# Package 'cOde'

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<b>Description</b> Generates all necessary C functions allowing the user to work with the compiled-code interface of ode() and bvptwp(). The implementation supports ``forcings" and ``events". Also provides functions to symbolically compute Jacobians, sensitivity equations and adjoint sensitivities being the basis for sensitivity analysis.					
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adjointSymb

Compute adjoint equations of a function symbolically

## **Description**

Compute adjoint equations of a function symbolically

## Usage

```
adjointSymb(f, states = names(f), parameters = NULL, inputs = NULL)
```

## **Arguments**

f Named vector of type character, the functions

states Character vector of the ODE states for which observations are available

parameters Character vector of the parameters

inputs Character vector of the "variable" input states, i.e. time-dependent parameters

(in contrast to the forcings).

#### **Details**

The adjoint equations are computed with respect to the functional

$$(x,u) \mapsto \int_0^T \|x(t) - x^D(t)\|^2 + \|u(t) - u^D(t)\|^2 dt,$$

where x are the states being constrained by the ODE, u are the inputs and xD and uD indicate the trajectories to be best possibly approached. When the ODE is linear with respect to u, the attribute inputs of the returned equations can be used to replace all occurences of u by the corresponding character in the attribute. This guarantees that the input course is optimal with respect to the above function.

## Value

Named vector of type character with the adjoint equations. The vector has attributes "chi" (integrand of the chisquare functional), "grad" (integrand of the gradient of the chisquare functional), "forcings" (character vector of the forcings necessary for integration of the adjoint equations) and "inputs" (the input expressed as a function of the adjoint variables).

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```
## Not run:
## Solve an optimal control problem:
library(bvpSolve)
# 02 + 0 <-> 03
# 03 is removed by a variable rate u(t)
f <- c(
 03 = "build_03 * 02 * 0 - decay_03 * 03 - u * 03",
 02 = \text{"-build}_03 * 02 * 0 + \text{decay}_03 * 03"
 0 = \text{"-build_03} * 02 * 0 + \text{decay_03} * 03"
)
# Compute adjoints equations and replace u by optimal input
f_a <- adjointSymb(f, states = c("03"), inputs = "u")
inputs <- attr(f_a, "inputs")</pre>
f_tot <- replaceSymbols("u", inputs, c(f, f_a))</pre>
forcings <- attr(f_a, "forcings")</pre>
# Initialize times, states, parameters
times <- seq(0, 15, by = .1)
boundary <- data.frame(</pre>
 name = c("03", "02", "0", "adj03", "adj02", "adj0"),
 yini = c(0.5, 2, 2.5, NA, NA, NA),
 yend = c(NA, NA, NA, 0, 0, 0)
pars <- c(build_03 = .2, decay_03 = .1, eps = 1)
# Generate ODE function
func <- funC(f = f_tot, forcings = forcings,</pre>
            jacobian = "full", boundary = boundary,
            modelname = "example5")
# Initialize forcings (the objective)
forcData <- data.frame(time = times,</pre>
                      name = rep(forcings, each=length(times)),
                      value = rep(
                        c(0.5, 0, 1, 1), each=length(times)))
forc <- setForcings(func, forcData)</pre>
# Solve BVP
out <- bvptwpC(x = times, func = func, parms = pars, forcings = forc)</pre>
# Plot solution
par(mfcol=c(1,2))
t <- out[,1]
M1 \leftarrow out[,2:4]
M2 \leftarrow with(list(uD = 0, 03 = out[,2],
```

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bvptwpC

Interface to bvptwp()

## **Description**

Interface to bvptwp()

## Usage

