Package 'adamethods'

August 4, 2020

Type Package

Title Archetypoid Algorithms and Anomaly Detection

Version 1.2.1

Date 2020-08-04

Author Guillermo Vinue, Irene Epifanio

Maintainer Guillermo Vinue <Guillermo.Vinue@uv.es>

Description Collection of several algorithms to obtain archetypoids with small and large databases, and with both classical multivariate data and functional data (univariate and multivariate). Some of these algorithms also allow to detect anomalies (outliers). Please see Vinue and Epifanio (2020) <doi:10.1007/s11634-020-00412-9>.

License GPL (>= 2)

URL https://www.r-project.org

Depends R (>= 3.4.0)

Imports Anthropometry, archetypes, FNN, foreach, graphics, nnls, parallel, stats, tolerance, univOutl, utils

Suggests doParallel, fda

LazyData true

RoxygenNote 6.1.1

NeedsCompilation no

Repository CRAN

Date/Publication 2020-08-04 12:30:14 UTC

R topics documented:

`adalara` *Multivariate parallel archetypoid algorithm for large applications (ADALARA)*

Description

The ADALARA algorithm is based on the CLARA clustering algorithm. This is the parallel version of the algorithm to try to get faster results. It allows to detect anomalies (outliers). There are two different methods to detect them: the adjusted boxplot (default and most reliable option) and tolerance intervals. If needed, tolerance intervals allow to define a degree of outlierness.

Usage

```
adalara(data, N, m, numArchoid, numRep, huge, prob, type_alg = "ada",
        compare = FALSE, vect_tol = c(0.95, 0.9, 0.85), alpha = 0.05,
        outl_degree = c("outl_strong", "outl_semi_strong", "outl_moderate"),
        method = "adjbox", frame)
```

Arguments

`data`	Data matrix. Each row corresponds to an observation and each column corresponds to a variable. All variables are numeric. The data must have row names so that the algorithm can identify the archetypoids in every sample.
`N`	Number of samples.
`m`	Sample size of each sample.
`numArchoid`	Number of archetypes/archetypoids.
`numRep`	For each `numArchoid`, run the archetype algorithm `numRep` times.
`huge`	Penalization added to solve the convex least squares problems.
`prob`	Probability with values in [0,1].
`type_alg`	String. Options are 'ada' for the non-robust adalara algorithm and 'ada_rob' for the robust adalara algorithm.
`compare`	Boolean argument to compute the robust residual sum of squares if `type_alg = "ada"` and the non-robust if `type_alg = "ada_rob"`.
`vect_tol`	Vector with the tolerance values. Default c(0.95, 0.9, 0.85). Needed if `method='toler'`.
`alpha`	Significance level. Default 0.05. Needed if `method='toler'`.
`outl_degree`	Type of outlier to identify the degree of outlierness. Default c("outl_strong", "outl_semi_strong", "outl_moderate"). Needed if `method='toler'`.
`method`	Method to compute the outliers. Options allowed are 'adjbox' for using adjusted boxplots for skewed distributions, and 'toler' for using tolerance intervals.
`frame`	Boolean value to indicate whether the frame is computed (Mair et al., 2017) or not. The frame is made up of a subset of extreme points, so the archetypoids are only computed on the frame. Low frame densities are obtained when only small portions of the data were extreme. However, high frame densities reduce this speed-up.

Value

A list with the following elements:

- cases Optimal vector of archetypoids.
- rss Optimal residual sum of squares.
- outliers: Outliers.

Author(s)

Guillermo Vinue, Irene Epifanio

References

Eugster, M.J.A. and Leisch, F., From Spider-Man to Hero - Archetypal Analysis in R, 2009. *Journal of Statistical Software* **30(8)**, 1-23, https://doi.org/10.18637/jss.v030.i08

Hubert, M. and Vandervieren, E., An adjusted boxplot for skewed distributions, 2008. *Computational Statistics and Data Analysis* **52(12)**, 5186-5201, https://doi.org/10.1016/j.csda.2007.11.008

Kaufman, L. and Rousseeuw, P.J., Clustering Large Data Sets, 1986. *Pattern Recognition in Practice*, 425-437.

Mair, S., Boubekki, A. and Brefeld, U., Frame-based Data Factorizations, 2017. Proceedings of the 34th International Conference on Machine Learning, Sydney, Australia, 1-9.

Moliner, J. and Epifanio, I., Robust multivariate and functional archetypal analysis with application to financial time series analysis, 2019. *Physica A: Statistical Mechanics and its Applications* **519**, 195-208. https://doi.org/10.1016/j.physa.2018.12.036

Vinue, G., Anthropometry: An R Package for Analysis of Anthropometric Data, 2017. *Journal of Statistical Software* **77(6)**, 1-39, https://doi.org/10.18637/jss.v077.i06

See Also

do_ada, do_ada_robust, adalara_no_paral

Examples

```
## Not run:
library(Anthropometry)
library(doParallel)

# Prepare parallelization (including the seed for reproducibility):
no_cores <- detectCores() - 1
cl <- makeCluster(no_cores)
registerDoParallel(cl)
clusterSetRNGStream(cl, iseed = 1)

# Load data:
data(mtcars)
data <- mtcars
n <- nrow(data)

# Arguments for the archetype/archetypoid algorithm:
# Number of archetypoids:
k <- 3
numRep <- 2
huge <- 200

# Size of the random sample of observations:
m <- 10
```

```
# Number of samples:
N <- floor(1 + (n - m)/(m - k))
N

prob <- 0.75

# ADALARA algorithm:
preproc <- preprocessing(data, stand = TRUE, percAccomm = 1)
data1 <- as.data.frame(preproc$data)

adalara_aux <- adalara(data1, N, m, k, numRep, huge, prob,
                       "ada_rob", FALSE, method = "adjbox", frame = FALSE)

#adalara_aux <- adalara(data1, N, m, k, numRep, huge, prob,
#                       "ada_rob", FALSE, vect_tol = c(0.95, 0.9, 0.85), alpha = 0.05,
#                   outl_degree = c("outl_strong", "outl_semi_strong", "outl_moderate"),
#                       method = "toler", frame = FALSE)

# Take the minimum RSS, which is in the second position of every sublist:
adalara <- adalara_aux[which.min(unlist(sapply(adalara_aux, function(x) x[2])))][[1]]
adalara

# End parallelization:
stopCluster(cl)

## End(Not run)
```

`adalara_no_paral` *Multivariate non-parallel archetypoid algorithm for large applications (ADALARA)*

Description

The ADALARA algorithm is based on the CLARA clustering algorithm. This is the non-parallel version of the algorithm. It allows to detect anomalies (outliers). There are two different methods to detect them: the adjusted boxplot (default and most reliable option) and tolerance intervals. If needed, tolerance intervals allow to define a degree of outlierness.

Usage

```
adalara_no_paral(data, seed, N, m, numArchoid, numRep, huge, prob, type_alg = "ada",
                 compare = FALSE, verbose = TRUE, vect_tol = c(0.95, 0.9, 0.85),
                alpha = 0.05, outl_degree = c("outl_strong", "outl_semi_strong",
                 "outl_moderate"), method = "adjbox", frame)
```

Arguments

data	Data matrix. Each row corresponds to an observation and each column corresponds to a variable. All variables are numeric. The data must have row names so that the algorithm can identify the archetypoids in every sample.
seed	Integer value to set the seed. This ensures reproducibility.
N	Number of samples.
m	Sample size of each sample.
numArchoid	Number of archetypes/archetypoids.
numRep	For each numArchoid, run the archetype algorithm numRep times.
huge	Penalization added to solve the convex least squares problems.
prob	Probability with values in [0,1].
type_alg	String. Options are 'ada' for the non-robust adalara algorithm and 'ada_rob' for the robust adalara algorithm.
compare	Boolean argument to compute the robust residual sum of squares if type_alg = "ada" and the non-robust if type_alg = "ada_rob".
verbose	Display progress? Default TRUE.
vect_tol	Vector the tolerance values. Default c(0.95, 0.9, 0.85). Needed if method='toler'.
alpha	Significance level. Default 0.05. Needed if method='toler'.
outl_degree	Type of outlier to identify the degree of outlierness. Default c("outl_strong", "outl_semi_strong", "outl_moderate"). Needed if method='toler'.
method	Method to compute the outliers. Options allowed are 'adjbox' for using adjusted boxplots for skewed distributions, and 'toler' for using tolerance intervals.
frame	Boolean value to indicate whether the frame is computed (Mair et al., 2017) or not. The frame is made up of a subset of extreme points, so the archetypoids are only computed on the frame. Low frame densities are obtained when only small portions of the data were extreme. However, high frame densities reduce this speed-up.

Value

A list with the following elements:

- cases Optimal vector of archetypoids.
- rss Optimal residual sum of squares.
- outliers: Outliers.

Author(s)

Guillermo Vinue, Irene Epifanio

References

Eugster, M.J.A. and Leisch, F., From Spider-Man to Hero - Archetypal Analysis in R, 2009. *Journal of Statistical Software* **30(8)**, 1-23, https://doi.org/10.18637/jss.v030.i08

Hubert, M. and Vandervieren, E., An adjusted boxplot for skewed distributions, 2008. *Computational Statistics and Data Analysis* **52(12)**, 5186-5201, https://doi.org/10.1016/j.csda.2007.11.008

Kaufman, L. and Rousseeuw, P.J., Clustering Large Data Sets, 1986. *Pattern Recognition in Practice*, 425-437.

Mair, S., Boubekki, A. and Brefeld, U., Frame-based Data Factorizations, 2017. Proceedings of the 34th International Conference on Machine Learning, Sydney, Australia, 1-9.

Moliner, J. and Epifanio, I., Robust multivariate and functional archetypal analysis with application to financial time series analysis, 2019. *Physica A: Statistical Mechanics and its Applications* **519**, 195-208. https://doi.org/10.1016/j.physa.2018.12.036

Vinue, G., Anthropometry: An R Package for Analysis of Anthropometric Data, 2017. *Journal of Statistical Software* **77(6)**, 1-39, https://doi.org/10.18637/jss.v077.i06

See Also

do_ada, do_ada_robust, adalara

Examples

```
## Not run:
library(Anthropometry)

# Load data:
data(mtcars)
data <- mtcars
n <- nrow(data)

# Arguments for the archetype/archetypoid algorithm:
# Number of archetypoids:
k <- 3
numRep <- 2
huge <- 200

# Size of the random sample of observations:
m <- 10
# Number of samples:
N <- floor(1 + (n - m)/(m - k))
N

prob <- 0.75

# ADALARA algorithm:
preproc <- preprocessing(data, stand = TRUE, percAccomm = 1)
data1 <- as.data.frame(preproc$data)
res_adalara <- adalara_no_paral(data1, 1, N, m, k,
                                numRep, huge, prob, "ada_rob", FALSE, TRUE,
```

```
                                method = "adjbox", frame = FALSE)

# Examine the results:
res_adalara

res_adalara1 <- adalara_no_paral(data1, 1, N, m, k,
                                numRep, huge, prob, "ada_rob", FALSE, TRUE,
                                vect_tol = c(0.95, 0.9, 0.85),
                          alpha = 0.05, outl_degree = c("outl_strong", "outl_semi_strong",
                                                        "outl_moderate"),
                                method = "toler", frame = FALSE)
res_adalara1


## End(Not run)
```

`archetypoids_funct` *Archetypoid algorithm with the functional Frobenius norm*

Description

Archetypoid algorithm with the functional Frobenius norm to be used with functional data.

Usage

```
archetypoids_funct(numArchoid, data, huge = 200, ArchObj, PM)
```

Arguments

`numArchoid`	Number of archetypoids.
`data`	Data matrix. Each row corresponds to an observation and each column corresponds to a variable. All variables are numeric.
`huge`	Penalization added to solve the convex least squares problems.
`ArchObj`	The list object returned by the `stepArchetypesRawData_funct` function.
`PM`	Penalty matrix obtained with `eval.penalty`.

Value

A list with the following elements:

- cases: Final vector of archetypoids.
- rss: Residual sum of squares corresponding to the final vector of archetypoids.
- archet_ini: Vector of initial archetypoids.
- alphas: Alpha coefficients for the final vector of archetypoids.
- resid: Matrix with the residuals.

