# Package 'lasso2' 

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while imposing an L1 constraint on the estimates, based on the algorithm of Osborne et al. (1998).
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aux

## Description

Generic function for extracting auxiliary information from fitted model objects.

## Usage

aux(object, ...)

## Arguments

object fitted model object (here typically of class l1celist, see aux.l1celist).
.. potentilly further arguments passed to methods.

## Details

See documentation (technical reports).

## Value

a matrix with the bound(s) (relative [if used] and absolute) and the Lagrangian(s) for the fitted model(s).

```
aux.l1celist Use 'aux()' on a 'llcelist' object
```


## Description

This is a method for the function aux () for objects inheriting from class l1celist. See aux for the general behavior of this function and for the interpretation of object.

```
Usage
    ## S3 method for class 'l1celist'
    aux(object, ...)
```


## Arguments

object fitted model object (here typically of class 11celist).
... potentially further arguments passed to methods.

```
coef.l1ce Coefficients of an 'llce' Object
```


## Description

This is a method for coef() for objects inheriting from class l1ce. See coef for the general behavior of this function and for the interpretation of object.

## Usage

\#\# S3 method for class 'l1ce'
coef(object, all=TRUE, constrained=FALSE, ...)

## Arguments

object an object of class l1ce, see help on l1ce. object.
all logical; if false, then only the non-zero coefficients are returned.
constrained logical; if true, then only the coefficients that were constrained are returned.
.. possibly further arguments (none at the moment).

```
coef.l1celist Coefficients of an 'llcelist' Object
```


## Description

This is a method for coef() for objects inheriting from class 11 celist. See coef for the general behavior of this function and for the interpretation of object.

```
Usage
    ## S3 method for class 'l1celist'
    coef(object, all=TRUE, constrained=FALSE, ...)
```


## Arguments

object an object of class l1celist, see help on 11celist. object.
all logical; if false, then the coefficients that are zero in all fitted models of the list are not returned.
constrained logical; if true, then only the coefficients that were constrained are returned.
... possibly further arguments (none at the moment).
deviance.gl1ce Deviance Method for 'gllce' Objects

## Description

This is a method of the generic function deviance() for objects inheriting from class gl1ce (see help(gl1ce.object)).

## Usage

\#\# S3 method for class 'gl1ce'
deviance(object, ...)

## Arguments

object an object inheriting from class gl1ce.
... possibly further arguments (none at the moment).

## See Also

deviance for the general behavior of this function and for the interpretation of object.

```
deviance.l1ce Deviance Method for 'llce' and 'llcelist' Objects
```


## Description

These are methods of the generic function deviance() for objects inheriting from class 11ce or l1celist (see help(l1ce.object) and help(l1celist.object)).

## Usage

\#\# S3 method for class 'l1ce'
deviance(object, ...)
\#\# S3 method for class 'l1celist'
deviance(object, ...)

## Arguments

object an object inheriting from class l1ce or l1celist, respectively.
.. possibly further arguments (none at the moment).

## See Also

deviance for the general behavior of this function and for the interpretation of object.

```
Extract.l1celist Extract Parts of a 'llcelist' Object
```


## Description

Allows the user to extract values from a l1celist object by using subscripts.

## Usage

\#\# S3 method for class 'l1celist'
$x[\ldots$, drop $=$ TRUE $]$
\#\# S3 method for class 'l1celist'
$x[[\ldots$, drop $=$ TRUE $]$ ]

## Arguments

$x \quad$ an object inheriting from class "l1celist".
... a specification of indices - see Extract.
drop logical defaulting to TRUE. If only one model is subscribed, then it is returned as an object of class "l1ce". If drop=F, then an object of class "l1celist" is always returned.

## Value

an object of class "l1celist" or class "l1ce" extracted from the original list.

Fitted Values for 'llce', 'llcelist' and 'gllce' Objects

## Description

These are methods of the generic function fitted() for objects inheriting from class 11ce or l1celist (see help(l1ce.object) and help(l1celist.object)).

## Usage

\#\# S3 method for class 'l1ce'
fitted(object, ...)
\#\# S3 method for class 'l1celist'
fitted(object, ...)

## Arguments

object an object inheriting from class l1ce or l1celist, e.g., an gl1ce one (see gl1ce.object).
... further potential arguments passed to methods.

## See Also

fitted for the general behavior of this function and for the interpretation of object.

```
gcv
```

Generalised Cross-Validation Score

## Description

Extracts the generalised cross-validation score(s) from fitted model objects.

## Usage

gcv(object, ...)

## Arguments

object fitted model object; see gcv methods for details.
... arguments passed to methods.

## Details

See documentation.

## Value

A vector (or matrix) with the bound(s) (relative [if used] and absolute), the Lagrangian(s) and the generalised cross-validation score(s) for the fitted model(s).

```
gcv.l1ce 'gcv()'Methods for 'llce' and 'llcelist' Objects.
```


## Description

This is a method for the function $\operatorname{gcv}()$ for objects inheriting from class 11 ce or 11 celist.

