Package 'drf'

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Title Distributional Random Forests

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BugReports https://github.com/lorismichel/mrf/issues

Description An implementation of distributional random forests as introduced in Cevid & Michel & Meinshausen & Buhlmann (2020) <arXiv:2005.14458>.

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LinkingTo Rcpp, RcppEigen

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drf *Distributional Random Forests*

Description

Trains a distributional random forest that can be used to estimate statistical functional F(P(Y | X)) for possibly multivariate response Y.

Usage

```
drf(
  X,
  Y,
  num.trees = 500,
  splitting.rule = "FourierMMD",
  num.features = 10,
  bandwidth = 1,
  node.scaling = FALSE,
  sample.weights = NULL,
  clusters = NULL,
  equalize.cluster.weights = FALSE,
  sample.fraction = 0.5,
  mtry = min(ceiling(sqrt(ncol(X)) + 20), ncol(X)),
  min.node.size = 15,
  honesty = TRUE,
  honesty.fraction = 0.5,
  honesty.prune.leaves = TRUE,
  alpha = 0.05,
  imbalance.penalty = 0,
  ci.group.size = 2,
  compute.oob.predictions = TRUE,
  num.threads = NULL,
  seed = stats::runif(1, 0, .Machine$integer.max)
)
```

Arguments

X	The covariates used in the regression. Can be either a matrix of numerical values, or a data.frame with characters and factors. In the latter case, one-hot-encoding will be implicitely used.
Y	The (multivariate) outcome. A matrix or data.frame of numeric values.
num.trees	Number of trees grown in the forest. Default is 500.
splitting.rule	a character value. The type of splitting rule used, can be either "CART" or "FourierMMD".

`num.features` a numeric value, in case of "FourierMMD", the number of random features to sample.

`bandwidth` a numeric value, the bandwidth of the Gaussian kernel used in case of "FourierMMD".

`node.scaling` a boolean value, should the responses be scaled or not by node.

`sample.weights` (experimental) Weights given to an observation in estimation. If NULL, each observation is given the same weight. Default is NULL.

`clusters` Vector of integers or factors specifying which cluster each observation corresponds to. Default is NULL (ignored).

`equalize.cluster.weights`
If FALSE, each unit is given the same weight (so that bigger clusters get more weight). If TRUE, each cluster is given equal weight in the forest. In this case, during training, each tree uses the same number of observations from each drawn cluster: If the smallest cluster has K units, then when we sample a cluster during training, we only give a random K elements of the cluster to the tree-growing procedure. When estimating average treatment effects, each observation is given weight 1/cluster size, so that the total weight of each cluster is the same. Note that, if this argument is FALSE, sample weights may also be directly adjusted via the sample.weights argument. If this argument is TRUE, sample.weights must be set to NULL. Default is FALSE.

`sample.fraction`
Fraction of the data used to build each tree. Note: If honesty = TRUE, these subsamples will further be cut by a factor of honesty.fraction. Default is 0.5.

`mtry` Number of variables tried for each split. Default is $\sqrt{p} + 20$ where p is the number of variables.

`min.node.size` A target for the minimum number of observations in each tree leaf. Note that nodes with size smaller than min.node.size can occur, as in the original randomForest package. Default is 5.

`honesty` Whether to use honest splitting (i.e., sub-sample splitting). Default is TRUE. For a detailed description of honesty, honesty.fraction, honesty.prune.leaves, and recommendations for parameter tuning, see the grf reference for more information (initial source) algorithm reference.

`honesty.fraction`
The fraction of data that will be used for determining splits if honesty = TRUE. Corresponds to set J1 in the notation of the paper. Default is 0.5 (i.e. half of the data is used for determining splits).

`honesty.prune.leaves`
If TRUE, prunes the estimation sample tree such that no leaves are empty. If FALSE, keep the same tree as determined in the splits sample (if an empty leave is encountered, that tree is skipped and does not contribute to the estimate). Setting this to FALSE may improve performance on small/marginally powered data, but requires more trees (note: tuning does not adjust the number of trees). Only applies if honesty is enabled. Default is TRUE.

