

# Package ‘mixEMM’

June 8, 2017

**Title** A Mixed-Effects Model for Analyzing Cluster-Level Non-Ignorable Missing Data

**Version** 1.0

**Date** 2017-06-06

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**Description** Contains functions for estimating a mixed-effects model for clustered data (or batch-processed data) with cluster-level (or batch-level) missing values in the outcome, i.e., the outcomes of some clusters are either all observed or missing altogether. The model is developed for analyzing incomplete data from labeling-based quantitative proteomics experiments but is not limited to this type of data. We used an expectation conditional maximization (ECM) algorithm for model estimation. The cluster-level missingness may depend on the average value of the outcome in the cluster (missing not at random).

**License** GPL

**RoxygenNote** 6.0.1

**NeedsCompilation** no

**Repository** CRAN

**Date/Publication** 2017-06-08 15:21:36 UTC

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mixEMM	<i>A mixed-effects model for analyzing cluster-level non-ignorable missing data</i>
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### Description

This function fits a mixed-effects model for clustered data with cluster-level missing values in the outcome.

### Usage

```
mixEMM(Ym, Xm, Zm, gamma, maxIter = 100, tol = 0.001)
```

### Arguments

Ym	is an N by p outcome data from N clusters/batches/experiments; p is the number of samples within each cluster. The first sample within each cluster is assumed to be a reference sample with different error variance. Missing values are coded as NAs.
Xm	is a covariate array of dimension N by k by p, where k is the number of covariates.
Zm	is a design array for random-effects, with a dimension of N by h by p, where h is the number of variables with random effects.
gamma	is the parameter for the missing-data mechanism. The missingness of the outcome in cluster i depends on the mean of the outcome. The missing probability is modelled as $\exp(-\text{gamma}0 - \text{gamma} \cdot \text{mean}(y))$ . The parameter gamma can be estimated by borrowing information across outcomes and finding the common missing-data patterns in the high-dimensional data. For example, by estimating the relationship the observed average value of $\bar{y}_i$ and the missing rate, or the parameter can be selected by the log-likelihood profile (see the Reference). If $\text{gamma} = 0$ , the missingness is ignorable. The parameter gamma0 does not affect the estimation of the EM algorithm, and is mostly determined by the missing rate. So it is set as 0 in the estimation here.
maxIter	the maximum number of iterations in the estimation of the EM algorithm.
tol	the tolerance level for the absolute change in the observed-data log-likelihood function.

### Details

The model consists of two parts, the outcome model and the missing-data model. The outcome model is a mixed-effects model,

$$\mathbf{y}_i = \mathbf{X}_i \boldsymbol{\alpha} + \mathbf{Z}_i \mathbf{b}_i + \mathbf{e}_i,$$

where  $\mathbf{y}_i$  is the outcome for the i-th cluster,  $\mathbf{X}_i$  is the covariate matrix,  $\boldsymbol{\alpha}$  is the fixed-effects,  $\mathbf{Z}_i$  is the design matrix for the random-effects  $\mathbf{b}_i$ , and  $\mathbf{e}_i$  is the error term.

The non-ignorable batch-level (or cluster-level) abundance-dependent missing-data model (BADMM) can be written as

$$\Pr(M_i = 1 | \mathbf{y}_i) = \exp(-\gamma_0 - \gamma \bar{y}_i),$$

where  $M_i$  is the missing indicator for the  $i$ -th cluster, and  $\bar{y}_i$  is the average of  $\mathbf{y}_i$ . If  $M_i = 1$ , the outcome of the  $i$ -th cluster  $\mathbf{y}_i$  would be missing altogether. The estimation of the mixEMM model is implemented via an ECM algorithm. If  $\gamma \neq 0$ , i.e., the missingness depends on the outcome, the missing-data mechanism is missing not at random (MNAR), otherwise it is missing completely at random (MCAR) for the current model. The parameter  $\gamma$  can be estimated by borrowing information across outcomes and finding the common missing-data patterns in the high-dimensional data. For example, by estimating the relationship the observed average value of  $\bar{y}_i$  and the missing rate, or the parameter can be selected by the log-likelihood profile (see the Reference).

### Value

A list containing

alpha.hat	the estimated fixed-effects.
alpha.se	the standard errors for the estimated fixed-effects.
sigma0.hat, sigma2.hat	the estimated sample error variances. It returns the variances for the first (reference) sample and the other samples within each cluster/batch.
D	the estimated covariance matrix for the random-effects.
RE	the estimated random-effects.
loglikelihood	the observed-data log-likelihood values.

### References

Chen, L. S., Wang, J., Wang, X., & Wang, P. (2017). A mixed-effects model for incomplete data from labeling-based quantitative proteomics experiments. *The Annals of Applied Statistics*, 11(1), 114-138. doi: [10.1214/16AOAS994](https://doi.org/10.1214/16AOAS994)

### Examples

```
data(sim_dat)

Z = sim_dat$X[, 1, , drop = FALSE]
fit0 = mixEMM(Ym = sim_dat$Ym, Xm = sim_dat$X, Zm = Z, gamma = 0.14)
```

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sim\_dat

*An example data set*

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### Description

This simulated data list is for demonstration.

**Value**

A list containing

- |       |   |
|-------|---|
| $Y_m$ | A $N$ by $p$ outcome data from $N$ clusters/batches/experiments; and $p$ is the number of samples within each cluster. The first sample within each cluster is a reference sample with a different error variance than other samples. Missing values are coded as NAs. Note the model allows unbalanced data. |
| $X$   | A covariate array of dimension of $N$ by $k$ by $p$ , where $k$ is the number of covariates.  |

**Examples**

```
data(sim_dat)
```

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