Package 'bpnreg'

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Type Package

Title Bayesian Projected Normal Regression Models for Circular Data

Version 1.0.3

Description Fitting Bayesian multiple and mixed-effect regression models for circular data based on the projected normal distribution. Both continuous and categorical predictors can be included. Sampling from the posterior is performed via an MCMC algorithm. Posterior descriptives of all parameters, model fit statistics and Bayes factors for hypothesis tests for inequality constrained hypotheses are provided. See Cremers, Mulder & Klugkist (2018) <doi:10.1111/bmsp.12108> and Nuñez-Antonio & Guttiérez-Peña (2014) <doi:10.1016/j.csda.2012.07.025>.

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License GPL-3

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BugReports https://github.com/joliencremers/bpnreg/issues

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BFc

Bayes Factors

Description

BF gives Bayes factors for inequality constrained hypotheses on circular mean differences.

Usage

BFc(object, hypothesis, type = "anchor")

Arguments

object	an object used to select a method.
hypothesis	the inequality constrained hypothesis to test.
type	type of hypothesis to test c("anchor", "isotropic").

Details

the methods BFc.bpnr and BFc.bpnme have their own help page.

Examples

```
library(bpnreg)
fit.Motor <- bpnr(pred.I = Phaserad ~ 1 + Cond, data = Motor,
its = 100, burn = 10, n.lag = 3)
BFc(fit.Motor, hypothesis = "Condsemi.imp < Condimp")</pre>
```

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BFc.bpnme

Description

Outputs Bayes Factors for inequality constrained hypotheses on the circular differences between several levels of a categorical variable and the baseline.

Usage

```
## S3 method for class 'bpnme'
BFc(object, hypothesis, type = "anchor")
```

Arguments

object	a bpnme object obtained from the function bpnme.
hypothesis	the inequality constrained hypothesis to test.
type	type of hypothesis to test c("anchor", "isotropic").

Value

Bayes Factors for inequality constrained hypotheses on mean differences.

Examples

```
library(bpnreg)
fit.Maps <- bpnme(pred.I = Error.rad ~ Maze + Trial.type + L.c + (1|Subject),
data = Maps, its = 100, burn = 1, n.lag = 1)
BFc(fit.Maps, hypothesis = "Maze1 < Trial.type1")</pre>
```

BFc.bpnr

Bayes Factors for a Bayesian circular regression model

Description

Outputs Bayes Factors for the circular differences between several levels of a categorical variable and the baseline.

Usage

```
## S3 method for class 'bpnr'
BFc(object, hypothesis, type = "anchor")
```

bpnme

Arguments

object	a bpnr object obtained from the function bpnr().
hypothesis	the inequality constrained hypothesis to test.
type	type of hypothesis to test c("anchor", "isotropic").

Value

Bayes Factors for inequality constrained hypotheses on mean differences.

Examples

```
library(bpnreg)
fit.Motor <- bpnr(pred.I = Phaserad ~ 1 + Cond, data = Motor,
its = 100, burn = 10, n.lag = 3)
BFc(fit.Motor, hypothesis = "Condsemi.imp < Condimp")</pre>
```

bpnme

Fit a Bayesian circular mixed-effects model

Description

This function fits a Bayesian circular mixed-effects model based on the projected normal distribution.

Usage

```
bpnme(pred.I, data, pred.II = pred.I, its = 1000, burn = 1,
    n.lag = 1, seed = NULL)
```

Arguments

pred.I	model equation for effects of component 1.
data	the dataframe used for analysis.
pred.II	model equation for effects of component 2.
its	output iterations of the MCMC sampler.
burn	number of burn-in iterations.
n.lag	amount of lag for the iterations and burn-in.
seed	user-specified random seed.

Details

Because the model is based on the projected normal distribution, a model equation has to be given for the fixed and random effects of the two components. By default the model equation of the second component pred.II is set to be equal to that of the first component. Note that the circular outcome needs to be measured in radians on a scale from 0 to 2π . For more information about the projected normal distribution see Presnell, Morrisson & Littell (1998).

A tutorial on how to use this function can be found in Cremers & Klugkist (2018). More details on the sampling algorithm and interpretation of the coefficients from the model can be found in Nuñez-Antonio & Guttiérrez-Peña (2014) and Cremers, Pennings, Mainhard & Klugkist (2019). The uninformative priors for the fixed effect regression coefficients of the two components are set to N(0, 10000). Note that the model is only developed for models with a single nesting variable.

Value

A bpnme object, which can be further analyzed using the associated functions traceplot.bpnme, BFc.bpnme, coef_lin.bpnme, coef_circ.bpnme, coef_ran.bpnme, residuals.bpnme, predict.bpnme, fit.bpnme and print.bpnme.

A bpnr object contains the following elements (some elements are not returned if not applicable)

Beta. I A matrix of posterior samples for the fixed effects coefficients for the first component.

Beta.II A matrix of posterior samples for the fixed effects coefficients for the second component.

B.I An array of posterior samples for the random effects coefficients for the first component.

B.II An array of posterior samples for the random effects coefficients for the second component.

VCovI An array of posterior samples for the random effect variances of the first component.

VCovII An array of posterior samples for the random effect variances of the second component.

predictiva A list containing the posterior density values for all timepoints of individuals in the dataset for all iterations. The rowsums of this matrix are the likelihood values for all iterations

circular.ri A vector of posterior samples for the circular random intercepts.

