

# Package ‘inference’

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**Type** Package

**Title** Methods for Causal Inference with Interference

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**Author** Bradley Saul

**Maintainer** Bradley Saul <bradleysaul@gmail.com>

**Description** Provides methods for estimating causal effects in the presence of interference described in B. Saul and M. Huggens (2017) <doi:10.18637/jss.v082.i02>. Currently it implements the inverse-probability weighted (IPW) estimators proposed by E.J. Tchetgen Tchetgen and T.J. Vanderweele (2012) <doi:10.1177/0962280210386779>.

**Depends** R (>= 3.1)

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**License** GPL (>= 2)

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diagnose_weights	<i>Plot histograms of weights from an interference object</i>
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## Description

Plot histograms of weights from an interference object

## Usage

```
diagnose_weights(obj, allocations = NULL, ...)
```

## Arguments

obj	an interference object
allocations	optional numeric vector of allocations for which to print histogram. If NULL (the default), five allocations selected evenly from the first allocation to the last are printed.
...	additional arguments passed to <a href="#">hist</a>

## Value

histogram of group-level weights

---

direct_effect	<i>Retrieve Direct Effect estimates</i>
---------------	---

---

**Description**

Retrieves the population average direct causal effect for a specified allocation:  $\hat{Y}(0, \alpha) - \hat{Y}(1, \alpha)$ .

**Usage**

```
direct_effect(object, allocation = NULL, trt.lv11 = 0)
```

**Arguments**

object	an object of class interference
allocation	the allocation scheme for which to estimate direct effects. If NULL, then returns all direct effects.
trt.lv11	Defaults to 0.

**Value**

a data.frame with requested values

---

get_args	<i>Get arguments from a function</i>
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**Description**

Extracts the names of the arguments from a function, and creates a list of those arguments where they exist in ... .

**Usage**

```
get_args(FUN, args_list = NULL, ...)
```

**Arguments**

FUN	function for which to find arguments
args_list	a list of arguments. Defaults to NULL.
...	any arguments. Those necessary for FUN must be named as appropriate for FUN

**Value**

list of arguments for FUN

**Examples**

```
myargs <- get_args(lm, formula = Sepal.Length ~ Sepal.Width, data = iris )
summary(do.call('lm', myargs))
```

---

indirect_effect	<i>Retrieve Indirect Effect estimates</i>
-----------------	---

---

**Description**

Retrieves the population average indirect causal effect for specified allocations:  $\hat{Y}(0, \alpha_1) - \hat{Y}(0, \alpha_2)$ . This is the effect due to the coverage (allocation) levels.

Retrieve Indirect Effect estimates

**Usage**

```
indirect_effect(object, allocation1, allocation2 = NULL, trt.lvl = 0)
```

```
ie(object, allocation1, allocation2 = NULL, trt.lvl = 0)
```

**Arguments**

object	an object of class interference
allocation1	the allocation scheme for which to estimate indirect effects
allocation2	the allocation scheme for which to estimate indirect effects. If NULL, then returns all indirect effects compared to allocation1.
trt.lvl	Defaults to 0.

**Value**

a data.frame with requested values

---

inference	<i>Methods for causal inference with interference</i>
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**Description**

Interference occurs when the treatment of one unit affects outcomes of other units. This package provides methods for estimating causal effects in the presence of interference. Currently it implements the IPW estimators proposed by [Tchetgen Tchetgen and Vanderweele \(2012\)](#) and developed further in [Heydrich-Perez et al. \(2014\)](#).

