Package 'cAIC4'

December 18, 2019

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Description

Provides functions for the estimation of the conditional Akaike information in generalized mixed-effect models fitted with (g)lmer() from 'lme4', lme() from 'nlme' and gamm() from 'mgcv'.

Details

The DESCRIPTION file:

Package: cAIC4 Type: Package

Title: Conditional Akaike Information Criterion for 'lme4' and 'nlme'

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Suggests: gamm4

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malnutrition

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Author(s)

Benjamin Saefken, David Ruegamer, Philipp Baumann and Rene-Marcel Kruse, with contributions from Sonja Greven and Thomas Kneib

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References

Saefken, B., Kneib T., van Waveren C.-S. and Greven, S. (2014) A unifying approach to the estimation of the conditional Akaike information in generalized linear mixed models. Electronic Journal Statistics Vol. 8, 201-225.

Greven, S. and Kneib T. (2010) On the behaviour of marginal and conditional AIC in linear mixed models. Biometrika 97(4), 773-789.

Efron, B. (2004) The estimation of prediction error. J. Amer. Statist. Ass. 99(467), 619-632.

See Also

1me4

Examples

```
b <- lmer(Reaction ~ Days + (Days | Subject), sleepstudy)
cAIC(b)</pre>
```

anocAIC

Comparison of several lmer objects via cAIC

Description

Takes one or more 1mer-objects and produces a table to the console.

Usage

```
anocAIC(object, ..., digits = 2)
```

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Arguments

object a fitted lme4-object

... additional objects of the same type

digits number of digits to print

Value

a table comparing the cAIC relevant information of all models

See Also

cAIC for the model fit.

cAIC

Conditional Akaike Information for 'lme4' and 'lme'

Description

Estimates the conditional Akaike information for models that were fitted in 'lme4' or with 'lme'. Currently all distributions are supported for 'lme4' models, based on parametric conditional bootstrap. For the Gaussian distribution (from a lmer or lme call) and the Poisson distribution analytical estimators for the degrees of freedom are available, based on Stein type formulas. Also the conditional Akaike information for generalized additive models based on a fit via the 'gamm4' or gamm calls from the 'mgcv' package can be estimated. A hands-on tutorial for the package can be found at https://arxiv.org/abs/1803.05664.

Usage

```
cAIC(object, method = NULL, B = NULL, sigma.penalty = 1, analytic = TRUE)
```

Arguments

object An object of class merMod either fitted by 1mer or glmer of the lme4-package

or an 1me object fro the nlme-package. Also objects returned form a gamm4 call

are possible.

method Either "conditionalBootstrap" for the estimation of the degrees of freedom

with the help of conditional Bootstrap or "steinian" for analytical representations based on Stein type formulas. The default is NULL. In this case the method is choosen automatically based on the family argument of the (g)lmer-object. For "gaussian" and "poisson" this is the Steinian type estimator, for all others it is the conditional Bootstrap. For models from the nlme package, only lme

objects, i.e., with gaussian response are supported.

B Number of Bootstrap replications. The default is NULL. Then B is the minimum

of 100 and the length of the response vector.

cAIC

sigma.penalty An integer value for additional penalization in the analytic Gaussian calculation

to account for estimated variance components in the residual (co-)variance. Per default sigma.penalty is equal 1, corresponding to a diagonal error covariance matrix with only one estimated parameter (sigma). If all variance components are known, the value should be set to 0. For individual weights (individual variances), this value should be set to the number of estimated weights. For lme objects the penalty term is automatically set by extracting the number of

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estimated variance components.

FALSE if the numeric hessian of the (restricted) marginal log-likelihood from the lmer optimization procedure should be used. Otherwise (default) TRUE, i.e. use a analytical version that has to be computed. Only used for the analytical

version of Gaussian responses.

