

Package ‘aucm’

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LazyLoad yes

LazyData yes

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Title AUC Maximization

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Depends R (>= 3.1.3), kyotil

Suggests RUnit, mvtnorm

Description Implements methods for identifying linear and nonlinear marker combinations that maximizes the Area Under the AUC Curve (AUC).

License GPL-2

NeedsCompilation yes

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auc	<i>AUC</i>
-----	------------

Description

AUC methods.

Usage

```
## S3 method for class 'auc'
coef(object, ...)
## S3 method for class 'auc'
predict(object, newdata, case.percentage = NULL, ...)
## S3 method for class 'auc'
print(x, ...)
## S3 method for class 'auc'
summary(object, ...)
## S3 method for class 'auc'
trainauc(fit, training.data = NULL, ...)
## S3 method for class 'auc'
ratio(fit)

## S3 method for class 'glm'
trainauc(fit, ...)
## S3 method for class 'glm'
ratio(fit)
```

Arguments

fit	an object that inherits from class 'auc' such as 'rauc' or 'sauc'
object	an object that inherits from class 'auc' such as 'rauc' or 'sauc'
x	an object that inherits from class 'auc' such as rauc, sauc or sauc.dca.
newdata	data at which to predict

`case.percentage` used for class prediction, defaults to NULL
`training.data` data frame used to compute auc based on a fit obtained by a call to `rauc`, `sauc` or `sauc.dca`
`...` arguments passed to or from methods

Author(s)

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 aucm

aucm

Description

Please see the Index link below for a list of available functions.

 bupa

Bupa Dataset

Description

Bupa Dataset

Usage

`data(bupa)`

Format

A data frame with 345 observations on the following 14 variables.

Case a numeric vector

V1 a numeric vector

V2 a numeric vector

V3 a numeric vector

V4 a numeric vector

V5 a numeric vector

V6 a numeric vector

y a numeric vector

V1.2 a numeric vector

V2.2 a numeric vector
V3.2 a numeric vector
V4.2 a numeric vector
V5.2 a numeric vector
V6.2 a numeric vector

Examples

```
data(bupa)
## maybe str(bupa) ; plot(bupa) ...
```

cleveland

Cleveland Dataset

Description

Cleveland Dataset

Usage

```
data(cleveland)
```

Format

A data frame with 297 observations on the following 15 variables.

V1 a numeric vector
V2 a numeric vector
V3 a numeric vector
V4 a numeric vector
V5 a numeric vector
V6 a numeric vector
V7 a numeric vector
V8 a numeric vector
V9 a numeric vector
V10 a numeric vector
V11 a numeric vector
V12 a numeric vector
V13 a numeric vector
case a logical vector
y a numeric vector

Examples

```
data(cleveland)
## maybe str(cleveland) ; plot(cleveland) ...
```

control.minQuad	<i>control.minQuad</i>
-----------------	------------------------

Description

Control function to [minQuad](#)

Usage

```
control.minQuad(
  maxit = 1e4, tol = 1e-04,
  q = 0,
  ws = c("v", "v2", "greedy", "rv2wg", "rvwg", "rv", "rv2"),
  method = c("default", "tron", "loqo", "exhaustive", "x"),
  optim.control = list(),
  rank = 0,
  DUP = FALSE,
  NAOK = FALSE,
  verbose = FALSE,
  ret.ws = FALSE,
  ret.data = FALSE
)
```

Arguments

rank	a nonnegative integer indicating the 'rank' of the design matrix, only used by by method 'exhaustive' or 'x'. if zero it is estimated by the singular value decomposition of each 'sub-matrix' associated with the sub-optimization problem in the decomposition method.
method	a character string (first letter is sufficient) indicating which quadratic optimizer to use, defaults to 'default'. See details.
optim.control	a list of control parameters to methods 'tron' or 'loqo'; 'tron' : list(maxfev = 1000,fatol = tol,frtol = tol,cgtol=tol,gtol=tol,fmin = -.Machine\$double.xmax), 'loqo' : list(bound = 10,margin=0.05,maxiter=40,sigfig = 7,inf = 1e6)
q	size of the working set, will be set to 2 for all methods except for method = 'tron' when it defaults to NULL. In that case workings set size is automatically chosen to be sqrt(#violators) at each iteration.
ws	a character string indicating the strategy of how to select the working set, defaults to "rv2wg", see details.
maxit	maximum number of iterations whose typeof returns "integer".
tol	tolerance for termination criterion whose typeof returns "double".

DUP	should arguments be passed by reference ? defaults to FALSE.
NAOK	should NA's,NaN's be allowed to be passed to C code (no checking) ? defaults to FALSE.
verbose	some output at each iteration, possible values are FALSE/TRUE or and integer if more details are wanted, defaults to FALSE.
ret.ws	defaults to FALSE, indicates whether to return the working set selected at each iteration.
ret.data	defaults to FALSE, indicates whether to return the data passed to minQuad.