Author(s)

Irene Epifanio

References

Epifanio, I., Functional archetype and archetypoid analysis, 2016. *Computational Statistics and Data Analysis* **104**, 24-34, https://doi.org/10.1016/j.csda.2016.06.007

See Also

archetypoids

Examples

```
## Not run:
library(fda)
?growth
str(growth)
hgtm <- t(growth$hgtm)
# Create basis:
basis_fd <- create.bspline.basis(c(1,ncol(hgtm)), 10)
PM <- eval.penalty(basis_fd)
# Make fd object:
temp_points <- 1:ncol(hgtm)
temp_fd <- Data2fd(argvals = temp_points, y = growth$hgtm, basisobj = basis_fd)
data_archs <- t(temp_fd$coefs)

lass <- stepArchetypesRawData_funct(data = data_archs, numArch = 3,
                                    numRep = 5, verbose = FALSE,
                                    saveHistory = FALSE, PM)

af <- archetypoids_funct(3, data_archs, huge = 200, ArchObj = lass, PM)
str(af)

## End(Not run)
```

---

archetypoids_funct_multiv

Archetypoid algorithm with the functional multivariate Frobenius norm

---

Description

Archetypoid algorithm with the functional multivariate Frobenius norm to be used with functional data.

Usage

```
archetypoids_funct_multiv(numArchoid, data, huge = 200, ArchObj, PM)
```

Arguments

numArchoid	Number of archetypoids.
data	Data matrix. Each row corresponds to an observation and each column corresponds to a variable. All variables are numeric.
huge	Penalization added to solve the convex least squares problems.
ArchObj	The list object returned by the stepArchetypesRawData_funct function.
PM	Penalty matrix obtained with eval.penalty.

Value

A list with the following elements:

- cases: Final vector of archetypoids.
- rss: Residual sum of squares corresponding to the final vector of archetypoids.
- archet_ini: Vector of initial archetypoids.
- alphas: Alpha coefficients for the final vector of archetypoids.
- resid: Matrix with the residuals.

Author(s)

Irene Epifanio

References

Epifanio, I., Functional archetype and archetypoid analysis, 2016. *Computational Statistics and Data Analysis* **104**, 24-34, https://doi.org/10.1016/j.csda.2016.06.007

See Also

archetypoids

Examples

```
## Not run:
library(fda)
?growth
str(growth)
hgtm <- growth$hgtm
hgtf <- growth$hgtf[,1:39]

# Create array:
nvars <- 2
data.array <- array(0, dim = c(dim(hgtm), nvars))
data.array[,,1] <- as.matrix(hgtm)
data.array[,,2] <- as.matrix(hgtf)
rownames(data.array) <- 1:nrow(hgtm)
colnames(data.array) <- colnames(hgtm)
str(data.array)
```

```
# Create basis:
nbasis <- 10
basis_fd <- create.bspline.basis(c(1,nrow(hgtm)), nbasis)
PM <- eval.penalty(basis_fd)
# Make fd object:
temp_points <- 1:nrow(hgtm)
temp_fd <- Data2fd(argvals = temp_points, y = data.array, basisobj = basis_fd)

X <- array(0, dim = c(dim(t(temp_fd$coefs[,,1])), nvars))
X[,,1] <- t(temp_fd$coef[,,1])
X[,,2] <- t(temp_fd$coef[,,2])

# Standardize the variables:
Xs <- X
Xs[,,1] <- scale(X[,,1])
Xs[,,2] <- scale(X[,,2])

lass <- stepArchetypesRawData_funct_multiv(data = Xs, numArch = 3,
                                           numRep = 5, verbose = FALSE,
                                           saveHistory = FALSE, PM)

afm <- archetypoids_funct_multiv(3, Xs, huge = 200, ArchObj = lass, PM)
str(afm)

## End(Not run)
```

`archetypoids_funct_multiv_robust` *Archetypoid algorithm with the functional multivariate robust Frobenius norm*

Description

Archetypoid algorithm with the functional multivariate robust Frobenius norm to be used with functional data.

Usage

```
archetypoids_funct_multiv_robust(numArchoid, data, huge = 200, ArchObj, PM, prob)
```

Arguments

`numArchoid`	Number of archetypoids.
`data`	Data matrix. Each row corresponds to an observation and each column corresponds to a variable. All variables are numeric.
`huge`	Penalization added to solve the convex least squares problems.
`ArchObj`	The list object returned by the `stepArchetypesRawData_funct` function.

PM	Penalty matrix obtained with eval.penalty.
prob	Probability with values in [0,1].

Value

A list with the following elements:

- cases: Final vector of archetypoids.
- rss: Residual sum of squares corresponding to the final vector of archetypoids.
- archet_ini: Vector of initial archetypoids.
- alphas: Alpha coefficients for the final vector of archetypoids.
- resid: Matrix with the residuals.

Author(s)

Irene Epifanio

References

Moliner, J. and Epifanio, I., Robust multivariate and functional archetypal analysis with application to financial time series analysis, 2019. *Physica A: Statistical Mechanics and its Applications* **519**, 195-208. https://doi.org/10.1016/j.physa.2018.12.036

See Also

archetypoids

Examples

```
## Not run:
library(fda)
?growth
str(growth)
hgtm <- growth$hgtm
hgtf <- growth$hgtf[,1:39]

# Create array:
nvars <- 2
data.array <- array(0, dim = c(dim(hgtm), nvars))
data.array[,,1] <- as.matrix(hgtm)
data.array[,,2] <- as.matrix(hgtf)
rownames(data.array) <- 1:nrow(hgtm)
colnames(data.array) <- colnames(hgtm)
str(data.array)

# Create basis:
nbasis <- 10
basis_fd <- create.bspline.basis(c(1,nrow(hgtm)), nbasis)
PM <- eval.penalty(basis_fd)
# Make fd object:
```

```
temp_points <- 1:nrow(hgtm)
temp_fd <- Data2fd(argvals = temp_points, y = data.array, basisobj = basis_fd)

X <- array(0, dim = c(dim(t(temp_fd$coefs[,,1])), nvars))
X[,,1] <- t(temp_fd$coef[,,1])
X[,,2] <- t(temp_fd$coef[,,2])

# Standardize the variables:
Xs <- X
Xs[,,1] <- scale(X[,,1])
Xs[,,2] <- scale(X[,,2])

lass <- stepArchetypesRawData_funct_multiv_robust(data = Xs, numArch = 3,
                                                  numRep = 5, verbose = FALSE,
                                                  saveHistory = FALSE, PM, prob = 0.8,
                                                  nbasis, nvars)

afmr <- archetypoids_funct_multiv_robust(3, Xs, huge = 200, ArchObj = lass, PM, 0.8)
str(afmr)

## End(Not run)
```

`archetypoids_funct_robust` *Archetypoid algorithm with the functional robust Frobenius norm*

Description

Archetypoid algorithm with the functional robust Frobenius norm to be used with functional data.

Usage

```
archetypoids_funct_robust(numArchoid, data, huge = 200, ArchObj, PM, prob)
```

Arguments

`numArchoid`	Number of archetypoids.
`data`	Data matrix. Each row corresponds to an observation and each column corresponds to a variable. All variables are numeric.
`huge`	Penalization added to solve the convex least squares problems.
`ArchObj`	The list object returned by the `stepArchetypesRawData_funct_robust` function.
`PM`	Penalty matrix obtained with `eval.penalty`.
`prob`	Probability with values in [0,1].

Value

A list with the following elements:

- cases: Final vector of archetypoids.
- rss: Residual sum of squares corresponding to the final vector of archetypoids.
- archet_ini: Vector of initial archetypoids.
- alphas: Alpha coefficients for the final vector of archetypoids.
- resid: Matrix with the residuals.

Author(s)

Irene Epifanio

References

Moliner, J. and Epifanio, I., Robust multivariate and functional archetypal analysis with application to financial time series analysis, 2019. *Physica A: Statistical Mechanics and its Applications* **519**, 195-208. https://doi.org/10.1016/j.physa.2018.12.036

See Also

archetypoids

Examples

```
## Not run:
library(fda)
?growth
str(growth)
hgtm <- t(growth$hgtm)
# Create basis:
basis_fd <- create.bspline.basis(c(1,ncol(hgtm)), 10)
PM <- eval.penalty(basis_fd)
# Make fd object:
temp_points <- 1:ncol(hgtm)
temp_fd <- Data2fd(argvals = temp_points, y = growth$hgtm, basisobj = basis_fd)
data_archs <- t(temp_fd$coefs)

lass <- stepArchetypesRawData_funct_robust(data = data_archs, numArch = 3,
                                           numRep = 5, verbose = FALSE,
                                           saveHistory = FALSE, PM, prob = 0.8)

afr <- archetypoids_funct_robust(3, data_archs, huge = 200, ArchObj = lass, PM, 0.8)
str(afr)

## End(Not run)
```

archetypoids_norm_frob *Archetypoid algorithm with the Frobenius norm*

Description

This function is the same as archetypoids but the 2-norm is replaced by the Frobenius norm. Thus, the comparison with the robust archetypoids can be directly made.

Usage

```
archetypoids_norm_frob(numArchoid, data, huge = 200, ArchObj)
```

Arguments

numArchoid	Number of archetypoids.
data	Data matrix. Each row corresponds to an observation and each column corresponds to a variable. All variables are numeric.
huge	Penalization added to solve the convex least squares problems.
ArchObj	The list object returned by the stepArchetypesRawData_norm_frob function.

Value

A list with the following elements:

- cases: Final vector of archetypoids.
- rss: Residual sum of squares corresponding to the final vector of archetypoids.
- archet_ini: Vector of initial archetypoids.
- alphas: Alpha coefficients for the final vector of archetypoids.
- resid: Matrix with the residuals.

Author(s)

Irene Epifanio

References

Eugster, M.J.A. and Leisch, F., From Spider-Man to Hero - Archetypal Analysis in R, 2009. *Journal of Statistical Software* **30(8)**, 1-23, https://doi.org/10.18637/jss.v030.i08

Moliner, J. and Epifanio, I., Robust multivariate and functional archetypal analysis with application to financial time series analysis, 2019. *Physica A: Statistical Mechanics and its Applications* **519**, 195-208. https://doi.org/10.1016/j.physa.2018.12.036

Vinue, G., Epifanio, I., and Alemany, S., Archetypoids: a new approach to define representative archetypal data, 2015. *Computational Statistics and Data Analysis* **87**, 102-115, https://doi.org/10.1016/j.csda.2015.01.018

Vinue, G., Anthropometry: An R Package for Analysis of Anthropometric Data, 2017. *Journal of Statistical Software* **77(6)**, 1-39, https://doi.org/10.18637/jss.v077.i06

See Also

archetypoids

Examples

```
data(mtcars)
data <- mtcars

k <- 3
numRep <- 2
huge <- 200

lass <- stepArchetypesRawData_norm_frob(data = data, numArch = k,
                                        numRep = numRep, verbose = FALSE)

res <- archetypoids_norm_frob(k, data, huge, ArchObj = lass)
str(res)
res$cases
res$rss
```

---

archetypoids_robust *Archetypoid algorithm with the robust Frobenius norm*

Description

Robust version of the archetypoid algorithm with the Frobenius form.

Usage

```
archetypoids_robust(numArchoid, data, huge = 200, ArchObj, prob)
```

Arguments

numArchoid	Number of archetypoids.
data	Data matrix. Each row corresponds to an observation and each column corresponds to a variable. All variables are numeric.
huge	Penalization added to solve the convex least squares problems.
ArchObj	The list object returned by the stepArchetypesRawData_robust function.
prob	Probability with values in [0,1].

Value

A list with the following elements:

- cases: Final vector of archetypoids.
- rss: Residual sum of squares corresponding to the final vector of archetypoids.

- archet_ini: Vector of initial archetypoids.
- alphas: Alpha coefficients for the final vector of archetypoids.
- resid: Matrix with the residuals.

