Package 'cobs'

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Author Pin T. Ng <pin.ng@nau.edu> and Martin Maechler</pin.ng@nau.edu>					
Maintainer Martin Maechler <maechler@stat.math.ethz.ch></maechler@stat.math.ethz.ch>					
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cobs

COnstrained B-Splines Nonparametric Regression Quantiles

Description

Computes constrained quantile curves using linear or quadratic splines. The median spline (L_1 loss) is a robust (constrained) smoother.

Usage

Arguments

Х	vector of covariate; missing values are omitted.	
У	vector of response variable. It must have the same length as x.	
constraint	character (string) specifying the kind of constraint; must be one of the values in the default list above; may be abbreviated. More flexible constraints can be specified via the pointwise argument (below).	
W	vector of weights the same length as $x(y)$ assigned to both x and y ; default to all weights being one.	
knots	vector of locations of the knot mesh; if missing, nknots number of knots will be created using the specified method and automatic knot selection will be carried out for regression B-spline (lambda=0); if not missing and length(knots)==nknots, the provided knot mesh will be used in the fit and no automatic knot selection will be performed; otherwise, automatic knots selection will be performed on the provided knots.	

nknots maximum number of knots; defaults to 6 for regression B-splines, 20 for smoothing B-splines. method character string specifying the method for generating nknots number of knots when knots is not provided; either "quantile" (equally spaced in percentile levels) or "uniform" (equally spaced knots); defaults to "quantile". degree degree of the splines; 1 for linear spline (equivalent to L_1 -roughness) and 2 for quadratic spline (corresponding to L_{∞} roughness); defaults to 2. desired quantile level; defaults to 0.5 (median). tau lambda penalty parameter λ $\lambda = 0$: no penalty (regression B-spline); $\lambda > 0$: smoothing B-spline with the given λ ; $\lambda < 0$: smoothing B-spline with λ chosen by a Schwarz-type information criterion. ic string indicating the information criterion used in knot deletion and addition for the regression B-spline method, i.e., when lambda == 0; "AIC" (Akaike-type, equivalently "aic") or "SIC" (Schwarz-type, equivalently "BIC", "sic" or "bic"). Defaults to "AIC". Note that the default was "SIC" up to cobs version 1.1-6 (dec.2008). knots.add logical indicating if an additional step of stepwise knot addition should be performed for regression B-splines. repeat.delete.add logical indicating if an additional step of stepwise knot deletion should be performed for regression B-splines. pointwise an optional three-column matrix with each row specifies one of the following constraints: (1,xi,yi): fitted value at xi will be \geq yi; (-1, xi, yi): fitted value at xi will be $\leq yi$; (0, xi, yi): fitted value at xi will be = yi; (2,xi,yi): derivative of the fitted function at xi will be yi. keep.data logical indicating if the x and y input vectors after removing NAs should be kept in the result. logical indicating if the pseudo design matrix \tilde{X} should be returned (as *sparse* keep.x.ps matrix). That is needed for interval prediction, predict.cobs(*,interval=..). flag for printing of interactive warning messages; true by default; set to FALSE if print.warn performing simulation. logical flag or integer for printing of intermediate messages; true by default. print.mesg Probably needs to be set to FALSE in simulations. trace integer ≥ 0 indicating how much diagnostics the low-level code in drqssbc2 should print; defaults to print.mesg. lambdaSet numeric vector of lambda values to use for grid search; in that case, defaults to a geometric sequence (a "grid in log scale") from lambda.lo to lambda.hi of

length lambda.length.

lambda.lo, lambda.hi

lower and upper bound of the grid search for lambda (when lambda < 0). The defaults are meant to keep everything scale-equivariant and are hence using the

factor

 $f = \sigma_x^d$, i.e., f.lambda <-sd(x)^degree.

Note however that currently the underlying algorithms in package quantreg are

not scale equivariant yet.

lambda.length number of grid points in the grid search for optimal lambda.

maxiter upper bound of the number of iterations; defaults to 100.

rq.tol numeric convergence tolerance for the interior point algorithm called from rq.fit.sfnc()

or rq.fit.sfn().

toler.kn numeric tolerance for shifting the boundary knots outside; defaults to 10^{-6} .

tol. ores tolerance for testing $|r_i| = 0$, passed to qbsks2 and drqssbc2.

nk. start number of starting knots used in automatic knot selection. Defaults to the mini-

mum of 2 knots.