N Number of observed cases.

its Number of output iterations.

n.lag One in n.lag iterations will be saved as output iteration. Set lag to 1 to save all iterations (default).

burn Burn-in time for the MCMC sampler.

- p1 Number of fixed effect parameters predicting the first component.
- p2 Number of fixed effect parameters predicting the second component.
- q1 Number of random effect parameters predicting the first component.
- q2 Number of random effect parameters predicting the second component.
- a.x A matrix of posterior samples for a.x which describes the location of the inflection point of the regression curve on the axis of the predictor.
- a.c A matrix of posterior samples for a.c which describes the location of the inflection point of the regression curve on the axis of the circular outcome.
- b.c A matrix of posterior samples for b.c which describes the slope of the tangent line at the inflection point.

bpnme

- SAM A matrix of posterior samples for the circular regression slopes at the mean.
- AS A matrix of posterior samples for the average slopes of the circular regression.
- SSD0 A matrix of posterior samples for the signed shortest distance to the origin.
- circ.diff A matrix of posterior samples for the circular difference found between levels of categorical variables and the intercept.
- cRSnum A string indicating whether there are continuous variables with a random slope
- cRScat A string indicating whether there are categorical variables with a random slope
- cRS A string indicating whether there are categorical or continuous variables with a random slope
- cRI A vector of posterior samples of the mean resultant length of the circular random intercept, a measure of concentration.
- Call The matched call.
- lin.coef.I The mean, mode, standard deviation and 95 posterior density of the linear fixed effect coefficients for B1.
- lin.coef.II The mean, mode, standard deviation and 95 confidence interval of the highest posterior density of the linear fixed effect coefficients for B2.
- circ.coef The mean, mode, standard deviation and 95 density for a.x, a.c, SSDO, and the circular fixed effect coefficients b.c, AS, and SAM
- circ.coef.cat The mean, mode, standard deviation and 95 confidence interval of the highest posterior density the circular difference between levels of categorical variables and the intercept.
- circ.coef.means The mean, mode, standard deviation and 95 confidence interval of the highest posterior density of circular means of the categorical variables.
- model.fit A list of information criteria for assessment of model fit.
- lin.res.varrand.I The mean, mode, standard deviation and 95 variances of the random intercepts and slopes of component I.
- lin.res.varrand.II The mean, mode, standard deviation and 95 of component II.
- circ.res.varrand The mean, mode, standard deviation and 95 random intercepts and slopes.
- mm A list of information, model matrices, sample size, etc. on the specified model.

Source

Cremers, J., Mainhard, M.T. & Klugkist, I. (2018). Assessing a Bayesian Embedding Approach to Circular Regression Models. Methodology, 14, 69-81.

Cremers, J. & Klugkist, I. (2018). One direction? A tutorial for circular data with examples in cognitive psychology. Frontiers in Psychology: Cognitive Science.

Cremers, J., Pennings, H.J.M., Mainhard, M.T. & Klugkist, I. (2019). Circular Modelling of Circumplex Measurements for Interpersonal Behavior. Assessment, Online First.

Nuñez-Antonio, G. & Gutiérrez-Peña, E. (2014). A Bayesian model for longitudinal circular data based on the projected normal distribution. Computational Statistics and Data Analysis, 71, 506-519.

Presnell, B., Morrison, S.P. & Littell, R.C. (1998). Projected multivariate linear models for directional data. Journal of the American Statistical Association, 93 (443), 1068 - 1077.

Examples

```
library(bpnreg)
bpnme(Error.rad ~ Maze + Trial.type + (1|Subject), Maps, its = 100)
```

bpnr

Fit a Bayesian circular regression model

Description

This function fits a Bayesian circular regression model based on the projected normal distribution.

Usage

```
bpnr(pred.I, data, pred.II = pred.I, its = 1000, burn = 1,
    n.lag = 1, seed = NULL)
```

Arguments

pred.I	model equation for effects of component 1.
data	the dataframe used for analysis.
pred.II	model equation for effects of component 2.
its	output iterations of the MCMC sampler.
burn	number of burn-in iterations.
n.lag	amount of lag for the iterations and burn-in.
seed	user-specified random seed.

Details

Because the model is based on the projected normal distribution, a model equation has to be given for two components. By default the equation of the second component pred. II is set to be equal to that of the first component. Note that the circular outcome needs to be measured in radians on a scale from 0 to 2π . For more information about the projected normal distribution see Presnell, Morrisson & Littell (1998).

A tutorial on how to use this function can be found in Cremers & Klugkist (2018). More details on the sampling algorithm and interpretation of the coefficients from the model can be found in Cremers, Mulder & Klugkist (2018) and Cremers, Mainhard & Klugkist (2018). The uninformative priors for the regression coefficients of the two components are set to N(0, 10000).