**References**

Saul, B. and Huggens, M. G. (2017). A Recipe for interference: Start with Causal Inference. Add Interference. Mix Well with R. *Journal of Statistical Software*, 82(2), 1-21. [doi:10.18637/jss.v082.i02](https://doi.org/10.18637/jss.v082.i02)

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interference                      *Estimate Causal Effects in presence of interference*

---

## Description

Estimate Causal Effects in presence of interference

## Usage

```
interference(formula, propensity_integrand = "logit_integrand",
  loglikelihood_integrand = propensity_integrand, allocations, data,
  model_method = "glmer", model_options = list(family = stats::binomial(link
  = "logit")), causal_estimation_method = "ipw",
  causal_estimation_options = list(variance_estimation = "robust"),
  conf.level = 0.95, rescale.factor = 1, integrate_allocation = TRUE,
  runSilent = TRUE, ...)
```

## Arguments

- formula**                      The formula used to define the causal model. Has a minimum of 4 parts, separated by | and ~ in a specific structure: outcome | exposure ~ propensity covariates | group. The order matters, and the pipes split the data frame into corresponding pieces. The part separated by ~ is passed to the chosen model\_method used to estimate or fix propensity parameters.
- propensity\_integrand**  
 A function, which may be created by the user, used to compute the IP weights. This defaults to logit\_integrand, which calculates the product of inverse logits for individuals in a group:  $\prod_{j=1}^{n_i} \{r \times h_{ij}(b_i)^{A_{ij}}\} \{1 - r \times h_{ij}(b_i)\}^{1 - A_{ij}} f_b(b_i; \theta_s)$  where
- $$h_{ij}(b_i) = \text{logit}^{-1}(\mathbf{X}_{ij}\theta_a + b_i)$$
- and  $b_i$  is a group-level random effect,  $f_b$  is a  $N(0, \theta_s)$  density, and  $r$  is a known randomization probability which may be useful if a participation vector is included in the formula. If no random effect was included in the formula, logit\_integrand essentially ignores the random effect and  $f_b(b_i, \theta_s)$  integrates to 1. See details for arguments that can be passed to logit\_integrand
- loglikelihood\_integrand**  
 A function, which may be created by the user, that defines the log likelihood of the logit model used for robust variance estimation. Generally, this will be the same function as propensity\_integrand. Indeed, this is the default.
- allocations**                      a vector of values in (0, 1). Increasing the number of elements of the allocation vector greatly increases computation time; however, a larger number of allocations will make plots look nicer. A minimum of two allocations is required.
- data**                              the analysis data frame. This must include all the variables defined in the formula.

<code>model_method</code>	the method used to estimate or set the propensity model parameters. Must be one of 'glm', 'glmer', or 'oracle'. Defaults to 'glmer'. For a fixed effects only model use 'glm', and to include random effects use 'glmer'. <code>logit_integrand</code> only supports a single random effect for the grouping variable, so if more random effects are included in the model, different <code>propensity_integrand</code> and <code>loglikelihood_integrand</code> functions should be defined. When the propensity parameters are known (as in simulations) or if estimating parameters by other methods, use the 'oracle' option. See <code>model_options</code> for details on how to pass the oracle parameters.
<code>model_options</code>	a list of options passed to the function in <code>model_method</code> . Defaults to <code>list(family = binomial(link = ...))</code> . When <code>model_method = 'oracle'</code> , the list must have two elements (1) <code>fixed_effects</code> and (2) <code>random_effects</code> . If the model did not include random effects, set <code>random_effects = NULL</code> .
<code>causal_estimation_method</code>	currently only supports 'ipw'.
<code>causal_estimation_options</code>	A list. Current options are: (1) <code>variance_estimation</code> is either 'naive' or 'robust'. See details. Defaults to 'robust'.
<code>conf.level</code>	level for confidence intervals. Defaults to 0.95.
<code>rescale.factor</code>	a scalar multiplication factor by which to rescale outcomes and effects. Defaults to 1.
<code>integrate_allocation</code>	Indicator of whether the integrand function uses the allocation parameter. Defaults to TRUE.
<code>runSilent</code>	if FALSE, status of computations are printed to console. Defaults to TRUE.
<code>...</code>	Used to pass additional arguments to internal functions such as <code>numDeriv::grad()</code> or <code>integrate()</code> . Additionally, arguments can be passed to the <code>propensity_integrand</code> and <code>loglikelihood_integrand</code> functions.