Details

cobs() computes the constraint quantile smoothing B-spline with penalty when lambda is not zero.

If lambda < 0, an optimal lambda will be chosen using Schwarz type information criterion.

If lambda > 0, the supplied lambda will be used.

If lambda = 0, cobs computes the constraint quantile regression B-spline with no penalty using the provided knots or those selected by Akaike or Schwarz information criterion.

Value

an object of class cobs, a list with components

call the cobs(..) call used for creation.

tau, degree same as input

constraint as input (but no more abbreviated).

pointwise as input.

coef B-spline coefficients.

knots the final set of knots used in the computation.

if1 exit code := 1 + ierr and ierr is the error from rq.fit.sfnc (package quantreg);

consequently, if 1 = 1 means "success"; all other values point to algorithmic

problems or failures.

icyc length 2: number of cycles taken to achieve convergence for final lambda, and

total number of cycles for all lambdas.

k the effective dimensionality of the final fit.

k0 (usually the same)

x.ps the pseudo design matrix X (as returned by qbsks2).

resid vector of residuals from the fit.

fitted	vector of fitted values from the fit.	
SSy	the sum of squares around centered y (e.g. for computation of \mathbb{R}^2 .)	
lambda	the penalty parameter used in the final fit.	
pp.lambda	vector of all lambdas used for lambda search when lambda < 0 on input.	
pp.sic	vector of Schwarz information criteria evaluated at pp.lambda; note that it is not quite sure how good these are for determining an optimal lambda.	

References

Ng, P. and Maechler, M. (2007) A Fast and Efficient Implementation of Qualitatively Constrained Quantile Smoothing Splines, *Statistical Modelling* **7(4)**, 315-328.

Koenker, R. and Ng, P. (2005) Inequality Constrained Quantile Regression, *Sankhya, The Indian Journal of Statistics* **67**, 418–440.

He, X. and Ng, P. (1999) COBS: Qualitatively Constrained Smoothing via Linear Programming; *Computational Statistics* **14**, 315–337.

Koenker, R. and Ng, P. (1996) A Remark on Bartels and Conn's Linearly Constrained L1 Algorithm, *ACM Transaction on Mathematical Software* **22**, 493–495.

Ng, P. (1996) An Algorithm for Quantile Smoothing Splines, *Computational Statistics & Data Analysis* **22**, 99–118.

Bartels, R. and Conn A. (1980) Linearly Constrained Discrete L_1 Problems, ACM Transaction on Mathematical Software **6**, 594–608.

A postscript version of the paper that describes the details of COBS can be downloaded from http://www.cba.nau.edu/pin-ng/cobs.html.

See Also

smooth.spline for unconstrained smoothing splines; bs for unconstrained (regression) B-splines.

Examples

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cobs-methods

Methods for COBS Objects

Description

Print, summary and other methods for cobs objects.

Usage

```
## S3 method for class 'cobs'
print(x, digits = getOption("digits"), ...)
## S3 method for class 'cobs'
summary(object, digits = getOption("digits"), ...)
## S3 method for class 'cobs'
coef(object, ...)
## S3 method for class 'cobs'
fitted(object, ...)
## S3 method for class 'cobs'
knots(Fn, ...)
## S3 method for class 'cobs'
residuals(object, ...)
```

Arguments

```
x, object, Fn object of class cobs.digits number of digits to use for printing.further arguments passed from and to methods.
```

Details

These are methods for fitted COBS objects, as computed by cobs.

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Value

print.cobs() returns its argument invisibly. The coef(), fitted(), knots(), and residuals() methods return a numeric vector.

Author(s)

Martin Maechler

See Also

predict.cobs for the predict method, plot.cobs for the plot method, and cobs for examples.