Author(s)

Irene Epifanio

References

Moliner, J. and Epifanio, I., Robust multivariate and functional archetypal analysis with application to financial time series analysis, 2019. *Physica A: Statistical Mechanics and its Applications* **519**, 195-208. https://doi.org/10.1016/j.physa.2018.12.036

See Also

archetypoids_norm_frob

Examples

```
data(mtcars)
data <- mtcars

k <- 3
numRep <- 2
huge <- 200

lass <- stepArchetypesRawData_robust(data = data, numArch = k,
                                     numRep = numRep, verbose = FALSE,
                                     saveHistory = FALSE, prob = 0.8)

res <- archetypoids_robust(k, data, huge, ArchObj = lass, 0.8)
str(res)
res$cases
res$rss
```

---

bisquare_function *Bisquare function*

Description

This function belongs to the bisquare family of loss functions. The bisquare family can better cope with extreme outliers.

Usage

```
bisquare_function(resid, prob, ...)
```

Arguments

resid	Vector of residuals, computed from the $m \times n$ residuals data matrix.
prob	Probability with values in [0,1].
...	Additional possible arguments.

Value

Vector of real numbers.

Author(s)

Irene Epifanio

References

Moliner, J. and Epifanio, I., Robust multivariate and functional archetypal analysis with application to financial time series analysis, 2019. *Physica A: Statistical Mechanics and its Applications* **519**, 195-208. https://doi.org/10.1016/j.physa.2018.12.036

Examples

```
resid <- c(2.47, 11.85)
bisquare_function(resid, 0.8)
```

---

do_ada *Run the whole classical archetypoid analysis with the Frobenius norm*

Description

This function executes the entire procedure involved in the archetypoid analysis. Firstly, the initial vector of archetypoids is obtained using the archetypal algorithm and finally, the optimal vector of archetypoids is returned.

Usage

```
do_ada(subset, numArchoid, numRep, huge, compare = FALSE,
               vect_tol = c(0.95, 0.9, 0.85), alpha = 0.05,
            outl_degree = c("outl_strong", "outl_semi_strong", "outl_moderate"),
               method = "adjbox", prob)
```

Arguments

subset	Data to obtain archetypes. In ADALARA this is a subset of the entire data frame.
numArchoid	Number of archetypes/archetypoids.
numRep	For each numArch, run the archetype algorithm numRep times.
huge	Penalization added to solve the convex least squares problems.
compare	Boolean argument to compute the robust residual sum of squares to compare these results with the ones provided by do_ada_robust.
vect_tol	Vector the tolerance values. Default c(0.95, 0.9, 0.85). Needed if method='toler'.
alpha	Significance level. Default 0.05. Needed if method='toler'.
outl_degree	Type of outlier to identify the degree of outlierness. Default c("outl_strong", "outl_semi_strong", "outl_moderate"). Needed if method='toler'.
method	Method to compute the outliers. Options allowed are 'adjbox' for using adjusted boxplots for skewed distributions, and 'toler' for using tolerance intervals.
prob	If compare=TRUE, probability with values in [0,1].

Value

A list with the following elements:

- cases: Final vector of archetypoids.
- alphas: Alpha coefficients for the final vector of archetypoids.
- rss: Residual sum of squares corresponding to the final vector of archetypoids.
- rss_rob: If compare=TRUE, this is the residual sum of squares using the robust Frobenius norm. Otherwise, NULL.
- resid: Vector with the residuals.
- outliers: Outliers.

Author(s)

Guillermo Vinue, Irene Epifanio

References

Eugster, M.J.A. and Leisch, F., From Spider-Man to Hero - Archetypal Analysis in R, 2009. *Journal of Statistical Software* **30(8)**, 1-23, https://doi.org/10.18637/jss.v030.i08

Vinue, G., Epifanio, I., and Alemany, S., Archetypoids: a new approach to define representative archetypal data, 2015. *Computational Statistics and Data Analysis* **87**, 102-115, https://doi.org/10.1016/j.csda.2015.01.018

Vinue, G., Anthropometry: An R Package for Analysis of Anthropometric Data, 2017. *Journal of Statistical Software* **77(6)**, 1-39, https://doi.org/10.18637/jss.v077.i06

See Also

stepArchetypesRawData_norm_frob, archetypoids_norm_frob

Examples

```
library(Anthropometry)
data(mtcars)
#data <- as.matrix(mtcars)
data <- mtcars

k <- 3
numRep <- 2
huge <- 200

preproc <- preprocessing(data, stand = TRUE, percAccomm = 1)
suppressWarnings(RNGversion("3.5.0"))
set.seed(2018)
res_ada <- do_ada(preproc$data, k, numRep, huge, FALSE, method = "adjbox")
str(res_ada)

res_ada1 <- do_ada(preproc$data, k, numRep, huge, FALSE,
                   vect_tol = c(0.95, 0.9, 0.85), alpha = 0.05,
                   outl_degree = c("outl_strong", "outl_semi_strong",
                                   "outl_moderate"), method = "toler")
str(res_ada1)

res_ada2 <- do_ada(preproc$data, k, numRep, huge, TRUE, method = "adjbox", prob = 0.8)
str(res_ada2)
```

---

do_ada_robust *Run the whole robust archetypoid analysis with the robust Frobenius norm*

Description

This function executes the entire procedure involved in the robust archetypoid analysis. Firstly, the initial vector of archetypoids is obtained using the robust archetypal algorithm and finally, the optimal vector of robust archetypoids is returned.

Usage

```
do_ada_robust(subset, numArchoid, numRep, huge, prob, compare = FALSE,
              vect_tol = c(0.95, 0.9, 0.85), alpha = 0.05,
            outl_degree = c("outl_strong", "outl_semi_strong", "outl_moderate"),
              method = "adjbox")
```

Arguments

subset	Data to obtain archetypes. In ADALARA this is a subset of the entire data frame.
numArchoid	Number of archetypes/archetypoids.

numRep	For each numArch, run the archetype algorithm numRep times.
huge	Penalization added to solve the convex least squares problems.
prob	Probability with values in [0,1].
compare	Boolean argument to compute the non-robust residual sum of squares to compare these results with the ones provided by do_ada.
vect_tol	Vector the tolerance values. Default c(0.95, 0.9, 0.85). Needed if method='toler'.
alpha	Significance level. Default 0.05. Needed if method='toler'.
outl_degree	Type of outlier to identify the degree of outlierness. Default c("outl_strong", "outl_semi_strong", "outl_moderate"). Needed if method='toler'.
method	Method to compute the outliers. Options allowed are 'adjbox' for using adjusted boxplots for skewed distributions, and 'toler' for using tolerance intervals.

Value

A list with the following elements:

- cases: Final vector of archetypoids.
- alphas: Alpha coefficients for the final vector of archetypoids.
- rss: Residual sum of squares corresponding to the final vector of archetypoids.
- rss_non_rob: If compare=TRUE, this is the residual sum of squares using the non-robust Frobenius norm. Otherwise, NULL.
- resid Vector of residuals.
- outliers: Outliers.

Author(s)

Guillermo Vinue, Irene Epifanio

References

Moliner, J. and Epifanio, I., Robust multivariate and functional archetypal analysis with application to financial time series analysis, 2019. *Physica A: Statistical Mechanics and its Applications* **519**, 195-208. https://doi.org/10.1016/j.physa.2018.12.036

See Also

stepArchetypesRawData_robust, archetypoids_robust

Examples

```
## Not run:
library(Anthropometry)
data(mtcars)
#data <- as.matrix(mtcars)
data <- mtcars

k <- 3
```

```
numRep <- 2
huge <- 200

preproc <- preprocessing(data, stand = TRUE, percAccomm = 1)
suppressWarnings(RNGversion("3.5.0"))
set.seed(2018)
res_ada_rob <- do_ada_robust(preproc$data, k, numRep, huge, 0.8,
                             FALSE, method = "adjbox")
str(res_ada_rob)

res_ada_rob1 <- do_ada_robust(preproc$data, k, numRep, huge, 0.8,
                             FALSE, vect_tol = c(0.95, 0.9, 0.85), alpha = 0.05,
                             outl_degree = c("outl_strong", "outl_semi_strong",
                                             "outl_moderate"),
                             method = "toler")
str(res_ada_rob1)

## End(Not run)
```

`do_alphas_rss` *Alphas and RSS of every set of archetypoids*

Description

In the ADALARA algorithm, every time that a set of archetypoids is computed using a sample of the data, the alpha coefficients and the associated residual sum of squares (RSS) for the entire data set must be computed.

Usage

```
do_alphas_rss(data, subset, huge, k_subset, rand_obs, alphas_subset,
              type_alg = "ada", PM, prob)
```

Arguments

`data`	Data matrix with all the observations.
`subset`	Data matrix with a sample of the `data` observations.
`huge`	Penalization added to solve the convex least squares problems.
`k_subset`	Archetypoids obtained from `subset`.
`rand_obs`	Sample observations that form `subset`.
`alphas_subset`	Alpha coefficients related to `k_subset`.
`type_alg`	String. Options are 'ada' for the non-robust multivariate adalara algorithm, 'ada_rob' for the robust multivariate adalara algorithm, 'fada' for the non-robust fda fadalara algorithm and 'fada_rob' for the robust fda fadalara algorithm.
`PM`	Penalty matrix obtained with `eval.penalty`. Needed when `type_alg = 'fada'` or `type_alg = 'fada_rob'`.
`prob`	Probability with values in [0,1]. Needed when `type_alg = 'ada_rob'` or `type_alg = 'fada_rob'`.

Value

A list with the following elements:

- rss Real number of the residual sum of squares.
- resid_rss Matrix with the residuals.
- alphas Matrix with the alpha values.

Author(s)

Guillermo Vinue

See Also

archetypoids_norm_frob

Examples

```
data(mtcars)
data <- mtcars
n <- nrow(data)
m <- 10

k <- 3
numRep <- 2
huge <- 200

suppressWarnings(RNGversion("3.5.0"))
set.seed(1)
rand_obs_si <- sample(1:n, size = m)

si <- data[rand_obs_si,]
ada_si <- do_ada(si, k, numRep, huge, FALSE)

k_si <- ada_si$cases
alphas_si <- ada_si$alphas
colnames(alphas_si) <- rownames(si)

rss_si <- do_alphas_rss(data, si, huge, k_si, rand_obs_si, alphas_si, "ada")
str(rss_si)
```

---

do_alphas_rss_multiv *Alphas and RSS of every set of multivariate archetypoids*

Description

In the ADALARA algorithm, every time that a set of archetypoids is computed using a sample of the data, the alpha coefficients and the associated residual sum of squares (RSS) for the entire data set must be computed.

Usage

```
do_alphas_rss_multiv(data, subset, huge, k_subset, rand_obs, alphas_subset,
                     type_alg = "ada", PM, prob, nbasis, nvars)
```

Arguments

data	Data matrix with all the observations.
subset	Data matrix with a sample of the data observations.
huge	Penalization added to solve the convex least squares problems.
k_subset	Archetypoids obtained from subset.
rand_obs	Sample observations that form subset.
alphas_subset	Alpha coefficients related to k_subset.
type_alg	String. Options are 'ada' for the non-robust multivariate adalara algorithm, 'ada_rob' for the robust multivariate adalara algorithm, 'fada' for the non-robust fda fadalara algorithm and 'fada_rob' for the robust fda fadalara algorithm.
PM	Penalty matrix obtained with eval.penalty. Needed when type_alg = 'fada' or type_alg = 'fada_rob'.
prob	Probability with values in [0,1]. Needed when type_alg = 'ada_rob' or type_alg = 'fada_rob'.
nbasis	Number of basis.
nvars	Number of variables.

Value

A list with the following elements:

- rss Real number of the residual sum of squares.
- resid_rss Matrix with the residuals.
- alphas Matrix with the alpha values.