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bpnr

Value

- A bpnr object, which can be further analyzed using the associated functions traceplot.bpnr, BFc.bpnr, coef_lin.bpnr, coef_circ.bpnr, residuals.bpnr,predict.bpnr, fit.bpnr and print.bpnr.
- A bpnr object contains the following elements (some elements are not returned if not applicable)
- B1 A matrix of posterior samples for the coefficients B1 of the first component.
- B2 A matrix of posterior samples for the coefficients B2 for the second component.
- Likelihood A matrix containing the posterior density values for all individuals in the dataset for all iterations. The rowsums of this matrix are the likelihood values for all iterations
- its Number of output iterations.
- n.lag One in n.lag iterations will be saved as output iteration. Set lag to 1 to save all iterations (default).
- burn-in Burn-in time for the MCMC sampler.
- p1 Number of parameters predicting the first component.
- p2 Number of parameters predicting the second component.
- theta The circular outcome vector measured in radians.
- a.x A matrix of posterior samples for a.x which describes the location of the inflection point of the regression curve on the axis of the predictor.
- a.c A matrix of posterior samples for a.c which describes the location of the inflection point of the regression curve on the axis of the circular outcome.
- b.c A matrix of posterior samples for b.c which describes the slope of the tangent line at the inflection point.
- SAM A matrix of posterior samples for the circular regression slopes at the mean.
- AS A matrix of posterior samples for the average slopes of the circular regression.
- SSD0 A matrix of posterior samples for the signed shortest distance to the origin.
- circ.diff A matrix of posterior samples for the circular difference between levels of categorical variables and the intercept.
- Call The matched call.
- lin.coef.I The mean, mode, standard deviation and 95 confidence interval of the highest posterior density of the linear coefficients for B1.
- lin.coef.II The mean, mode, standard deviation and 95 density of the linear coefficients for B2.
- circ.coef The mean, mode, standard deviation and 95 confidence interval of the highest posterior density for the a.x, a.c, b.c, AS, SAM and SSDO of the circular coefficients.
- circ.coef.cat The mean, mode, standard deviation and 95 density the circular difference between levels of categorical variables and the intercept.
- circ.coef.means The mean, mode, standard deviation and 95 circular means of the categorical variables.
- model.fit A list of information criteria for assessment of model fit.
- mm A list of information, model matrices, sample size, etc. on the specified model.

Source

Cremers, J., Mulder, K.T. & Klugkist, I. (2018). Circular interpretation of regression coefficients. British Journal of Mathematical and Statistical Psychology, 71(1), 75-95.

Cremers, J., Mainhard, M.T. & Klugkist, I. (2018). Assessing a Bayesian Embedding Approach to Circular Regression Models. Methodology, 14, 69-81.

Cremers, J. & Klugkist, I. (2018). One direction? A tutorial for circular data with examples in cognitive psychology. Frontiers in Psychology: Cognitive Science.

Presnell, B., Morrison, S.P. & Littell, R.C. (1998). Projected multivariate linear models for directional data. Journal of the American Statistical Association, 93 (443), 1068 - 1077.

Examples

library(bpnreg)
bpnr(Phaserad ~ Cond + AvAmp, Motor)

bpnreg

bpnreg: A package to analyze Bayesian projected normal circular regression models

Description

This package contains functions to analyze circular regression type models (multivariate and mixedeffects). It is based on the 'embedding' approach to circular modelling and makes use of the projected normal distribution. Its estimation method is a Bayesian MCMC sampler. Further technical details can be found in Cremers, Mulder & Klugkist (2018) and Cremers & Klugkist (2018).

Details

A tutorial on how to use this package can be found in Cremers & Klugkist (2018). More details on the sampling algorithm and interpretation of the coefficients from the model can be found in Cremers, Mulder & Klugkist (2018), Nuñez-Antonio & Gutiérrez-Peña, Cremers, Mainhard & Klugkist (2018) and Cremers, Pennings, Mainhard & Klugkist (2019).

Functions

The main functions of the package are:

bpnr, which runs an MCMC sampler in C++ and returns an S3 object of type bpnr, which can be further analyzed through associated functions.

bpnme, which runs an MCMC sampler in R and returns an S3 object of type bpnme, which can be further analyzed through associated functions.

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circ_coef

Datasets

Datasets included in this package are:

Motor, A dataset from a study by Puglisi et.al. (2017) on the role of attention in human motor resonance.

Maps, A dataset from a study by Warren et.al. (2017) on the geometry of human knowledge of navigation space.

Source

Cremers, J., Pennings, H.J.M., Mainhard, M.T. & Klugkist, I. (2019). Circular Modelling of Circumplex Measurements for Interpersonal Behavior. Assessment.

Cremers, J., Mulder, K.T. & Klugkist, I. (2018). Circular interpretation of regression coefficients. British Journal of Mathematical and Statistical Psychology, 71(1), 75-95.

Cremers, J., Mainhard, M.T. & Klugkist, I. (2018). Assessing a Bayesian Embedding Approach to Circular Regression Models. Methodology, 14, 69-81.

Cremers, J. & Klugkist, I. (2018). One direction? A tutorial for circular data with examples in cognitive psychology. Frontiers in Psychology: Cognitive Science.

Nuñez-Antonio, G. & Gutiérrez-Peña, E. (2014). A Bayesian model for longitudinal circular data based on the projected normal distribution. Computational Statistics and Data Analysis, 71, 506-519.

circ_coef

Compute circular coefficients from linear coefficients

Description

circ_coef computes the coordinates of the inflection point of a circular effect, the slope at the inflection point and the unsigned and signed shortest distance to the origin.

Usage

circ_coef(a1, a2, b1, b2)

Arguments

a1	intercept of the first linear component.
a2	intercept of the second linear component.
b1	slope of the first linear component.
b2	slope of the second linear component.