```
bvptwpC(yini = NULL, x, func, yend = NULL, parms, xguess = NULL,
  yguess = NULL, ...)
```

## Arguments

yini	named vector of type numeric. Initial values to be overwritten.
X	vector of type numeric. Integration times
func	return value from funC() with a boundary argument.
yend	named vector of type numeric. End values to be overwritten.
parms	named vector of type numeric. The dynamic parameters.
xguess	vector of type numeric, the x values
yguess	matrix with as many rows as variables and columns as x values
	further arguments going to bvptwp()

#### **Details**

See bvpSolve-package for a full description of possible arguments

#### Value

matrix with times and states

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```
## Not run:
## Boundary value problem: Ozon formation with fixed ozon/oxygen ratio
## at final time point
library(bvpSolve)
# 02 + 0 <-> 03
# diff = 02 - 03
# build_03 = const.
f <- c(
 03 = "build_03 * 02 * 0 - decay_03 * 03"
 02 = \text{"-build}_03 * 02 * 0 + \text{decay}_03 * 03"
 0 = \text{"-build_03} * 02 * 0 + \text{decay_03} * 03\text{"},
 diff = "-2 * build_03 * 02 * 0 + 2 * decay_03 * 03",
 build_03 = "0"
)
bound <- data.frame(</pre>
   name = names(f),
   yini = c(0, 3, 2, 3, NA),
   yend = c(NA, NA, NA, 0, NA)
)
# Generate ODE function
func <- funC(f, jacobian="full", boundary = bound, modelname = "example4")</pre>
# Initialize times, states, parameters and forcings
times <- seq(0, 15, by = .1)
pars < c(decay_03 = .1)
xguess <- times
yguess <- matrix(c(1, 1, 1, 1, 1), ncol=length(times),
                nrow = length(f)
# Solve BVP
out <- bvptwpC(x = times, func = func, parms = pars,
             xguess = xguess, yguess = yguess)
# Solve BVP for different ini values, end values and parameters
yini <- c(03 = 2)
yend <- c(diff = 0.2)
pars < c(decay_03 = .01)
out <- bvptwpC(yini = yini, yend = yend, x = times, func = func,
      parms = pars, xguess = xguess, yguess = yguess)
# Plot solution
par(mfcol=c(1,2))
t <- out[,1]
M1 <- out[,2:5]
```

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compileAndLoad

Compile and load shared object implementing the ODE system.

#### Description

Compile and load shared object implementing the ODE system.

#### **Usage**

```
compileAndLoad(filename, dllname, fcontrol, verbose)
```

## Arguments

filename Full file name of the source file.

dllname Base name for source and dll file.

fcontrol Interpolation method for forcings.

verbose Print compiler output or not.

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forcData

Forcings data.frame

## Description

Forcings data.frame

funC 7

:

Generate C code for a function and compile it

## Description

Generate C code for a function and compile it

## Usage

```
funC(f, forcings = NULL, events = NULL, fixed = NULL,
  outputs = NULL, jacobian = c("none", "full", "inz.lsodes",
  "jacvec.lsodes"), rootfunc = NULL, boundary = NULL, compile = TRUE,
  fcontrol = c("nospline", "einspline"), nGridpoints = -1,
  includeTimeZero = TRUE, precision = 1e-05, modelname = NULL,
  verbose = FALSE, solver = c("deSolve", "Sundials"))
```

## Arguments

f	Named character vector containing the right-hand sides of the ODE. You may use the key word time in your equations for non-autonomous ODEs.
forcings	Character vector with the names of the forcings
events	data.frame of events with columns "var" (character, the name of the state to be affected), "time" (numeric or character, time point), "value" (numeric or character, value), "method" (character, either "replace" or "add"). See events. If "var" and "time" are characters, their values need to be speciefied in the parameter vector when calling odeC. An event function is generated and compiled with the ODE.
fixed	character vector with the names of parameters (initial values and dynamic) for which no sensitivities are required (will speed up the integration).
outputs	Named character vector for additional output variables, see arguments nout and outnames of lsode
jacobian	Character, either "none" (no jacobian is computed), "full" (full jacobian is computed and written as a function into the C file) or "inz.lsodes" (only the non-zero elements of the jacobian are determined, see lsodes)
rootfunc	Named character vector. The root function (see Isoda). Besides the variable names (names(f)) also other symbols are allowed that are treated like new parameters.
boundary	data.frame with columns name, yini, yend specifying the boundary condition set-up. NULL if not a boundary value problem
compile	Logical. If FALSE, only the C file is written
fcontrol	Character, either "nospline" (default, forcings are handled by deSolve) or "einspline" (forcings are handled as splines within the C code based on the einspline library).

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nGridpoints

Integer, defining for which time points the ODE is evaluated or the solution is returned: Set -1 to return only the explicitly requested time points (default). If additional time points are introduced through events, they will not be returned. Set >= 0 to introduce additional time points between tmin and tmax where the ODE is evaluated in any case. Additional time points that might be introduced by events will be returned. If splines are used with fcontrol = "einspline", nGridpoinnts also indicates the number of spline nodes.

includeTimeZero

Logical. Include t = 0 in the integration time points if TRUE (default). Consequently, integration starts at t = 0 if only positive time points are provided by the user and at train if also positive time points are provided.

user and at tmin, if also negtive time points are provided.

precision Numeric. Only used when fcontrol = "einspline".

modelname Character. The C file is generated in the working directory and is named <mod-

elname>.c. If NULL, a random name starting with ".f" is chosen, i.e. the file is

hidden on a UNIX system.

verbose Print compiler output to R command line.

solver Select the solver suite as either deSolve or Sundials (not available any more).