Author(s)

Guillermo Vinue

See Also

archetypoids_norm_frob

Examples

```
## Not run:
library(fda)
?growth
str(growth)
hgtm <- growth$hgtm
hgtf <- growth$hgtf[,1:39]
```

```
# Create array:
nvars <- 2
data.array <- array(0, dim = c(dim(hgtm), nvars))
data.array[,,1] <- as.matrix(hgtm)
data.array[,,2] <- as.matrix(hgtf)
rownames(data.array) <- 1:nrow(hgtm)
colnames(data.array) <- colnames(hgtm)
str(data.array)

# Create basis:
nbasis <- 10
basis_fd <- create.bspline.basis(c(1,nrow(hgtm)), nbasis)
PM <- eval.penalty(basis_fd)
# Make fd object:
temp_points <- 1:nrow(hgtm)
temp_fd <- Data2fd(argvals = temp_points, y = data.array, basisobj = basis_fd)

X <- array(0, dim = c(dim(t(temp_fd$coefs[,,1])), nvars))
X[,,1] <- t(temp_fd$coef[,,1])
X[,,2] <- t(temp_fd$coef[,,2])

# Standardize the variables:
Xs <- X
Xs[,,1] <- scale(X[,,1])
Xs[,,2] <- scale(X[,,2])
# We have to give names to the dimensions to know the
# observations that were identified as archetypoids.
dimnames(Xs) <- list(paste("Obs", 1:dim(hgtm)[2], sep = ""),
                     1:nbasis,
                     c("boys", "girls"))

n <- dim(Xs)[1]
# Number of archetypoids:
k <- 3
numRep <- 20
huge <- 200

# Size of the random sample of observations:
m <- 15
# Number of samples:
N <- floor(1 + (n - m)/(m - k))
N
prob <- 0.75
data_alg <- Xs

nbasis <- dim(data_alg)[2] # number of basis.
nvars <- dim(data_alg)[3] # number of variables.
n <- nrow(data_alg)

suppressWarnings(RNGversion("3.5.0"))
set.seed(1)
rand_obs_si <- sample(1:n, size = m)
```

```
si <- apply(data_alg, 2:3, function(x) x[rand_obs_si])

fada_si <- do_fada_multiv_robust(si, k, numRep, huge, 0.8, FALSE, PM)

k_si <- fada_si$cases
alphas_si <- fada_si$alphas
colnames(alphas_si) <- rownames(si)

rss_si <- do_alphas_rss_multiv(data_alg, si, huge, k_si, rand_obs_si, alphas_si,
                               "fada_rob", PM, 0.8, nbasis, nvars)
str(rss_si)

## End(Not run)
```

`do_clean` *Cleaning outliers*

Description

Cleaning of the most remarkable outliers. This improves the performance of the archetypoid algorithm since it is not affected by spurious points.

Usage

```
do_clean(data, num_pts, range = 1.5, out_perc = 80)
```

Arguments

`data`	Data frame with (temporal) points in the rows and observations in the columns.
`num_pts`	Number of temporal points.
`range`	Same parameter as in function `boxplot`. A value of 1.5 is enough to detect amplitude and shift outliers, while a value of 3 is needed to detect isolated outliers.
`out_perc`	Minimum number of temporal points (in percentage) to consider the observation as an outlier. Needed when `range=1.5`.

Value

Numeric vector with the outliers.

Author(s)

Irene Epifanio

See Also

`boxplot`

Examples

```
data(mtcars)
data <- mtcars
num_pts <- ncol(data)
do_clean(t(data), num_pts, 1.5, 80)
```

`do_clean_multiv` *Cleaning multivariate functional outliers*

Description

Cleaning of the most remarkable multivariate functional outliers. This improves the performance of the archetypoid algorithm since it is not affected by spurious points.

Usage

```
do_clean_multiv(data, num_pts, range = 1.5, out_perc = 80, nbasis, nvars)
```

Arguments

`data`	Data frame with (temporal) points in the rows and observations in the columns.
`num_pts`	Number of temporal points.
`range`	Same parameter as in function `boxplot`. A value of 1.5 is enough to detect amplitude and shift outliers, while a value of 3 is needed to detect isolated outliers.
`out_perc`	Minimum number of temporal points (in percentage) to consider the observation as an outlier. Needed when `range=1.5`.
`nbasis`	Number of basis.
`nvars`	Number of variables.

Value

List with the outliers for each variable.

Author(s)

Irene Epifanio

See Also

`boxplot`

Examples

```
## Not run:
library(fda)
?growth
str(growth)
hgtm <- growth$hgtm
hgtf <- growth$hgtf[,1:39]

# Create array:
nvars <- 2
data.array <- array(0, dim = c(dim(hgtm), nvars))
data.array[,,1] <- as.matrix(hgtm)
data.array[,,2] <- as.matrix(hgtf)
rownames(data.array) <- 1:nrow(hgtm)
colnames(data.array) <- colnames(hgtm)
str(data.array)

# Create basis:
nbasis <- 10
basis_fd <- create.bspline.basis(c(1,nrow(hgtm)), nbasis)
PM <- eval.penalty(basis_fd)
# Make fd object:
temp_points <- 1:nrow(hgtm)
temp_fd <- Data2fd(argvals = temp_points, y = data.array, basisobj = basis_fd)

X <- array(0, dim = c(dim(t(temp_fd$coefs[,,1])), nvars))
X[,,1] <- t(temp_fd$coef[,,1])
X[,,2] <- t(temp_fd$coef[,,2])

# Standardize the variables:
Xs <- X
Xs[,,1] <- scale(X[,,1])
Xs[,,2] <- scale(X[,,2])

x1 <- t(Xs[,,1])
for (i in 2:nvars) {
 x12 <- t(Xs[,,i])
 x1 <- rbind(x1, x12)
}
data_all <- t(x1)

num_pts <- ncol(data_all) / nvars
range <- 3
outl <- do_clean_multiv(t(data_all), num_pts, range, out_perc, nbasis, nvars)
outl

## End(Not run)
```

do_fada *Run the whole functional archetypoid analysis with the Frobenius norm*

Description

This function executes the entire procedure involved in the functional archetypoid analysis. Firstly, the initial vector of archetypoids is obtained using the functional archetypal algorithm and finally, the optimal vector of archetypoids is returned.

Usage

```
do_fada(subset, numArchoid, numRep, huge, compare = FALSE, PM,
              vect_tol = c(0.95, 0.9, 0.85), alpha = 0.05,
            outl_degree = c("outl_strong", "outl_semi_strong", "outl_moderate"),
              method = "adjbox", prob)
```

Arguments

subset	Data to obtain archetypes. In fadalara this is a subset of the entire data frame.
numArchoid	Number of archetypes/archetypoids.
numRep	For each numArch, run the archetype algorithm numRep times.
huge	Penalization added to solve the convex least squares problems.
compare	Boolean argument to compute the robust residual sum of squares to compare these results with the ones provided by do_fada_robust.
PM	Penalty matrix obtained with eval.penalty.
vect_tol	Vector the tolerance values. Default c(0.95, 0.9, 0.85). Needed if method='toler'.
alpha	Significance level. Default 0.05. Needed if method='toler'.
outl_degree	Type of outlier to identify the degree of outlierness. Default c("outl_strong", "outl_semi_strong", "outl_moderate"). Needed if method='toler'.
method	Method to compute the outliers. Options allowed are 'adjbox' for using adjusted boxplots for skewed distributions, and 'toler' for using tolerance intervals.
prob	If compare=TRUE, probability with values in [0,1].

Value

A list with the following elements:

- cases: Final vector of archetypoids.
- alphas: Alpha coefficients for the final vector of archetypoids.
- rss: Residual sum of squares corresponding to the final vector of archetypoids.
- rss_rob: If compare_robust=TRUE, this is the residual sum of squares using the robust Frobenius norm. Otherwise, NULL.
- resid: Vector of residuals.
- outliers: Outliers.

Author(s)

Guillermo Vinue, Irene Epifanio

References

Epifanio, I., Functional archetype and archetypoid analysis, 2016. *Computational Statistics and Data Analysis* **104**, 24-34, https://doi.org/10.1016/j.csda.2016.06.007

See Also

stepArchetypesRawData_funct, archetypoids_funct

Examples

```
## Not run:
library(fda)
?growth
str(growth)
hgtm <- t(growth$hgtm)

# Create basis:
basis_fd <- create.bspline.basis(c(1,ncol(hgtm)), 10)
PM <- eval.penalty(basis_fd)
# Make fd object:
temp_points <- 1:ncol(hgtm)
temp_fd <- Data2fd(argvals = temp_points, y = growth$hgtm, basisobj = basis_fd)
data_archs <- t(temp_fd$coefs)

suppressWarnings(RNGversion("3.5.0"))
set.seed(2018)
res_fada <- do_fada(subset = data_archs, numArchoid = 3, numRep = 5, huge = 200,
                    compare = FALSE, PM = PM, method = "adjbox")
str(res_fada)

suppressWarnings(RNGversion("3.5.0"))
set.seed(2018)
res_fada1 <- do_fada(subset = data_archs, numArchoid = 3, numRep = 5, huge = 200,
                     compare = FALSE, PM = PM,
                     vect_tol = c(0.95, 0.9, 0.85), alpha = 0.05,
                    outl_degree = c("outl_strong", "outl_semi_strong", "outl_moderate"),
                     method = "toler")
str(res_fada1)

res_fada2 <- do_fada(subset = data_archs, numArchoid = 3, numRep = 5, huge = 200,
                    compare = TRUE, PM = PM, method = "adjbox", prob = 0.8)
str(res_fada2)


## End(Not run)
```

`do_fada_multiv` *Run the whole archetypoid analysis with the functional multivariate Frobenius norm*

Description

This function executes the entire procedure involved in the functional archetypoid analysis. Firstly, the initial vector of archetypoids is obtained using the functional archetypal algorithm and finally, the optimal vector of archetypoids is returned.

Usage

```
do_fada_multiv(subset, numArchoid, numRep, huge, compare = FALSE, PM,
               method = "adjbox", prob)
```

Arguments

`subset`	Data to obtain archetypes. In fadalara this is a subset of the entire data frame.
`numArchoid`	Number of archetypes/archetypoids.
`numRep`	For each `numArch`, run the archetype algorithm `numRep` times.
`huge`	Penalization added to solve the convex least squares problems.
`compare`	Boolean argument to compute the robust residual sum of squares to compare these results with the ones provided by `do_fada_robust`.
`PM`	Penalty matrix obtained with `eval.penalty`.
`method`	Method to compute the outliers. So far the only option allowed is 'adjbox' for using adjusted boxplots for skewed distributions. The use of tolerance intervals might also be explored in the future for the multivariate case.
`prob`	If `compare=TRUE`, probability with values in [0,1].

Value

A list with the following elements:

- cases: Final vector of archetypoids.
- alphas: Alpha coefficients for the final vector of archetypoids.
- rss: Residual sum of squares corresponding to the final vector of archetypoids.
- rss_rob: If `compare_robust=TRUE`, this is the residual sum of squares using the robust Frobenius norm. Otherwise, NULL.
- resid: Vector of residuals.
- outliers: Outliers.

Author(s)

Guillermo Vinue, Irene Epifanio

References

Epifanio, I., Functional archetype and archetypoid analysis, 2016. *Computational Statistics and Data Analysis* **104**, 24-34, https://doi.org/10.1016/j.csda.2016.06.007

See Also

stepArchetypesRawData_funct_multiv, archetypoids_funct_multiv

Examples

```
## Not run:
library(fda)
?growth
str(growth)
hgtm <- growth$hgtm
hgtf <- growth$hgtf[,1:39]

# Create array:
nvars <- 2
data.array <- array(0, dim = c(dim(hgtm), nvars))
data.array[,,1] <- as.matrix(hgtm)
data.array[,,2] <- as.matrix(hgtf)
rownames(data.array) <- 1:nrow(hgtm)
colnames(data.array) <- colnames(hgtm)
str(data.array)

# Create basis:
nbasis <- 10
basis_fd <- create.bspline.basis(c(1,nrow(hgtm)), nbasis)
PM <- eval.penalty(basis_fd)
# Make fd object:
temp_points <- 1:nrow(hgtm)
temp_fd <- Data2fd(argvals = temp_points, y = data.array, basisobj = basis_fd)

X <- array(0, dim = c(dim(t(temp_fd$coefs[,,1])), nvars))
X[,,1] <- t(temp_fd$coef[,,1])
X[,,2] <- t(temp_fd$coef[,,2])

# Standardize the variables:
Xs <- X
Xs[,,1] <- scale(X[,,1])
Xs[,,2] <- scale(X[,,2])

suppressWarnings(RNGversion("3.5.0"))
set.seed(2018)
res_fada <- do_fada_multiv(subset = Xs, numArchoid = 3, numRep = 5, huge = 200,
                           compare = FALSE, PM = PM, method = "adjbox")
str(res_fada)

## End(Not run)
```

`do_fada_multiv_robust` *Run the whole archetypoid analysis with the functional multivariate robust Frobenius norm*

Description

This function executes the entire procedure involved in the functional archetypoid analysis. Firstly, the initial vector of archetypoids is obtained using the functional archetypal algorithm and finally, the optimal vector of archetypoids is returned.