## Usage

```
## S3 method for class 'l1ce'
gcv(object, type = c("OPT", "Tibshirani"),
    gen.inverse.diag = 0, ...)
## S3 method for class 'l1celist'
gcv(object, type = c("OPT", "Tibshirani"),
    gen.inverse.diag = 0, ...)
```


## Arguments

object an object of class l1ce or l1celist.
type character (string) indicating whether to use the covariance formula of Osborne, Presnell and Turlach or the formula of Tibshirani.
gen.inverse.diag
if Tibshirani's formula for the covariance matrix is used, this value is used for the diagonal elements of the generalised inverse that appears in the formula that corresponds to parameters estimated to be zero. The default is 0 , i.e. use the Moore-Penrose inverse. Tibshirani’s code uses gen.inverse.diag $=1 \mathrm{e} 11$.
... further potential arguments passed to methods.

## Details

See documentation.

## See Also

gcv for the general behavior of this function; l1ce. object and l1celist. object for description of the object argument.

## Description

Fit a generalized regression problem while imposing an L1 constraint on the parameters. Returns an object of class gl1ce.

## Usage

```
gl1ce(formula, data = sys.parent(), weights, subset, na.action,
            family = gaussian, control = glm.control(...), sweep.out = ~ 1,
            x = FALSE, y = TRUE, contrasts = NULL, standardize = TRUE,
            guess.constrained.coefficients = double(p), bound = 0.5, ...)
## S3 method for class 'gl1ce'
family(object, ...)
```


## Arguments

| formula | a formula, with the response on the left hand side of a $\sim$ operator, and the terms, <br> separated by a + operator, on the right hand side. |
| :--- | :--- |
| data | a data.frame in which to interpret the variables named in the formula, the <br> weights, the subset and the sweep. out argument. If this is missing, then the <br> variables in the formula should be globally available. <br> weights <br> vector of observation weights. The length of weights must be the same as <br> the number of observations. The weights must be strictly positive, since zero <br> weights are ambiguous, compared to use of the subset argument. <br> expression saying which subset of the rows of the data should be used in the fit. |
| nabset $\quad$This can be a logical vector (which is replicated to have length equal to the num- <br> ber of observations), or a numeric vector indicating which observation numbers <br> are to be included, or a character vector of the row names to be included. All <br> observations are included by default. |  |
| a function to be applied to the model.frame after any subset argument has been |  |
| used. The default (with na.fail) is to create an error if any missing values |  |
| are found. A possible alternative is na. omit, which deletes observations that |  |
| contain one or more missing values. |  |


| sweep.out | a formula object, variables whose parameters are not put under the constraint are swept out first. The variables should appear on the right of $\mathrm{a} \sim$ operator and be separated by + operators. Default is $\sim 1$, i.e. the constant term is not under the constraint. If this parameter is NULL, then all parameters are put under the constraint. |
| :---: | :---: |
| x | logical flag: if TRUE, the model matrix is returned in component $x$. |
| y | logical flag: if TRUE, the response is returned in component $y$ |
| contrasts | a list giving contrasts for some or all of the factors appearing in the model formula. The elements of the list should have the same name as the variable and should be either a contrast matrix (specifically, any full-rank matrix with as many rows as there are levels in the factor), or else a function to compute such a matrix given the number of levels. |
| standardize | logical flag: if TRUE, then the columns of the model matrix that correspond to parameters that are constrained are standardized to have empirical variance one. The standardization is done after taking possible weights into account and after sweeping out variables whose parameters are not constrained. |
| guess.constrained.coefficients |  |
|  | initial guess for the parameters that are constrained. |
| bound | numeric, either a single number or a vector: the constraint(s) that is/are put onto the L1 norm of the parameters. |
|  | potential arguments for glm.control, as default for the control argument above. |
| object | an R object of class "gl1ce". |

## Value

an object of class gl1ce is returned by gl1ce(). See gl1ce. object for details.

## References

See the references in l1ce.
Justin Lokhorst (1999). The LASSO and Generalised Linear Models, Honors Project, Nov.1999, Dept.Statist., Univ. of Adelaide. Available as file 'Doc/justin. lokhorst.ps.gz' in both shar files from http://www.maths.uwa.edu.au/~berwin/software/lasso.html.

## See Also

glm for unconstrained generalized regression modeling.

## Examples

```
## example from base:
data(esoph)
summary(esoph)
## effects of alcohol, tobacco and interaction, age-adjusted
modEso <- formula(cbind(ncases, ncontrols) ~ agegp + tobgp * alcgp)
glm.E <- glm(modEso, data = esoph, family = binomial())
```

```
gl1c.E <- gl1ce(modEso, data = esoph, family = binomial())
gl1c.E
plot(residuals(gl1c.E) ~ fitted(gl1c.E))
sg1c <- summary(gl1c.E)
sg1c
## Another comparison glm() / gl1c.E:
plot(predict(glm.E, type="link"), predict(glm.E, type="response"),
    xlim = c(-3,0))
points(predict(gl1c.E, type="link"), predict(gl1c.E, type="response"),
        col = 2, cex = 1.5)
labels(gl1c.E)#-- oops! empty!!
```

```
gl1ce.object Generalized Ll Constrained Estimation Model Object
```


## Description

These are objects of class gl1ce They represent the fit of a generalized regression model under an L1 constraint on (some of) the parameters.