Value

A dataframe containing the coordinates of the inflection point of a circular effect, the slope at the inflection point and the unsigned and signed shortest distance to the origin.

circ_coef_rcpp

Description

Compute circular coefficients

Usage

circ_coef_rcpp(a1, a2, b1, b2)

Arguments

a1	intercept estimate of component I
a2	intercept estimate of component I
b1	slope estimate of component I.
b2	slope estimate of component I.

coef_circ Circular coefficients

Description

coef_circ gives posterior summaries of the circular coefficients.

Usage

```
coef_circ(object, type = "continuous", units = "radians")
```

Arguments

object	an object used to select a method.
type	one of c("continuous", "categorical") to get either the coefficients for the continuous or categorical predictor variables.
units	one of c("degrees", "radians") to get categorical coefficients estimates and estimates for a_c in degrees or radians.

Details

the methods coef_circ.bpnr and coef_circ.bpnme have their own help page.

coef_circ.bpnme

Examples

```
library(bpnreg)
fit.Motor <- bpnr(pred.I = Phaserad ~ 1 + Cond, data = Motor,
its = 100, burn = 10, n.lag = 3)
coef_circ(fit.Motor)
coef_circ(fit.Motor, type = "categorical")</pre>
```

coef_circ.bpnme Obtain the circular coefficients of a Bayesian circular mixed-effects model

Description

Gives the coefficients tables of the circular coefficients for a Bayesian circular mixed-effects model.

Usage

```
## S3 method for class 'bpnme'
coef_circ(object, type = "continuous",
    units = "radians")
```

Arguments

object	a bpnme object obtained from the function bpnme
type	one of c("continuous", "categorical") to get either the coefficients for the continuous or categorical predictor variables
units	one of c("degrees", "radians") to get categorical coefficients estimates and estimates for a_c in degrees or radians.

Value

A matrix or list with posterior summaries of the circular coefficients in a Bayesian circular mixedeffects model.

```
library(bpnreg)
fit.Maps <- bpnme(pred.I = Error.rad ~ Maze + Trial.type + L.c + (1|Subject),
data = Maps,
its = 100, burn = 1, n.lag = 1)
coef_circ(fit.Maps)</pre>
```

 $coef_circ.bpnr$

Description

Gives the coefficients tables of the circular coefficients for a Bayesian circular regression model.

Usage

```
## S3 method for class 'bpnr'
coef_circ(object, type = "continuous",
    units = "radians")
```

Arguments

object	a bpnr object obtained from the function bpnr
type	one of c("continuous", "categorical") to get either the coefficients for the continuous or categorical predictor variables
units	one of c("degrees", "radians") to get categorical coefficients estimates and estimates for a_c in degrees or radians.

Value

A matrix or list with posterior summaries of the circular coefficients in a Bayesian circular regression model.

Examples

```
library(bpnreg)
fit.Motor <- bpnr(pred.I = Phaserad ~ 1 + Cond, data = Motor,
its = 100, burn = 10, n.lag = 3)
coef_circ(fit.Motor)
coef_circ(fit.Motor, type = "categorical")</pre>
```

coef_lin Linear coefficients

Description

coef_lin gives posterior summaries of the linear coefficients.

Usage

coef_lin(object)

coef_lin.bpnme

Arguments

object an object used to select a method.

Details

the methods coef_lin.bpnr and coef_lin.bpnme have their own help page.

Examples

```
library(bpnreg)
fit.Motor <- bpnr(pred.I = Phaserad ~ 1 + Cond, data = Motor,
its = 100, burn = 10, n.lag = 3)
coef_lin(fit.Motor)</pre>
```

<pre>coef_lin.bpnme</pre>	Obtain	the	linear	coefficients	of	а	Bayesian	circular	mixed-effects
	model								

Description

Gives the coefficients tables of the linear coefficients for a Bayesian circular mixed-effects model.

Usage

S3 method for class 'bpnme'
coef_lin(object)

Arguments

object a bpnme object obtained from the function bpnme.

Value

A matrix with posterior summaries of the linear coefficients in a Bayesian circular mixed-effects model.

```
library(bpnreg)
fit.Maps <- bpnme(pred.I = Error.rad ~ Maze + Trial.type + L.c + (1|Subject),
data = Maps,
its = 100, burn = 1, n.lag = 1)
coef_lin(fit.Maps)</pre>
```

coef_lin.bpnr

Description

Gives the coefficients tables of the linear coefficients for a circular regression model.

Usage

```
## S3 method for class 'bpnr'
coef_lin(object)
```

Arguments

object a bpnr object obtained from the function bpnr.

Value

A matrix with posterior summaries of the linear coefficients in a Bayesian circular regression model.

Examples

```
library(bpnreg)
fit.Motor <- bpnr(pred.I = Phaserad ~ 1 + Cond, data = Motor,
its = 100, burn = 10, n.lag = 3)
coef_lin(fit.Motor)</pre>
```

coef_ran

Random effect variances

Description

coef_ran gives posterior summaries of the circular or linear random effect variances.

Usage

coef_ran(object, type = "linear")

Arguments

object	an object used to select a method.
type	one of c("linear", "circular") to get either the linear or circular random
	effect variances.

coef_ran.bpnme

Details

the method coef_ran.bpnme has its own help page.

Examples

```
library(bpnreg)
fit.Maps <- bpnme(pred.I = Error.rad ~ Maze + Trial.type + L.c + (1|Subject),
data = Maps,
its = 100, burn = 1, n.lag = 1)
coef_ran(fit.Maps)
coef_ran(fit.Maps, type = "circular")</pre>
```

coef_ran.bpnme	Obtain random effect variances of a Bayesian circular mixed-effects
	model

Description

Gives posterior summaries of the circular or linear random effect variances.

