

# Package ‘mlt’

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**Description** Likelihood-based estimation of conditional transformation models via the most likely transformation approach described in Hothorn et al. (2018) <DOI:10.1111/sjos.12291>.

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mlt-package

*General Information on the mlt Package*

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**Description**

The **mlt** package implements maximum likelihood estimation in conditional transformation models as introduced by Hothorn et al. (2018).

An introduction to the package is available in the `mlt` package vignette from package `mlt.docreg` (Hothorn, 2018).

A short talk on most likely transformations is available from <https://channel9.msdn.com/Events/useR-international-R-User-conference/useR2016/Most-Likely-Transformations>.

**Author(s)**

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**References**

Torsten Hothorn, Lisa Moest, Peter Buehlmann (2018), Most Likely Transformations, *Scandinavian Journal of Statistics*, **45**(1), 110–134, doi: [10.1111/sjos.12291](https://doi.org/10.1111/sjos.12291).

Torsten Hothorn (2018), Most Likely Transformations: The `mlt` Package, *Journal of Statistical Software*, forthcoming. URL: <https://cran.r-project.org/package=mlt.docreg>.

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confband*Confidence Bands*

---

**Description**

Confidence bands for transformation, distribution, survivor or cumulative hazard functions

**Usage**

```
confband(object, newdata, level = 0.95, ...)
## S3 method for class 'mlt'
confband(object, newdata, level = 0.95,
         type = c("trafo", "distribution", "survivor", "cumhazard"),
         K = 20, cheat = K, ...)
```

**Arguments**

object	an object of class <code>mlt</code>
newdata	a data frame of observations
level	the confidence level
type	the function to compute the confidence band for
K	number of grid points the function is evaluated at
cheat	number of grid points the function is evaluated at when using the quantile obtained for K grid points
...	additional arguments to <code>confint.glm</code>

**Details**

The function is evaluated at K grid points and simultaneous confidence intervals are then interpolated in order to construct the band.

A smoother band can be obtained by setting `cheat` to something larger than K: The quantile is obtained for K grid points but the number of evaluated grid points `cheat` can be much larger at no additional cost. Technically, the nominal level is not maintained in this case but the deviation will be small for reasonably large K.

**Value**

For each row in `newdata` the function and corresponding confidence band evaluated at the K (or `cheat`) grid points is returned.

---

ctm

*Conditional Transformation Models*


---

**Description**

Specification of conditional transformation models

**Usage**

```
ctm(response, interacting = NULL, shifting = NULL, data = NULL,
     todistr = c("Normal", "Logistic", "MinExtrVal", "MaxExtrVal", "Exponential"),
     sumconstr = inherits(interacting, c("formula", "formula_basis")), ...)
```

**Arguments**

response	a basis function, ie, an object of class <code>basis</code>
interacting	a basis function, ie, an object of class <code>basis</code>
shifting	a basis function, ie, an object of class <code>basis</code>
data	either a <code>data.frame</code> containing the model variables or a formal description of these variables in an object of class <code>vars</code>

<code>todistr</code>	a character vector describing the distribution to be transformed
<code>sumconstr</code>	a logical indicating if sum constraints shall be applied
<code>...</code>	arguments to <code>as.basis</code> when <code>shifting</code> is a formula

### Details

This function only specifies the model which can then be fitted using `mlt`. The shift term is positive by default.

Possible choices of the distributions the model transforms to (the inverse link functions) include the standard normal ("Normal"), the standard logistic ("Logistic"), the standard minimum extreme value ("MinExtrVal", also known as Gompertz distribution), and the standard maximum extreme value ("MaxExtrVal", also known as Gumbel distribution) distributions. The exponential distribution ("Exponential") can be used to fit Aalen additive hazard models.

### Value

An object of class `ctm`.