## Details

The residuals, fitted values, coefficients, and effects should be extracted by the generic functions of the same name, rather than by the $\$$ operator.

## GENERATION

This class of objects is returned from the gl1ce function to represent a fitted model.

## METHODS

The gl1ce class of objects has methods for the following generic functions: deviance, predict, print, residuals, summary. Other generic functions are inherited from the class 11 ce.

## STRUCTURE

The following components must be included in a legitimate gl1ce object.
coefficients the coefficients of the fit of the response to the columns of the model matrix. The names of the coefficients are the names of the columns of the model matrix.
residuals the residuals from the fit. If weights were used, then the residuals are the raw residuals the weights are not taken into account. If you need residuals that all have the same variance, then use the residuals function with type="pearson".
fitted.values the fitted values from the fit. If weights were used, the fitted values are not adjusted for the weights.
family the family of which the fitted regression model belongs, eg., binomial(link=probit).
bound the (absolute) L1 constraint imposed on the parameters.
Lagrangian the value of the Lagrangian that enforces the constraint at the solution.
$\mathbf{x t x}$ the moment matrix of the variables that are under the constraint. (After taking weights, sweepout variables and standardization into account).
$\mathbf{x t r}$ the product of the design matrix of the variables that are under the constraint (after taking weights, sweep-out variables and standardization into account) with the residual vector.
constrained.coefficients the coefficients on the scale on which they are constrained. Useful as initial value for further fits.
sweep.out information on the variables that are not under the constraint and on which the other variables and the response is projected first. Optional, not present if sweep. out $=$ NULL.
assign the list of assignments of coefficients (and effects) to the terms in the model. The names of this list are the names of the terms. The ith element of the list is the vector saying which coefficients correspond to the $i$ th term. It may be of length 0 if there were no estimable effects for the term. See also R. assign below.
terms an object of mode expression and class term summarizing the formula. Used by various methods, but typically not of direct relevance to users.
call an image of the call that produced the object, but with the arguments all named and with the actual formula included as the formula argument.
contrasts a list containing sufficient information to construct the contrasts used to fit any factors occurring in the model. The list contains entries that are either matrices or character vectors. When a factor is coded by contrasts, the corresponding contrast matrix is stored in this list. Factors that appear only as dummy variables and variables in the model that are matrices correspond to character vectors in the list. The character vector has the level names for a factor or the column labels for a matrix.
$\mathbf{x}$ optionally the model matrix, if $\mathrm{x}=\mathrm{T}$.
$\mathbf{y}$ optionally the response, if $\mathrm{y}=\mathrm{T}$.

## See Also

gl1ce, coefficients.

Iowa The Iowa Wheat Yield Data

## Description

The data gives the pre-season and three growing months' precipitation, the mean temperatures for the three growing months and harvest month, the year, and the yield of wheat for the USA state of Iowa, for the years 1930-1962.

## Usage

data(Iowa)

## Format

The data frame has the following components:
Year Year of measurement (surrogate for variety improvements)
Rain0 Pre-season rainfall (in.)
Temp1 Mean temperature for the first growing month (deg. F)
Rain1 Rainfall for the first growing month (in.)
Temp2 Mean temperature for the second growing month (deg. F)
Rain2 Rainfall for the second growing month (in.)
Temp3 Mean temperature for the third growing month (deg. F)
Rain3 Rainfall for the third growing month (in.)
Temp4 Mean temperature for the harvest month (deg. F)
Yield Yield of wheat in Iowa for the given year (bush./acre)

## CATEGORY

Multiple regression; diagnostics.

## Source

CAED Report, 1964. Quoted in Draper and Smith, Applied Regression Analysis.

## Examples

data(Iowa)
pairs(Iowa)
is.formula Tests for Formula Objects

## Description

is. formula returns TRUE if $x$ is an object of class "formula", and FALSE otherwise.

## Usage

is.formula(x)

## Arguments

11ce Regression Fitting With L1-constraint on the Parameters

## Description

Returns an object of class "l1ce" or "licelist" that represents fit(s) of linear models while imposing L1 constraint(s) on the parameters.