Details

Four quadratic optimizers are available within `minQuad`, "default", "tron", "loqo" and "exhaustive" (optimizer 'x' is a slightly faster implementation of the exhaustive method). For working set size $q = 2$, the 'default' option is a fast implementation that loosely minimizes the quadratic objective function, which is often sufficient to achieve convergence in the DCA-loop in `rauc`. For working set size $q = 2$, the 'default' option minimizes the quadratic objective function by "solving" an associated equation at each data point. The "exhaustive" method is a brute-force method that gives an exact solution to each quadratic sub-problem in `minQuad` and should probably not be used beyond working set size $q = 8, 10$ on most computers. Method 'tron' is a positive semidefinite quadratic optimizer and thus well suited for low-rank problems - for this method 'q' can be larger, ~100 or perhaps even ~1000. Method 'loqo' is a positive definite quadratic optimizer that accepts 'm' constraints specified by $(m \times n)$ matrix A in the form $v \leq A * x \leq v+r$ with both v and r finite. The default value of the size of the working set 'q' is 0. This means that if 'method' is 'tron' then 'q' is automatically set to the $\sqrt{\text{no. of violators}}$ at the current iteration in `minQuad` (rounded up). Otherwise 'q' defaults to 2 but may be set to any nonzero integer that is greater than 1. The "ws" argument sets the type of strategy to select the working set. Denote the two sets of violators as $V_0 = \{1 \text{ if } (a[p] > 0.0), (df[p] > 0.0), 0 \text{ ow.}\}$, $V_C = \{1 \text{ if } (a[p] < C), (df[p] < 0.0), 0 \text{ ow.}\}$ where "df[a]" stands for the gradient of the objective function at 'a'. "greedy" selects the extremes pairs (max,min) from the two sets (M,m) where $M = \{-df[i], a[i] < C\}$ and $m = \{-df[j] \mid a[j] > 0\}$. "v" selects from violators $V = V_0 \cup V_C$ ranked by $|df|$. "v2" selects separately from V_0 and V_C separately, ranked by $|df|$. "rv" selects without replacement (WOR) from all violators. "rvwg" selects WOR from all violators V with probability $\sim |df[V]|$. "rv2wg" selects WOR from the two sets of violators V_0 and V_C with probability $\sim |df[V]|$.

Value

A list with the following elements:

convergence	0 if converged, 1 if maximum iteration is reached.
alpha	estimated vector of coefficients.
value	value of the objective function.
iterations	number of iterations until convergence or "maxit" reached.
epsilon	stopping rule value to be compared to "tol".
n	
nSV	$\#\{0 < a\}$, no. of support vectors.
nBSV	$\#\{a=C\}$, no. of bounded support vectors.

nFSV #{ $0 < \alpha < C$ }, no. of unbounded support vectors.
 control the control argument.
 ws if requested, the working set selected at current iteration.

Author(s)

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References

Combining Biomarkers Nonlinearly for Classification Using the Area Under the ROC Curve Y. FONG, S. YIN, Y. HUANG *Biometrika* (2012), pp 1-28
Newton's method for large bound-constrained optimization problems Lin, C.J. and More, J.J. *SIAM Journal on Optimization* (1999), volume 9, pp 1100-1127.
kernlab - An S4 Package for Kernel Methods in R. Alexandros Karatzoglou, Alex Smola, Kurt Hornik, Achim Zeileis *Journal of Statistical Software* (2004) 11(9), 1-20. URL <http://www.jstatsoft.org/v11/i09/>

See Also

[rauc](#), [minQuad](#)

dcsauc	<i>AUC optimization with DCA</i>
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Description

optimizes SAUC using a smoothed DCA algorithm.

Usage

```
dcsauc (formula, data, ...)
srauc (formula, data, ...)
auc.dca (formula, data,
         type="srauc",
         kernel="linear", para=NULL,
         lambda=.1, zeta=.1, b=10, s=1, epsilon=1e-3,
         method="tron", decomposition=TRUE,
         dca.control = list(maxit=1e3, abstol=1e-5, coef.init=NULL, lincomb.init=NULL),
         tron.control = list(q=50, maxfev=1e3, gtol=1e-2, frtol=1e-12, K.thresh=1, verbose=0),
         return.K=FALSE, verbose = FALSE
)
```

Arguments

formula	formula, e.g. $y \sim x1 + x2$
data	a data frame
type	string. Either <code>srauc</code> or <code>dcsauc</code>
kernel	See getK for more details
para	See getK for more details
lambda	scale parameter of the penalty function, defaults to 1
zeta	parameter ($\rightarrow 0+$) in writing sigmoid function as difference of two convex functions.
b	'decay rate' parameter in sigmoid function $1/(exp(bx))$
s	the parameter in <code>rauc</code>
epsilon	the parameter in the approximation of a hinge function
method	the optimizer to use, "tron", or an <code>optim</code> method
decomposition	Boolean. If TRUE, decomposition strategy is used if <code>tron</code> is the method
dca.control	list of control parameters for the DCA algorithm
tron.control	list of control parameters to 'tron' optimizer
return.K	logical, whether to return the Kernel matrix
verbose	logical, whether to print info as alg. progresses
...	parameters passed to <code>auc.dca</code>

Details

`dcsauc` and `srauc` pass directly to `auc.dca` with the name-sake type.