Usage

S3 method for class 'bpnme'
coef_ran(object, type = "linear")

Arguments

object	a bpnme object obtained from the function bpnme.
type	one of c("linear", "circular") to get either the linear or circular random effect variances

Value

A matrix with posterior summaries of the random effect variances.

```
library(bpnreg)
fit.Maps <- bpnme(pred.I = Error.rad ~ Maze + Trial.type + L.c + (1|Subject),
data = Maps,
its = 100, burn = 1, n.lag = 1)
coef_ran(fit.Maps)
coef_ran(fit.Maps, type = "circular")</pre>
```

DIC_reg

Description

Compute Model Fit Measures Regression Model

Usage

DIC_reg(Output, X1, X2)

Arguments

Output	output from the circular regression function Regression()
X1	model matrix for the first component
X2	model matrix for the second component

eigen_val

Compute Eigenvalues

Description

Compute Eigenvalues

Usage

eigen_val(X)

Arguments

X A matrix.

eigen_vec

Compute Eigenvectors

Description

Compute Eigenvectors

Usage

eigen_vec(X)

Arguments

X A matrix.

fit

Description

fit gives several model fit statistics.

Usage

fit(object)

Arguments

object an object used to select a method.

Details

the methods fit.bpnr and fit.bpnme have their own help page.

Examples

```
library(bpnreg)
fit.Motor <- bpnr(pred.I = Phaserad ~ 1 + Cond, data = Motor,
its = 100, burn = 10, n.lag = 3)
fit(fit.Motor)</pre>
```

fit.bpnme

Model fit for a Bayesian circular mixed-effects model

Description

Outputs several model fit statistics for the Bayesian circular mixed-effects model

Usage

```
## S3 method for class 'bpnme'
fit(object)
```

Arguments

object a bpnme object obtained from the function bpnme.

Value

a matrix containing the computed log pointwise predictive density (lppd), Deviance Information Criterion (DIC), an alternative version of the DIC (DIC_alt), and the Watanabe-Akaike Information Criterion computed in two different ways (WAIC, WAIC2). The matrix also contains the number of parameters or 'effective number' of parameters that the several statistics are based on. Computation of the criteria is done according to Gelman et.al (2014) in *Bayesian Data Analysis*.

Examples

```
library(bpnreg)
fit.Maps <- bpnme(pred.I = Error.rad ~ Maze + Trial.type + L.c + (1|Subject),
data = Maps,
its = 100, burn = 1, n.lag = 1)
fit(fit.Maps)</pre>
```

fit.bpnr

Model fit for a Bayesian circular regression model

Description

Outputs several model fit statistics for the Bayesian circular regression model

Usage

S3 method for class 'bpnr'
fit(object)

Arguments

object a bpnr object obtained from the function bpnr().

Value

a matrix containing the computed log pointwise predictive density (lppd), Deviance Information Criterion (DIC), an alternative version of the DIC (DIC_alt), and the Watanabe-Akaike Information Criterion computed in two different ways (WAIC, WAIC2). The matrix also contains the number of parameters or 'effective number' of parameters that the several statistics are based on. Computation of the criteria is done according to Gelman et.al (2014) in *Bayesian Data Analysis*.

Examples

```
library(bpnreg)
fit.Motor <- bpnr(pred.I = Phaserad ~ 1 + Cond, data = Motor,
its = 100, burn = 10, n.lag = 3)
fit(fit.Motor)</pre>
```

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hmode

Description

Estimate the mode by finding the highest posterior density interval

Usage

hmode(x, cip)

Arguments

х	a sample from which to estimate the interval
cip	bandwidth for the algorithm, ranging from $0 \mbox{ to } 1$

Value

a scalar containing the estimate of the mode

hmodeC

Estimate the mode by finding the highest posterior density interval

Description

Estimate the mode by finding the highest posterior density interval

Usage

hmodeC(x, cip)

Arguments

Х	a sample from which to estimate the interval
cip	bandwidth for the algorithm, ranging from 0 to 1

Value

a scalar containing the estimate of the mode

hmodeci

Description

Find the highest density interval.

Usage

hmodeci(x, cip)

Arguments

х	a sample from which to estimate the interval
cip	bandwidth for the algorithm, ranging from 0 to 1

Value

a vector of length 2 containing the lower and upper bound of the interval.

hmodeciC Find the highest density interval of a circular variable	
---	--

Description

Find the highest density interval of a circular variable

Usage

hmodeciC(x, cip)

Arguments

Х	a sample from which to estimate the interval
cip	bandwidth for the algorithm, ranging from 0 to 1

Value

a vector of length 2 containing the lower and upper bound of the interval

hpd_est

Description

Compute the 95 percent HPD of a vector of linear data

Usage

hpd_est(x)

Arguments

х

a vector of linear data

Examples

library(bpnreg) hpd_est(Motor\$AvAmp)

hpd_est_circ Compute the 95 percent HPD of a vector of circular data

Description

Compute the 95 percent HPD of a vector of circular data

Usage

hpd_est_circ(x)

Arguments

x a vector of circular data

```
library(bpnreg)
hpd_est_circ(subset(Motor, Cond = "exp")$Phaserad)
```

Description

Compute the Likelihood of the PN distribution

Usage

lik(X1, X2, theta, b1, b2, n)

Arguments

X1	the model matrix of the first component
X2	the model matrix of the second component
theta	a circular outcome value
b1	estimated linear coefficients of the first component
b2	estimated linear coefficients of the second component
n	sample size
 theta b1 b2 n	a circular outcome value estimated linear coefficients of the first component estimated linear coefficients of the second component sample size

Maps

The geometry of human knowledge of navigation space.