## Usage

11ce(formula, data = sys.parent(), weights, subset, na.action, sweep. out $=\sim 1, x=$ FALSE, $y=$ FALSE, contrasts $=$ NULL, standardize $=$ TRUE, trace = FALSE, guess.constrained.coefficients = double(p), bound $=0.5$, absolute.t $=$ FALSE)

## Arguments

formula a formula object, with the response on the left of a $\sim$ operator, and the terms, separated by + operators, on the right.
data a data.frame in which to interpret the variables named in the formula, the weights, the subset and the sweep. out argument. If this is missing, then the variables in the formula should be globally available.
weights vector of observation weights. The length of weights must be the same as the number of observations. The weights must be nonnegative and it is strongly recommended that they be strictly positive, since zero weights are ambiguous, compared to use of the subset argument.
subset expression saying which subset of the rows of the data should be used in the fit. This can be a logical vector (which is replicated to have length equal to the number of observations), or a numeric vector indicating which observation numbers are to be included, or a character vector of the row names to be included. All observations are included by default.
na.action a function to filter missing data. This is applied to the model.frame after any subset argument has been used. The default (with na.fail) is to create an error if any missing values are found. A possible alternative is na.omit, which deletes observations that contain one or more missing values.
sweep.out a formula object, variables whose parameters are not put under the constraint are swept out first. The variables should appear on the right of a $\sim$ operator and be separated by + operators. Default is $\sim 1$, i.e. the constant term is not under the constraint. If this parameter is NULL, then all parameters are put under the constraint.
x
$y \quad$ logical indicating if the response should be returned in component $y$.

```
contrasts a list giving contrasts for some or all of the factors appearing in the model
            formula. The elements of the list should have the same name as the variable
            and should be either a contrast matrix (specifically, any full-rank matrix with as
                    many rows as there are levels in the factor), or else a function to compute such
                    a matrix given the number of levels.
standardize logical flag: if TRUE, then the columns of the model matrix that correspond to
            parameters that are constrained are standardized to have emprical variance one.
                        The standardization is done after taking possible weights into account and after
                        sweeping out variables whose parameters are not constrained; see vignette for
                details.
trace logical flag: if TRUE, then the status during each iteration of the fitting is re- ported.
guess.constrained.coefficients initial guess for the parameters that are constrained.
bound numeric, either a single number or a vector: the constraint(s) that is/are put onto the L1 norm of the parameters.
absolute.t logical flag: if TRUE, then bound is an absolute bound and all entries in bound can be any positive number. If FALSE, then bound is a relative bound and all entries must be between 0 and 1 ; see vignette for details.
```


## Value

an object of class l1ce (if bound was a single value) or l1celist (if bound was a vector of values) is returned. See 11ce. object and l1celist. object for details.

## References

Osborne, M.R., Presnell, B. and Turlach, B.A. (2000) On the LASSO and its Dual, Journal of Computational and Graphical Statistics 9(2), 319-337.
Tibshirani, R. (1996) Regression shrinkage and selection via the lasso, Journal of the Royal Statistical Society, Series B 58(1), 267-288.

## Examples

```
data(Iowa)
l1c.I <- l1ce(Yield ~ ., Iowa, bound = 10, absolute.t=TRUE)
11c.I
## The same, printing information in each step:
l1ce(Yield ~ ., Iowa, bound = 10, trace = TRUE, absolute.t=TRUE)
data(Prostate)
l1c.P <- l1ce(lpsa ~ ., Prostate, bound=(1:30)/30)
length(l1c.P)# 30 l1ce models
l1c.P # -- MM: too large; should do this in summary(.)!
plot(resid(l1c.I) ~ fitted(l1c.I))
```

```
abline(h = 0, lty = 3, lwd = .2)
```

11ce.object Ll Constrainted Estimation Model Object

## Description

These are objects of class "l1ce". They represent the fit of a regression model under an L1 constraint on (some of) the parameters.

## Details

The residuals, fitted values, coefficients, and effects should be extracted by the generic functions of the same name, rather than by the $\$$ operator.

## GENERATION

This class of objects is returned from the 11 ce function to represent a fitted model.

## METHODS

The "l1ce" class of objects has methods for the following generic functions: coef, deviance, fitted, formula, gcv, labels, predict, print, residuals, summary, vcov.

## STRUCTURE

The following components must be included in a legitimate l1ce object.
coefficients the coefficients of the fit of the response to the columns of the model matrix. The names of the coefficients are the names of the columns of the model matrix.
residuals the residuals from the fit. If weights were used, then the residuals are the raw residuals the weights are not taken into account. If you need residuals that all have the same variance, then use the residuals function with type="pearson".
fitted.values the fitted values from the fit. If weights were used, the fitted values are not adjusted for the weights.
bound the (absolute) L1 constraint imposed on the parameters.
relative.bound optional, the (relative) L 1 constraint imposed on the parameters. Present if absolute. $\mathrm{t}=\mathrm{F}$.
Lagrangian the value of the Lagrangian that enforces the constraint at the solution.
$\mathbf{x t x}$ the moment matrix of the variables that are under the constraint. (After taking weights, sweepout variables and standardization into account).
$\mathbf{x t r}$ the product of the design matrix of the variables that are under the constraint (after taking weights, sweep-out variables and standardization into account) with the residual vector.
constrained.coefficients the coefficients on the scale on which they are constrained. Useful as initial value for further fits.
sweep.out Optional information on the variables that are not under the constraint and on which the other variables and the response is projected first. Optional, not present if sweep. out = NULL.
assign the list of assignments of coefficients (and effects) to the terms in the model. The names of this list are the names of the terms. The ith element of the list is the vector saying which coefficients correspond to the $i$ th term. It may be of length 0 if there were no estimable effects for the term. See also R. assign below.
terms an object of mode expression and class term summarizing the formula. Used by various methods, but typically not of direct relevance to users.
call an image of the call that produced the object, but with the arguments all named and with the actual formula included as the formula argument.
contrasts a list containing sufficient information to construct the contrasts used to fit any factors occurring in the model. The list contains entries that are either matrices or character vectors. When a factor is coded by contrasts, the corresponding contrast matrix is stored in this list. Factors that appear only as dummy variables and variables in the model that are matrices correspond to character vectors in the list. The character vector has the level names for a factor or the column labels for a matrix.
$\mathbf{x}$ optionally the model matrix, if $x=T R U E$.
$\mathbf{y}$ optionally the response, if $\mathrm{y}=$ TRUE.