Examples

```
#
#
#dat = sim.dat.1(n=100,seed=1)
#dat.test = sim.dat.1(n=1e3,seed=1000)
#
#t.1 = system.time({
#  fit.1=sauc.dca(y~x1+x2, dat, zeta=.1)
#})
#
#t.2 = system.time({
#  fit.2=sauc.dca(y~x1+x2, dat, zeta=1)
#})
#
## compare time
#rbind(t.1, t.2)[,3]
#
## compare performance
#RUnit::checkEqualsNumeric(
#  c(fit.1$train.auc, fit.2$train.auc)
```



```
#, c(0.7291917, 0.7282913), tolerance=1e-6)  
#
```

*get.X.diff**get.X.diff*

Description

computes X.diff matrix

Usage

```
get.X.diff (x1,...)  
## Default S3 method:  
get.X.diff(x1,x2,...)  
## S3 method for class 'formula'  
get.X.diff(formula, data,...)
```

Arguments

x1	data matrix from the case group, dimension n1 x d
x2	data matrix from the non-case group, dimension n2 x d
formula	a formula
data	a data frame
...	arguments passed 'to' or 'from' methods

Details

In `get.X.diff.formula`, `x` is the case predictors and `x2` control.

Value

A $(n1*n2) \times d$ matrix

Author(s)

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Krisztian Sebestyen <>

Examples

```

dat = sim.dat.1(n=100,seed=1)
X1 = as.matrix(subset(dat, y==0, select=c(x1,x2)))
X2 = as.matrix(subset(dat, y==1, select=c(x1,x2)))
X.diff = get.X.diff (X1, X2)
dim(X1)
dim(X2)
dim(X.diff)

```

getQ

getQ

Description

getQ calculates Q or Q.pred matrix depending on the value of do.pred.

Usage

```
getQ (K,n1,n2,call.C=TRUE,do.pred=FALSE)
```

Arguments

K	kernel matrix of dimension (n1+n2) by (n1+n2) or n.pred by (n1+n2). The (n1+n2) observations must be ordered case followed by non-case
n1	number of cases
n2	number of non-cases
call.C	boolean. If TRUE, make .C call, otherwise compute Q in R.
do.pred	boolean. If TRUE, K is a n.pred by (n1+n2) matrix; otherwise, it is a (n1+n2) by (n1+n2) matrix.

Value

A n1*n2 by n1*n2 matrix if do.pred is FALSE, or n.pred by n1*n2 matrix if do.pred is TRUE

Author(s)

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Examples

```

dat = sim.dat.1(n=100,seed=1)
dat=rbind(subset(dat, y==1), subset(dat, y==0))
X = as.matrix(subset(dat, select=c(x1,x2)))
n1=sum(dat$y)
n2=sum(1-dat$y)

K = kyotil::getK(X,"linear", 1)
Q1 = getQ(K,n1=n1,n2=n2,call.C=FALSE)
Q2 = getQ(K,n1=n1,n2=n2,call.C=TRUE)
all(Q2-Q1<1e-6)

# compare to a direct computation
X.diff=get.X.diff(X[1:n1,], X[1:n2+n1,])
Q3 = tcrossprod(X.diff, X.diff)
all(Q3-Q1<1e-6)

# two printouts of Q2 should not be different
Q2[1:3,1:3]
K = kyotil::getK(X,"rbf", 1)
Q4 = getQ(K,n1=n1,n2=n2,call.C=TRUE)
Q2[1:3,1:3]
Q4[1:3,1:3]

K = kyotil::getK(X[1:10,],"linear", 1, X2=X)
Q5 = getQ(K,n1=n1,n2=n2,call.C=FALSE,do.pred=TRUE)
Q6 = getQ(K,n1=n1,n2=n2,call.C=TRUE,do.pred=TRUE)
dim(Q5)
dim(Q6)
all(Q5-Q6<1e-6)

```

grid.auc

grid.auc

Description

grid search for beta that maximize (penalized, partial) auc/sauc/rauc eauc maximizes empirical AUC, but only works with two covariates

Usage

```

grid.auc (formula, dat, beta, approx.type=NULL, approx.param=1, lambda=0, loss=TRUE,
         t0=NULL, t1=NULL,ret.vcov = FALSE)
eauc (formula, dat,t0 = NULL, t1 = NULL)

```

Arguments

formula	a formula
dat	a data frame
beta	a matrix of coefficients
approx.type	a string. If NULL, AUC is computed. If "phi", normal CDF approximation SAUC is computed. If "logistic", logistic approximation SAUC is computed. If "rauc", ramp AUC approximation is computed. Defaults to NULL
approx.param	's' for rauc, 'h' for sauc
loss	a boolean. TRUE is default and means 1-(p)RAUC is computed. If lambda is not 0, loss is forced to be TRUE internally.
t0	a number between 0 and 1 that is the lower boundary of pAUC
t1	a number between 0 and 1 that is the upper boundary of pAUC
lambda	a number that scales the L2 penalty, default to 0, meaning no penalty. If lambda is not 0, loss is forced to be TRUE.
ret.vcov	logical, whether to return an estimate of the covariance matrix of 'beta' for normal or logistic sigmoid functions.