## Details

The following formula includes a random effect for the group: `outcome | exposure ~ propensity covariates + (1|group)`. In this instance, the group variable appears twice. If the study design includes a "participation" variable, this is easily added to the formula: `outcome | exposure | participation ~ propensity covariates | group`.

`logit_integrand` has two options that can be passed via the `...` argument:

- `randomization`: a scalar. This is the  $r$  in the formula just above. It defaults to 1 in the case that a participation vector is not included. The vaccine study example demonstrates use of this argument.
- `integrate_allocation`: TRUE/FALSE. When group sizes grow large (over 1000), the product term of `logit_integrand` tends quickly to 0. When set to TRUE, the IP weights tend less quickly to 0. Defaults to FALSE.

If the true propensity model is known (e.g. in simulations) use `variance_estimation = 'naive'`; otherwise, use the default `variance_estimation = 'robust'`. Refer to the web appendix of [Heydrich-Perez et al. \(2014\)](#) for complete details.

**Value**

Returns a list of overall and group-level IPW point estimates, overall and group-level IPW point estimates (using the weight derivatives), derivatives of the loglikelihood, the computed weight matrix, the computed weight derivative array, and a summary.

**References**

- Saul, B. and Hudgens, M. G. (2017). A Recipe for inference: Start with Causal Inference. Add Interference. Mix Well with R. Journal of Statistical Software, 82(2), 1-21. doi:10.18637/jss.v082.i02
- Perez-Heydrich, C., Hudgens, M. G., Halloran, M. E., Clemens, J. D., Ali, M., & Emch, M. E. (2014). Assessing effects of cholera vaccination in the presence of interference. Biometrics, 70(3), 731-741.
- Tchetgen Tchetgen, E. J., & VanderWeele, T. J. (2012). On causal inference in the presence of interference. Statistical Methods in Medical Research, 21(1), 55-75.

---

logit_integrand	<i>Default integrand for the group-level propensity score</i>
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---

**Description**

Computes the following function:

$$\prod_{j=1}^n (rh_j(b))^{A_j} (1 - rh_j(b))^{1-A_j} f_b(b; \theta_b)$$

where  $r$  is the randomization scheme.  $X$  is the covariate(s) vectors.  $fixef$  is the vector of fixed effects.  $b$  is the random (group-level) effect.  $raneff$  is the random effect variance.

**Usage**

```
logit_integrand(b, X, A, parameters, allocation = A, randomization = 1)
```

**Arguments**

- |               |  |
|---------------|--|
| b             | vector argument of values necessary for <code>integrate</code> .   |
| X             | n by length(fixed effects) matrix of covariates.   |
| A             | vector of binary treatments  |
| parameters    | vector of fixed effect (and random effect if applicable). Random effect should be last element in vector.                |
| allocation    | The allocation strategy. Defaults to A so that is essentially ignored if allocation is not set to a value within (0, 1). |
| randomization | Randomization probability. Defaults to 1.  |

**Value**

value of the integrand

---

log_likelihood	<i>Log Likelihood</i>
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---

**Description**

Used by `score_matrix` to compute the log likelihood.

**Usage**

```
log_likelihood(parameters, integrand, ...)
```

**Arguments**

parameters	vector of parameters passed to integrand
integrand	Defaults to logit_integrand
...	additional arguments passed to integrand function.

**Value**

value of log likelihood

---

overall_effect	<i>Retrieve Overall Effect Estimates</i>
----------------	--

---

**Description**

Retrieves the population average overall causal effect:  $\hat{Y}(\alpha1) - \hat{Y}(\alpha2)$

**Usage**

```
overall_effect(object, allocation1, allocation2 = NULL)
```

```
oe(object, allocation1, allocation2 = NULL)
```

**Arguments**

object	an object of class interference
allocation1	the allocation scheme for which to estimate overall effects
allocation2	the allocation scheme for which to estimate overall effects

**Value**

a data.frame with a single row with requested values

---

print.interference      *Prints a summary of an interference object*

---

### Description

Prints a summary of an interference object

### Usage

```
## S3 method for class 'interference'  
print(x, ...)
```

### Arguments

x	object of class 'interference'
...	ignored

---

score\_calc      *Compute scores for a single group*

---

### Description

Used by [score\\_matrix](#) to log likelihood derivatives for a single group.