Examples

```
example(cobs)
Sbs # uses print.*
summary(Sbs)
coef(Sbs)
knots(Sbs)
```

conreg

Convex / Concave Regression

Description

Compute a univariate concave or convex regression, i.e., for given vectors, x, y, w in \mathbb{R}^n , where x has to be strictly sorted $(x_1 < x_2 < \ldots < x_n)$, compute an n-vector m minimizing the weighted sum of squares $\sum_{i=1}^n w_i (y_i - m_i)^2$ under the constraints

$$(m_i - m_{i-1})/(x_i - x_{i-1}) \ge (m_{i+1} - m_i)/(x_{i+1} - x_i),$$

for $1 \le i \le n$ and $m_0 := m_{n+1} := -\infty$, for concavity. For convexity (convex=TRUE), replace \ge by \le and $-\infty$ by $+\infty$.

Usage

```
conreg(x, y = NULL, w = NULL, convex = FALSE,
    method = c("Duembgen06_R", "SR"),
    tol = c(1e-10, 1e-7), maxit = c(500, 20),
    adjTol = TRUE, verbose = FALSE)
```

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Arguments

x,y	numeric vectors giving the values of the predictor and response variable. Alto		
	natively a single "plotting" structure (two-column matrix / y-values only / list,		
	etc) can be specified: see xy.coords.		
W	for method "Duembgen06_R" only: optional vector of weights of the same length		

as x; defaults to all 1.

1 1 1 1 1 10

convex logical indicating if convex or concave regression is desired.

method a character string indicating the method used,

"Duembgen06_R" is an active set method written by Lutz Duembgen (University of Berne, CH) in Matlab in 2006 and translated to R by Martin Maechler.

"SR" is an R interface to the C code of a Support Reduction algorithm written by Piet Groeneboom (TU Delft, NL) and donated to the **cobs** package in July 2012.

tol convergence tolerance(s); do not make this too small!

maxit maximal number of (outer and inner) iterations of knot selection.

adjTol (for "Duembgen06_R" only:) logical indicating if the convergence test tolerance

is to be adjusted (increased) in some cases.

verbose logical or integer indicating if (and how much) knot placement and fitting itera-

tions should be "reported".

Details

Both algorithms need some numerical tolerances because of rounding errors in computation of finite difference ratios. The active-set "Duembgen06_R" method notably has two different such tolerances which were both $1e-7=10^7$ up to March 2016.

The two default tolerances (and the exact convergence checks) may change in the future, possibly to become more adaptive.

Value

an object of class conreg which is basically a list with components

x sorted (and possibly aggregated) abscissa values x.

y corresponding y values.

w corresponding weights, **only** for "Duembgen06_R".

yf corresponding fitted values.

convex logical indicating if a convex or a concave fit has been computed.

iKnots integer vector giving indices of the *knots*, i.e. locations where the fitted curve has

kinks. Formally, these are exactly those indices where the constraint is fulfilled

strictly, i.e., those i where

$$(m_i - m_{i-1})/(x_i - x_{i-1}) > (m_{i+1} - m_i)/(x_{i+1} - x_i).$$

call the call to conreg() used.

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iter

integer (vector of length one or two) with the number of iterations used (in the outer and inner loop for "Duembgen06_R").

Note that there are several methods defined for conreg objects, see predict.conreg or methods(class = "conreg").

Notably print and plot; also predict, residuals, fitted, knots.

Also, interpSplineCon() to construct a more smooth (*cubic*) spline, and isIsplineCon() which checks if the int is strictly concave or convex the same as the conreg() result from which it was constructed.

Author(s)

Lutz Duembgen programmed the original Matlab code in July 2006; Martin Maechler ported it to R, tested, catch infinite loops, added more options, improved tolerance, etc; from April 27, 2007.

See Also

isoreg for isotone (monotone) regression; CRAN packages ftnonpar, cobs, logcondens.