Details

eauc is a shortcut for grid.auc when empirical AUC is the objective function. When loss is FALSE, the criterion function is $\text{mean}_{i,j}(\text{loss})$. When loss is TRUE, including when lambda is not 0, the criterion function is $\text{sum}_{i,j}(\text{loss}) + 0.5 * \text{lambda} * \text{pen}$, i.e. the penalty is added to the sum of penalty and not mean of the penalty

Value

A $n \times n$ matrix

Author(s)

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 Youyi Fong <youyifong@gmail.com>
 Krisztian Sebestyen <>

Examples

```
library(aucm)

dat = sim.dat.1(n=200, seed=1)
beta=cbind(4, 4*seq(-1,0,length=100))
dim(beta)

fit = eauc(y~x1+x2, dat)

## Not run:
```

```

# not run due to r cmd check requirements

par(mfrow=c(3,2))

out1 = grid.auc (y~x1+x2, dat, beta, approx.param=1, loss=FALSE, t0=NULL, t1=NULL, lambda=0,
  approx.type="rauc")
plot(out1$pars[2,]/out1$pars[1,],out1$vals,type="l",xlab=expression(beta[2]/beta[1]),main="RAUC")

# penalized RAUC
out2 = grid.auc (y~x1+x2, dat, beta, approx.param=1, loss=TRUE, t0=NULL, t1=NULL, lambda=0,
  approx.type="rauc")
out3 = grid.auc (y~x1+x2, dat, beta, approx.param=1, loss=TRUE, t0=NULL, t1=NULL, lambda=30,
  approx.type="rauc")
plot(out2$pars[2,]/out2$pars[1,],out2$vals,type="l",xlab=expression(beta[2]/beta[1]),
  main="penalized RAUC loss")
lines(out3$pars[2,]/out3$pars[1,],out3$vals,type="l",col=2)
out2$par
out3$par

# pRAUC
out4 = grid.auc (y~x1+x2, dat, beta, approx.param=1, loss=FALSE, t0=0, t1=0.5, lambda=0,
  approx.type="rauc")
out5 = grid.auc (y~x1+x2, dat, beta, approx.param=1, loss=FALSE, t0=0.5, t1=1, lambda=0,
  approx.type="rauc")
plot(out4$pars[2,]/out4$pars[1,],out4$vals,type="l",xlab=expression(beta[2]/beta[1]),main="pRAUC")
plot(out5$pars[2,]/out5$pars[1,],out5$vals,type="l",xlab=expression(beta[2]/beta[1]),main="pRAUC")
out4$par
out5$par

# penalized pRAUC
out6 = grid.auc (y~x1+x2, dat, beta, approx.param=1, loss=TRUE, t0=0, t1=0.5, lambda=0,
  approx.type="rauc")
out7 = grid.auc (y~x1+x2, dat, beta, approx.param=1, loss=TRUE, t0=0, t1=0.5, lambda=10,
  approx.type="rauc")
plot(out6$pars[2,]/out6$pars[1,],out6$vals,type="l",xlab=expression(beta[2]/beta[1]),
  main="penalized pRAUC loss")
lines(out7$pars[2,]/out7$pars[1,],out7$vals,type="l",col=2)
out6$par
out7$par

## End(Not run)

```

 kyphosis

Kyphosis Data

Description

Kyphosis Data

Usage

```
data(kyphosis)
```

Format

A data frame with 81 observations on the following 5 variables.

`Kyphosis` a factor with levels absent present

`Age` a numeric vector

`Number` a numeric vector

`Start` a numeric vector

`y` a numeric vector

Examples

```
data(kyphosis)
## maybe str(kyphosis) ; plot(kyphosis) ...
```

minQuad

minQuad

Description

minimizes the objective function $0.5a'Qa + b'a$ with respect to "a" subject to $0 \leq a \leq C$, or to the constraints $\text{lower} \leq a \leq \text{upper}$, $v \leq Ax \leq v + r$.

Usage

```
minQuad(H,b,C = 1.0,n1=0,n2=0,
  mem.efficient = FALSE,alpha = NULL,
  lower = NULL,upper = NULL,mat.constr = NULL, lhs.constr = NULL,rhs.constr = NULL,
  control = list(DUP = TRUE,maxit = 1e4, tol = 1e-04,
    verbose = FALSE, ret.ws = FALSE,ret.data = FALSE,
    rank = 0,
    method = c("default","tron","loqo","exhaustive","x"),
    optim.control = list(),
    q = 2,
    ws = c("v","v2","greedy","rv2wg","rvwg","rv","rv2")
  )
)
```

Arguments

H	A symmetric matrix whose <code>typeof</code> returns "double" of dimension (n x n). If <code>mem.efficient = FALSE</code> n = n1*n2 matches the length of the vector 'b' else n = n1 + n2, see details, defaults to NULL.
b	a numeric vector of length 'n' whose <code>typeof</code> returns "double".
C	a numeric variable whose <code>typeof</code> returns "double", defaults to 1.0 . It is the upper bound on alpha's, where the lower bound is 0.0 .
n1,n2	integer variables giving the specific values for n1 = #{diseased}, n2 = #{non-diseased}subjects if <code>mem.efficient = TRUE</code> .
mem.efficient	logical, if FALSE then 'H' is represented by the (n1n2 x n1n2) matrix 'Q' else by the (n1+n2 x n1+n2) matrix 'K', defaults to FALSE.
alpha	a length-n1n2 vector vector of initial values for "alpha", whose <code>typeof</code> returns "double", defaults to NULL, in which case it is set to 0.5C.
control	a list with control parameters. See <code>control.minQuad</code>
mat.constr	m x n constraint matrix for loqo optimizer
lhs.constr	numeric of length 'm', the left hand side constraints for loqo optimizer
rhs.constr	numeric of length 'm', the left hand side for constraints for loqo optimizer
lower	numeric of length 'n', the lower bounds on primal variables for loqo optimizer
upper	numeric of length 'n', the upper bounds on primal variables for loqo optimizer