`alpha` A tuning parameter that controls the maximum imbalance of a split. Default is 0.05.

`imbalance.penalty`
: A tuning parameter that controls how harshly imbalanced splits are penalized. Default is 0.

`ci.group.size`
: The forest will grow ci.group.size trees on each subsample. In order to provide confidence intervals, ci.group.size must be at least 2. Default is 2.

`compute.oob.predictions`
: Whether OOB predictions on training set should be precomputed. Default is TRUE.

`num.threads`
: Number of threads used in training. By default, the number of threads is set to the maximum hardware concurrency.

`seed`
: The seed of the C++ random number generator.

Value

A trained distributional random forest object.

Examples

```
# Train a distributional random forest with CART splitting rule.
n <- 100
p <- 2
X <- matrix(rnorm(n * p), n, p)
Y <- X + matrix(rnorm(n * p), ncol=p)
drf.forest <- drf(X = X, Y = Y)

# Predict conditional correlation.
X.test <- matrix(0, 101, p)
X.test[, 1] <- seq(-2, 2, length.out = 101)
cor.pred <- predict(drf.forest, X.test, functional = "cor")

# Predict on out-of-bag training samples.
cor.oob.pred <- predict(drf.forest,  functional = "cor")

# Train a distributional random forest with "FourierMMD" splitting rule.
n <- 50
p <- 2
X <- matrix(rnorm(n * p), n, p)
Y <- X + matrix(rnorm(n * p), ncol=p)
drf.forest <- drf(X = X, Y = Y, splitting.rule = "FourierMMD", num.features = 10)

# Predict conditional correlation.
X.test <- matrix(0, 101, p)
X.test[, 1] <- seq(-2, 2, length.out = 101)
cor.pred <- predict(drf.forest, X.test, functional = "cor")

# Predict on out-of-bag training samples.
cor.oob.pred <- predict(drf.forest,  functional = "cor")
```

get_sample_weights *Given a trained forest and test data, compute the training sample weights for each test point.*

Description

During normal prediction, these weights are computed as an intermediate step towards producing estimates. This function allows for examining the weights directly, so they could be potentially be used as the input to a different analysis.

Usage

```
get_sample_weights(forest, newdata = NULL, num.threads = NULL)
```

Arguments

forest	The trained forest.
newdata	Points at which predictions should be made. If NULL, makes out-of-bag predictions on the training set instead (i.e., provides predictions at Xi using only trees that did not use the i-th training example).#' @param max.depth Maximum depth of splits to consider.
num.threads	Number of threads used in training. If set to NULL, the software automatically selects an appropriate amount.

Value

A sparse matrix where each row represents a test sample, and each column is a sample in the training data. The value at (i, j) gives the weight of training sample j for test sample i.

Examples

```
n <- 50
p <- 2
X <- matrix(rnorm(n * p), n, p)
Y <- X + matrix(rnorm(n * p), ncol=p)
drf.forest <- drf(X = X, Y = Y, splitting.rule = "FourierMMD", num.features = 10)
sample.weights.oob <- get_sample_weights(drf.forest)

n.test <- 15
X.test <- matrix(2 * runif(n.test * p) - 1, n.test, p)
sample.weights <- get_sample_weights(drf.forest, X.test)
```

get_tree *Retrieve a single tree from a trained forest object.*

Description

Retrieve a single tree from a trained forest object.

Usage

```
get_tree(forest, index)
```

Arguments

forest	The trained forest.
index	The index of the tree to retrieve.