Details

analytic

For method = "steinian" and an object of class merMod computed the analytic representation of the corrected conditional AIC in Greven and Kneib (2010). This is based on a the Stein formula and uses implicit differentiation to calculate the derivative of the random effects covariance parameters w.r.t. the data. The code is adapted form the one provided in the supplementary material of the paper by Greven and Kneib (2010). The supplied merMod model needs to be checked if a random effects covariance parameter has an optimum on the boundary, i.e. is zero. And if so the model needs to be refitted with the according random effect terms omitted. This is also done by the function and the refitted model is also returned. Notice that the boundary tol argument in lmerControl has an impact on whether a parameter is estimated to lie on the boundary of the parameter space. For estimated error variance the degrees of freedom are increased by one per default. sigma.penalty can be set manually for merMod models if no (0) or more than one variance component (>1) has been estimated. For lme objects this value is automatically defined.

If the object is of class merMod and has family = "poisson" there is also an analytic representation of the conditional AIC based on the Chen-Stein formula, see for instance Saefken et. al (2014). For the calculation the model needs to be refitted for each observed response variable minus the number of response variables that are exactly zero. The calculation therefore takes longer then for models with Gaussian responses. Due to the speed and stability of 'lme4' this is still possible, also for larger datasets.

If the model has Bernoulli distributed responses and method = "steinian", cAIC calculates the degrees of freedom based on a proposed estimator by Efron (2004). This estimator is asymptotically unbiased if the estimated conditional mean is consistent. The calculation needs as many model refits as there are data points.

Another more general method for the estimation of the degrees of freedom is the conditional bootstrap. This is proposed in Efron (2004). For the B boostrap samples the degrees of freedom are estimated by

$$\frac{1}{B-1}\sum_{i=1}^n \theta_i(z_i)(z_i-\bar{z}),$$

where $\theta_i(z_i)$ is the i-th element of the estimated natural parameter.

For models with no random effects, i.e. (g)lms, the cAIC function returns the AIC of the model with scale parameter estimated by REML.

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Value

A cAIC object, which is a list consisting of: 1. the conditional log likelihood, i.e. the log likelihood with the random effects as penalized parameters; 2. the estimated degrees of freedom; 3. a list element that is either NULL if no new model was fitted otherwise the new (reduced) model, see details; 4. a boolean variable indicating whether a new model was fitted or not; 5. the estimator of the conditional Akaike information, i.e. minus twice the log likelihood plus twice the degrees of freedom.

WARNINGS

Currently the cAIC can only be estimated for family equal to "gaussian", "poisson" and "binomial". Neither negative binomial nor gamma distributed responses are available. Weighted Gaussian models are not yet implemented.

Author(s)

Benjamin Saefken, David Ruegamer

References

Saefken, B., Ruegamer, D., Kneib, T. and Greven, S. (2018): Conditional Model Selection in Mixed-Effects Models with cAIC4. https://arxiv.org/abs/1803.05664

Saefken, B., Kneib T., van Waveren C.-S. and Greven, S. (2014) A unifying approach to the estimation of the conditional Akaike information in generalized linear mixed models. Electronic Journal Statistics Vol. 8, 201-225.

Greven, S. and Kneib T. (2010) On the behaviour of marginal and conditional AIC in linear mixed models. Biometrika 97(4), 773-789.

Efron, B. (2004) The estimation of prediction error. J. Amer. Statist. Ass. 99(467), 619-632.

See Also

```
lme4-package, lmer, glmer
```

```
### Three application examples
b <- lmer(Reaction ~ Days + (Days | Subject), sleepstudy)
cAIC(b)

b2 <- lmer(Reaction ~ (1 | Days) + (1 | Subject), sleepstudy)
cAIC(b2)

b2ML <- lmer(Reaction ~ (1 + Days | Subject), sleepstudy, REML = FALSE)
cAIC(b2ML)

### Demonstration of boundary case
## Not run:
set.seed(2017-1-1)</pre>
```