Examples

```
## Generated data :
N <- 100
f \leftarrow function(X) 4*X*(1 - X)
xx <- seq(0,1, length=501)# for plotting true f()
set.seed(1)# -> conreg does not give convex cubic
x <- sort(runif(N))</pre>
y < -f(x) + 0.2 * rnorm(N)
plot(x,y, cex = 0.6)
lines(xx, f(xx), col = "blue", lty=2)
rc <- conreg(x,y)</pre>
lines(rc, col = 2, force.iSpl = TRUE)
 # 'force.iSpl': force the drawing of the cubic spline through the kinks
title("Concave Regression in R")
y2 <- y
## Trivial cases work too:
(r.1 <- conreg(1,7))
(r.2 <- conreg(1:2,7:6))
(r.3 <- conreg(1:3,c(4:5,1)))
```

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conreg-methods

Summary Methods for 'conreg' Objects

Description

Methods for conreg objects

Usage

```
## S3 method for class 'conreg'
fitted(object, ...)
## S3 method for class 'conreg'
residuals(object, ...)
## S3 method for class 'conreg'
knots(Fn, ...)
## S3 method for class 'conreg'
lines(x, type = "1", col = 2, lwd = 1.5, show.knots = TRUE,
      add.iSpline = TRUE, force.iSpl = FALSE, ...)
## S3 method for class 'conreg'
plot(x, type = "l", col = 2, lwd = 1.5, show.knots = TRUE,
    add.iSpline = TRUE, force.iSpl = FALSE,
    xlab = "x", ylab = expression(s[c](x)),
    sub = "simple concave regression", col.sub = col, ...)
## S3 method for class 'conreg'
predict(object, x, deriv = 0, ...)
## S3 method for class 'conreg'
print(x, digits = max(3, getOption("digits") - 3), ...)
```

Arguments

an R object of class conreg, i.e., typically the result of conreg(..). For object, Fn, x predict(), x is a numeric vector of abscissa values at which to evaluate the concave/convex spline function. type, col, lwd, xlab, ylab, sub, col.sub plotting arguments as in plot. default. show.knots logical indicating the spline knots should be marked additionally. logical indicating if an interpolation spline should be considered for plotting. add.iSpline This is only used when it is itself concave/convex, unless force. iSpl is TRUE. force.iSpl logical indicating if an interpolating spline is drawn even when it is not convex/concave. deriv for predict, integer specifying the derivate to be computed; currently must be 0 or 1.

drqssbc2

```
digits number of significant digits for printing.
... further arguments, potentially passed to methods.
```

Author(s)

Martin Maechler

See Also

```
conreg, ....
```

Examples

```
example(conreg, echo = FALSE)
class(rc) # "conreg"
rc # calls the print method
knots(rc)
plot(rc)
## and now _force_ the not-quite-concave cubic spline :
plot(rc, force.iSpl=TRUE)
xx <- seq(-0.1, 1.1, length=201) # slightly extrapolate
## Get function s(x) and first derivative s'(x):
yx <- predict(rc, xx)</pre>
y1 \leftarrow predict(rc, xx, deriv = 1)
op <- par(las=1)
plot(xx, yx, type = "l",
     main="plot(xx, predict(conreg(.), xx))")
par(new=TRUE) # draw the first derivative "on top"
plot(xx, y1, type = "l", col = "blue",
     axes = FALSE, ann = FALSE)
abline(h = 0, lty="1A", col="blue")
axis(4, col="blue", col.axis="blue", col.ticks="blue")
mtext("first derivative s'(.)", col="blue")
par(op)
```

drqssbc2

Regression Quantile Smoothing Spline with Constraints

Description

Estimate the B-spline coefficients for a regression quantile *smoothing* spline with optional constraints, using Ng(1996)'s algorithm.

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Usage

Arguments

x numeric vector, sorted increasingly, the abscissa values

y numeric, same length as x, the observations.

numeric vector of weights, same length as x, as in cobs.

pw penalty weights vector passed to 11.design2 or loo.design2. **FIXME**: This

is currently unused.

knots numeric vector of knots for the splines.

degree integer, must be 1 or 2.