### References

Torsten Hothorn, Lisa Moest, Peter Buehlmann (2018), Most Likely Transformations, *Scandinavian Journal of Statistics*, **45**(1), 110–134, doi: [10.1111/sjos.12291](https://doi.org/10.1111/sjos.12291).

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ctm-methods

*Methods for ctm Objects*

---

### Description

Methods for objects of class `ctm`

### Usage

```
## S3 method for class 'ctm'
variable.names(object,
               which = c("all", "response", "interacting", "shifting"),
               ...)
## S3 method for class 'ctm'
coef(object, ...)
```

### Arguments

<code>object</code>	an unfitted conditional transformation model as returned by <code>ctm</code>
<code>which</code>	a character specifying which names shall be returned
<code>...</code>	additional arguments

### Details

`coef` can be used to get and set model parameters.

---

`mlt`*Most Likely Transformations*

---

## Description

Likelihood-based model estimation in conditional transformation models

## Usage

```
mlt(model, data, weights = NULL, offset = NULL, fixed = NULL, theta = NULL,  
     pstart = NULL, scale = FALSE, dofit = TRUE, optim = mltoptim(), ...)
```

## Arguments

<code>model</code>	a conditional transformation model as specified by <code>ctm</code>
<code>data</code>	a <code>data.frame</code> containing all variables specified in <code>model</code>
<code>weights</code>	an optional vector of weights
<code>offset</code>	an optional vector of offset values
<code>fixed</code>	a named vector of fixed regression coefficients; the names need to correspond to column names of the design matrix
<code>theta</code>	optional starting values for the model parameters
<code>pstart</code>	optional starting values for the distribution function evaluated at the data
<code>scale</code>	a logical indicating if (internal) scaling shall be applied to the model coefficients
<code>dofit</code>	a logical indicating if the model shall be fitted to the data (TRUE) or not
<code>optim</code>	a list of functions implementing suitable optimisers
<code>...</code>	additional arguments, currently ignored

## Details

This function fits a conditional transformation model by searching for the most likely transformation as described in Hothorn et al. (2017).

## Value

An object of class `mlt` with corresponding methods.

## References

Torsten Hothorn, Lisa Moest, Peter Buehlmann (2018), Most Likely Transformations, *Scandinavian Journal of Statistics*, **45**(1), 110–134, doi: [10.1111/sjos.12291](https://doi.org/10.1111/sjos.12291).

**Examples**

```

### set-up conditional transformation model for conditional
### distribution of dist given speed
dist <- numeric_var("dist", support = c(2.0, 100), bounds = c(0, Inf))
speed <- numeric_var("speed", support = c(5.0, 23), bounds = c(0, Inf))
ctmm <- ctm(response = Bernstein_basis(dist, order = 4, ui = "increasing"),
            interacting = Bernstein_basis(speed, order = 3))

### fit model
(mltm <- mlt(ctmm, data = cars))

### plot data
plot(cars)
### predict quantiles and overlay data with model via a "quantile sheet"
q <- predict(mltm, newdata = data.frame(speed = 0:24), type = "quantile",
            p = 2:8 / 10, K = 500)
tmp <- apply(q, 1, function(x) lines(0:24, x, type = "l"))

```

mlt-methods

*Methods for mlt Objects***Description**

Methods for objects of class mlt

**Usage**

```

## S3 method for class 'mlt'
coef(object, fixed = TRUE, ...)
coef(object) <- value
## S3 method for class 'mlt'
weights(object, ...)
## S3 method for class 'mlt'
logLik(object, parm = coef(object, fixed = FALSE), w = NULL, newdata, ...)
## S3 method for class 'mlt'
vcov(object, parm = coef(object, fixed = FALSE), complete = FALSE, ...)
Hessian(object, ...)
## S3 method for class 'mlt'
Hessian(object, parm = coef(object, fixed = FALSE), ...)
Gradient(object, ...)
## S3 method for class 'mlt'
Gradient(object, parm = coef(object, fixed = FALSE), ...)
## S3 method for class 'mlt'
estfun(object, parm = coef(object, fixed = FALSE),
        w = NULL, newdata, ...)
## S3 method for class 'mlt'