deleteZeroComponents

```
n <- 50
beta <- 2
x <- rnorm(n)
eta <- x*beta
id \leftarrow gl(5,10)
epsvar <- 1
data \leftarrow data.frame(x = x, id = id)
y_wo_bi <- eta + rnorm(n, 0, sd = epsvar)</pre>
# use a very small RE variance
ranvar <- 0.05
nrExperiments <- 100
sim <- sapply(1:nrExperiments, function(j){</pre>
b_i <- scale(rnorm(5, 0, ranvar), scale = FALSE)</pre>
y <- y_wo_bi + model.matrix(~ -1 + id) %*% b_i
data$y <- y
mixedmod <- lmer(y \sim x + (1 | id), data = data)
linmod <- lm(y \sim x, data = data)
c(cAIC(mixedmod)$caic, cAIC(linmod)$caic)
})
rownames(sim) <- c("mixed model", "linear model")</pre>
boxplot(t(sim))
## End(Not run)
```

Description

Is used in the cAIC function if method = "steinian" and family = "gaussian". The function deletes all random effects terms from the call if corresponding variance parameter is estimated to zero and updates the model in merMod.

Usage

```
deleteZeroComponents(m)
## S3 method for class 'lme'
```

```
deleteZeroComponents(m)
## S3 method for class 'merMod'
deleteZeroComponents(m)
```

Arguments

m

An object of class merMod fitted by 1mer of the lme4-package or of class 1me.

Details

For merMod class models: Uses the cnms slot of m and the relative covariance factors to rewrite the random effects part of the formula, reduced by those parameters that have an optimum on the boundary. This is necessary to obtain the true conditional corrected Akaike information. For the theoretical justification see Greven and Kneib (2010). The reduced model formula is then updated. The function deleteZeroComponents is then called iteratively to check if in the updated model there are relative covariance factors parameters on the boundary.

For 1me class models: ...

Value

An updated object of class merMod or of class 1me.

NULL

NULL

WARNINGS

For models called via gamm4 or gamm no automated update is available. Instead a warning with terms to omit from the model is returned.

Author(s)

Benjamin Saefken \& David Ruegamer \& Philipp Baumann

References

Greven, S. and Kneib T. (2010) On the behaviour of marginal and conditional AIC in linear mixed models. Biometrika 97(4), 773-789.

See Also

```
lme4-package, lmer, getME
```

```
## Currently no data with variance equal to zero...
b <- lmer(Reaction ~ Days + (Days | Subject), sleepstudy)
deleteZeroComponents(b)</pre>
```

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getcondLL

Function to calculate the conditional log-likelihood

Description

Function to calculate the conditional log-likelihood

Usage

```
getcondLL(object)
## S3 method for class 'lme'
getcondLL(object)
## S3 method for class 'merMod'
getcondLL(object)
```

Arguments

object

An object of class merMod either fitted by lmer or glmer of the 'lme4' package.

Value

conditional log-likelihood value

NULL

NULL

getWeights

Optimize weights for model averaging.

Description

Function to constructed an optimal vector of weights for model averaging of Linear Mixed Models based on the proposal of Zhang et al. (2014) of using Stein's Formular to derive a suitable criterion based on the conditional Akaike Information Criterion as proposed by Greven and Kneib. The underlying optimization used is a customized version of the Augmented Lagrangian Method.

Usage

```
getWeights(models)
```

Arguments

models

An list object containing all considered candidate models fitted by lmer of the lme4-package or of class lme.

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Value

An updated object containing a vector of weights for the underlying candidate models, value of the object given said weights as well as the time needed.

WARNINGS

For models called via gamm4 or gamm no weight determination via this function is currently possible.

Author(s)

Benjamin Saefken & Rene-Marcel Kruse

References

Greven, S. and Kneib T. (2010) On the behaviour of marginal and conditional AIC in linear mixed models. Biometrika 97(4), 773-789.

Zhang, X., Zou, G., & Liang, H. (2014). Model averaging and weight choice in linear mixed-effects models. Biometrika, 101(1), 205-218.