Usage

```
do_fada_multiv_robust(subset, numArchoid, numRep, huge, prob, compare = FALSE, PM,
                      method = "adjbox")
```

Arguments

`subset`	Data to obtain archetypes. In fadalara this is a subset of the entire data frame.
`numArchoid`	Number of archetypes/archetypoids.
`numRep`	For each `numArch`, run the archetype algorithm `numRep` times.
`huge`	Penalization to solve the convex least squares problem, see `archetypoids`.
`prob`	Probability with values in [0,1].
`compare`	Boolean argument to compute the non-robust residual sum of squares to compare these results with the ones provided by `do_fada`.
`PM`	Penalty matrix obtained with `eval.penalty`.
`method`	Method to compute the outliers. So far the only option allowed is 'adjbox' for using adjusted boxplots for skewed distributions. The use of tolerance intervals might also be explored in the future for the multivariate case.

Value

A list with the following elements:

- cases: Final vector of archetypoids.
- alphas: Alpha coefficients for the final vector of archetypoids.
- rss: Residual sum of squares corresponding to the final vector of archetypoids.
- rss_non_rob: If `compare=TRUE`, this is the residual sum of squares using the non-robust Frobenius norm. Otherwise, NULL.
- resid Vector of residuals.
- outliers: Outliers.
- local_rel_imp Matrix with the local (casewise) relative importance (in percentage) of each variable for the outlier identification. Only for the multivariate case. It is relative to the outlier observation itself. The other observations are not considered for computing this importance. This procedure works because the functional variables are in the same scale, after standardizing. Otherwise, it couldn't be interpreted like that.

- margi_rel_imp Matrix with the marginal relative importance of each variable (in percentage) for the outlier identification. Only for the multivariate case. In this case, the other points are considered, since the value of the outlier observation is compared with the remaining points.

Author(s)

Guillermo Vinue, Irene Epifanio

References

Moliner, J. and Epifanio, I., Robust multivariate and functional archetypal analysis with application to financial time series analysis, 2019. *Physica A: Statistical Mechanics and its Applications* **519**, 195-208. https://doi.org/10.1016/j.physa.2018.12.036

See Also

stepArchetypesRawData_funct_multiv_robust, archetypoids_funct_multiv_robust

Examples

```
## Not run:
library(fda)
?growth
str(growth)
hgtm <- growth$hgtm
hgtf <- growth$hgtf[,1:39]

# Create array:
nvars <- 2
data.array <- array(0, dim = c(dim(hgtm), nvars))
data.array[,,1] <- as.matrix(hgtm)
data.array[,,2] <- as.matrix(hgtf)
rownames(data.array) <- 1:nrow(hgtm)
colnames(data.array) <- colnames(hgtm)
str(data.array)

# Create basis:
nbasis <- 10
basis_fd <- create.bspline.basis(c(1,nrow(hgtm)), nbasis)
PM <- eval.penalty(basis_fd)
# Make fd object:
temp_points <- 1:nrow(hgtm)
temp_fd <- Data2fd(argvals = temp_points, y = data.array, basisobj = basis_fd)

X <- array(0, dim = c(dim(t(temp_fd$coefs[,,1])), nvars))
X[,,1] <- t(temp_fd$coef[,,1])
X[,,2] <- t(temp_fd$coef[,,2])

# Standardize the variables:
Xs <- X
Xs[,,1] <- scale(X[,,1])
Xs[,,2] <- scale(X[,,2])
```

```
suppressWarnings(RNGversion("3.5.0"))
set.seed(2018)
res_fada <- do_fada_multiv_robust(subset = Xs, numArchoid = 3, numRep = 5, huge = 200,
                                  prob = 0.75, compare = FALSE, PM = PM, method = "adjbox")
str(res_fada)
res_fada$cases
#[1]  8 24 29
res_fada$rss
#[1] 2.301741

## End(Not run)
```

`do_fada_robust` *Run the whole archetypoid analysis with the functional robust Frobenius norm*

Description

This function executes the entire procedure involved in the functional archetypoid analysis. Firstly, the initial vector of archetypoids is obtained using the functional archetypal algorithm and finally, the optimal vector of archetypoids is returned.

Usage

```
do_fada_robust(subset, numArchoid, numRep, huge, prob, compare = FALSE, PM,
               vect_tol = c(0.95, 0.9, 0.85), alpha = 0.05,
             outl_degree = c("outl_strong", "outl_semi_strong", "outl_moderate"),
               method = "adjbox")
```

Arguments

`subset`	Data to obtain archetypes. In fadalara this is a subset of the entire data frame.
`numArchoid`	Number of archetypes/archetypoids.
`numRep`	For each `numArch`, run the archetype algorithm `numRep` times.
`huge`	Penalization added to solve the convex least squares problems.
`prob`	Probability with values in [0,1].
`compare`	Boolean argument to compute the non-robust residual sum of squares to compare these results with the ones provided by `do_fada`.
`PM`	Penalty matrix obtained with `eval.penalty`.
`vect_tol`	Vector the tolerance values. Default c(0.95, 0.9, 0.85). Needed if `method='toler'`.
`alpha`	Significance level. Default 0.05. Needed if `method='toler'`.
`outl_degree`	Type of outlier to identify the degree of outlierness. Default c("outl_strong", "outl_semi_strong", "outl_moderate"). Needed if `method='toler'`.
`method`	Method to compute the outliers. Options allowed are 'adjbox' for using adjusted boxplots for skewed distributions, and 'toler' for using tolerance intervals.

Value

A list with the following elements:

- cases: Final vector of archetypoids.
- alphas: Alpha coefficients for the final vector of archetypoids.
- rss: Residual sum of squares corresponding to the final vector of archetypoids.
- rss_non_rob: If `compare=TRUE`, this is the residual sum of squares using the non-robust Frobenius norm. Otherwise, NULL.
- resid: Vector of residuals.
- outliers: Outliers.

Author(s)

Guillermo Vinue, Irene Epifanio

References

Moliner, J. and Epifanio, I., Robust multivariate and functional archetypal analysis with application to financial time series analysis, 2019. *Physica A: Statistical Mechanics and its Applications* **519**, 195-208. https://doi.org/10.1016/j.physa.2018.12.036

See Also

stepArchetypesRawData_funct_robust, archetypoids_funct_robust

Examples

```
## Not run:
library(fda)
?growth
str(growth)
hgtm <- t(growth$hgtm)

# Create basis:
basis_fd <- create.bspline.basis(c(1,ncol(hgtm)), 10)
PM <- eval.penalty(basis_fd)
# Make fd object:
temp_points <- 1:ncol(hgtm)
temp_fd <- Data2fd(argvals = temp_points, y = growth$hgtm, basisobj = basis_fd)
data_archs <- t(temp_fd$coefs)

suppressWarnings(RNGversion("3.5.0"))
set.seed(2018)
res_fada_rob <- do_fada_robust(subset = data_archs, numArchoid = 3, numRep = 5, huge = 200,
                               prob = 0.75, compare = FALSE, PM = PM, method = "adjbox")
str(res_fada_rob)

suppressWarnings(RNGversion("3.5.0"))
set.seed(2018)
res_fada_rob1 <- do_fada_robust(subset = data_archs, numArchoid = 3, numRep = 5, huge = 200,
```

```
                                prob = 0.75, compare = FALSE, PM = PM,
                                vect_tol = c(0.95, 0.9, 0.85), alpha = 0.05,
                          outl_degree = c("outl_strong", "outl_semi_strong", "outl_moderate"),
                                method = "toler")
str(res_fada_rob1)

## End(Not run)
```

---

do_knno *kNN for outlier detection*

Description

Ramaswamy et al. proposed the k-nearest neighbors outlier detection method (kNNo). Each point's anomaly score is the distance to its kth nearest neighbor in the data set. Then, all points are ranked based on this distance. The higher an example's score is, the more anomalous it is.

Usage

```
do_knno(data, k, top_n)
```

Arguments

data	Data observations.
k	Number of neighbors of a point that we are interested in.
top_n	Total number of outliers we are interested in.

Value

Vector of outliers.

Author(s)

Guillermo Vinue

References

Ramaswamy, S., Rastogi, R. and Shim, K. Efficient Algorithms for Mining Outliers from Large Data Sets. SIGMOD'00 Proceedings of the 2000 ACM SIGMOD international conference on Management of data, 2000, 427-438.

Examples

```
data(mtcars)
data <- as.matrix(mtcars)
outl <- do_knno(data, 3, 2)
outl
data[outl,]
```

do_outl_degree *Degree of outlierness*

Description

Classification of outliers according to their degree of outlierness. They are classified using the tolerance proportion. For instance, outliers from a 95

Usage

```
do_outl_degree(vect_tol = c(0.95, 0.9, 0.85), resid_vect, alpha = 0.05,
            outl_degree = c("outl_strong", "outl_semi_strong", "outl_moderate"))
```

Arguments

vect_tol	Vector the tolerance values. Default c(0.95, 0.9, 0.85).
resid_vect	Vector of n residuals, where n was the number of rows of the data matrix.
alpha	Significance level. Default 0.05.
outl_degree	Type of outlier to identify the degree of outlierness. Default c("outl_strong", "outl_semi_strong", "outl_moderate").

Value

List with the type outliers.

Author(s)

Guillermo Vinue

See Also

outl_toler

Examples

```
do_outl_degree(0.95, 1:100, 0.05, "outl_strong")
```

fadalara *Functional parallel archetypoid algorithm for large applications (FADALARA)*

Description

The FADALARA algorithm is based on the CLARA clustering algorithm. This is the parallel version of the algorithm. It allows to detect anomalies (outliers). In the univariate case, there are two different methods to detect them: the adjusted boxplot (default and most reliable option) and tolerance intervals. In the multivariate case, only adjusted boxplots are used. If needed, tolerance intervals allow to define a degree of outlierness.

Usage

```
fadalara(data, N, m, numArchoid, numRep, huge, prob, type_alg = "fada",
         compare = FALSE, PM, vect_tol = c(0.95, 0.9, 0.85), alpha = 0.05,
         outl_degree = c("outl_strong", "outl_semi_strong", "outl_moderate"),
         method = "adjbox", multiv, frame)
```

Arguments

data	Data matrix. Each row corresponds to an observation and each column corresponds to a variable. All variables are numeric. The data must have row names so that the algorithm can identify the archetypoids in every sample.
N	Number of samples.
m	Sample size of each sample.
numArchoid	Number of archetypes/archetypoids.
numRep	For each numArch, run the archetype algorithm numRep times.
huge	Penalization added to solve the convex least squares problems.
prob	Probability with values in [0,1].
type_alg	String. Options are 'fada' for the non-robust fadalara algorithm, whereas 'fada_rob' is for the robust fadalara algorithm.
compare	Boolean argument to compute the robust residual sum of squares if type_alg = "fada" and the non-robust if type_alg = "fada_rob".
PM	Penalty matrix obtained with eval.penalty.
vect_tol	Vector the tolerance values. Default c(0.95, 0.9, 0.85). Needed if method='toler'.
alpha	Significance level. Default 0.05. Needed if method='toler'.
outl_degree	Type of outlier to identify the degree of outlierness. Default c("outl_strong", "outl_semi_strong", "outl_moderate"). Needed if method='toler'.
method	Method to compute the outliers. Options allowed are 'adjbox' for using adjusted boxplots for skewed distributions, and 'toler' for using tolerance intervals. The tolerance intervals are only computed in the univariate case, i.e., method='toler' only valid if multiv=FALSE.

multiv	Multivariate (TRUE) or univariate (FALSE) algorithm.
frame	Boolean value to indicate whether the frame is computed (Mair et al., 2017) or not. The frame is made up of a subset of extreme points, so the archetypoids are only computed on the frame. Low frame densities are obtained when only small portions of the data were extreme. However, high frame densities reduce this speed-up.