Details

The function `minQuad` passes its arguments by "reference" via the `.C` function call to C if `DUP = FALSE` to avoid copying the large matrix "Q". When 'H' = 'Q', 'Q' is a symmetric matrix and should have numeric type "double", be of type "matrix" not of "data.frame": `is.matrix(.)` should return "TRUE". We do not make an extra copy by tranposing Q but access the 'flattened' vector in C directly since 'Q' is symmetric. When `'mem.efficient' = TRUE` 'H' = $K_{\{n1+n2 \times n1+n2\}}$ and may be obtained by the function `getK`. 'K' is relevant to AUC estimation, see `rauc` for more details. The "ws" argument sets the type of strategy to select the working set. Denote the two sets of violators as $V0 = \{1 \text{ if } (a[p] > 0.0), (df[p] > 0.0), 0 \text{ ow.}\}$, $VC = \{1 \text{ if } (a[p] < C), (df[p] < 0.0), 0 \text{ ow.}\}$ where "df[a]" stands for the gradient of the objective function at 'a'. "greedy" selects the extremes pairs (max,min) from the two sets (M,m) where $M = \{-df[i], a[i] < C\}$ and $m = \{-df[j] \mid a[j] > 0\}$. "v" selects from violators $V = V0 \cup VC$ ranked by `ldf`. "v2" selects separately from V0 and VC separately, ranked by `ldf`. "rv" selects without replacement (WOR) from all violators. "rvwg" selects WOR from all violators V with probability $\sim |df[V]|$. "rv2wg" selects WOR from the two sets of violators V0 and VC with probability $\sim |df[V]|$. Three methods are available, "tron", "hideo" and "exhaustive". Optimizer 'x' is a slightly faster implementation of the exhaustive method, whereas 'default' is a fast implementation for q = 2 only. The "exhaustive" method should probably not be used beyond working set size q = 8,10 on most computers. The 'loqo' optimizer accepts constraints of the form $v \leq A \cdot x \leq v + r$, $lower \leq x \leq upper$. $v = lhs.constr$ and $r = rhs.constr - lhs.constr$. The entries in 'v','r' and 'A' must be finite. When `verbose` is TRUE, each DCA iteration prints one line. Delta means, for the linear kernel, $\max(\text{abs}((\text{beta.new}-\text{beta.init})/\text{beta.init}))$, and for the nonlinear kernel the difference in penalized RAUC loss. epsilon is the KKT criterion of `minQuad`.

Value

A list with the following elements:

convergence	0 if converged, 1 if maximum iteration is reached.
alpha	estimated vector of coefficients.
value	value of the objective function.
iterations	number of iterations until convergence or "maxit" reached.
epsilon	stopping rule value to be compared to "tol".
n	
nSV	$\#\{0 < a\}$, no. of support vectors.
nBSV	$\#\{a=C\}$, no. of bounded support vectors.
nFSV	$\#\{0 < \alpha < C\}$, no. of unbounded support vectors.
control	the control argument.
ws	if requested, the working set selected at current iteration.

Author(s)

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 Shuxin Yin <>

References

Combining Biomarkers Nonlinearly for Classification Using the Area Under the ROC Curve Y. FONG, S. YIN, Y. HUANG *Biometrika* (2012), pp 1-28

Newton's method for large bound-constrained optimization problems Lin, C.J. and More, J.J. *SIAM Journal on Optimization* (1999), volume 9, pp 1100-1127.

kernlab - An S4 Package for Kernel Methods in R. Alexandros Karatzoglou, Alex Smola, Kurt Hornik, Achim Zeileis *Journal of Statistical Software* (2004) 11(9), 1-20. URL <http://www.jstatsoft.org/v11/i09/>

See Also

[control.minQuad,rauc](#)

ramp.f	<i>ramp.f</i>
--------	---------------

Description

computes ramp function value from paired difference of linear combinations

Usage

```
ramp.f (eta,s,loss=TRUE)
```

Arguments

eta	a vector of paired difference of linear combinations
s	absolute value of the slope parameter
loss	a boolean. If TRUE, return loss function i.e. 1 - RAUC. If FALSE, return RAUC. Default to TRUE, because we minimize loss.

Value

A vector of same size as eta

Author(s)

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Examples

```
dat = sim.dat.1(n=100,seed=1)
X1 = as.matrix(subset(dat, y==0, select=c(x1,x2)))
X2 = as.matrix(subset(dat, y==1, select=c(x1,x2)))
X.diff = get.X.diff (X1, X2)
dim(X1)
dim(X2)
dim(X.diff)
aux = ramp.f(X.diff %*% c(1,1), s=1)
length(aux)
mean(aux)
aux = ramp.f(X.diff %*% c(1,1), s=1, loss=FALSE)
length(aux)
mean(aux)
```

 rauc

rauc

Description

minimizes 1 - (p)AUC plus a penalty

Usage

```
rauc (formula, dat, s = 1, lambda=1, kernel="linear", para=NULL, start.method="rlogit",
eta0.init=NULL, beta.init = NULL, eta.diff.init=NULL,
maxit=50, tol=1e-5, minQuad.control = control.minQuad(),
init.alpha.from.previous = TRUE, mem.efficient = TRUE,
ret.vcov = FALSE, garbage.collection = TRUE, verbose = FALSE, ...
)
```