Nocedal, J., & Wright, S. (2006). Numerical optimization. Springer Science & Business Media.

See Also

```
lme4-package, lmer, getME
```

guWahbaData 11

baData from Gu and Wahba (1991)

Description

Data from Gu and Wahba (1991) which is used for demonstrative purposes to exemplarily fit a generalized additive mixed model.

References

Gu and Wahba (1991) Minimizing GCV/GML scores with multiple smoothing parameters via the Newton method. SIAM J. Sci. Statist. Comput. 12:383-398

modelAvg

Model Averaging for Linear Mixed Models

Description

Function to perform Model Averaging for Linear Mixed Models based on the weight selection criterion Model Averaging as proposed by Zhang et al.(2014)

Usage

```
modelAvg(models, opt = TRUE)
```

Arguments

models A list object containing all considered candidate models fitted by 1mer of the

lme4-package or of class 1me.

opt logical. If TRUE (the default) the model averaging approach with optimial

weights is calculated. If FALSE the underlying weights as smoothed weights

as proposed by Buckland et al. (1997)

Value

An object containing the function calls of the underlying candidate models, the values of the model averaged fixed effects, the values of the model averaged random effects the results of the weight optimization process, as well as a list of the candidate models themselvs

Author(s)

Benjamin Saefken & Rene-Marcel Kruse

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References

Greven, S. and Kneib T. (2010) On the behaviour of marginal and conditional AIC in linear mixed models. Biometrika 97(4), 773-789.

Zhang, X., Zou, G., & Liang, H. (2014). Model averaging and weight choice in linear mixed-effects models. Biometrika, 101(1), 205-218.

See Also

```
1me4-package, 1mer
```

Examples

predictMA

Prediction of model averaged linear mixed models

Description

Function to perform prediction for model averaged linear mixed models based on the weight selection criterion as proposed by Zhang et al.(2014)

Usage

```
predictMA(object, new.data)
```

Arguments

object A object created by the model averaging function.

new.data Object that contains the data on which the prediction is to be based on.

Value

An object that containing predictions that are calculated on the basis of dataset and the underlying averaged model.

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Author(s)

Benjamin Saefken & Rene-Marcel Kruse

References

Greven, S. and Kneib T. (2010) On the behaviour of marginal and conditional AIC in linear mixed models. Biometrika 97(4), 773-789.

See Also

```
1me4-package, 1mer
```

Examples

print.cAIC

Print method for cAIC

Description

Print method for cAIC

Usage

```
## S3 method for class 'cAIC'
print(x, ..., digits = 2)
```

Arguments

```
    x a cAIC object
    ... further arguments passed to generic print function (not in use).
    digits number of digits to print
```

stepcAIC

Function to stepwise select the (generalized) linear mixed model fitted via (g)lmer() or (generalized) additive (mixed) model fitted via gamm4() with the smallest cAIC.

Description

The step function searches the space of possible models in a greedy manner, where the direction of the search is specified by the argument direction. If direction = "forward" / = "backward", the function adds / exludes random effects until the cAIC can't be improved further. In the case of forward-selection, either a new grouping structure, new slopes for the random effects or new covariates modeled nonparameterically must be supplied to the function call. If direction = "both", the greedy search is alternating between forward and backward steps, where the direction is changed after each step

Usage

```
stepcAIC(
  object,
  numberOfSavedModels = 1,
  groupCandidates = NULL,
  slopeCandidates = NULL,
  fixEfCandidates = NULL,
  numberOfPermissibleSlopes = 2,
  allowUseAcross = FALSE,
  allowCorrelationSel = FALSE,
  allowNoIntercept = FALSE,
  direction = "backward",
  trace = FALSE,
  steps = 50,
  keep = NULL,
  numCores = 1,
  data = NULL,
  returnResult = TRUE,
  calcNonOptimMod = TRUE,
  bsType = "tp",
  digits = 2,
  printValues = "caic",
)
```