Defaults to deSolve.

#### **Details**

The function replaces variables by arrays y[i], etc. and replaces "^" by pow() in order to have the correct C syntax. The file name of the C-File is derived from f. I.e. funC(abc, ... will generate a file abc.c in the current directory. Currently, only explicit ODE specification is supported, i.e. you need to have the right-hand sides of the ODE.

#### Value

the name of the generated shared object file together with a number of attributes

```
## Not run:
# Exponential decay plus constant supply
f <- c(x = "-k*x + supply")
func <- funC(f, forcings = "supply")

# Example 2: root function
f <- c(A = "-k1*A + k2*B", B = "k1*A - k2*B")
rootfunc <- c(steadyState = "-k1*A + k2*B - tol")

func <- funC(f, rootfunc = rootfunc, modelname = "test")

yini <- c(A = 1, B = 2)
parms <- c(k1 = 1, k2 = 5, tol = 0.1)
times <- seq(0, 10, len = 100)

odeC(yini, times, func, parms)

## End(Not run)</pre>
```

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getSymbols

Get symbols from a character

## **Description**

Get symbols from a character

## Usage

```
getSymbols(char, exclude = NULL)
```

## Arguments

char Character vector (e.g. equation)

exclude Character vector, the symbols to be excluded from the return value

## Value

character vector with the symbols

#### **Examples**

```
getSymbols(c("A*AB+B^2"))
```

jacobianSymb

Compute Jacobian of a function symbolically

## **Description**

Compute Jacobian of a function symbolically

## Usage

```
jacobianSymb(f, variables = NULL)
```

#### **Arguments**

f named vector of type character, the functions

variables other variables, e.g. paramters, f depends on. If variables is given, f is derived

with respect to variables instead of names(f)

## Value

named vector of type character with the symbolic derivatives

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#### **Examples**

```
jacobianSymb(c(A="A*B", B="A+B"))
jacobianSymb(c(x="A*B", y="A+B"), c("A", "B"))
```

odeC

Interface to ode()

## Description

```
Interface to ode()
```

#### Usage

```
odeC(y, times, func, parms, ...)
```

## **Arguments**

y named vector of type numeric. Initial values for the integration

times vector of type numeric. Integration times. If includeTimeZero is TRUE (see

funC), the times vector is augmented by t = 0. If nGridpoints (see funC) was set  $\geq 0$ , uniformly distributed time points between the first and last time point are introduced and the solution is returned for these time points, too. Any additional time points that are introduced during integration (e.g. event time points)

are returned unless nGridpoints = -1 (the default).

func return value from funC()

parms named vector of type numeric.

... further arguments going to ode()

#### **Details**

See deSolve-package for a full description of possible arguments

#### Value

matrix with times and states

odeC

```
# 02 + 0 <-> 03
f <- c(
 03 = " (build_03 + u_build) * 02 * 0 - (decay_03 + u_degrade) * <math>03",
 02 = "-(build_03 + u_build) * 02 * 0 + (decay_03 + u_degrade) * 03",
  0 = "-(build_03 + u_build) * 02 * 0 + (decay_03 + u_degrade) * 03"
)
# Generate ODE function
forcings <- c("u_build", "u_degrade")</pre>
func <- funC(f, forcings = forcings, modelname = "test",</pre>
            fcontrol = "nospline", nGridpoints = 10)
# Initialize times, states, parameters and forcings
times <- seq(0, 8, by = .1)
yini < -c(03 = 0, 02 = 3, 0 = 2)
pars <- c(build_03 = 1/6, decay_03 = 1)
forc <- setForcings(func, forcData)</pre>
# Solve ODE
out <- odeC(y = yini, times = times, func = func, parms = pars,
           forcings = forc)
# Plot solution
par(mfcol=c(1,2))
t1 <- unique(forcData[,2])</pre>
M1 <- matrix(forcData[,3], ncol=2)</pre>
t2 <- out[,1]
M2 \leftarrow out[,2:4]
M3 <- out[,5:6]
matplot(t1, M1, type="l", lty=1, col=1:2, xlab="time", ylab="value",
main="forcings", ylim=c(0, 4))
matplot(t2, M3, type="1", lty=2, col=1:2, xlab="time", ylab="value",
main="forcings", add=TRUE)
legend("topleft", legend = c("u_build", "u_degrade"), lty=1, col=1:2)
matplot(t2, M2, type="1", lty=1, col=1:3, xlab="time", ylab="value",
main="response")
legend("topright", legend = c("03", "02", "0"), lty=1, col=1:3)
## Ozone formation and decay, modified by events
f <- c(
 03 = " (build_03 + u_build) * 02 * 0 -
        (decay_03 + u_degrade) * 03",
```