## See Also

l1ce, coefficients.
l1celist.object Object of Several L1 Constrained Estimation Models

## Description

These are objects of class "l1celist" They represent the fits of several regression models under an L1 constraint on (some of the parameters).

## Details

The residuals, fitted values, coefficients, and effects should be extracted by the generic functions of the same name, rather than by using the [[]] and the $\$$ operator.

## GENERATION

This class of objects is returned from the 11 ce function to represent a fitted model.

## METHODS

The "l1celist" class of objects has methods for the following generic functions: [, [[, aux, coef, deviance, fitted, formula, gcv, labels, plot, print, residuals, vcov.

## STRUCTURE

An object of class l1celist is a list of lists. Each component of the list is a list with the information of an object of class l1ce that is unique for that information. All shared information is stored as attributes.
Each component of the list must include the following components for it to be a legitimate 11 celist object.
coefficients the coefficients of the fit of the response to the columns of the model matrix. The names of the coefficients are the names of the columns of the model matrix.
residuals the residuals from the fit. If weights were used, then the residuals are the raw residuals the weights are not taken into account. If you need residuals that all have the same variance, then use the residuals function with type="pearson".
fitted.values the fitted values from the fit. If weights were used, the fitted values are not adjusted for the weights.
bound the (absolute) L1 constraint imposed on the parameters.
relative.bound optional, the (relative) L1 constraint imposed on the parameters. Present if absolute. $\mathrm{t}=\mathrm{F}$.
Lagrangian the value of the Lagrangian that enforces the constraint at the solution.
xtr the product of the design matrix of the variables that are under the constraint (after taking weights, sweep-out variables and standardization into account) with the residual vector.
constrained.coefficients the coefficients on the scale on which they are constrained. Useful as initial value for further fits.

## See Also

l1ce, coefficients.
labels.l1ce 'Labels' Method for 'llce' and 'llcelist' Objects

## Description

This is a method for the labels() function for objects inheriting from class l1ce or l1celist (see help(l1ce.object) and help(l1celist.object)). See labels or labels.default for the general behavior of this function and for the interpretation of object.

## Usage

\#\# S3 method for class 'l1ce'
labels(object, ...)
\#\# S3 method for class 'l1celist'
labels(object, ...)

## Arguments

object fitted model of class "l1ce" or "l1celist", respectively.
.. potentially further arguments passed to method.
merge. formula Merge Formula With Right Hand Side of Second Formula

## Description

This is method for formulas of the merge generic function. Here it is support for the function 11ce and not intended to be called directly by users.

```
Usage
\#\# S3 method for class 'formula'
merge (x, y, ...)
```


## Arguments

$\mathrm{x}, \mathrm{y} \quad$ formulas.
... potentially further arguments passed to methods.

## Examples

```
merge(y ~ x1, ~ x2) ## -> y ~ x1 + x2
f2 <- merge(y ~ x1*x2, z ~ (x2+x4)^3)
f. <- merge(y ~ x1*x2, ~ (x2+x4)^3) # no LHS for 2nd term
f2
stopifnot(f2 == f.)
```

    plot.11celist Plot Method for 'llcelist' Objects
    
## Description

Plots a l1celist object on the current graphics device.

```
Usage
\#\# S3 method for class 'l1celist'
plot( \(x\), plot=TRUE, all=TRUE, constrained=FALSE,
type = "b", xlab = "bounds", ylab = "coeff | bounds", ...)
```


## Arguments

$x \quad$ fitted model object of class 11 celist.
plot logical; if TRUE a matplot() of all the coefficients in the list against the relative bound (absolute bound if relative is not present) is plotted. Otherwise no plot is done.
all logical; if FALSE, then only the non-zero coefficients are returned.
constrained if TRUE then only the coefficients that were constrained are returned.
type, xlab, ylab, ...
further arguments with useful defaults passed to matplot.

## Value

A matrix with the bound(s) (relative [if used] and absolute), the Lagrangian(s) and coefficints of the fitted model(s).