Tlambda vector of smoothing parameter values λ ; if it is longer than one, an "optimal"

value will be selected from these.

constraint see cobs (but cannot be abbreviated here).

ptConstr list of pointwise constraints; notably equal, smaller, greater and gradient

are 3-column matrices specifying the respective constraints. May have 0 rows if

there are no constraints of the corresponding kind.

maxiter maximal number of iterations; defaults to 100.

trace integer or logical indicating the tracing level of the *underlying* algorithms; not

much implemented (due to lack of trace in quantreg ...)

nrq integer, = n, the number of observations.

nl1 integer, number of observations in the l1 norm that correspond to roughness

measure (may be zero).

neqc integer giving the number of equations.

niqc integer giving the number of inequality constraints; of the same length as constraint.

nvar integer giving the number of equations *and* constraints.

tau desired quantile level; defaults to 0.5 (median).

select.lambda logical indicating if an optimal lambda should be selected from the vector of

Tlambda.

give.pseudo.x logical indicating if the pseudo design matrix \tilde{X} should be returned (as sparse

matrix).

rq.tol numeric convergence tolerance for the interior point algorithm called from rq.fit.sfnc()

or rq.fit.sfn(). Note that (for scale invariance) this has to be in units of y,

which the default makes use of.

tol. 0 res tolerance used to check for zero residuals, i.e., $|r_i| < tol * mean(|r_i|)$.

drgssbc2

print.warn logical indicating if warnings should be printed, when the algorithm seems to have behaved somewhat unexpectedly.

rq.print.warn logical indicating if warnings should be printed from inside the rq.* function

calls, see below.

Details

This is an auxiliary function for cobs, possibly interesting on its own. Depending on degree, either 11.design2 or loo.design2 are called for construction of the sparse design matrix.

Subsequently, either rq.fit.sfnc or rq.fit.sfn is called as the main "work horse".

This documentation is currently sparse; read the source code!

Value

a list with components

comp1 Description of 'comp1'
comp2 Description of 'comp2'

Author(s)

Pin Ng; this help page: Martin Maechler.

References

Ng, P. (1996) An Algorithm for Quantile Smoothing Splines, *Computational Statistics* & *Data Analysis* 22, 99–118.

See Also

The main function cobs and its auxiliary qbsks2 which calls drqssbc2() repeatedly.

```
11. design2 and loo. design2; further rq.fit.sfnc and rq.fit.sfn from package quantreg.
```

Examples

```
set.seed(1243)

x <- 1:32

fx <- (x-5)*(x-15)^2*(x-21)

y <- fx + round(rnorm(x,s = 0.25),2)
```

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DublinWind

Daily Wind Speeds in Dublin

Description

The DublinWind data frame is basically the time series of daily average wind speeds from 1961 to 1978, measured in Dublin, Ireland. These are 6574 observations (18 full years among which four leap years).

Usage

data(DublinWind)

Format

This data frame contains the following columns:

speed numeric vector of average daily wind speed in knots

day an integer vector giving the day number of the year, i.e., one of 1:366.

Details

The periodic pattern along the 18 years measured and the autocorrelation are to be taken into account for analysis, see the references. This is Example 3 of the COBS paper.

Source

From shar file available from http://www.cba.nau.edu/pin-ng/cobs.html

Has also been available from Statlib; then, with more variables, e.g., in help(wind,package = "gstat") from CRAN package gstat.

References

Haslett, J. and Raftery, A. (1989) Space-Time Modelling with Long-Memory Dependence: Assessing Ireland's Wind Power Resource (with Discussion: 22-50). *Applied Statistics* **38**, 1–50. doi: 10.2307/2347679

COBS: Qualitatively Constrained Smoothing via Linear Programming; *Computational Statistics* **14**, 315–337.

He, X. and Ng, P. (1999) COBS: Qualitatively Constrained Smoothing via Linear Programming; *Computational Statistics* **14**, 315–337.

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Examples

```
data(DublinWind)
str(DublinWind)
plot(speed ~ day, data = DublinWind)# not so nice; want time scale
## transform 'day' to correct "Date" object; and then plot
Dday \leftarrow seq(from = as.Date("1961-01-01"), by = 1,
            length = nrow(DublinWind))
plot(speed ~ Dday, data = DublinWind, type = "1",
     main = paste("DublinWind speed daily data, n=",
                  nrow(DublinWind)))
##--- ^{\sim} He & Ng "Example 3" \% much more is in ../tests/wind.R
co.o50 <-
 with(DublinWind, ## use nknots > (default) 6 :
  cobs(day, speed, knots.add = TRUE, constraint= "periodic", nknots = 10,
       tau = .5, method = "uniform"))
summary(co.o50)
lines(Dday, fitted(co.o50), col=2, lwd = 2)
## the periodic "smooth" function - in one period
plot(predict(co.o50), type = "o", cex = 0.2, col=2,
     xlab = "day", ylim = c(0,20)
points(speed ~ day, data = DublinWind, pch = ".")
```

exHe

Small Dataset Example of He

Description

The exHe data frame has 10 rows and 2 columns. It is an example for which smooth.spline cannot be used.