Description

A dataset from a study by Warren et.al. (2017) on the geometry of human knowledge of navigation space.

Usage

Maps

Format

A data frame with 160 rows and 8 variables:

Subject a numeric variable indicating the participant number

- Trial.no a numeric variable indicating the trial number of the target a participant had to locate (1-8)
- **Maze** a between subjects factor variable indicating the type of maze a participant was in (0 = Euclidean, 1 = non-Euclidean)
- **Trial.type** a within subjects factor indicating the type of target (0 = standard, 1 = probe)
- Error a numeric variable containing the angular error in degrees
- Learn a numeric variable indicating the number of trials a participant completed in the training phase

L.c mean centered Learning

Error.rad a numeric variable containing the angular error in radians

lik

mean_circ

Details

In their study Warren et.al. (2017) conduct an experiment in which a total of 20 participants used virtual reality headsets to navigate through one of two versions of a virtual maze. One version of the maze is the standard or Euclidean maze. The other version of the maze, the non-Euclidean maze, has exactly the same layout as the standard maze apart from that it contains wormholes by which participants can be 'teleported' from one place in the maze to another.

In a training phase participants had learned to navigate between different pairs of start and target objects in one of two versions of the maze. The number of trials each participants completed in this training phase was recorded.

In the test phase of the experiment participants first walked to a start object. When they had reached this object the maze disappeared and only a "textured groundplane" of the maze remained visible. The participants then turned toward the location of the target object that they had remembered during the training phase and started to walk toward the target. The angular difference, angular error, between the initial walking direction of a participant from the start object and the location of the target object was recorded as an outcome variable in the experiment. The angular error is a circular variable and can be described and analyzed using circular statistics.

Apart from the between-subjects factor, the type of maze, the experiment also included a withinsubjects factor, trial number. All participants had to complete 8 trials in the test phase of the experiment. In each of these trials they had to walk to a specific target object. An additional withinsubjects factor is the type of target object. Pairs of start and target objects were of two types: probe and standard. The probe objects were located near the entrance and exit of a wormhole whereas the standard objects were located at some distance from the wormholes. For each of these two types of objects participants had to find 4 different targets resulting in a total of 8 trials per participant.

Source

https://doi.org/10.1016/j.cognition.2017.05.020

mean_circ

Compute the mean of a vector of circular data

Description

Compute the mean of a vector of circular data

Usage

```
mean_circ(theta, units = "radians")
```

Arguments

theta	a circular variable in radians or degrees.
units	measurement units of the circular variable c("radians", "degrees").

Examples

```
library(bpnreg)
mean_circ(subset(Motor, Cond == "exp")$PhaseDiff, units = "degrees")
```

mmme

Create model matrices for a circular mixed-effects regression model

Description

Create model matrices for a circular mixed-effects regression model

Usage

mmme(pred.I, data, pred.II)

Arguments

pred.I	model equation for effects of component 1
data	the dataframe used for analysis
pred.II	model equation for effects of component 2

mmr

Create model matrices circular regression

Description

Create model matrices circular regression

Usage

mmr(pred.I, data, pred.II)

Arguments

pred.I	model equation for effects of component 1
data	the dataframe used for analysis
pred.II	model equation for effects of component 2

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mode_est

Description

Compute the mode of a vector of linear data

Usage

mode_est(x)

Arguments

х

a vector of linear data

Examples

library(bpnreg)
mode_est(Motor\$AvAmp)

mode_est_circ Compute the mode of a vector of circular data

Description

Compute the mode of a vector of circular data

Usage

mode_est_circ(x)

Arguments

x a vector of circular data

```
library(bpnreg)
mode_est_circ(subset(Motor, Cond = "exp")$Phaserad)
```

Motor

Description

A dataset from a study by Puglisi et.al. (2017) on the role of attention in human motor resonance.

Usage

Motor

Format

A data frame with 42 rows and 4 variables:

- **Cond** a factor variable indicating the condition a participant was placed in; 1 = 'explicit', 2 = 'semi.implicit' or 3 = 'implicit'
- PhaseDiff a numeric variable the phase difference between 'observer' and 'mover' in degrees
- AvAmp a numeric variable indicating the average amplitude of the hand movement of the 'observer'

Phaserad a numeric variable the phase difference between 'observer' and 'mover' in radians

Details

In their research Puglisi et.al. (2017) conduct a between subjects experiment in which 'observers' in multiple degrees of explicitness are asked to look at the movement of a hand of the 'mover' or other object in order to evaluate the role of attention in motor resonant response.

The experiment has four conditions:

1. The 'explicit observation' condition (n = 14), where observers are explicitly instructed to observe the hand.

2. The 'semi-implicit observation' condition (n = 14) where the observers have to do a task that requires implicit observation of the hand.

3. The 'implicit observation' condition (n = 14), where observers have to do a task that is independent of the observation of the hand that is moving in front of them.

4. A baseline condition (n=14) where there is no moving hand but observers have to look at an inanimate object that moves in an identical manner to the hand.