## Examples

```
data(Prostate)
l1c.P <- l1ce(lpsa ~ ., Prostate, bound=(1:20)/20)
length(l1c.P)# 20 l1ce models
plot(l1c.P)
```

predict.gl1ce Prediction Method for a 'gllce' Object

## Description

This is a method for the generic function predict for class "gl1ce", typically produced from gl1ce(). When newdata is missing, the fitted values are extracted, otherwise returns new predictions.

## Usage

\#\# S3 method for class 'gl1ce'
predict(object, newdata, type=c("link", "response"),
se.fit = FALSE, ...)

## Arguments

object a fitted gl1ce object.
newdata a data frame containing the values at which predictions are required. This argument can be missing, in which case predictions are made at the same values used to compute the object. Only those predictors referred to in the right side of the formula in object need be present by name in newdata.

| type | type of predictions, with choices "link" (the default), or "response". The default <br> produces predictions on the scale of the additive predictors, and with newdata <br> missing, predict() is simply an extractor function for this component of a <br> gl1ce object. If "response" is selected, the predictions are on the scale of the <br> response, and are monotone transformations of the additive predictors, using the <br> inverse link function. |
| :--- | :--- |
| se.fit | logical indicating if standard errors should be returned as well. Not yet avail- <br> able. |
| $\ldots$ | further potential arguments passed to methods. |

## Value

a vector of predictions.

## Warning

predict can produce incorrect predictions when the newdata argument is used if the formula in object involves data-dependent transformations, such as poly (Age, 3)
or sqrt(Age - min(Age)).

## Examples

```
## start with
example(gl1ce)
predict(gl1c.E, new = esoph[1:7,])# type 'link'
predict(gl1c.E, new = esoph[1:7,], type = "response")
## identities / consistency checks :
stopifnot(predict(gl1c.E, type = "response") == fitted(gl1c.E),
            all.equal(predict(gl1c.E)[1:7],
                as.vector(predict(gl1c.E, new = esoph[1:7,]))),
            all.equal(fitted(gl1c.E)[1:7],
                as.vector(predict(gl1c.E, new = esoph[1:7,], type = "response")))
            )
```

```
predict.l1ce Predict Method for 'llce' Objects
```


## Description

This is a method for the generic function predict for class "l1ce", typically produced from l1ce(). When newdata is missing, the fitted values are extracted, otherwise returns new predictions.

## Usage

\#\# S3 method for class 'l1ce'
predict(object, newdata, type $=c($ "response"), se.fit $=$ FALSE, ...)

## Arguments

object a fitted l1ce object.
newdata a data frame containing the values at which predictions are required. This argument can be missing, in which case predictions are made at the same values used to compute the object. Only those predictors referred to in the right side of the formula in object need be present by name in newdata.
type currrently only "response".
se.fit logical indicating if standard errors should be returned as well. Not yet available.
... further potential arguments passed to methods.

## Value

a vector of predictions.

## Warning

predict can produce incorrect predictions when the newdata argument is used if the formula in object involves transformations, such as poly (Age, 3) or sqrt(Age - min(Age)).
MM: Not sure this is true for R ....

## Examples

```
data(Iowa)
l1c.I <- l1ce(Yield ~ ., Iowa, bound = 10, absolute.t=TRUE)
p10 <- predict(l1c.I, newdata = Iowa[10:19,])
stopifnot(all.equal(p10, fitted(l1c.I)[10:19]))
```

```
print.l1ce Print Methods for 'llce', 'llcelist' and 'gllce' Objects
```


## Description

These are methods of the generic print() function for objects inheriting from class $11 \mathrm{ce}, 11 \mathrm{cel}$ ist or gl1ce (see help(l1ce.object), help(l1celist.object) or help(gl1ce.object)). See print or print. default for the general behavior of this function.

## Usage

```
## S3 method for class 'l1ce'
print(x, ...)
## S3 method for class 'l1celist'
print(x, ...)
## S3 method for class 'gl1ce'
print(x, ...)
```


## Arguments

fitted model of class " 11 ce" or "l1celist", respectively.
... potentially further arguments passed to method.
Prostate Prostate Cancer Data

## Description

These data come from a study that examined the correlation between the level of prostate specific antigen and a number of clinical measures in men who were about to receive a radical prostatectomy. It is data frame with 97 rows and 9 columns.

## Usage

data(Prostate)

## Format

The data frame has the following components:
lcavol $\log$ (cancer volume)
lweight $\log$ (prostate weight)
age age
lbph $\log$ (benign prostatic hyperplasia amount)
svi seminal vesicle invasion
$\operatorname{lcp} \log$ (capsular penetration)
gleason Gleason score
pgg45 percentage Gleason scores 4 or 5
lpsa $\log$ (prostate specific antigen)

## Source

Stamey, T.A., Kabalin, J.N., McNeal, J.E., Johnstone, I.M., Freiha, F., Redwine, E.A. and Yang, N. (1989)

Prostate specific antigen in the diagnosis and treatment of adenocarcinoma of the prostate: II. radical prostatectomy treated patients, Journal of Urology 141(5), 1076-1083.