Usage

```
data(exHe)
```

Format

This data frame contains the following columns:

```
x only values 0, 1, and 2.
```

y 10 randomly generated values

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Details

Xuming He wrote about this **JUST FOR FUN:**

I was testing COBS using the following "data". For comparison, I tried smooth.spline in S+. I never got an answer back! No warning messages either. The point is that even the well-tested algorithm like smooth.spline could leave you puzzled.

To tell you the truth, the response values here were generated by white noise. An ideal fitted curve would be a flat line. See for yourself what COBS would do in this case.

Source

Originally found at the bottom of http://ux6.cso.uiuc.edu/~x-he/ftp.html, the web resource directory of Xuming He at the time, say 2006.

See Also

cobs

Examples

globtemp

Annual Average Global Surface Temperature

Description

Time Series of length 113 of annual average global surface temperature deviations from 1880 to 1992.

Usage

```
data(globtemp)
```

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Details

This is Example 1 of the COBS paper, where the hypothesis of a monotonely increasing trend is considered; Koenker and Schorfheide (1994) consider modeling the autocorrelations.

Source

'temp.data' in file 'cobs.shar' available from http://www.cba.nau.edu/pin-ng/cobs.html.

References

He, X. and Ng, P. (1999) COBS: Qualitatively Constrained Smoothing via Linear Programming; *Computational Statistics* **14**, 315–337.

Koenker, R. and Schorfheide F. (1994) Quantile Spline Models for Global Temperature Change; *Climate Change* **28**, 395–404.

Examples

```
data(globtemp)
plot(globtemp, main = "Annual Global Temperature Deviations")
str(globtemp)
## forget about time-series, just use numeric vectors:
year <- as.vector(time(globtemp))</pre>
temp <- as.vector(globtemp)</pre>
##---- Code for Figure 1a of He and Ng (1999) ------
a50 <- cobs(year, temp, knots.add = TRUE, degree = 1, constraint = "increase")
summary(a50)
## As suggested in the warning message, we increase the number of knots to 9
a50 <- cobs(year, temp, nknots = 9, knots.add = TRUE, degree = 1,
            constraint = "increase")
summary(a50)
## Here, we use the same knots sequence chosen for the 50th percentile
a10 <- cobs(year, temp, nknots = length(a50$knots), knots = a50$knot,
            degree = 1, tau = 0.1, constraint = "increase")
summary(a10)
a90 <- cobs(year, temp, nknots = length(a50$knots), knots = a50$knot,
            degree = 1, tau = 0.9, constraint = "increase")
summary(a90)
which(hot.idx <- temp >= a90$fit)
which(cold.idx <- temp <= a10$fit)
normal.idx <- !hot.idx & !cold.idx
plot(year, temp, type = "n", ylab = "Temperature (C)", ylim = c(-.7,.6))
lines(predict(a50, year, interval = "both"), col = 2)
lines(predict(a10, year, interval = "both"), col = 3)
lines(predict(a90, year, interval = "both"), col = 3)
points(year, temp, pch = c(1,3)[2 - normal.idx])
```

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```
## label the "hot" and "cold" days
text(year[hot.idx], temp[hot.idx] + .03, labels = year[hot.idx])
text(year[cold.idx], temp[cold.idx] - .03, labels = year[cold.idx])
```

interpSplineCon

(Cubic) Interpolation Spline from "conreg"

Description

```
From a "conreg" object representing a linear spline,
```

interpSplineCon() produces the corresponding (cubic) spline (via package **splines**' interpSpline()) by interpolating at the knots, thus "smoothing the kinks".

isIsplineCon() determines if the spline fulfills the same convexity / concavity constraints as the underlying "conreg" object.

Usage