Arguments

formula	formula, e.g. $y \sim x_1 + x_2$
dat	Data frame
s	absolute value of the slope, default to 1 - REMOVE THIS, the pair (s, lambda) is redundant
lambda	scale parameter in front of the penalty function, default to 1
kernel	See getK for more details
para	See getK for more details
start.method	a string. When kernel is linear: If "rlogit", robust logistic fit is used as beta.init. If "1", a vector of 1 is used as beta.init. If "0", a vector of 0 is used as beta.init.
eta0.init	a vector of the same length as the number of rows in dat
beta.init	a vector of length equal to no. of covariates (without intercept) of initial values for linear kernel.
eta.diff.init	a vector of the same length as the number of rows in dat
maxit	maximum number of iterations in the DCA algorithm
tol	absolute tolerance in RAUC if kernel is not linear, relative tolerance in coefficients if kernel is linear.
minQuad.control	control parameters passed to method minQuad, please see minQuad .
init.alpha.from.previous	defaults to TRUE, if TRUE then after the first iteration minQuad receives as the initial "alpha" the estimate of "alpha" from the previous iteration in dca algorithm.
mem.efficient	if TRUE, the small matrix 'K' instead of 'Q' is used in computations, defaults to TRUE.

ret.vcov logical, whether to return an estimate of the covariance matrix of 'beta' for normal or logistic sigmoid functions.

garbage.collection logical, whether to call `gc` at end of each DCA iteration

verbose prints information at each iteration, defaults to FALSE

... for debugging purposes only

Value

A list with the following elements:

convergence 0 if converged, 1 if maximum iteration is reached.

value value of the objective function.

iterations number of iterations until convergence or 'maxit' reached.

Author(s)

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Examples

```
## Not run:

# options(path.svml = 'D:/downloaded_scientific_programs/svmlight')
# options(path.svml = '~/bin/svmlight')

#####
# a linear example

dat = sim.dat.1(n=200,seed=1)

# convergence takes long, to pass CRAN check, set maxit=1

fit1 = rauc (y~x1+x2, dat, lambda=2, kernel="linear", maxit=2)
#fit2 = rauc.linear (y~x1+x2, dat, lambda=2, verbose=TRUE)
#aux2=fit2$X %*% fit2$coefficients
#all(fit1$linear.combination-aux2<1e-2)
fit1$train.auc # 0.7206015

fit3 = rauc (y~x1+x2, dat, lambda=2, kernel="rbf", para=1, verbose=TRUE)
fit3$train.auc # 0.7773434

fit4 = svml (y~x1+x2, dat, kernel="r", fitted=FALSE, cost=1e4)
```

```

fast.auc(predict(fit4, dat)$posterior[,1], dat$y) # 0.7921805
tune.svm1(y~x1+x2, dat, kernel="r")
#      1      10      100      1000      10000      1e+05
#0.7027569 0.7254135 0.7517794 0.7653133 0.7921805 0.6674687

# glm derived score for comparision
fit.glm=glm(y~x1+x2, dat, family="binomial")
fast.auc(fit1$X %*% fit.glm$coef[-1], fit1$y) #

# add outliers
dat = sim.dat.1(n=200,seed=1, add.outliers=TRUE)

fit3 = rauc (y~x1+x2, dat, lambda=2, kernel="rbf", para=1, verbose=TRUE)
fit3$train.auc # 0.7066667

fit4 = svm1 (y~x1+x2, dat, kernel="r", fitted=FALSE, cost=1e4)
fast.auc(predict(fit4, dat)$posterior[,1], dat$y) # 0.6910101
tune.svm1(y~x1+x2, dat, kernel="r")
#      1      10      100      1000      10000      1e+05
#0.6485859 0.6705051 0.6722222 0.6767677 0.6910101 0.5007071

#####
# a nonlinear example

dat=skin.orange (n=100,seed=1,noise=FALSE)
dim(dat)

# nonlinear kernel fit
fit1 = rauc (y~x1+x2+x3+x4, dat, lambda=2, kernel="rbf", para=1, verbose=TRUE)
# glm fit
fit.glm=glm(y~x1+x2+x3+x4, dat, family="binomial")
# linear kernel fit
fit2 = rauc (y~x1+x2+x3+x4, dat, lambda=2, kernel="linear", start.method = "rlogit", verbose=TRUE)

# training data prediction
fast.auc(fit1$linear.combination, fit1$y)
fast.auc(fit1$X %*% fit.glm$coef[-1], fit1$y)
fast.auc(fit2$linear.combination, fit2$y)

# test data prediction
newdata=skin.orange (n=1000,seed=2,noise=FALSE)
fast.auc(predict(fit1, newdata), newdata$y)
fast.auc(as.matrix(subset(newdata, select=c(x1,x2,x3,x4))) %*% fit.glm$coef[-1], newdata$y)
fast.auc(predict(fit2, newdata), newdata$y)

##### IMPROVEMENTS #####

## rank = 2 problem

```

```

dat = sim.dat.1(n=300,seed=1,add.outliers = TRUE,std.dev = 1.0);fm = y~x1+x2

## linear kernel and random working set selection - low rank (2) problem
## setting initial alpha (to be passed to minQuad at each iteration in dca-loop)
# to estimate from previous dca() iteration
## size of working set is automatically set
set.seed(100)
fit.lin = rauc (fm, dat,lambda=.1,kernel="linear",
verbose=TRUE,maxit = 100,tol = 1e-5,
init.alpha.from.previous = TRUE,mem.efficient = TRUE,
minQuad.control = control.minQuad(
      verbose = 1,maxit = 1e6,tol = 1e-4,
      method = "tron",
      working.set= "rv2wg")
)

## 'rbf' kernel and random working set selection
## low rank mapped to possibly infinite rank problem try larger working set 'q' set.seed(100)
## size of working set is set to q = 100
fit.rbf = rauc (fm, dat,lambda=.1,kernel="rbf",para = 1, verbose=TRUE,maxit = 100,tol = 1e-5,
init.alpha.from.previous = TRUE,mem.efficient = TRUE,
minQuad.control = control.minQuad(
      verbose = 1,maxit = 1e6,tol = 1e-4,
      q = 100,
      method = "tron",
      working.set= "rv2wg")
)

## End(Not run)