The idea of motor resonance is then that the 'observer', because they are looking explicitly or implicitly at the hand of the 'mover', starts moving his or her hand in the same manner. This is the resonant response. In each condition the hand movements of the observers were measured and the phase difference between the observers' hand and the hand they observed (the movers' hand) was calculated. This was not done for the baseline condition because in this condition there was no periodic pattern of movement in the 'observers' hand.

The phase difference is a circular variable and can be described and analyzed using circular statistics.

Source

https://doi.org/10.1371/journal.pone.0177457

mvrnorm_arma_eigen Sample from a multivariate normal distribution

Description

Sample from a multivariate normal distribution

Usage

mvrnorm_arma_eigen(n, mu, sigma)

Arguments

n	An integer indicating the number of samples to take.
mu	A mean vector.
sigma	A variance-covariance matrix.

ormal regression model	A Gibbs sampler for a projected m	pnr
ormal regression model	A Gibbs sampler for a projected n	pnr

Description

A Gibbs sampler for a projected normal regression model

Usage

```
pnr(theta, X1r, X2r, its, lag, burn)
```

Arguments

theta	A vector with the circular dependent variable.
X1r	A model matrix for component I.
X2r	A model matrix for component II.
its	An integer specifying the number of iterations
lag	An integer specifying the amount of lag.
burn	An integer specifying the number of burn-in iterations.

predict.bpnme

Description

Outputs predicted values for a Bayesian circular mixed-effects model for each iteration of the MCMC sampler.

Usage

```
## S3 method for class 'bpnme'
predict(object, ...)
```

Arguments

object	a bpnme object obtained from the function bpnme.
	further arguments passed to or from other methods.

Value

a matrix (rows = N, columns = iterations) containing predicted values for the circular outcome for each iteration of the MCMC sampler.

Examples

```
library(bpnreg)
fit.Motor <- bpnr(pred.I = Phaserad ~ 1 + Cond, data = Motor,
its = 100, burn = 10, n.lag = 3)
predict(fit.Motor)</pre>
```

predict.bpnr

Predicted values for a Bayesian circular regression model

Description

Outputs predicted values for a Bayesian circular regression model for each iteration of the MCMC sampler.

Usage

```
## S3 method for class 'bpnr'
predict(object, ...)
```

print.bpnme

Arguments

object	a bpnr object obtained from the function bpnr.
	further arguments passed to or from other methods.

Value

a matrix (rows = N, columns = iterations) containing predicted values for the circular outcome for each iteration of the MCMC sampler.

Examples

```
library(bpnreg)
fit.Motor <- bpnr(pred.I = Phaserad ~ 1 + Cond, data = Motor,
its = 100, burn = 10, n.lag = 3)
predict(fit.Motor)</pre>
```

```
print.bpnme
```

Print output from a Bayesian circular mixed-effects model

Description

Prints selected output from a Bayesian circular mixed-effects model.

Usage

S3 method for class 'bpnme'
print(x, ...)

Arguments

Х	a bpnme object obtained from the function bpnme().
	further arguments passed to or from other methods.

Value

A print of selected output from a Bayesian circular mixed-effects model.

```
library(bpnreg)
fit.Maps <- bpnme(pred.I = Error.rad ~ Maze + Trial.type + L.c + (1|Subject),
data = Maps,
its = 100, burn = 1, n.lag = 1)
print(fit.Maps)</pre>
```

print.bpnr

Description

Prints selected output from a Bayesian circular regression model.

Usage

```
## S3 method for class 'bpnr'
print(x, ...)
```

Arguments

х	a bpnr object obtained from the function bpnr.
	further arguments passed to or from other methods.

Value

A print of selected output from a Bayesian circular regression model.

Examples

```
library(bpnreg)
fit.Motor <- bpnr(pred.I = Phaserad ~ 1 + Cond, data = Motor,
its = 100, burn = 10, n.lag = 3)
print(fit.Motor)</pre>
```

residuals.bpnme Residuals for a Bayesian circular mixed-effects model

Description

Outputs residuals for a Bayesian circular mixed-effects model for each iteration of the MCMC sampler.

Usage

```
## S3 method for class 'bpnme'
residuals(object, type = "arc", ...)
```

residuals.bpnr

Arguments

object	a bpnme object obtained from the function bpnme.
type	the type of residuals, one of c("arc", "cos"). The "arc" residuals are based on a computation of the circular arc length between predicted value and original outcome. The "cos" residuals are based on the cosine of the difference between predicted value and original outcome.
	further arguments passed to or from other methods.

Value

a matrix (rows = N, columns = iterations) containing residuals for each iteration of the MCMC sampler.

Examples

```
library(bpnreg)
fit.Maps <- bpnme(pred.I = Error.rad ~ Maze + Trial.type + L.c + (1|Subject),
data = Maps,
its = 100, burn = 1, n.lag = 1)
residuals(fit.Maps)
residuals(fit.Maps, type = "cos")</pre>
```

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1 corduaro. opin	nesianais joi	a Daye	sian circular	regression model

Description

Outputs residuals for a Bayesian circular regression model for each iteration of the MCMC sampler.

Usage

```
## S3 method for class 'bpnr'
residuals(object, type = "arc", ...)
```

Arguments

object	a bpnr object obtained from the function bpnr.
type	the type of residuals, one of c("arc", "cos"). The "arc" residuals are based on a computation of the circular arc length between predicted value and original outcome. The "cos" residuals are based on the cosine of the difference between predicted value and original outcome.
	further arguments passed to or from other methods.