Arguments

```
object object returned by [lme4]{lmer}, [lme4]{glmer} or [gamm4]{gamm4} numberOfSavedModels
```

integer defining how many additional models to be saved during the step procedure. If 1 (DEFAULT), only the best model is returned. Any number k greater 1

will return the k best models. If 0, all models will be returned (not recommended for larger applications).

groupCandidates

character vector containing names of possible grouping variables for new random effects. Group nesting must be specified manually, i.e. by listing up the string of the groups in the manner of lme4. For example groupCandidates = c("a","b","a/b").

slopeCandidates

character vector containing names of possible new random effects

fixEfCandidates

character vector containing names of possible (non-)linear fixed effects in the GAMM; NULL for the (g)lmer-use case

numberOfPermissibleSlopes

how much slopes are permissible for one grouping variable

allowUseAcross allow slopes to be used in other grouping variables

allowCorrelationSel

logical; FALSE does not allow correlations of random effects to be (de-)selected (default)

allowNoIntercept

direction

logical; FALSE does not allow random effects without random intercept character vector indicating the direction ("both", "backward", "forward")

trace logical; should information be printed during the execution of stepcAIC?

steps maximum number of steps to be considered

keep list(\$fixed,\$random) of formulae; which splines / fixed (fixed) or random effects

(random) to be kept during selection; specified terms must be included in the

original model

numCores the number of cores to be used in calculations; parallelization is done by using

parallel::mclapply

data.frame supplying the data used in object. data must also include variables,

which are considered for forward updates.

returnResult logical; whether to return the result (best model and corresponding cAIC)

calcNonOptimMod

logical; if FALSE, models which failed to converge are not considered for cAIC

calculation

bsType type of splines to be used in forward gamm4 steps

digits number of digits used in printing the results

printValues what values of c("cll", "df", "caic", "refit") to print in the table of com-

parisons

... further options for cAIC call

Value

if returnResult is TRUE, a list with the best model finalModel, additionalModels if numberOfSavedModels was specified and the corresponding cAIC bestCAIC is returned.

Note that if trace is set to FALSE and returnResult is also FALSE, the function call may not be meaningful

Details

Note that the method can not handle mixed models with uncorrelated random effects and does NOT reduce models to such, i.e., the model with $(1 + s \mid g)$ is either reduced to $(1 \mid g)$ or $(0 + s \mid g)$ but not to $(1 + s \mid g)$.

Author(s)