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```
02 = "-(build_03 + u_build) * 02 * 0 +
         (decay_03 + u_degrade) * 03",
  0 = "-(build_03 + u_build) * 02 * 0 +
         (decay_03 + u_degrade) * 03",
  u_build = "0",  # piecewise constant
  u_degrade = "0"  # piecewise constant
# Define parametric events
events.pars <- data.frame(</pre>
  var = c("u_degrade", "u_degrade", "u_build"),
  time = c("t_on", "t_off", "2"),
  value = c("plus", "minus", "2"),
  method = "replace"
)
# Declar parameteric events when generating funC object
func <- funC(f, forcings = NULL, events = events.pars, modelname = "test",</pre>
             fcontrol = "nospline", nGridpoints = -1)
# Set Parameters
yini <- c(03 = 0, 02 = 3, 0 = 2, u_build = 1, u_degrade = 1)
times <- seq(0, 8, by = .1)
pars <- c(build_03 = 1/6, decay_03 = 1, t_on = exp(rnorm(1, 0)), t_off = 6, plus = 3, minus = 1)
# Solve ODE with additional fixed-value events
out <- odeC(y = yini, times = times, func = func, parms = pars)</pre>
# Plot solution
par(mfcol=c(1,2))
t2 <- out[,1]
M2 <- out[,2:4]
M3 <- out[,5:6]
matplot(t2, M3, type="1", lty=2, col=1:2, xlab="time", ylab="value",
        main="events")
legend("topleft", legend = c("u_build", "u_degrade"), lty=1, col=1:2)
matplot(t2, M2, type="l", lty=1, col=1:3, xlab="time", ylab="value",
        main="response")
legend("topright", legend = c("03", "02", "0"), lty=1, col=1:3)
## End(Not run)
```

oxygenData

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## **Description**

Forcings data.frame

prodSymb

Compute matrix product symbolically

## Description

Compute matrix product symbolically

#### Usage

```
prodSymb(M, N)
```

## **Arguments**

M matrix of type character
N matrix of type character

#### Value

Matrix of type character, the matrix product of M and N

reduceSensitivities reduceSensitivities

## Description

reduceSensitivities

## Usage

```
reduceSensitivities(sens, vanishing)
```

## Arguments

sens Named character, the sensitivity equations vanishing Character, names of the vanishing sensitivities

## **Details**

Given the set vanishing of vanishing sensitivities, the algorithm determins sensitivities that vanish as a consequence of the first set.

## Value

Named character, the sensitivity equations with zero entries for vanishing sensitivities.

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replaceNumbers

Replace integer number in a character vector by other double

## **Description**

Replace integer number in a character vector by other double

## Usage

```
replaceNumbers(x)
```

## **Arguments**

Х

vector of type character, the object where the replacement should take place

#### Value

vector of type character, conserves the names of x.

replaceOperation

Replace a binary operator in a string by a function

## Description

Replace a binary operator in a string by a function

#### Usage

```
replaceOperation(what, by, x)
```

## **Arguments**

what character, the operator symbol, e.g. "^" by character, the function string, e.g. "pow"

x vector of type character, the object where the replacement should take place

## Value

vector of type character

```
replaceOperation("^", "pow", "(x^2 + y^2)^.5")
```

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Replace symbols in a character vector by other symbols

## **Description**

Replace symbols in a character vector by other symbols

## Usage

```
replaceSymbols(what, by, x)
```

## Arguments

what	vector of type character, the symbols to be replaced, e.g. c("A", "B")
by	vector of type character, the replacement, e.g. $c("x[0]", "x[1]")$
x	vector of type character, the object where the replacement should take place

## Value

vector of type character, conserves the names of x.

## **Examples**