## Examples

```
data(Prostate)
attach(Prostate)
pairs(Prostate, col = 1+svi, pch = gleason - 5,
    main = paste("Prostate data, n = ", nrow(Prostate)))
detach()
l1c.P <- l1ce(lcavol ~ ., data = Prostate)
coef(l1c.P)[coef(l1c.P) != 0] ## only age, lcp, lpsa (+ intercept)
summary(l1c.P)
```

qr.rtr.inv
Reconstruct the Inverse of $R$ ' $R$ from a $Q R$ Object

## Description

From a QR object, compute the inverse matrix which is implicitely (but not explicitly!) used to solve the underlying least squares problem.

## Usage

qr.rtr.inv(qr)

## Arguments

qr
\"qr\" object, typically resulting from qr(.).

## Value

The $p \times p$ matrix $\left(R^{\prime} R\right)^{-1}$ or equivalently, the inverse of $X^{\prime} X$ (i.e. $t(X) \% * \% \mathrm{X}$ in R ).

## See Also

qr, qr.R, backsolve.

## Examples

```
(h3 <- 1/outer(0:5, 1:3, "+"))
rtr <- qr.rtr.inv(qr(h3))
all.equal(c(rtr %*% 1:3), solve(crossprod(h3), 1:3))
```


## Description

Computes one of the four types of residuals available for gl1ce objects. This is a method for the function residuals() for objects inheriting from class gl1ce. As several types of residuals are available for gl1ce objects, there is an additional optional argument type.

## Usage

```
    ## S3 method for class 'gl1ce'
    residuals(object,
        type=c("deviance", "pearson", "working", "response"), ...)
```


## Arguments

object an object inheriting from class gl1ce representing a fitted model.
type type of residuals, with choices "deviance", "pearson", "working" or "response"; the first is the default.
$\ldots \quad$ possibly further arguments (none at the moment).

## Value

A numeric vector of residuals. See Statistical Models in $S$ for detailed definitions of each type of residual. The sum of squared deviance residuals add up to the deviance. The pearson residuals are standardized residuals on the scale of the response. The working residuals reside on the object, and are the residuals from the final fit. The response residuals are simply y - fitted(object). The summary () method for gl1ce objects produces deviance residuals. The residuals component of a gl1ce object contains the working residuals.

## References

Chambers, J.M., and Hastie, T.J. (1991). Statistical Models in S, pp. 204-206.

## See Also

gl1ce for examples; fitted.l1ce is used for fitted values.

```
residuals.l1ce Residuals of 'llce' or 'llcelist' Objects
```


## Description

This is a method for the function residuals for objects inheriting from class l1ce or l1celist (see help(l1ce.object) and help(l1celist.object)). See residuals for the general behavior of this function and for the interpretation of object and type.

## Usage

\#\# S3 method for class 'l1ce'
residuals(object, type, ...)
\#\# S3 method for class 'l1celist'
residuals(object, type, ...)

## Arguments

object an object inheriting from class 11 ce representing a fitted model.
type type of residuals, with choices "deviance", "pearson", "working" or "response"; the first is the default.
... possibly further arguments (none at the moment).

## Description

Returns (and prints) a summary list for fitted generalized L1 constrained regression models.

## Usage

```
## S3 method for class 'gl1ce'
summary(object, dispersion = NULL, correlation = FALSE, ...)
## S3 method for class 'summary.gl1ce'
print(x, digits = max(3, getOption("digits") - 3), ...)
```


## Arguments

object fitted gl1ce model object. This is assumed to be the result of some fit that produces an object inheriting from the class gl1ce, in the sense that the components returned by the gl1ce() function will be available.
dispersion prescribed dispersion, see summary.glm.
correlation logical indicating if the correlation matrix should be returned as well.
$x \quad$ object of class summary.gl1ce.
digits, ... further arguments for the print method.

## Details

This function is a method for the generic function summary for class gl1ce. It can be invoked by calling summary for an object of the appropriate class, or directly by calling summary.gl1ce regardless of the class of the object.

## Value

an object of class summary.gl1ce (for which there's a print method). It is basically a list with the following components:

| call | as contained on object |
| :--- | :--- |
| residuals | the deviance residuals, as produced by residuals(object, type = "deviance"). |
| coefficients | the coefficients of the model. |
| family | the family of models to which object belongs, along with the variance and link <br> functions for that model. |
| bound | the bound used in fitting this model |
| Lagrangian | the Lagrangian of the model |

## Description

Returns a summary list for a regression model with an L1 constraint on the parameters. A null value will be returned if printing is invoked.