David Ruegamer

```
(fm3 <- lmer(strength ~ 1 + (1|sample) + (1|batch), Pastes))</pre>
fm3_step <- stepcAIC(fm3, direction = "backward", trace = TRUE, data = Pastes)</pre>
fm3_min <- lm(strength ~ 1, data=Pastes)</pre>
fm3_min_step <- stepcAIC(fm3_min, groupCandidates = c("batch", "sample"),</pre>
direction="forward", data=Pastes, trace=TRUE)
fm3_min_step <- stepcAIC(fm3_min, groupCandidates = c("batch", "sample"),</pre>
direction="both", data=Pastes, trace=TRUE)
# try using a nested group effect which is actually not nested -> warning
fm3_min_step <- stepcAIC(fm3_min, groupCandidates = c("batch", "sample", "batch/sample"),</pre>
                          direction="both", data=Pastes, trace=TRUE)
Pastes$time <- 1:dim(Pastes)[1]</pre>
fm3_slope <- lmer(data=Pastes, strength ~ 1 + (1 + time | cask))</pre>
fm3_slope_step <- stepcAIC(fm3_slope,direction="backward", trace=TRUE, data=Pastes)</pre>
fm3_min <- lm(strength ~ 1, data=Pastes)</pre>
fm3_min_step <- stepcAIC(fm3_min,groupCandidates=c("batch","sample"),</pre>
direction="forward", data=Pastes,trace=TRUE)
fm3_inta <- lmer(strength ~ 1 + (1|sample:batch), data=Pastes)</pre>
fm3_inta_step <- stepcAIC(fm3_inta,groupCandidates=c("batch","sample"),</pre>
direction="forward", data=Pastes,trace=TRUE)
fm3_min_step2 <- stepcAIC(fm3_min,groupCandidates=c("cask","batch","sample"),</pre>
direction="forward", data=Pastes,trace=TRUE)
fm3_min_step3 <- stepcAIC(fm3_min,groupCandidates=c("cask","batch","sample"),</pre>
direction="both", data=Pastes,trace=TRUE)
## Not run:
```

```
fm3_inta_step2 <- stepcAIC(fm3_inta,direction="backward",</pre>
data=Pastes,trace=TRUE)
## End(Not run)
##### create own example
na <- 20
nb <- 25
n <- 400
a <- sample(1:na,400,replace=TRUE)</pre>
b <- factor(sample(1:nb,400,replace=TRUE))</pre>
x <- runif(n)</pre>
y < -2 + 3 * x + a*.02 + rnorm(n) * .4
a <- factor(a)
c <- interaction(a,b)</pre>
y <- y + as.numeric(as.character(c))*5</pre>
df <- data.frame(y=y,x=x,a=a,b=b,c=c)</pre>
smallMod <- lm(y \sim x)
## Not run:
# throw error
stepcAIC(smallMod, groupCandidates=c("a","b","c"), data=df, trace=TRUE, returnResult=FALSE)
smallMod <- lm(y ~ x, data=df)
# throw error
stepcAIC(smallMod, groupCandidates=c("a","b","c"), data=df, trace=TRUE, returnResult=FALSE)
# get it all right
mod <- stepcAIC(smallMod, groupCandidates=c("a","b","c"),</pre>
                 data=df, trace=TRUE,
                 direction="forward", returnResult=TRUE)
# make some more steps...
stepcAIC(smallMod, groupCandidates=c("a","b","c"), data=df, trace=TRUE,
         direction="both", returnResult=FALSE)
mod1 \leftarrow lmer(y \sim x + (1|a), data=df)
stepcAIC(mod1, groupCandidates=c("b","c"), data=df, trace=TRUE, direction="forward")
stepcAIC(mod1, groupCandidates=c("b","c"), data=df, trace=TRUE, direction="both")
mod2 <- lmer(y \sim x + (1|a) + (1|c), data=df)
stepcAIC(mod2, data=df, trace=TRUE, direction="backward")
mod3 \leftarrow lmer(y \sim x + (1|a) + (1|a:b), data=df)
```

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```
stepcAIC(mod3, data=df, trace=TRUE, direction="backward")
## End(Not run)
```

summaryMA

Summary of model averaged linear mixed models

Description

Function to generate a summary of the results of the model averaging process.

Usage

```
summaryMA(object, randeff = FALSE)
```

Arguments

object A object created by the model averaging function.

randeff logical. Indicator whether the model averaged random effects should also be

part of the output. The default setting is FALSE.

Value

Outputs a summary of the model averaged random and fixed effects, as well as the calculated weights of the individual candidate models.

Author(s)

Benjamin Saefken & Rene-Marcel Kruse

References

Greven, S. and Kneib T. (2010) On the behaviour of marginal and conditional AIC in linear mixed models. Biometrika 97(4), 773-789.

See Also

```
1me4-package, 1mer
```

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Examples

Zambia

Subset of the Zambia data set on childhood malnutrition

Description

Data analyzed by Kandala et al. (2001) which is used for demonstrative purposes to estimate linear mixed and additive models using a stepwise procedure on the basis of the cAIC. The full data set is available at http://www.uni-goettingen.de/de/551625.html.

References

Kandala, N. B., Lang, S., Klasen, S., Fahrmeir, L. (2001): Semiparametric Analysis of the Socio-Demographic and Spatial Determinants of Undernutrition in Two African Countries. Research in Official Statistics, 1, 81-100.

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