Value

A list with the following elements:

- cases Vector of archetypoids.
- rss Optimal residual sum of squares.
- outliers: Outliers.
- alphas: Matrix with the alpha coefficients.
- local_rel_imp Matrix with the local (casewise) relative importance (in percentage) of each variable for the outlier identification. Only for the multivariate case. It is relative to the outlier observation itself. The other observations are not considered for computing this importance. This procedure works because the functional variables are in the same scale, after standardizing. Otherwise, it couldn't be interpreted like that.
- margi_rel_imp Matrix with the marginal relative importance of each variable (in percentage) for the outlier identification. Only for the multivariate case. In this case, the other points are considered, since the value of the outlier observation is compared with the remaining points.

Author(s)

Guillermo Vinue, Irene Epifanio

References

Epifanio, I., Functional archetype and archetypoid analysis, 2016. *Computational Statistics and Data Analysis* **104**, 24-34, https://doi.org/10.1016/j.csda.2016.06.007

Hubert, M. and Vandervieren, E., An adjusted boxplot for skewed distributions, 2008. *Computational Statistics and Data Analysis* **52(12)**, 5186-5201, https://doi.org/10.1016/j.csda.2007.11.008

Kaufman, L. and Rousseeuw, P.J., Clustering Large Data Sets, 1986. *Pattern Recognition in Practice*, 425-437.

Mair, S., Boubekki, A. and Brefeld, U., Frame-based Data Factorizations, 2017. Proceedings of the 34th International Conference on Machine Learning, Sydney, Australia, 1-9.

Moliner, J. and Epifanio, I., Robust multivariate and functional archetypal analysis with application to financial time series analysis, 2019. *Physica A: Statistical Mechanics and its Applications* **519**, 195-208. https://doi.org/10.1016/j.physa.2018.12.036

See Also

do_fada, do_fada_robust

Examples

```
## Not run:
library(fda)
?growth
str(growth)
hgtm <- growth$hgtm
hgtf <- growth$hgtf[,1:39]

# Create array:
nvars <- 2
data.array <- array(0, dim = c(dim(hgtm), nvars))
data.array[,,1] <- as.matrix(hgtm)
data.array[,,2] <- as.matrix(hgtf)
rownames(data.array) <- 1:nrow(hgtm)
colnames(data.array) <- colnames(hgtm)
str(data.array)

# Create basis:
nbasis <- 10
basis_fd <- create.bspline.basis(c(1,nrow(hgtm)), nbasis)
PM <- eval.penalty(basis_fd)
# Make fd object:
temp_points <- 1:nrow(hgtm)
temp_fd <- Data2fd(argvals = temp_points, y = data.array, basisobj = basis_fd)

X <- array(0, dim = c(dim(t(temp_fd$coefs[,,1])), nvars))
X[,,1] <- t(temp_fd$coef[,,1])
X[,,2] <- t(temp_fd$coef[,,2])

# Standardize the variables:
Xs <- X
Xs[,,1] <- scale(X[,,1])
Xs[,,2] <- scale(X[,,2])
# We have to give names to the dimensions to know the
# observations that were identified as archetypoids.
dimnames(Xs) <- list(paste("Obs", 1:dim(hgtm)[2], sep = ""),
                     1:nbasis,
                     c("boys", "girls"))

n <- dim(Xs)[1]
# Number of archetypoids:
k <- 3
numRep <- 20
huge <- 200

# Size of the random sample of observations:
m <- 15
# Number of samples:
N <- floor(1 + (n - m)/(m - k))
N
prob <- 0.75
data_alg <- Xs
```

```
# Parallel:
# Prepare parallelization (including the seed for reproducibility):
library(doParallel)
no_cores <- detectCores() - 1
no_cores
cl <- makeCluster(no_cores)
registerDoParallel(cl)
clusterSetRNGStream(cl, iseed = 2018)
res_fl <- fadalara(data = data_alg, N = N, m = m, numArchoid = k, numRep = numRep,
                   huge = huge, prob = prob, type_alg = "fada_rob", compare = FALSE,
                  PM = PM, method = "adjbox", multiv = TRUE, frame = FALSE) # frame = TRUE
stopCluster(cl)

res_fl_copy <- res_fl
res_fl <- res_fl[which.min(unlist(sapply(res_fl, function(x) x[2])))][[1]]
str(res_fl)
res_fl$cases
res_fl$rss
as.vector(res_fl$outliers)

## End(Not run)
```

`fadalara_no_paral` *Functional non-parallel archetypoid algorithm for large applications (FADALARA)*

Description

The FADALARA algorithm is based on the CLARA clustering algorithm. This is the non-parallel version of the algorithm. It allows to detect anomalies (outliers). In the univariate case, there are two different methods to detect them: the adjusted boxplot (default and most reliable option) and tolerance intervals. In the multivariate case, only adjusted boxplots are used. If needed, tolerance intervals allow to define a degree of outlierness.

Usage

```
fadalara_no_paral(data, seed, N, m, numArchoid, numRep, huge, prob, type_alg = "fada",
              compare = FALSE, verbose = TRUE, PM, vect_tol = c(0.95, 0.9, 0.85),
                alpha = 0.05, outl_degree = c("outl_strong", "outl_semi_strong",
                  "outl_moderate"), method = "adjbox", multiv, frame)
```

Arguments

`data`	Data matrix. Each row corresponds to an observation and each column corresponds to a variable (temporal point). All variables are numeric. The data must have row names so that the algorithm can identify the archetypoids in every sample.

seed	Integer value to set the seed. This ensures reproducibility.
N	Number of samples.
m	Sample size of each sample.
numArchoid	Number of archetypes/archetypoids.
numRep	For each numArch, run the archetype algorithm numRep times.
huge	Penalization added to solve the convex least squares problems.
prob	Probability with values in [0,1].
type_alg	String. Options are 'fada' for the non-robust fadalara algorithm, whereas 'fada_rob' is for the robust fadalara algorithm.
compare	Boolean argument to compute the robust residual sum of squares if type_alg = "fada" and the non-robust if type_alg = "fada_rob".
verbose	Display progress? Default TRUE.
PM	Penalty matrix obtained with eval.penalty.
vect_tol	Vector the tolerance values. Default c(0.95, 0.9, 0.85). Needed if method='toler'.
alpha	Significance level. Default 0.05. Needed if method='toler'.
outl_degree	Type of outlier to identify the degree of outlierness. Default c("outl_strong", "outl_semi_strong", "outl_moderate"). Needed if method='toler'.
method	Method to compute the outliers. Options allowed are 'adjbox' for using adjusted boxplots for skewed distributions, and 'toler' for using tolerance intervals. The tolerance intervals are only computed in the univariate case, i.e., method='toler' only valid if multiv = FALSE.
multiv	Multivariate (TRUE) or univariate (FALSE) algorithm.
frame	Boolean value to indicate whether the frame is computed (Mair et al., 2017) or not. The frame is made up of a subset of extreme points, so the archetypoids are only computed on the frame. Low frame densities are obtained when only small portions of the data were extreme. However, high frame densities reduce this speed-up.

Value

A list with the following elements:

- cases Vector of archetypoids.
- rss Optimal residual sum of squares.
- outliers: Vector of outliers.
- alphas: Matrix with the alpha coefficients.
- local_rel_imp Matrix with the local (casewise) relative importance (in percentage) of each variable for the outlier identification. Only for the multivariate case. It is relative to the outlier observation itself. The other observations are not considered for computing this importance. This procedure works because the functional variables are in the same scale, after standardizing. Otherwise, it couldn't be interpreted like that.
- margi_rel_imp Matrix with the marginal relative importance of each variable (in percentage) for the outlier identification. Only for the multivariate case. In this case, the other points are considered, since the value of the outlier observation is compared with the remaining points.

Author(s)

Guillermo Vinue, Irene Epifanio

References

Epifanio, I., Functional archetype and archetypoid analysis, 2016. *Computational Statistics and Data Analysis* **104**, 24-34, https://doi.org/10.1016/j.csda.2016.06.007

Hubert, M. and Vandervieren, E., An adjusted boxplot for skewed distributions, 2008. *Computational Statistics and Data Analysis* **52(12)**, 5186-5201, https://doi.org/10.1016/j.csda.2007.11.008

Kaufman, L. and Rousseeuw, P.J., Clustering Large Data Sets, 1986. *Pattern Recognition in Practice*, 425-437.

Mair, S., Boubekki, A. and Brefeld, U., Frame-based Data Factorizations, 2017. Proceedings of the 34th International Conference on Machine Learning, Sydney, Australia, 1-9.

Moliner, J. and Epifanio, I., Robust multivariate and functional archetypal analysis with application to financial time series analysis, 2019. *Physica A: Statistical Mechanics and its Applications* **519**, 195-208. https://doi.org/10.1016/j.physa.2018.12.036

See Also

fadalara

Examples

```
## Not run:
library(fda)
?growth
str(growth)
hgtm <- growth$hgtm
hgtf <- growth$hgtf[,1:39]

# Create array:
nvars <- 2
data.array <- array(0, dim = c(dim(hgtm), nvars))
data.array[,,1] <- as.matrix(hgtm)
data.array[,,2] <- as.matrix(hgtf)
rownames(data.array) <- 1:nrow(hgtm)
colnames(data.array) <- colnames(hgtm)
str(data.array)

# Create basis:
nbasis <- 10
basis_fd <- create.bspline.basis(c(1,nrow(hgtm)), nbasis)
PM <- eval.penalty(basis_fd)
# Make fd object:
temp_points <- 1:nrow(hgtm)
temp_fd <- Data2fd(argvals = temp_points, y = data.array, basisobj = basis_fd)

X <- array(0, dim = c(dim(t(temp_fd$coefs[,,1])), nvars))
```

```
X[,,1] <- t(temp_fd$coef[,,1])
X[,,2] <- t(temp_fd$coef[,,2])

# Standardize the variables:
Xs <- X
Xs[,,1] <- scale(X[,,1])
Xs[,,2] <- scale(X[,,2])
# We have to give names to the dimensions to know the
# observations that were identified as archetypoids.
dimnames(Xs) <- list(paste("Obs", 1:dim(hgtm)[2], sep = ""),
                     1:nbasis,
                     c("boys", "girls"))

n <- dim(Xs)[1]
# Number of archetypoids:
k <- 3
numRep <- 20
huge <- 200

# Size of the random sample of observations:
m <- 15
# Number of samples:
N <- floor(1 + (n - m)/(m - k))
N
prob <- 0.75
data_alg <- Xs

seed <- 2018
res_fl <- fadalara_no_paral(data = data_alg, seed = seed, N = N, m = m,
                            numArchoid = k, numRep = numRep, huge = huge,
                            prob = prob, type_alg = "fada_rob", compare = FALSE,
                            verbose = TRUE, PM = PM, method = "adjbox", multiv = TRUE,
                            frame = FALSE) # frame = TRUE

str(res_fl)
res_fl$cases
res_fl$rss
as.vector(res_fl$outliers)

## End(Not run)
```

`frame_in_r` *Compute archetypes frame*

Description

Computing the frame with the approach by Mair et al. (2017).

Usage

```
frame_in_r(X)
```

Arguments

X	Data frame.

Value

Vector with the observations that belong to the frame.

Author(s)

Sebastian Mair, code kindly provided by him.

References

Mair, S., Boubekki, A. and Brefeld, U., Frame-based Data Factorizations, 2017. Proceedings of the 34th International Conference on Machine Learning, Sydney, Australia, 1-9.

Examples

```
## Not run:
X <- mtcars
q <- frame_in_r(X)
H <- X[q,]
q

## End(Not run)
```

---

frobenius_norm *Frobenius norm*

Description

Computes the Frobenius norm.

Usage

```
frobenius_norm(m)
```

Arguments

m	Data matrix with the residuals. This matrix has the same dimensions as the original data matrix.

