ...)
```

# Arguments

х	an object.
	further arguments for methods.
ndim	currently not used.

#### Details

These functions give the core data in various common forms.

The data values can be extracted as a vector from a periodic time series object, say x, with as.vector(x) or as(x, "vector"). Similarly, as.matrix() and as(x, "matrix") extract the data as a matrix containing one column per variable. For multivariate time series the vector returned by as.vector(x) (or as(x, "vector")) is equivalent to as.vector(as.matrix(x)).

Vec() is like as.vector() but returns the result as a matrix with one column (column vector), as is usual in matrix calculus. The default does literally this:

The most common representation of data in statistics is matrix-like with one column per variable. The descriptions of algorithms for multivariate time series however usually define the vector of observations at a given time to be a column vector. In particular, implementations of the Kalman filter often require precisely this arrangement.

In that case the data matrix is the transposed of the more common one and the vectorising operation stacks the observations, not the variables.

The functions tsMatrix(), tsVector() and tsVec() provide the analogues of as.vector(), as.matrix() and Vec() for the "transposed" arrangement.

These functions may look redundant since they are simple combinations of the above and traspose operations. Having functions makes for more readable programming. They may be more efficient, as well, for example if the underlying time series class stores the data in the transposed format.

pcMatrix() and pcArray() also give the core data. Effectively, they give an additional dimension to the seasons. The season becomes the first dimension since for column oriented data the season changes fastest. pcMatrix is most suitable for univariate time series, pcArray() for multivariate. Note that pcArray() easily extends to multiple periodicities although currently (2019-04-19) there are no methods that exploit this.

For univariate time series, in the matrix returned by pcMatrix() each row represents the data for one season and each column for one cycle. For multivariate time series, the matrices for each variable are put next to each other.

pcArray() returns the data as an array, whose last dimension corresponds to variables. In the default case the array is 3-dimensional with dimensions (season, year, variable).

pctsArray() is a variant of pcArray() corresponding to the arrangement of tsMatrix(). The ordering of the dimensions here is (variable, season, cycle).

#### Value

vector, matrix or array, as indicated by the name of the function and described in Details.

#### Author(s)

Georgi N. Boshnakov

## Examples

```
## window to make number of years different from number of months
ap <- pcts(window(AirPassengers, start = c(1956, 1)))
class( as.vector(ap) )
class( as(ap, "vector") )
```

```
dim( as.matrix(ap)
                      )
dim( as(ap, "matrix") )
dim( tsMatrix(ap) )
class( tsVector(ap) )
dim( tsVec(ap)
                  )
dim( pcMatrix(ap)
                   )
dim( pcArray(ap)
                    )
dim( pctsArray(ap) )
dfr <- pcts(dataFranses1996)</pre>
dim(dfr)
                             # c(148, 19)
nSeasons(dfr)
                             # 4
length(as.vector(dfr))
all.equal(as.vector(dfr)[1:148],
                                       as.matrix(dfr)[ , 1]) # TRUE
all.equal(tsVector(dfr)[1:19], unname(as.matrix(dfr)[1, ])) # TRUE
dim( as.matrix(dfr) ) # c(148, 19)
dim( tsMatrix(dfr) ) # c(19, 148)
all.equal(tsMatrix(dfr)[ , 1], as.matrix(dfr)[1, ]) # TRUE
dim( Vec(dfr)
              )
dim( tsVec(dfr) )
all.equal(tsVec(dfr)[1:19], unname(as.matrix(dfr)[1, ])) # TRUE
dim( pcMatrix(dfr) ) \# c(4, 703), one row for each season
dim( pcArray(dfr)
                    ) # c(4, 37, 19), note: 703 == 37*19
dim( pctsArray(dfr) ) # c(19, 4, 37), note: 703 == 37*19
```

zoo-class

Class zoo made S4

#### Description

Class zoo made S4

#### **Objects from the Class**

A virtual Class: No objects may be created from it.

S4 Class "zoo" is derived from its namesake in package **zoo** for use as a super class for periodic time series classes and in S4 method signatures.

# Slots

.S3Class: Object of class "character" ~~

# Extends

Class "oldClass", directly. Class "AnyTimeSeries", directly.

#### Methods

No methods defined with class "zoo" in the signature.

## See Also

PeriodicTS\_zooreg, zooreg and package zoo

#### Examples

showClass("zoo")

zooreg-class Virtual S4 class zooreg

# Description

Virtual S4 class zooreg.

# **Objects from the Class**

A virtual Class: No objects may be created from it.

S4 Class "zooreg" is derived from its namesake in package **zoo** for use as a super class for periodic time series classes and in S4 method signatures.

# Slots

.S3Class: Object of class "character" ~~

# Extends

Class "zoo", directly. Class "AnyTimeSeries", directly. Class "oldClass", by class "zoo", distance 2.

#### Methods

No methods defined with class "zooreg" in the signature.

#### See Also

PeriodicTS\_zooreg, zoo and package zoo

### Examples

showClass("zooreg")

[-methods

#### Description

Indexing of objects from classes in package pcts.

#### Methods

```
signature(x = "BasicCycle", i = "ANY", j = "missing", drop = "ANY")
signature(x = "BasicCycle", i = "missing", j = "missing", drop = "ANY")
signature(x = "PeriodicMTS", i = "ANY", j = "missing", drop = "ANY")
signature(x = "PeriodicVector", i = "ANY", j = "MNY", drop = "ANY")
signature(x = "PeriodicVector", i = "ANY", j = "missing", drop = "ANY")
signature(x = "PeriodicVector", i = "ANY", j = "missing", drop = "ANY")
signature(x = "PeriodicVector", i = "missing", j = "missing", drop = "ANY")
signature(x = "PeriodicVector", i = "missing", j = "missing", drop = "ANY")
signature(x = "PeriodicVector", i = "missing", j = "missing", drop = "ANY")
signature(x = "PeriodicVector", i = "missing", j = "missing", drop = "ANY")
signature(x = "VirtualPeriodicAutocovarianceModel", i = "missing", j = "missing", drop = "ANY")
signature(x = "VirtualPeriodicAutocovarianceModel", i = "missing", j = "missing", drop = "ANY")
signature(x = "VirtualPeriodicAutocovarianceModel", i = "missing", j = "missing", drop = "ANY")
signature(x = "VirtualPeriodicAutocovarianceModel", i = "numeric", j = "missing", drop = "ANY")
```

#### Author(s)

Georgi N. Boshnakov

[<--methods

Index assignments for objects from classes in package pcts

# Description

Index assignments for objects from classes in package pcts.

# Methods

```
signature(x = "PeriodicVector", i = "ANY", j = "ANY", value = "ANY")
signature(x = "PeriodicVector", i = "missing", j = "ANY", value = "ANY")
signature(x = "BasicCycle", i = "ANY", j = "missing", value = "ANY")
signature(x = "BasicCycle", i = "missing", j = "missing", value = "ANY")
signature(x = "PeriodicAutocovarianceModel", i = "ANY", j = "ANY", value = "ANY")
```

# Author(s)

Georgi N. Boshnakov

[[-methods Methods for function' [[' in package 'pcts'

# Description

Methods for function `[[` in package 'pcts'.

#### Methods

```
signature(x = "PeriodicMTS", i = "ANY", j = "ANY")
signature(x = "VirtualPeriodicAutocovarianceModel", i = "numeric", j = "ANY")
```

\$-methods

Methods for function\$ in package 'pcts'

# Description

Methods for function\$ in package 'pcts'.

# Methods

signature(x = "PeriodicMTS")

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