```
interpSplineCon(object, ...)
isIsplineCon(object, isp, ...)
```

Arguments

Value

```
interpSplineCon() returns the interpSpline() interpolation spline object.
```

isIsplineCon() is TRUE (or FALSE), indicating if the convexity/concavity constraints are fulfilled (in knot intervals).

Author(s)

Martin Maechler

See Also

```
conreg, interpSpline.
```

mk.pt.constr

Examples

mk.pt.constr

COBS auxiliary for constructing pointwise constraint specifications

Description

COBS (cobs) auxiliary function for constructing the pointwise constraint specification list from the pointwise 3-column matrix (as used as argument in cobs).

Usage

```
mk.pt.constr(pointwise)
```

Arguments

pointwise numeric 3-column matrix, see pointwise in cobs.

Value

A list with components

n.equal number of equality constraintsn.greater number of "greater" constraintsn.smaller number of "smaller" constraintsn.gradient number of gradient constraints

Unless the input pointwise was NULL, the result also has corresponding components:

equal 3-column matrix of equality constraints
greater 3-column matrix of "greater" constraints
smaller 3-column matrix of "smaller" constraints
gradient 3-column matrix of gradient constraints

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Author(s)

Martin Maechler

Examples

```
## from ?cobs:  x \leftarrow seq(-1,3,,150)   con \leftarrow rbind(c(1,min(x),0), # f(min(x)) >= 0   c(-1,max(x),1), # f(max(x)) <= 1   c(0, 0, 0.5))# f(0) = 0.5   r \leftarrow mk.pt.constr(con)   str(r)
```

plot.cobs

Plot Method for COBS Objects

Description

The plot method for cobs objects. If there was lambda selection, it provides two plots by default.

Usage

Arguments

```
object of class cobs.
Х
which
                   integer vector specifying which plots should be drawn;
show.k
                   logical indicating if the "effective dimensionality" k should also be shown. Only
                   applicable when which contains 1.
col, 1.col, k.col
                   colors for plotting; k.col only applies when show.k is true in the first plot
                   (which == 1) where 1.col[2] and k.col[2] are only used as well, for denoting
                   "doubtful" points; col is only used for the 2nd plot (which == 2).
                   line width and point size for the 2nd plot (i.e. which == 2).
lwd, cex
                   y-axis limits, see axis, with a smart default.
vlim
xlab, ylab, main
                   axis annotation; see also axis.
subtit
                   a vector of length 2, specifying a sub title for each plot (according to which).
                   further arguments passed and to internal plot methods.
```

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Details

plot(.) produces two side-by-side plots in case there was a search for the optimal lambda(which = 1:2), and only the (second) data plus spline curve plot otherwise (which = 2).

Author(s)

Martin Maechler

See Also

There are several other methods for COBS objects, see, e.g. summary.cobs or predict.cobs. cobs for examples.

Examples

```
example(cobs)

plot(Sbs)
plot(fitted(Sbs), resid(Sbs),
    main = "Tukey-Anscombe plot for cobs()",
    sub = deparse(Sbs$call))
```

predict.cobs

Predict method for COBS Fits

Description

Compute predicted values and simultaneous or pointwise confidence bounds for cobs objects.

Usage

Arguments

object	object of class cobs.
Z	vector of grid points at which the fitted values are evaluated; defaults to an equally spaced grid with nz grid points between minz and maxz. Note that now z may lie outside of the knots interval which was not allowed originally.
deriv	scalar integer specifying (the order of) the derivative that should be computed.
minz	numeric needed if z is not specified; defaults to $min(x)$ or the first knot if knots are given.

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maxz analogous to minz; defaults to max(x) or the last knot if knots are given.

nz number of grid points in z if that is not given; defaults to 100.

interval type of interval calculation, see below

level confidence level

... further arguments passed to and from methods.

Value

a matrix of predictions and bounds if interval is set (not "none"). The columns are named z, fit, further cb.lo and cb.up for the simultaneous confidence band, and ci.lo and ci.up the pointwise confidence intervals according to specified level.

If z has been specified, it is unchanged in the result.

Author(s)

Martin Maechler, based on He and Ng's code in cobs().

See Also

cobs the model fitting function.

Examples

qbsks2

Quantile B-Spline with Fixed Knots

Description

Compute B-spline coefficients for regression quantile B-spline with stepwise knots selection and quantile B-spline with fixed knots **regression spline**, using Ng (1996)'s algorithm.

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Usage