Value

A DRF tree object containing the below attributes. drawn_samples: a list of examples that were used in training the tree. This includes examples that were used in choosing splits, as well as the examples that populate the leaf nodes. Put another way, if honesty is enabled, this list includes both subsamples from the split (J1 and J2 in the notation of the paper). num_samples: the number of examples used in training the tree. nodes: a list of objects representing the nodes in the tree, starting with the root node. Each node will contain an 'is_leaf' attribute, which indicates whether it is an interior or leaf node. Interior nodes contain the attributes 'left_child' and 'right_child', which give the indices of their children in the list, as well as 'split_variable', and 'split_value', which describe the split that was chosen. Leaf nodes only have the attribute 'samples', which is a list of the training examples that the leaf contains. Note that if honesty is enabled, this list will only contain examples from the second subsample that was used to 'repopulate' the tree (J2 in the notation of the paper).

Examples

```
n <- 50
p <- 2
X <- matrix(rnorm(n * p), n, p)
Y <- X + matrix(rnorm(n * p), ncol=p)
drf.forest <- drf(X = X, Y = Y, splitting.rule = "FourierMMD", num.features = 10)

# Examine a particular tree.
q.tree <- get_tree(drf.forest, 3)
q.tree$nodes
```

leaf_stats.default *A default leaf_stats for forests classes without a leaf_stats method that always returns NULL.*

Description

A default leaf_stats for forests classes without a leaf_stats method that always returns NULL.

Usage

```
## Default S3 method:
leaf_stats(forest, samples, ...)
```

Arguments

forest	Any forest
samples	The samples to include in the calculations.
...	Additional arguments (currently ignored).

leaf_stats.drf *Calculate summary stats given a set of samples for regression forests.*

Description

Calculate summary stats given a set of samples for regression forests.

Usage

```
## S3 method for class 'drf'
leaf_stats(forest, samples, ...)
```

Arguments

forest	The DRF forest
samples	The samples to include in the calculations.
...	Additional arguments (currently ignored).

Value

A named vector containing summary stats

plot.drf_tree *Plot a DRF tree object.*

Description

Plot a DRF tree object.

Usage

```
## S3 method for class 'drf_tree'
plot(x, ...)
```

Arguments

x	The tree to plot
...	Additional arguments (currently ignored).

predict.drf *Predict with a drf forest*

Description

Predict with a drf forest

Usage

```
## S3 method for class 'drf'
predict(
  object,
  newdata = NULL,
  transformation = NULL,
  functional = NULL,
  num.threads = NULL,
  ...
)
```

Arguments

object	The trained drf forest.
newdata	Points at which predictions should be made. If NULL, makes out-of-bag predictions on the training set instead (i.e., provides predictions at Xi using only trees that did not use the i-th training example). Note that this matrix (or vector) should have the number of columns as the training matrix, and that the columns must appear in the same order.

`transformation` a function giving a transformation of the responses, by default if NULL, the identity `function(y) y` is used.

`functional` which type of statistical functional. One option between:

- "mean"the conditional mean, the returned value is a list containing a matrix `mean` of size `n x f`, where `n` denotes the number of observation in `newdata` and `f` the dimension of the `transformation`.
- "sd"the conditional standard deviation, the returned value is a list containing a matrix `sd` of size `n x f`, where `n` denotes the number of observation in `newdata` and `f` the dimension of the `transformation`.
- "quantile"the conditional quantiles, the returned value is a list containing an array `quantile` of size `n x f x q`, where `n` denotes the number of observation in `newdata`, `f` the dimension of the `transformation` and `q` the number of desired quantiles.
- "cor"the conditional correlation, the returned value is a list containing an array `cor` of size `n x f x f`, where `n` denotes the number of observation in `newdata`, `f` the dimension of the `transformation`.
- "cov"the conditional covariance, the returned value is a list containing an array `cor` of size `n x f x f`, where `n` denotes the number of observation in `newdata`, `f` the dimension of the `transformation`.
- "cdf"the conditional cumulative distribution function, the returned value is a list containing a list of functions `cdf` of size `n`, where `n` denotes the number of observation in `newdata`. Here the transformation should be uni-dimensional.
- "normalPredictionScore"a prediction score based on an asymptotic normality assumption, the returned value is a list containing a list of functions `normalPredictionScore` of size `n`, where `n` denotes the number of observation in `newdata`. Here the transformation should be uni-dimensional.