### Usage

```
score_calc(parameters, integrand, hide.errors = TRUE, ...)
```

### Arguments

parameters	vector of parameters passed to integrand
integrand	function to used for the integrand. Defaults to <a href="#">logit_integrand</a> .
hide.errors	Hide errors printed from <a href="#">grad</a> . Defaults to true.
...	additional arguments pass to the integrand function.

### Value

length(theta) vector of scores

---

score_matrix	<i>Calculate matrix of log Likelihood derivatives</i>
--------------	---

---

**Description**

Calculate matrix of log Likelihood derivatives

**Usage**

```
score_matrix(integrand, X, A, G, parameters, runSilent = TRUE, ...)
```

**Arguments**

integrand	function passed to <code>log_likelihood</code> . Defaults to <code>logit_integrand</code>
X	covariate matrix
A	vector of treatment assignments
G	vector of group assignments
parameters	vector of parameters passed to <code>integrand</code>
runSilent	If FALSE, prints errors to console. Defaults to TRUE.
...	additional arguments passed to <code>integrand</code> or <code>grad</code> . For example, one can change the method argument in <code>grad</code> .

**Value**

N X length(params) matrix of scores

---

total_effect	<i>Retrieve Total Effect estimates</i>
--------------	--

---

**Description**

Retrieves the population average total causal effect for specified allocations:  $\hat{Y}(0, \alpha_1) - \hat{Y}(1, \alpha_2)$

**Usage**

```
total_effect(object, allocation1, allocation2 = NULL, trt.lv11 = 0)
```

```
te(object, allocation1, allocation2 = NULL, trt.lv11 = 0)
```

**Arguments**

object	an object of class <code>interference</code>
allocation1	the allocation scheme for which to estimate total effects
allocation2	the allocation scheme for which to estimate total effects If NULL, then returns all indirect effects compared to allocation1.
trt.lv11	Defaults to 0.

**Value**

a data.frame with requested values

---

vaccinesim

*Vaccine Study Sample Data*

---

**Description**

A sample dataset based on the simulations of a cholera vaccine trial in [Heydrich-Perez et al. \(2014\)](#) except with 3000 individuals in 250 groups rather than 10000 in 500.

**Format**

a dataset with 6 variables and 3000 rows

- Y the outcome (0 - no cholera; 1 - cholera)
- X1 an individual's age (in decades)
- X2 an individual's distance from river
- A an indicator of vaccination (0 - no vaccine; 1 - vaccine)
- B an indicator of participation (0 - did not participate in vaccine trial, 1 - did participate)
- group group membership

**References**

Perez-Heydrich, C., Hudgens, M. G., Halloran, M. E., Clemens, J. D., Ali, M., & Emch, M. E. (2014). Assessing effects of cholera vaccination in the presence of interference. *Biometrics*, 70(3), 731-741.

---

voters

*Voting Contagion Experiment Data*

---

**Description**

A dataset of a voting contagion experiment. See [Nickerson 2008](#) for more details. The variables used in the package vignette are documented here.

**Format**

a dataset with 21 variables and 7722 rows

- familyhousehold ID
- denver1 = subject in Denver, 0 = Minneapolis
- treatment1 = voting encouragement, 2 = recycling message, 3 = not contacted
- reached1 = subject answered door, 0 = not
- hsecontact1 = household contacted by canvassers, 0 = not
- voted02p1 = voted in '02 primary, 0 = not
- partyparty affiliation
- ageage
- gendergender

**References**

Nickerson, D. W. (2008). Is voting contagious? Evidence from two field experiments. *American Political Science Review*, 102(01), 49-57.