```
replaceSymbols(c("A", "B"), c("x[0]", "x[1]"), c("A*B", "A+B+C"))
```

sensitivitiesSymb

Compute sensitivity equations of a function symbolically

## Description

Compute sensitivity equations of a function symbolically

## Usage

```
sensitivitiesSymb(f, states = names(f), parameters = NULL,
inputs = NULL, events = NULL, reduce = FALSE)
```

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## Arguments

f	named vector of type character, the functions
states	Character vector. Sensitivities are computed with respect to initial values of these states
parameters	Character vector. Sensitivities are computed with respect to initial values of these parameters
inputs	Character vector. Input functions or forcings. They are excluded from the computation of sensitivities.
events	data.frame of events with columns "var" (character, the name of the state to be affected), "time" (numeric or character, time point), "value" (numeric or character, value), "method" (character, either "replace" or "add"). See events. Within sensitivitiesSymb() a data.frame of additional events is generated to reset the sensitivities appropriately, depending on the event method.
reduce	Logical. Attempts to determine vanishing sensitivities, removes their equations and replaces their right-hand side occurences by 0.

#### **Details**

The sensitivity equations are ODEs that are derived from the original ODE f. They describe the sensitivity of the solution curve with respect to parameters like initial values and other parameters contained in f. These equtions are also useful for parameter estimation by the maximum-likelihood method. For consistency with the time-continuous setting provided by adjointSymb, the returned equations contain attributes for the chisquare functional and its gradient.

### Value

Named vector of type character with the sensitivity equations. Furthermore, attributes "chi" (the integrand of the chisquare functional), "grad" (the integrand of the gradient of the chisquare functional), "forcings" (Character vector of the additional forcings being necessare to compute chi and grad) and "yini" (The initial values of the sensitivity equations) are returned.

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```
# Compute sensitivity equations
f_s <- sensitivitiesSymb(f)</pre>
# Generate ODE function
func <- funC(c(f, f_s))
# Initialize times, states, parameters and forcings
times <- seq(0, 15, by = .1)
yini <- c(03 = 0, 02 = 3, 0 = 2, attr(f_s, "yini"))
pars <- c(build_03 = .1, decay_03 = .01)
# Solve ODE
out <- odeC(y = yini, times = times, func = func, parms = pars)
# Plot solution
par(mfcol=c(2,3))
t <- out[,1]
M1 <- out[,2:4]
M2 \leftarrow out[,5:7]
M3 <- out[,8:10]
M4 <- out[,11:13]
M5 <- out[,14:16]
M6 <- out[,17:19]
matplot(t, M1, type="l", lty=1, col=1:3,
       xlab="time", ylab="value", main="solution")
legend("topright", legend = c("03", "02", "0"), lty=1, col=1:3)
matplot(t, M2, type="1", lty=1, col=1:3,
       xlab="time", ylab="value", main="d/(d 03)")
matplot(t, M3, type="1", lty=1, col=1:3,
       xlab="time", ylab="value", main="d/(d 02)")
matplot(t, M4, type="l", lty=1, col=1:3,
       xlab="time", ylab="value", main="d/(d 0)")
matplot(t, M5, type="l", lty=1, col=1:3,
       xlab="time", ylab="value", main="d/(d build_03)")
matplot(t, M6, type="l", lty=1, col=1:3,
       xlab="time", ylab="value", main="d/(d decay_03)")
## End(Not run)
## Not run:
## Estimate parameter values from experimental data
library(deSolve)
# 02 + 0 <-> 03
# diff = 02 - 03
# build_03 = const.
f <- c(
 03 = "build_03 * 02 * 0 - decay_03 * 03",
```