`num.threads` Number of threads used in training. If set to NULL, the software automatically selects an appropriate amount.

`...` additional parameters.

Value

a list containing an entry with the same name as the functional selected.

Examples

```
# Train a distributional random forest with CART splitting rule.
n <- 50
p <- 2
X <- matrix(rnorm(n * p), n, p)
Y <- X + matrix(rnorm(n * p), ncol=p)
drf.forest <- drf(X = X, Y = Y)

# Predict conditional correlation.
X.test <- matrix(0, 101, p)
X.test[, 1] <- seq(-2, 2, length.out = 101)
cor.pred <- predict(drf.forest, X.test, functional = "cor")
```

```
# Predict on out-of-bag training samples.
cor.oob.pred <- predict(drf.forest,  functional = "cor")

# Train a distributional random forest with "FourierMMD" splitting rule.
n <- 100
p <- 2
X <- matrix(rnorm(n * p), n, p)
Y <- X + matrix(rnorm(n * p), ncol=p)
drf.forest <- drf(X = X, Y = Y, splitting.rule = "FourierMMD", num.features = 10)

# Predict conditional correlation.
X.test <- matrix(0, 101, p)
X.test[, 1] <- seq(-2, 2, length.out = 101)
cor.pred <- predict(drf.forest, X.test, functional = "cor")

# Predict on out-of-bag training samples.
cor.oob.pred <- predict(drf.forest,  functional = "cor")
```

`print.drf` *Print a DRF forest object.*

Description

Print a DRF forest object.

Usage

```
## S3 method for class 'drf'
print(x, decay.exponent = 2, max.depth = 4, ...)
```

Arguments

`x`	The tree to print.
`decay.exponent`	A tuning parameter that controls the importance of split depth.
`max.depth`	The maximum depth of splits to consider.
`...`	Additional arguments (currently ignored).

print.drf_tree *Print a DRF tree object.*

Description

Print a DRF tree object.

Usage

```
## S3 method for class 'drf_tree'
print(x, ...)
```

Arguments

x	The tree to print.
...	Additional arguments (currently ignored).

split_frequencies *Calculate which features the forest split on at each depth.*

Description

Calculate which features the forest split on at each depth.

Usage

```
split_frequencies(forest, max.depth = 4)
```

Arguments

forest	The trained forest.
max.depth	Maximum depth of splits to consider.

Value

A matrix of split depth by feature index, where each value is the number of times the feature was split on at that depth.

Examples

```
n <- 50
p <- 2
X <- matrix(rnorm(n * p), n, p)
Y <- X + matrix(rnorm(n * p), ncol=p)
drf.forest <- drf(X = X, Y = Y, splitting.rule = "FourierMMD", num.features = 10)

# Calculate the split frequencies for this forest.
split_frequencies(drf.forest)
```

`variable_importance` *Calculate a simple measure of 'importance' for each feature.*

Description

A simple weighted sum of how many times feature i was split on at each depth in the forest.

Usage

```
variable_importance(forest, decay.exponent = 2, max.depth = 4)
```

Arguments

`forest`	The trained forest.
`decay.exponent`	A tuning parameter that controls the importance of split depth.
`max.depth`	Maximum depth of splits to consider.

Value

A list specifying an 'importance value' for each feature.

Examples

```
n <- 50
p <- 2
X <- matrix(rnorm(n * p), n, p)
Y <- X + matrix(rnorm(n * p), ncol=p)
drf.forest <- drf(X = X, Y = Y, splitting.rule = "FourierMMD", num.features = 10)

# Calculate the 'importance' of each feature.
variable_importance(drf.forest)
```

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