Value

a matrix (rows = N, columns = iterations) containing residuals for each iteration of the MCMC sampler.

Examples

```
library(bpnreg)
fit.Motor <- bpnr(pred.I = Phaserad ~ 1 + Cond, data = Motor,
its = 100, burn = 10, n.lag = 3)
residuals(fit.Motor)
residuals(fit.Motor, type = "cos")</pre>
```

rho

Compute a mean resultant length

Description

Compute a mean resultant length

Usage

rho(theta)

Arguments

theta a circular variable in radians.

rho_circ

Compute the mean resultant length of a vector of circular data

Description

Compute the mean resultant length of a vector of circular data

Usage

```
rho_circ(theta, units = "radians")
```

Arguments

theta	a circular variable in radians or degrees.
units	measurement units of the circular variable c("radians", "degrees")

Examples

```
library(bpnreg)
rho_circ(subset(Motor, Cond == "exp")$PhaseDiff, units = "degrees")
```

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sd_circ

Description

Compute the standard deviation of a vector of circular data

Usage

```
sd_circ(theta, units = "radians")
```

Arguments

theta	a circular variable in radians or degrees.
units	measurement units of the circular variable c("radians", "degrees")

Examples

```
library(bpnreg)
sd_circ(subset(Motor, Cond == "exp")$PhaseDiff, units = "degrees")
```

slice_rcpp	A slice sampler	for the latent	lengths r
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Description

A slice sampler for the latent lengths r

Usage

slice_rcpp(X1, X2, theta, b1, b2, n, r)

Arguments

X1	A model matrix for component I.
X2	A model matrix for component II.
theta	A vector with the circular dependent variable.
b1	A matrix containing the coefficients of component I for the current iteration.
b2	A matrix containing the coefficients of component II for the current iteration
n	An integer indicating the sample size of the data.
r	A matrix with the estimates of r of the previous iteration.

theta_bar

Description

Compute a mean direction

Usage

theta_bar(theta)

Arguments

theta a circular variable in radians.

traceplot

Traceplots

Description

Traceplot function for a bpnr object or bpnme object.

Usage

```
traceplot(object, parameter = "SAM", variable = NULL)
```

Arguments

object	an object used to select a method.
parameter	one of c("B1", "B2", Beta.I", "Beta.II", a.x", "a.c", "b.c", "SAM", "AS", "SSDO", "circ.diff", " to indicate for which parameter a traceplot is required. B1, Beta.I, B2 and Beta.II are the linear intercepts and coefficients of the first and second compo- nent for a regression model and the fixed effects coefficients of a mixed-effects model. circ.diff are the circular differences with the intercept on the outcome variable for the different levels of categorical variables. VCovI and VCovII are the linear random effect variances and cRI and cRS are the variances of the cir- cular random intercept and circular random slope.
variable	a character string with variable name(s) to indicate for which variable(s) a tra- ceplot is required.

```
library(bpnreg)
fit.Motor <- bpnr(pred.I = Phaserad ~ 1 + Cond, data = Motor,
its = 100, burn = 10, n.lag = 3)
traceplot(fit.Motor, parameter = "B1")</pre>
```

traceplot.bpnme

Description

General plot function for a bpnme object.

Usage

```
## S3 method for class 'bpnme'
traceplot(object, parameter = "SAM", variable = NULL)
```

Arguments

object	a bpnme object obtained from the function bpnme
parameter	one of c(Beta.I", "Beta.II", a.x", "a.c", "b.c", "SAM", "AS", "SSDO", "circ.diff", "VCovI", "VC to indicate for which parameter a traceplot is required. Beta.I and Beta.II are the fixed effects coefficients of a mixed-effects model. circ.diff are the circu- lar differences with the intercept on the outcome variable for the different levels of categorical variables. VCovI and VCovII are the linear random effect vari- ances and cRI and cRS are the variances of the circular random intercept and circular random slope.
variable	a character string with variable name(s) to indicate for which variable(s) a tra- ceplot is required. This cannot be used in combination with the parameters c("VCovI", "VCovII", "cRI", "cRS").

Examples

```
library(bpnreg)
fit.Maps <- bpnme(pred.I = Error.rad ~ Maze + Trial.type + L.c + (1|Subject),
data = Maps,
its = 100, burn = 1, n.lag = 1)
traceplot(fit.Maps)</pre>
```

traceplot.bpnr Traceplots for a Bayesian circular regression model

Description

General plot function for a bpnr object.

Usage

```
## S3 method for class 'bpnr'
traceplot(object, parameter = "SAM", variable = NULL)
```

Arguments

object	a bpnr object obtained from the function bpnr
parameter	one of c("B1", "B2", "a.x", "a.c", "b.c", "SAM", "AS", "SSDO", "circ.diff") to indicate for which parameter a traceplot is required. B1 and B2 are the linear intercepts and coefficients of the first and second component. circ.diff are the circular differences with the intercept on the outcome variable for the different levels of categorical variables.
variable	a character string with variable name(s) to indicate for which variable(s) a tra- ceplot is required.

```
library(bpnreg)
fit.Motor <- bpnr(pred.I = Phaserad ~ 1 + Cond, data = Motor,
its = 100, burn = 10, n.lag = 3)
traceplot(fit.Motor, parameter = "B1")</pre>
```

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