Details

Residuals are vectors. If there are p variables (columns), for every observation there is a residual that there is a p-dimensional vector. If there are n observations, the residuals are an n times p matrix.

Value

Real number.

Author(s)

Guillermo Vinue, Irene Epifanio

References

Eugster, M.J.A. and Leisch, F., From Spider-Man to Hero - Archetypal Analysis in R, 2009. *Journal of Statistical Software* **30(8)**, 1-23, https://doi.org/10.18637/jss.v030.i08

Vinue, G., Epifanio, I., and Alemany, S.,Archetypoids: a new approach to define representative archetypal data, 2015. *Computational Statistics and Data Analysis* **87**, 102-115, https://doi.org/10.1016/j.csda.2015.01.018

Vinue, G., Anthropometry: An R Package for Analysis of Anthropometric Data, 2017. *Journal of Statistical Software* **77(6)**, 1-39, https://doi.org/10.18637/jss.v077.i06

Examples

```
mat <- matrix(1:4, nrow = 2)
frobenius_norm(mat)
```

---

frobenius_norm_funct *Functional Frobenius norm*

Description

Computes the functional Frobenius norm.

Usage

```
frobenius_norm_funct(m, PM)
```

Arguments

m	Data matrix with the residuals. This matrix has the same dimensions as the original data matrix.
PM	Penalty matrix obtained with eval.penalty.

Details

Residuals are vectors. If there are p variables (columns), for every observation there is a residual that there is a p-dimensional vector. If there are n observations, the residuals are an n times p matrix.

Value

Real number.

Author(s)

Irene Epifanio

References

Epifanio, I., Functional archetype and archetypoid analysis, 2016. *Computational Statistics and Data Analysis* **104**, 24-34, https://doi.org/10.1016/j.csda.2016.06.007

Examples

```
library(fda)
mat <- matrix(1:9, nrow = 3)
fbasis <- create.fourier.basis(rangeval = c(1, 32), nbasis = 3)
PM <- eval.penalty(fbasis)
frobenius_norm_funct(mat, PM)
```

---

frobenius_norm_funct_multiv

Functional multivariate Frobenius norm

Description

Computes the functional multivariate Frobenius norm.

Usage

```
frobenius_norm_funct_multiv(m, PM)
```

Arguments

m	Data matrix with the residuals. This matrix has the same dimensions as the original data matrix.
PM	Penalty matrix obtained with eval.penalty.

Details

Residuals are vectors. If there are p variables (columns), for every observation there is a residual that there is a p-dimensional vector. If there are n observations, the residuals are an n times p matrix.

Value

Real number.

Author(s)

Irene Epifanio

References

Epifanio, I., Functional archetype and archetypoid analysis, 2016. *Computational Statistics and Data Analysis* **104**, 24-34, https://doi.org/10.1016/j.csda.2016.06.007

Examples

```
mat <- matrix(1:400, ncol = 20)
PM <- matrix(1:100, ncol = 10)
frobenius_norm_funct_multiv(mat, PM)
```

---

frobenius_norm_funct_multiv_robust

Functional multivariate robust Frobenius norm

Description

Computes the functional multivariate robust Frobenius norm.

Usage

```
frobenius_norm_funct_multiv_robust(m, PM, prob, nbasis, nvars)
```

Arguments

m	Data matrix with the residuals. This matrix has the same dimensions as the original data matrix.
PM	Penalty matrix obtained with eval.penalty.
prob	Probability with values in [0,1].
nbasis	Number of basis.
nvars	Number of variables.

Details

Residuals are vectors. If there are p variables (columns), for every observation there is a residual that there is a p-dimensional vector. If there are n observations, the residuals are an n times p matrix.

Value

Real number.

Author(s)

Irene Epifanio

References

Moliner, J. and Epifanio, I., Robust multivariate and functional archetypal analysis with application to financial time series analysis, 2019. *Physica A: Statistical Mechanics and its Applications* **519**, 195-208. https://doi.org/10.1016/j.physa.2018.12.036

Examples

```
mat <- matrix(1:400, ncol = 20)
PM <- matrix(1:100, ncol = 10)
frobenius_norm_funct_multiv_robust(mat, PM, 0.8, 10, 2)
```

---

frobenius_norm_funct_robust

Functional robust Frobenius norm

Description

Computes the functional robust Frobenius norm.

Usage

```
frobenius_norm_funct_robust(m, PM, prob)
```

Arguments

m	Data matrix with the residuals. This matrix has the same dimensions as the original data matrix.
PM	Penalty matrix obtained with eval.penalty.
prob	Probability with values in [0,1].

Details

Residuals are vectors. If there are p variables (columns), for every observation there is a residual that there is a p-dimensional vector. If there are n observations, the residuals are an n times p matrix.

Value

Real number.

Author(s)

Irene Epifanio

References

Moliner, J. and Epifanio, I., Robust multivariate and functional archetypal analysis with application to financial time series analysis, 2019. *Physica A: Statistical Mechanics and its Applications* **519**, 195-208. https://doi.org/10.1016/j.physa.2018.12.036

Examples

```
library(fda)
mat <- matrix(1:9, nrow = 3)
fbasis <- create.fourier.basis(rangeval = c(1, 32), nbasis = 3)
PM <- eval.penalty(fbasis)
frobenius_norm_funct_robust(mat, PM, 0.8)
```

---

frobenius_norm_robust *Robust Frobenius norm*

Description

Computes the robust Frobenius norm.

Usage

```
frobenius_norm_robust(m, prob)
```

Arguments

m	Data matrix with the residuals. This matrix has the same dimensions as the original data matrix.
prob	Probability with values in [0,1].

Details

Residuals are vectors. If there are p variables (columns), for every observation there is a residual that there is a p-dimensional vector. If there are n observations, the residuals are an n times p matrix.

Value

Real number.

Author(s)

Irene Epifanio

References

Moliner, J. and Epifanio, I., Robust multivariate and functional archetypal analysis with application to financial time series analysis, 2019. *Physica A: Statistical Mechanics and its Applications* **519**, 195-208. https://doi.org/10.1016/j.physa.2018.12.036

Examples

```
mat <- matrix(1:4, nrow = 2)
frobenius_norm_robust(mat, 0.8)
```

`int_prod_mat` *Interior product between matrices*

Description

Helper function to compute the Frobenius norm.

Usage

```
int_prod_mat(m)
```

Arguments

`m`	Data matrix.

Value

Data matrix.

Author(s)

Irene Epifanio

References

Moliner, J. and Epifanio, I., Robust multivariate and functional archetypal analysis with application to financial time series analysis, 2019. *Physica A: Statistical Mechanics and its Applications* **519**, 195-208. https://doi.org/10.1016/j.physa.2018.12.036

Examples

```
mat <- matrix(1:4, nrow = 2)
int_prod_mat(mat)
```

`int_prod_mat_funct` *Interior product between matrices for FDA*

Description

Helper function to compute the Frobenius norm in the functional data analysis (FDA) scenario.

Usage

```
int_prod_mat_funct(m, PM)
```

Arguments

`m`	Data matrix.
`PM`	Penalty matrix obtained with `eval.penalty`.

Value

Data matrix.

Author(s)

Irene Epifanio

References

Moliner, J. and Epifanio, I., Robust multivariate and functional archetypal analysis with application to financial time series analysis, 2019. *Physica A: Statistical Mechanics and its Applications* **519**, 195-208. https://doi.org/10.1016/j.physa.2018.12.036

Examples

```
library(fda)
mat <- matrix(1:9, nrow = 3)
fbasis <- create.fourier.basis(rangeval = c(1, 32), nbasis = 3)
PM <- eval.penalty(fbasis)
int_prod_mat_funct(mat, PM)
```

int_prod_mat_sq *Squared interior product between matrices*

Description

Helper function to compute the robust Frobenius norm.

Usage

```
int_prod_mat_sq(m)
```

Arguments

m	Data matrix.

Value

Data matrix.

Author(s)

Irene Epifanio

References

Moliner, J. and Epifanio, I., Robust multivariate and functional archetypal analysis with application to financial time series analysis, 2019. *Physica A: Statistical Mechanics and its Applications* **519**, 195-208. https://doi.org/10.1016/j.physa.2018.12.036

Examples

```
mat <- matrix(1:4, nrow = 2)
int_prod_mat_sq(mat)
```

int_prod_mat_sq_funct *Squared interior product between matrices for FDA*

Description

Helper function to compute the robust Frobenius norm in the functional data analysis (FDA) scenario.

Usage

```
int_prod_mat_sq_funct(m, PM)
```

Arguments

m	Data matrix.
PM	Penalty matrix obtained with eval.penalty.

Value

Data matrix.

Author(s)

Irene Epifanio

References

Moliner, J. and Epifanio, I., Robust multivariate and functional archetypal analysis with application to financial time series analysis, 2019. *Physica A: Statistical Mechanics and its Applications* **519**, 195-208. https://doi.org/10.1016/j.physa.2018.12.036

Examples

```
library(fda)
mat <- matrix(1:9, nrow = 3)
fbasis <- create.fourier.basis(rangeval = c(1, 32), nbasis = 3)
PM <- eval.penalty(fbasis)
int_prod_mat_sq_funct(mat, PM)
```

---

outl_toler *Tolerance outliers*

Description

Outliers according to a tolerance interval. This function is used by the archetypoid algorithms to identify the outliers. See the function nptol.int in package tolerance.

Usage

```
outl_toler(p_tol = 0.95, resid_vect, alpha = 0.05)
```

Arguments

p_tol	The proportion of observations to be covered by this tolerance interval.
resid_vect	Vector of n residuals, where n was the number of rows of the data matrix.
alpha	Significance level.

Value

Vector with the outliers.

Author(s)

Guillermo Vinue

References

Young, D., tolerance: An R package for estimating tolerance intervals, 2010. *Journal of Statistical Software*, **36(5)**, 1-39, https://doi.org/10.18637/jss.v036.i05

See Also

adalara, fadalara, do_outl_degree

Examples

```
outl_toler(0.95, 1:100, 0.05)
```

---

stepArchetypesRawData_funct

Archetype algorithm to raw data with the functional Frobenius norm

---

Description

This is a slight modification of stepArchetypesRawData to use the functional archetype algorithm with the Frobenius norm.

Usage

```
stepArchetypesRawData_funct(data, numArch, numRep = 3,
                            verbose = TRUE, saveHistory = FALSE, PM)
```

Arguments

data	Data to obtain archetypes.
numArch	Number of archetypes to compute, from 1 to numArch.
numRep	For each numArch, run the archetype algorithm numRep times.
verbose	If TRUE, the progress during execution is shown.
saveHistory	Save execution steps.
PM	Penalty matrix obtained with eval.penalty.

Value

A list with the archetypes.

Author(s)

Irene Epifanio

References

Cutler, A. and Breiman, L., Archetypal Analysis. *Technometrics*, 1994, **36(4)**, 338-347, https://doi.org/10.2307/1269949

Epifanio, I., Functional archetype and archetypoid analysis, 2016. *Computational Statistics and Data Analysis* **104**, 24-34, https://doi.org/10.1016/j.csda.2016.06.007

Eugster, M.J.A. and Leisch, F., From Spider-Man to Hero - Archetypal Analysis in R, 2009. *Journal of Statistical Software* **30(8)**, 1-23, https://doi.org/10.18637/jss.v030.i08

Examples

```
## Not run:
library(fda)
?growth
str(growth)
hgtm <- t(growth$hgtm)
# Create basis:
basis_fd <- create.bspline.basis(c(1,ncol(hgtm)), 10)
PM <- eval.penalty(basis_fd)
# Make fd object:
temp_points <- 1:ncol(hgtm)
temp_fd <- Data2fd(argvals = temp_points, y = growth$hgtm, basisobj = basis_fd)
data_archs <- t(temp_fd$coefs)

lass <- stepArchetypesRawData_funct(data = data_archs, numArch = 3,
                                    numRep = 5, verbose = FALSE,
                                    saveHistory = FALSE, PM)
str(lass)
length(lass[[1]])
class(lass[[1]])
class(lass[[1]][[5]])

## End(Not run)
```

`stepArchetypesRawData_funct_multiv` *Archetype algorithm to raw data with the functional multivariate Frobenius norm*

Description

This is a slight modification of `stepArchetypesRawData` to use the functional archetype algorithm with the multivariate Frobenius norm.