```

```

mkgrid(object, n, ...)
## S3 method for class 'mlt'
bounds(object)
## S3 method for class 'mlt'
variable.names(object, ...)
## S3 method for class 'mlt_fit'
update(object, weights = stats::weights(object),
        subset = NULL, offset = object$offset, theta = coef(object, fixed = FALSE),
        ...)
## S3 method for class 'mlt'
as.mlt(object)

```

### Arguments

object	a fitted conditional transformation model as returned by <code>mlt</code>
fixed	a logical indicating if only estimated coefficients ( <code>fixed = FALSE</code> ) should be returned
value	coefficients to be assigned to the model
parm	model parameters
w	model weights
weights	model weights
newdata	an optional data frame of new observations. Allows evaluation of the log-likelihood for a given model object on these new observations. The parameters <code>parm</code> and <code>w</code> are ignored in this situation.
n	number of grid points
subset	an optional integer vector indicating the subset of observations to be used for fitting.
offset	an optional vector of offset values
theta	optional starting values for the model parameters
complete	currently ignored
...	additional arguments

### Details

`coef` can be used to get and set model parameters, `weights` and `logLik` extract weights and evaluate the log-likelihood (also for parameters other than the maximum likelihood estimate). `Hessian` returns the Hessian and `vcov` the inverse thereof. `Gradient` gives the gradient (sum of the score contributions) and `estfun` the score contribution by each observation. `mkgrid` generates a grid of all variables (as returned by `variable.names`) in the model. `update` allows refitting the model with alternative weights and potentially different starting values. `bounds` gets bounds for bounded variables in the model.

---

`mltoptim` *Control Optimisation*

---

### Description

Define optimisers and their control parameters

### Usage

```
mltoptim(auglag = list(maxtry = 5, kkt2.check = FALSE),
         spg = list(maxit = 10000, quiet = TRUE, checkGrad = FALSE),
         nloptr = NULL, trace = FALSE)
```

### Arguments

<code>auglag</code>	A list with control parameters for the <code>auglag</code> optimiser. <code>maxtry</code> is the number of times the algorithm is started on random starting values in case it failed with the precomputed ones.
<code>spg</code>	A list with control parameters for the <code>BBoptim</code> optimiser (calling <code>spg</code> internally).
<code>nloptr</code>	A list with control parameters for the <code>nloptr</code> optimiser. This is still experimental and thus switched off (defaulting to <code>NULL</code> ).
<code>trace</code>	A logical switching trace reports by the optimisers off.

### Details

This function sets-up functions to be called in `mlt` internally.

### Value

A list of functions with arguments `theta` (starting values), `f` (log-likelihood), `g` (scores), `ui` and `ci` (linear inequality constraints). Adding further such functions is a way to add more optimisers to `mlt`. The first one in this list converging defines the resulting model.

---

plot-predict-simulate *Plots, Predictions and Samples from mlt Objects*

---

### Description

Plot, predict and sample from objects of class `mlt`



**Usage**

```

## S3 method for class 'ctm'
plot(x, newdata, type = c("distribution", "survivor", "density",
  "logdensity", "hazard", "loghazard", "cumhazard", "logcumhazard", "odds",
  "logodds", "quantile", "trafo"),
  q = NULL, prob = 1:(K - 1) / K, K = 50, col = rgb(.1, .1, .1, .1), lty = 1,
  add = FALSE, ...)
## S3 method for class 'mlt'
plot(x, ...)
## S3 method for class 'ctm'
predict(object, newdata, type = c("trafo", "distribution",
  "survivor", "density", "logdensity", "hazard", "loghazard", "cumhazard",
  "logcumhazard", "odds", "logodds", "quantile"),
  terms = c("bresponse", "binteracting", "bshifting"),
  q = NULL, prob = NULL, K = 50, interpolate = TRUE, ...)
## S3 method for class 'mlt'
predict(object, newdata = object$data, ...)
## S3 method for class 'ctm'
simulate(object, nsim = 1, seed = NULL, newdata, K = 50, q = NULL,
  interpolate = TRUE, bysim = TRUE, ...)
## S3 method for class 'mlt'
simulate(object, nsim = 1, seed = NULL, newdata = object$data, bysim = TRUE, ...)