## Usage

```
## S3 method for class 'l1ce'
summary(object, correlation = TRUE,
            type = c("OPT", "Tibshirani"),
            gen.inverse.diag = 0, sigma = NULL, ...)
## S3 method for class 'summary.l1ce'
print(x, digits = max(3, getOption("digits") - 3), ...)
```


## Arguments

object fitted model of class "l1ce".
correlation logical indicating if the correlation matrix for the coefficients should be included in the summary.
type character string specifying whether to use the covariance formula of Osborne, Presnell and Turlach or the formula of Tibshirani.

```
gen.inverse.diag
    if Tibshirani's formula for the covariance matrix is used, this value is used for
    the diagonal elements of the generalised inverse that appears in the formula that
    corresponds to parameters estimated to be zero. The default is 0, i.e. use the
    Moore-Penrose inverse. Tibshirani's code uses gen.inverse.diag=1e11.
sigma the residual standard error estimate. If not provided, then it is estimated by the
    deviance of the model divided by the error degrees of freedom.
x an R object of class summary.l1ce.
digits number of significant digits to use.
... further potential arguments passed to methods.
```


## Details

This function is a method for the generic function summary () for class "l1ce". It can be invoked by calling summary $(x)$ for an object $x$ of the appropriate class, or directly by calling summary. $11 \mathrm{ce}(x)$ regardless of the class of the object.

## Value

an object of class summary.l1ce (for which there's a print method). It is basically a list with the following components:

```
correlation the computed correlation coefficient matrix for the coefficients in the model.
cov.unscaled the unscaled covariance matrix; i.e, a matrix such that multiplying it by an es-
    timate of the error variance produces an estimated covariance matrix for the
    coefficients.
df the number of degrees of freedom for the model and for residuals.
coefficients a matrix with three columns, containing the coefficients, their standard errors
    and the corresponding t statistic.
residuals the model residuals. These are the weighted residuals if weights were given in
    the model.
sigma the residual standard error estimate.
terms the terms object used in fitting this model.
call the call object used in fitting this model.
bound the bound used in fitting this model.
relative.bound the relative bound used in fitting this model (may not be present).
Lagrangian the Lagrangian of the model.
```


## See Also

l1ce, 11ce. object, summary.

## Examples

```
data(Prostate)
summary(l1ce(lpsa ~ .,Prostate))
# Produces the following output:
## Not run:
Call:
    l1ce(formula = lpsa ~ ., data = Prostate)
Residuals:
        Min 1Q Median 3Q Max
    -1.636 -0.4119 0.076 0.452 1.83
Coefficients:
            Value Std. Error Z score Pr(>|Z|)
(Intercept) 0.7285 1.3898 0.5242 0.6002
    lcavol 0.4937 0.0919 5.3711 0.0000
    lweight 0.2682 0.1774 1.5115 0.1307
            age 0.0000 0.0111 0.0000 1.0000
            lbph 0.0093 0.0587 0.1581 0.8744
            svi 0.4551 0.2525 1.8023 0.0715
            lcp 0.0000 0.0947 0.0000 1.0000
        gleason 0.0000 0.1685 0.0000 1.0000
            pgg45 0.0002 0.0046 0.0391 0.9688
Residual standard error: 0.7595 on 88.36 degrees of freedom
The relative L1 bound was : 0.5
The absolute L1 bound was : 0.9219925
The Lagrangian for the bound is: 13.05806
Correlation of Coefficients:
            (Intercept) lcavol lweight age lbph svi lcp gleason
    lcavol 0.1988
lweight -0.4815 -0.2071
            age -0.3938 -0.0603-0.0974
            lbph 0.3629 -0.0201 -0.5165 -0.1303
            svi -0.0624
            lcp 0.0457
    gleason -0.7666 -0.2009 0.1163-0.0774 -0.0617 0.1084-0.0243
    pgg45 0.4988 0.0956 -0.0380-0.0630-0.1111-0.1921-0.2935-0.6526
## End(Not run)
```


## Description

Calculates the trace of a matrix

## Usage

tr (mat)

## Arguments

mat a square matrix.

## Value

The trace of the matrix, i.e. the sum of its diagonal elements, is returned.

## Examples

```
    tr(cbind(1,1:3,4:2)) # 5
```

    vcov.l1ce Variance-Covariance Matrix of 'llce' or 'llcelist' Objects
    
## Description

This is a method for the function $\operatorname{vcov}()$ for objects inheriting from class l1ce or l1celist (see help(l1ce.object) and help(l1celist.object)). See vcov for the general behavior of this function.

## Usage

```
## S3 method for class 'l1ce'
vcov(object, type = c("OPT", "Tibshirani"),
    gen.inverse.diag = 0, ...)
    ## S3 method for class 'l1celist'
    vcov(object, type = c("OPT", "Tibshirani"),
    gen.inverse.diag = 0, ...)
```


## Arguments

object an object of class l1ce or l1celist.
type character indicating whether to use the covariance formula of Osborne, Presnell and Turlach or the formula of Tibshirani.
gen.inverse.diag
if Tibshirani's formula for the covariance matrix is used, this value is used for the diagonal elements of the generalised inverse that appears in the formula that corresponds to parameters estimated to be zero. The default is 0 , i.e. use the Moore-Penrose inverse. Tibshirani's code uses gen. inverse.diag = 1e11.
... further potential arguments passed to methods.

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