Usage

```
stepArchetypesRawData_funct_multiv(data, numArch, numRep = 3,
                                   verbose = TRUE, saveHistory = FALSE, PM)
```

Arguments

data	Data to obtain archetypes.
numArch	Number of archetypes to compute, from 1 to numArch.
numRep	For each numArch, run the archetype algorithm numRep times.
verbose	If TRUE, the progress during execution is shown.
saveHistory	Save execution steps.
PM	Penalty matrix obtained with eval.penalty.

Value

A list with the archetypes.

Author(s)

Irene Epifanio

References

Cutler, A. and Breiman, L., Archetypal Analysis. *Technometrics*, 1994, **36(4)**, 338-347, https://doi.org/10.2307/1269949

Epifanio, I., Functional archetype and archetypoid analysis, 2016. *Computational Statistics and Data Analysis* **104**, 24-34, https://doi.org/10.1016/j.csda.2016.06.007

Eugster, M.J.A. and Leisch, F., From Spider-Man to Hero - Archetypal Analysis in R, 2009. *Journal of Statistical Software* **30(8)**, 1-23, https://doi.org/10.18637/jss.v030.i08

Examples

```
## Not run:
library(fda)
?growth
str(growth)
hgtm <- growth$hgtm
hgtf <- growth$hgtf[,1:39]

# Create array:
nvars <- 2
data.array <- array(0, dim = c(dim(hgtm), nvars))
data.array[,,1] <- as.matrix(hgtm)
data.array[,,2] <- as.matrix(hgtf)
rownames(data.array) <- 1:nrow(hgtm)
colnames(data.array) <- colnames(hgtm)
str(data.array)

# Create basis:
nbasis <- 10
basis_fd <- create.bspline.basis(c(1,nrow(hgtm)), nbasis)
PM <- eval.penalty(basis_fd)
# Make fd object:
```

```
temp_points <- 1:nrow(hgtm)
temp_fd <- Data2fd(argvals = temp_points, y = data.array, basisobj = basis_fd)

X <- array(0, dim = c(dim(t(temp_fd$coefs[,,1])), nvars))
X[,,1] <- t(temp_fd$coef[,,1])
X[,,2] <- t(temp_fd$coef[,,2])

# Standardize the variables:
Xs <- X
Xs[,,1] <- scale(X[,,1])
Xs[,,2] <- scale(X[,,2])

lass <- stepArchetypesRawData_funct_multiv(data = Xs, numArch = 3,
                                           numRep = 5, verbose = FALSE,
                                           saveHistory = FALSE, PM)

str(lass)
length(lass[[1]])
class(lass[[1]])
class(lass[[1]][[5]])

## End(Not run)
```

`stepArchetypesRawData_funct_multiv_robust` *Archetype algorithm to raw data with the functional multivariate robust Frobenius norm*

Description

This is a slight modification of `stepArchetypesRawData` to use the functional archetype algorithm with the multivariate Frobenius norm.

Usage

```
stepArchetypesRawData_funct_multiv_robust(data, numArch, numRep = 3,
                    verbose = TRUE, saveHistory = FALSE, PM, prob, nbasis, nvars)
```

Arguments

`data`	Data to obtain archetypes.
`numArch`	Number of archetypes to compute, from 1 to `numArch`.
`numRep`	For each `numArch`, run the archetype algorithm `numRep` times.
`verbose`	If TRUE, the progress during execution is shown.
`saveHistory`	Save execution steps.
`PM`	Penalty matrix obtained with `eval.penalty`.

prob	Probability with values in [0,1].
nbasis	Number of basis.
nvars	Number of variables.

Value

A list with the archetypes.

Author(s)

Irene Epifanio

References

Cutler, A. and Breiman, L., Archetypal Analysis. *Technometrics*, 1994, **36(4)**, 338-347, https://doi.org/10.2307/1269949

Epifanio, I., Functional archetype and archetypoid analysis, 2016. *Computational Statistics and Data Analysis* **104**, 24-34, https://doi.org/10.1016/j.csda.2016.06.007

Eugster, M.J.A. and Leisch, F., From Spider-Man to Hero - Archetypal Analysis in R, 2009. *Journal of Statistical Software* **30(8)**, 1-23, https://doi.org/10.18637/jss.v030.i08

Moliner, J. and Epifanio, I., Robust multivariate and functional archetypal analysis with application to financial time series analysis, 2019. *Physica A: Statistical Mechanics and its Applications* **519**, 195-208. https://doi.org/10.1016/j.physa.2018.12.036

Examples

```
## Not run:
library(fda)
?growth
str(growth)
hgtm <- growth$hgtm
hgtf <- growth$hgtf[,1:39]

# Create array:
nvars <- 2
data.array <- array(0, dim = c(dim(hgtm), nvars))
data.array[,,1] <- as.matrix(hgtm)
data.array[,,2] <- as.matrix(hgtf)
rownames(data.array) <- 1:nrow(hgtm)
colnames(data.array) <- colnames(hgtm)
str(data.array)

# Create basis:
nbasis <- 10
basis_fd <- create.bspline.basis(c(1,nrow(hgtm)), nbasis)
PM <- eval.penalty(basis_fd)
# Make fd object:
temp_points <- 1:nrow(hgtm)
temp_fd <- Data2fd(argvals = temp_points, y = data.array, basisobj = basis_fd)
```

```
X <- array(0, dim = c(dim(t(temp_fd$coefs[,,1])), nvars))
X[,,1] <- t(temp_fd$coef[,,1])
X[,,2] <- t(temp_fd$coef[,,2])

# Standardize the variables:
Xs <- X
Xs[,,1] <- scale(X[,,1])
Xs[,,2] <- scale(X[,,2])

lass <- stepArchetypesRawData_funct_multiv_robust(data = Xs, numArch = 3,
                                                  numRep = 5, verbose = FALSE,
                                                  saveHistory = FALSE, PM, prob = 0.8,
                                                  nbasis, nvars)
str(lass)
length(lass[[1]])
class(lass[[1]])
class(lass[[1]][[5]])

## End(Not run)
```

`stepArchetypesRawData_funct_robust` *Archetype algorithm to raw data with the functional robust Frobenius norm*

Description

This is a slight modification of `stepArchetypesRawData` to use the functional archetype algorithm with the functional robust Frobenius norm.

Usage

```
stepArchetypesRawData_funct_robust(data, numArch, numRep = 3,
                                   verbose = TRUE, saveHistory = FALSE, PM, prob)
```

Arguments

`data`	Data to obtain archetypes.
`numArch`	Number of archetypes to compute, from 1 to `numArch`.
`numRep`	For each `numArch`, run the archetype algorithm `numRep` times.
`verbose`	If TRUE, the progress during execution is shown.
`saveHistory`	Save execution steps.
`PM`	Penalty matrix obtained with `eval.penalty`.
`prob`	Probability with values in [0,1].

Value

A list with the archetypes.

Author(s)

Irene Epifanio

References

Cutler, A. and Breiman, L., Archetypal Analysis. *Technometrics*, 1994, **36(4)**, 338-347, https://doi.org/10.2307/1269949

Epifanio, I., Functional archetype and archetypoid analysis, 2016. *Computational Statistics and Data Analysis* **104**, 24-34, https://doi.org/10.1016/j.csda.2016.06.007

Eugster, M.J.A. and Leisch, F., From Spider-Man to Hero - Archetypal Analysis in R, 2009. *Journal of Statistical Software* **30(8)**, 1-23, https://doi.org/10.18637/jss.v030.i08

Moliner, J. and Epifanio, I., Robust multivariate and functional archetypal analysis with application to financial time series analysis, 2019. *Physica A: Statistical Mechanics and its Applications* **519**, 195-208. https://doi.org/10.1016/j.physa.2018.12.036

Examples

```
## Not run:
library(fda)
?growth
str(growth)
hgtm <- t(growth$hgtm)
# Create basis:
basis_fd <- create.bspline.basis(c(1,ncol(hgtm)), 10)
PM <- eval.penalty(basis_fd)
# Make fd object:
temp_points <- 1:ncol(hgtm)
temp_fd <- Data2fd(argvals = temp_points, y = growth$hgtm, basisobj = basis_fd)
data_archs <- t(temp_fd$coefs)

lass <- stepArchetypesRawData_funct_robust(data = data_archs, numArch = 3,
                                           numRep = 5, verbose = FALSE,
                                           saveHistory = FALSE, PM, prob = 0.8)
str(lass)
length(lass[[1]])
class(lass[[1]])
class(lass[[1]][[5]])

## End(Not run)
```

stepArchetypesRawData_norm_frob
Archetype algorithm to raw data with the Frobenius norm

Description

This is a slight modification of stepArchetypesRawData to use the archetype algorithm with the Frobenius norm.

Usage

```
stepArchetypesRawData_norm_frob(data, numArch, numRep = 3,
                                verbose = TRUE, saveHistory = FALSE)
```

Arguments

data	Data to obtain archetypes.
numArch	Number of archetypes to compute, from 1 to numArch.
numRep	For each numArch, run the archetype algorithm numRep times.
verbose	If TRUE, the progress during execution is shown.
saveHistory	Save execution steps.

Value

A list with the archetypes.

Author(s)

Irene Epifanio

References

Eugster, M.J.A. and Leisch, F., From Spider-Man to Hero - Archetypal Analysis in R, 2009. *Journal of Statistical Software* **30(8)**, 1-23, https://doi.org/10.18637/jss.v030.i08

Moliner, J. and Epifanio, I., Robust multivariate and functional archetypal analysis with application to financial time series analysis, 2019. *Physica A: Statistical Mechanics and its Applications* **519**, 195-208. https://doi.org/10.1016/j.physa.2018.12.036

Vinue, G., Epifanio, I., and Alemany, S., Archetypoids: a new approach to define representative archetypal data, 2015. *Computational Statistics and Data Analysis* **87**, 102-115, https://doi.org/10.1016/j.csda.2015.01.018

Vinue, G., Anthropometry: An R Package for Analysis of Anthropometric Data, 2017. *Journal of Statistical Software* **77(6)**, 1-39, https://doi.org/10.18637/jss.v077.i06

See Also

stepArchetypesRawData, stepArchetypes

Examples

```
data(mtcars)
data <- as.matrix(mtcars)

numArch <- 5
numRep <- 2

lass <- stepArchetypesRawData_norm_frob(data = data, numArch = 1:numArch,
                                        numRep = numRep, verbose = FALSE)

str(lass)
length(lass[[1]])
class(lass[[1]])
```

---

stepArchetypesRawData_robust

Archetype algorithm to raw data with the robust Frobenius norm

---

Description

This is a slight modification of `stepArchetypesRawData` to use the archetype algorithm with the robust Frobenius norm.

Usage

```
stepArchetypesRawData_robust(data, numArch, numRep = 3,
                             verbose = TRUE, saveHistory = FALSE, prob)
```

Arguments

`data`	Data to obtain archetypes.
`numArch`	Number of archetypes to compute, from 1 to `numArch`.
`numRep`	For each `numArch`, run the archetype algorithm `numRep` times.
`verbose`	If TRUE, the progress during execution is shown.
`saveHistory`	Save execution steps.
`prob`	Probability with values in [0,1].

Value

A list with the archetypes.

Author(s)

Irene Epifanio

References

Moliner, J. and Epifanio, I., Robust multivariate and functional archetypal analysis with application to financial time series analysis, 2019. *Physica A: Statistical Mechanics and its Applications* **519**, 195-208. https://doi.org/10.1016/j.physa.2018.12.036

See Also

stepArchetypesRawData_norm_frob

Examples

```
data(mtcars)
data <- as.matrix(mtcars)

numArch <- 5
numRep <- 2

lass <- stepArchetypesRawData_robust(data = data, numArch = 1:numArch,
                                     numRep = numRep, verbose = FALSE,
                                     saveHistory = FALSE, prob = 0.8)
str(lass)
length(lass[[1]])
class(lass[[1]])
```

Index