```

rlogit

rlogit

Description

Robust logistic regression estimator of Bianco and Yohai

Usage

```

rlogit (formula, dat, const=0.5, kmax=1e3, maxhalf=10, verbose=FALSE)
## S3 method for class 'rlogit'
coef(object,...)
## S3 method for class 'rlogit'
trainauc(fit, training.data=NULL, ...)
## S3 method for class 'rlogit'
predict(object, newdata, ...)
## S3 method for class 'rlogit'
ratio(fit)
logistic.f(eta,h,loss=TRUE)

```

Arguments

<code>formula</code>	a formula specifying the model to be fit.
<code>dat</code>	a data frame containing the outcome and covariates in the model
<code>const</code>	tuning constant used in the computation of the estimator, defaults to 0.5
<code>kmax</code>	maximum number of iterations before convergence, defaults to 1000
<code>maxhalf</code>	max number of step-halving ,defaults to 10
<code>verbose</code>	logical
<code>object</code>	an object of class 'rlogit'
<code>fit</code>	an object that inherits from class 'auc' such as 'rauc' or 'sauc'
<code>newdata</code>	data at which to predict
<code>training.data</code>	data frame used to compute auc based on a fit obtained by a call to rauc, sauc or sauc.dca
<code>eta,h</code>	logistic.f computes for loss = FALSE expit(eta/h) or expit(-eta/h) for loss = TRUE
<code>loss</code>	a boolean. if TRUE (default) logistic loss is assumed.
<code>...</code>	arguments passed to or from methods

Details

This program computes the estimator of Bianco and Yohai (1996) in logistic regression. By default, an intercept term is included and p parameters are estimated. The outcome is coded as a 0/1 binomial variable.

If `initwml == TRUE`, a weighted ML estimator is computed with weights derived from the MCD estimator computed on the explanatory variables. If `initwml == FALSE`, a classical ML fit is performed. When the explanatory variables contain binary observations, it is recommended to set `initwml` to `FALSE` or to modify the code of the algorithm to compute the weights only on the continuous variables.

Value

A list with the following components:

<code>convergence</code>	logical, was convergence achieved
<code>objective</code>	value of the objective function at the minimum
<code>coef</code>	estimates for the parameters
<code>sterror</code>	standard errors of the parameters (if convergence is TRUE)

Author(s)

Christophe Croux, Gentiane Haesbroeck. Thanks to Kristel Joossens and Valentin Todorov for improving the code.

References

Implementing the Bianco and Yohai estimator for Logistic Regression
 Croux, C., and Haesbroeck, G. (2003)
 Computational Statistics and Data Analysis, 44, 273-295

Examples

```
set.seed(1)
x0 <- matrix(rnorm(100,1))
y <- as.numeric(runif(100)>0.5)      # numeric(runif(100)>0.5)
dat=data.frame(y=y, x=x0)
rlogit(y~x, dat)
```

 roc

ROC and AUC

Description

ROC/AUC methods. `fast.auc` calculates the AUC using a sort operation, instead of summing over pairwise differences in R.
`computeRoc` computes an ROC curve.
`plotRoc` plots an ROC curve.
`addRoc` adds an ROC curve to a plot.
`classification.error` computes classification error

Usage

```
fast.auc (score, outcome, t0 = 0, t1 = 1, reverse.sign.if.nece = TRUE, quiet = FALSE)
computeRoc (score, outcome, reverse.sign.if.nece = TRUE, cutpoints
            = NULL)
plotRoc(x, add = FALSE, type = "l", diag.line=TRUE,...)
addRoc (x,...)
classification.error(score, outcome, threshold=NULL, verbose=FALSE)
```

Arguments

<code>score</code>	a vector. Linear combination or score.
<code>outcome</code>	a vector of 0 and 1. Outcome.
<code>t0</code>	a number between 0 and 1 that is the lower boundary of pAUC
<code>t1</code>	a number between 0 and 1 that is the upper boundary of pAUC

<code>reverse.sign.if.nece</code>	a boolean. If TRUE, score is multiplied by -1 if AUC is less than 0.5.
<code>x</code>	a list of two elements: sensitivity and specificity.
<code>diag.line</code>	boolean. If TRUE, a diagonal line is plotted
<code>add</code>	boolean. If TRUE, add to existing plot. If FALSE, create a new plot.
<code>quiet</code>	boolean
<code>cutpoints</code>	cutpoints
<code>threshold</code>	threshold
<code>verbose</code>	boolean
<code>type</code>	line type for lines
<code>...</code>	arguments passed to plot or lines

Details

These functions originally come from Thomas Lumley and Tianxi Cai et al.

Value

`computeRoc` returns a list of sensitivity and specificity.
`plotRoc` and `addRoc` plots ROC curves.