---

wght_calc	<i>Compute IPW weight</i>
-----------	---------------------------

---

**Description**

Calculates the IPW for a single group. Used by [wght\\_matrix](#) to create a matrix of weights for each group and allocation scheme.

**Usage**

```
wght_calc(parameters, integrand, allocation, integrate_allocation = TRUE, ...)
```

**Arguments**

parameters	vector of parameter values
integrand	function to pass to the argument 'f' of <a href="#">integrate</a> .
allocation	the allocation ratio for which to compute the weight
integrate_allocation	Indicator of whether the integrand function uses the allocation parameter. Defaults to TRUE.
...	other arguments passed to integrand.

**Details**

If allocation is an argument in the integrand function and `integrate_allocation == TRUE`, then the weight is calculated as:

$$\frac{1}{Pr(A|X)}$$

Otherwise, the weight is computed by:

$$\frac{\prod_{j=1}^n \alpha_j^A (1 - \alpha)^{(1 - A_j)}}{Pr(A|X)}$$

**Value**

scalar result of the integral

---

wght_deriv_array	<i>Create an array of group weight derivatives</i>
------------------	--

---

**Description**

Uses [wght\\_deriv\\_calc](#) to compute the weight derivatives for each group per coverage level

**Usage**

```
wght_deriv_array(parameters, integrand, allocations, X, A, G,
  runSilent = TRUE, integrate_allocation = TRUE, ...)
```

**Arguments**

parameters	vector of parameters passed to integrand
integrand	function to pass to the argument 'f' of <a href="#">integrate</a> .
allocations	coverage levels in [0, 1]. Can be vector.
X	covariate matrix
A	vector of treatment assignments
G	vector of group assignments
runSilent	if FALSE, errors are printed to console. Defaults to TRUE.
integrate_allocation	Indicator of whether the integrand function uses the allocation parameter. Defaults to TRUE.
...	other arguments passed to integrand.

**Value**

a `length(unique(group)) X length(params) X length(alphas)` array of group weight derivatives

---

wght_deriv_calc	<i>Compute the derivative(s) of a weight</i>
-----------------	--

---

**Description**

Takes the derivative of the `wght_calc` function with respect to each parameter in `params`.

**Usage**

```
wght_deriv_calc(integrand, parameters, allocation,
               integrate_allocation = TRUE, ...)
```

**Arguments**

<code>integrand</code>	function to pass to the argument 'f' of <code>integrate</code> .
<code>parameters</code>	vector of parameter values
<code>allocation</code>	the allocation ratio for which to compute the weight
<code>integrate_allocation</code>	Indicator of whether the integrand function uses the allocation parameter. Defaults to TRUE.
<code>...</code>	other arguments passed to <code>integrand</code> .

**Value**

vector of derivatives with respect to element of `params`

---

wght_matrix	<i>Creates a number of groups by number of allocation schemes matrix of group weights. Allocation schemes are selected by the user.</i>
-------------	---

---

**Description**

Groups should be numbered 1, ..., N

**Usage**

```
wght_matrix(integrand, allocations, X, A, G, parameters, runSilent = TRUE,
           integrate_allocation = TRUE, ...)
```

**Arguments**

integrand	function to pass to the argument 'f' of <a href="#">integrate</a> .
allocations	coverage levels in [0, 1]. Can be vector.
X	covariate matrix
A	vector of treatment assignments
G	vector of group assignments
parameters	vector of parameters passed to integrand
runSilent	if FALSE, errors are printed to console. Defaults to TRUE.
integrate_allocation	Indicator of whether the integrand function uses the allocation parameter. Defaults to TRUE.
...	other arguments passed to integrand.

**Value**

a  $\text{length}(\text{unique}(\text{group})) \times \text{length}(\text{alphas})$  matrix of group weights

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