```
qbsks2(x,y,w,pw, knots,nknots, degree,Tlambda, constraint, ptConstr,
    maxiter, trace, nrq,nl1, neqc, tau, select.lambda,
    ks, do.select, knots.add, repeat.delete.add, ic, print.mesg,
    give.pseudo.x = TRUE,
    rq.tol = 1e-8, tol.kn = 1e-6, tol.0res = 1e-6, print.warn, nk.start)
```

numeric vector, sorted increasingly, the abscissa values

Arguments x

numeric, same length as x, the observations. y numeric vector of weights, same length as x, as in cobs. W penalty weights vector pw knots numeric vector of knots of which nknots will be used. number of knots to be used. nknots degree integer specifying polynomial degree; must be 1 or 2. Tlambda (vector of) smoothing parameter(s) λ , see drqssbc2. constraint string (or empty) specifying the global constraints; see cobs. ptConstr list of pointwise constraints. maxiter non-negative integer: maximal number of iterations, passed to drgssbc2. trace integer or logical indicating the tracing level of the underlying algorithms; not implemented (due to lack of trace in quantreg ...) nrq,nl1,neqc integers specifying dimensionalities, directly passed to drqssbc2, see there. tau desired quantile level (in interval (0, 1)). select.lambda passed to drgssbc2, see there. number used as offset in SIC/AIC/BIC. do.select logical indicating if knots shall be selected (instead of used as specified). knots.add, repeat.delete.add logicals, see cobs. information criterion to use, see cobs. ic an integer indicating how qbsks2() should print message about its current stages. print.mesg logical indicating if the pseudo design matrix \tilde{X} should be returned (as *sparse* give.pseudo.x matrix). numeric convergence tolerance for the interior point algorithm called from rq.fit.sfnc() rq.tol or rq.fit.sfn().

tol.kn "tolerance" for shifting the outer knots.

tol. 0res tolerance passed to drqssbc2.

print.warn flag indicating if and how much warnings and information is to be printed; cur-

rently just passed to drqssbc2.

nk.start number of starting knots used in automatic knot selection.

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Details

This is an auxiliary function for cobs(*,lambda = 0), possibly interesting on its own. This documentation is currently sparse; read the source code!

Value

a list with components

coef .. fidel ..

k dimensionality of model fit.

if1 integer "flag"; the return code.

icyc integer of length 2, see cobs.

knots the vector of inner knots.

nknots the number of inner knots.

nvar the number of "variables", i.e. unknowns including constraints.

lambda the penalty factor, chosen or given.

pseudo.x the pseudo design matrix X, as returned from drqssbc2.

Author(s)

Pin Ng; this help page: Martin Maechler.

References

Ng, P. (1996) An Algorithm for Quantile Smoothing Splines, *Computational Statistics* & *Data Analysis* 22, 99–118.

See also the references in cobs.

See Also

the main function cobs; further drqssbc2 which is called from qbsks2().

USArmyRoofs Roof Quality in US Army Bases

Description

The USArmyRoofs data frame has 153 observations of roof sections of US Army bases and 2 columns, age and fci. This is Example 2 of He & Ng (1999).

Usage

data(USArmyRoofs)

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Format

This data frame contains the following columns:

age numeric vector giving the roof's age in years.

fci numeric, giving the FCI, the flash condition index, i.e., the percentage of flashing which is in good condition.

Source

From shar file available from http://www.cba.nau.edu/pin-ng/cobs.html

References

He, X. and Ng, P. (1999) COBS: Qualitatively Constrained Smoothing via Linear Programming; *Computational Statistics* **14**, 315–337.

Examples

```
data(USArmyRoofs)
plot(fci ~ age, data = USArmyRoofs, main = "US Army Roofs data")
```

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