Author(s)

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 Krisztian Sebastyen <>

Examples

```
n=1e2
score=c(rnorm(n/2,1), rnorm(n/2,0))
outcome=rep(1:0, each=n/2)
# cannot print due to r cmd check
#plotRoc(computeRoc(score, outcome))

# commented out b/c slower on pc and cause note when r cmd check
## test, fast.auc2 is a version without all the checking
#score=rnorm(1e5)
#outcome=rbinom(1e5,1,.5)
#system.time(for (i in 1:1e2) fast.auc(score,outcome)) # 4.9 sec
#system.time(for (i in 1:1e2) fast.auc2(score,outcome)) # 3.8 sec
```

sample.for.cv	<i>sample.for.cv</i>
---------------	----------------------

Description

sample.for.cv does sampling for cross validation

Usage

```
sample.for.cv (dat, v, seed)
```

Arguments

dat	a data frame. One of the columns must be named y and y should be 0/1 with 1 for case and 0 for control
v	v-fold cross validation
seed	seed for random number generators

Details

case and controls are sampled separately

Value

A list of two vector of integers: train and test, which refer to the rows of dat

Author(s)

Youyi Fong <youyifong@gmail.com>

sauc.phi	<i>sauc.phi</i>
----------	-----------------

Description

sauc.phi optimizes Normal CDF approximation of AUC using Newton Raphson

Usage

```
sauc.phi (formula,dat,constrain.method="L2",h.method="Lin",start.method="rlogit",
opt.method = "Lin", upper = NULL, verbose = FALSE, ret.vcov = FALSE, truth = NULL,
beta.init=NULL)
```

Arguments

formula	a formula
dat	a data frame
constrain.method	a string. If "L2", L2 norm is constrained to 1. If "beta1", beta1 is fixed to 1. Default "L2".
h.method	a string. If "Lin", Lin et al, data dependent. If "Vexler", $(n1*n2)^{-0.1}$ Vexler et al (2006). If "MH", Ma and Huang. Default "Lin".
start.method	a string. If "rlogit", robust logistic fit is used as beta.init. If "1", a vector of 1 is used as beta.init. Default "rlogit".
opt.method	character string, possible values are "truth","YH","Lin", please see code for more details
upper	required for opt.method = 'YH'
verbose	logical
ret.vcov	logical, whether to return an estimate of the covariance matrix of 'beta' for normal or logistic sigmoid functions.
truth	numeric, it will be returned as the result of the fit, please see code for more details
beta.init	vector. Initial values for coefficients.

Details

If an error happens during optimization (typically due to solve()), the errors are caught and NAs are returned.

Author(s)

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 Ying Huang <>
 Youyi Fong <youyifong@gmail.com>

Examples

```
seed=26
seed=16
seed=3
dat.train = sim.dat.1(n=200, seed=seed, add.outliers=TRUE)
fits=list()
fits[[1]]=sauc.phi(y~x1+x2, dat.train,constrain.method="L2",h.method="Lin")
fits[[2]]=sauc.phi(y~x1+x2, dat.train,constrain.method="L2",h.method="MH")
fits[[3]]=sauc.phi(y~x1+x2, dat.train,constrain.method="beta1",h.method="Lin")
fits[[4]]=sauc.phi(y~x1+x2, dat.train,constrain.method="beta1",h.method="MH")
# not a good combination of constrain.method and h.method
sapply(fits, function(x) ratio(x)[2])
```

```
# explosion
seed=954
dat.train = sim.dat.1(n=200, seed=seed, add.outliers=TRUE)
fit.1 = sauc.phi(y~x1+x2, dat.train, constrain.method="L2", h.method="Lin")
ratio(fit.1)
```

simulations

Simulate datasets

Description

sim.dat.1 simulates a dataset with two covariates to reproduce Pepe Figure 1. skin.orange simulates a skin of orange dataset as in Hastie et al.

Usage

```
sim.dat.1(n, seed, add.outliers=FALSE, std.dev = 0.2)
```

Arguments

n	sample size
seed	seed for random number generator
add.outliers	boolean. If TRUE, 10% of data are replaced by a contaminating distribution
std.dev	standard deviation in data generating process

Value

A data frame with n rows, and 4 columns: y, x1, x2, and eta, where eta is the linear combination $X \cdot \beta$.

Author(s)

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Examples

```
dat = sim.dat.1(n=100, seed=1)
nrow(dat)

dat = sim.dat.1(n=100, seed=1, add.outliers=TRUE)
nrow(dat)
```

`tune.it`*tune.it*

Description

Tuning methods.

Usage

```
tune.it (formula, dat.train, dat.tune, method, kernel, verbose=TRUE, step.size = 2)
get.gamma0 (formula, dat.train)
```

Arguments

<code>formula</code>	a formula object.
<code>dat.train</code>	a data frame. Training data
<code>dat.tune</code>	a data frame. Tuning data. If NULL, gacv is done.
<code>method</code>	a string. "svm" or "rauc"
<code>kernel</code>	a string. "rbf" or "linear"
<code>verbose</code>	logical
<code>step.size</code>	step size for lambda as in $\text{step.size}^{\text{seq}(-3,3,1)}$, please see code for more details

Value

`tune.it` returns a vector of one or two elements: lamcost and gamma, depending on the kernel.
`get.gamma0` returns $.5/\text{quantile}(\text{dist.}, c(.9,.75,.5))$, where `dist.` is the Euclidian distance between objects from two classes.

Author(s)

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