```

**Arguments**

object	a fitted conditional transformation model as returned by <a href="#">mlt</a> or an unfitted conditional transformation model as returned by <a href="#">ctm</a>
x	a fitted conditional transformation model as returned by <a href="#">mlt</a>
newdata	an optional data frame of observations
type	type of prediction or plot to generate
q	quantiles at which to evaluate the model
prob	probabilities for the evaluation of the quantile function (type = "quantile")
terms	terms to evaluate for the predictions, corresponds to the argument response, interacting and shifting in <a href="#">ctm</a>
K	number of grid points to generate (in the absence of q)
col	color for the lines to plot
lty	line type for the lines to plot
add	logical indicating if a new plot shall be generated (the default)
interpolate	logical indicating if quantiles shall be interpolated linearly
nsim	number of samples to generate
seed	optional seed for the random number generator
bysim	logical, if TRUE a list with nsim elements is returned, each element is of length nrow(newdata) and contains one sample from the conditional distribution for each row of newdata. If FALSE, a list of length nrow(newdata) is returned, its

ith element of length `nsim` contains `nsim` samples from the conditional distribution given `newdata[i,]`.

... additional arguments

### Details

`plot` evaluates the transformation function over a grid of `q` values for all observations in `newdata` and plots these functions (according to `type`). `predict` evaluates the transformation function over a grid of `q` values for all observations in `newdata` and returns the result as a matrix (where `_columns_` correspond to `_rows_` in `newdata`). Note that the `predict` method for `ctm` objects requires all model coefficients to be specified in this unfitted model. `simulate` draws samples from object by numerical inversion of the quantile function.

Note that offsets are ALWAYS IGNORED when computing predictions. If you want the methods to pay attention to offsets, specify them as a variable in the model with fixed regression coefficient using the `fixed` argument in `mlt`.

---

R

*Response Variable*


---

### Description

Represent a possibly censored or truncated response variable

### Usage

```
R(object, ...)
## S3 method for class 'numeric'
R(object = NA, cleft = NA, cright = NA,
  tleft = NA, tright = NA, tol = sqrt(.Machine$double.eps), ...)
## S3 method for class 'ordered'
R(object, cleft = NA, cright = NA, ...)
## S3 method for class 'integer'
R(object, cleft = NA, cright = NA, bounds = c(min(object), Inf), ...)
## S3 method for class 'factor'
R(object, ...)
## S3 method for class 'Surv'
R(object, ...)
as.Surv(object)
## S3 method for class 'response'
as.Surv(object)
```

### Arguments

<code>object</code>	A vector of (conceptually) exact measurements or an object of class <code>response</code> (for <code>as.Surv</code> ) or a list.
<code>cleft</code>	A vector of left borders of censored measurements

<code>cright</code>	A vector of right borders of censored measurements
<code>tleft</code>	A vector of left truncations
<code>tright</code>	A vector of right truncations
<code>tol</code>	Tolerance for checking if <code>cleft &lt; cright</code>
<code>bounds</code>	Range of possible values for integers
<code>...</code>	other arguments, ignored except for <code>tleft</code> and <code>tright</code> to <code>R.ordered</code> and <code>R.integer</code>

### Details

R is basically an extension of [Surv](#) for the representation of arbitrarily censored or truncated measurements at any scale.

R applied to a list calls R for each of the list elements and returns a joint object.

### Examples

```
### ordered factor
R(gl(3, 3, labels = LETTERS[1:3]))
```

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