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```
02 = \text{"-build}_03 * 02 * 0 + \text{decay}_03 * 03",
  0 = \text{"-build_03} * 02 * 0 + \text{decay_03} * 03"
)
# Compute sensitivity equations and get attributes
f_s <- sensitivitiesSymb(f)</pre>
chi <- attr(f_s, "chi")</pre>
grad <- attr(f_s, "grad")</pre>
forcings <- attr(f_s, "forcings")</pre>
# Generate ODE function
func <- funC(f = c(f, f_s, chi, grad), forcings = forcings,
              fcontrol = "nospline", modelname = "example3")
# Initialize times, states, parameters
times <- seq(0, 15, by = .1)
yini < -c(03 = 0, 02 = 2, 0 = 2.5)
yini_s <- attr(f_s, "yini")</pre>
yini_chi <- c(chi = 0)
yini_grad <- rep(0, length(grad)); names(yini_grad) <- names(grad)</pre>
pars <- c(build_03 = .2, decay_03 = .1)
# Initialize forcings (the data)
data(oxygenData)
forcData <- data.frame(time = oxygenData[,1],</pre>
                        name = rep(
                          colnames(oxygenData[,-1]),
                           each=dim(oxygenData)[1]),
                        value = as.vector(oxygenData[,-1]))
forc <- setForcings(func, forcData)</pre>
# Solve ODE
out <- odeC(y = c(yini, yini_s, yini_chi, yini_grad),</pre>
            times = times, func = func, parms = pars, forcings = forc,
            method = "lsodes")
# Plot solution
par(mfcol=c(1,2))
t <- out[,1]
M1 <- out[,2:4]
M2 <- out[,names(grad)]</pre>
tD <- oxygenData[,1]
M1D <- oxygenData[,2:4]</pre>
matplot(t, M1, type="l", lty=1, col=1:3,
        xlab="time", ylab="value", main="states")
matplot(tD, M1D, type="b", lty=2, col=1:3, pch=4, add=TRUE)
legend("topright", legend = names(f), lty=1, col=1:3)
matplot(t, M2, type="1", lty=1, col=1:5,
        xlab="time", ylab="value", main="gradient")
legend("topleft", legend = names(grad), lty=1, col=1:5)
# Define objective function
```

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```
obj <- function(p) {</pre>
  out <- odeC(y = c(p[names(f)], yini_s, yini_chi, yini_grad),</pre>
              times = times, func = func, parms = p[names(pars)],
      forcings = forc, method="lsodes")
  value <- as.vector(tail(out, 1)[,"chi"])</pre>
  gradient <- as.vector(</pre>
    tail(out, 1)[,paste("chi", names(p), sep=".")])
  hessian <- gradient%*%t(gradient)</pre>
  return(list(value = value, gradient = gradient, hessian = hessian))
}
# Fit the data
myfit <- optim(par = c(yini, pars),</pre>
               fn = function(p) obj(p)$value,
                gr = function(p) obj(p)$gradient,
               method = "L-BFGS-B",
               lower=0,
               upper=5)
# Model prediction for fit parameters
prediction <- odeC(y = c(myfit*par[1:3], yini_s, yini_chi, yini_grad),</pre>
                   times = times, func = func, parms = myfit$par[4:5],
   forcings = forc, method = "lsodes")
# Plot solution
par(mfcol=c(1,2))
t <- prediction[,1]
M1 <- prediction[,2:4]
M2 <- prediction[,names(grad)]</pre>
tD <- oxygenData[,1]</pre>
M1D <- oxygenData[,2:4]
matplot(t, M1, type="l", lty=1, col=1:3,
        xlab="time", ylab="value", main="states")
matplot(tD, M1D, type="b", lty=2, col=1:3, pch=4, add=TRUE)
legend("topright", legend = names(f), lty=1, col=1:3)
matplot(t, M2, type="l", lty=1, col=1:5,
        xlab="time", ylab="value", main="gradient")
legend("topleft", legend = names(grad), lty=1, col=1:5)
## End(Not run)
```

setForcings

Generate interpolation spline for the forcings and write into list of matrices

20 sumSymb

## **Description**

Generate interpolation spline for the forcings and write into list of matrices

#### Usage

```
setForcings(func, forcings)
```

## **Arguments**

func result from funC()

forcings data.frame with columns name (factor), time (numeric) and value (numeric)

#### **Details**

Splines are generated for each name in forcings and both, function value and first derivative are evaluated at the time points of the data frame.

#### Value

list of matrices with time points and values assigned to the forcings interface of deSolve

#### **Examples**

```
f <- c(x = "-k*x + a - b") func <- funC(f, forcings = c("a", "b")) forcData <- rbind( \\ data.frame(name = "a", time = c(0, 1, 10), value = c(0, 5, 2)), \\ data.frame(name = "b", time = c(0, 5, 10), value = c(1, 3, 6))) forc <- setForcings(func, forcData)
```

sumSymb

Compute matrix sumSymbolically

#### **Description**

Compute matrix sumSymbolically

### Usage

```
sumSymb(M, N)
```

#### **Arguments**

M matrix of type character
N matrix of type character

#### Value

Matrix of type character, the matrix sum of M and N

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