Package 'RNOmni'

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Title Rank Normal Transformation Omnibus Test

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Description Genetic association tests that use the rank-based inverse normal transformation (INT). These tests are recommend for continuous traits with non-normally distributed residuals. INT-based tests robustly control the type I error in settings where standard linear regression does not. Moreover, INT-based tests dominate standard linear regression in terms of power. INT-based tests may be classified into two types: tests that directly transform the phenotype (D-INT) and tests that transform phenotypic residuals (I-INT). Our omnibus test (O-INT) adaptively combines D-INT and I-INT into a single robust and statistically powerful approach.
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Author Zachary McCaw [aut, cre]
Maintainer Zachary McCaw <zmccaw@g.harvard.edu></zmccaw@g.harvard.edu>
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BAT Basic Association Test

Description

Conducts tests of association between the loci in G and the untransformed phenotype y, adjusting for the model matrix X.

Usage

```
BAT(y, G, X = NULL, test = "Score", simple = FALSE,
   parallel = FALSE)
```

Arguments

У	Numeric phenotype vector.
G	Obs by snp genotype matrix.
X	Model matrix of covariates and structure adjustments. Should include an intercept. Omit to perform marginal tests of association.
test	Either Score or Wald.
simple	Return the p-values only?
parallel	Logical indicating whether to run in parallel. Must register parallel backend first.

Value

If simple=T, returns a vector of p-values, one for each column of G. If simple=F, returns a numeric matrix, including the Wald or Score statistic, its standard error, the Z-score, and the p-value.

See Also

Direct INT DINT, indirect INT IINT, omnibus INT OINT.

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Examples

```
## Not run:
set.seed(100);
# Design matrix
X = cbind(1,rnorm(1e3));
# Genotypes
G = replicate(1e3,rbinom(n=1e3,size=2,prob=0.25));
storage.mode(G) = "numeric";
# Phenotype
y = as.numeric(X%*%c(1,1))+rnorm(1e3);
# Association test
p = BAT(y=y,G=G,X=X,simple=T);
## End(Not run)
```

cov

Correlation

Description

Calculates the correlation between two vectors.

Usage

```
cov(A, B, cor = FALSE)
```

Arguments

A First matrix.

B Second matrix.

cor Return correlation matrix?

Value

Numeric matrix.

DINT

Direct-INT

Description

Applies the rank-based inverse normal transformation (rankNorm) to the phenotype y. Conducts tests of association between the loci in G and transformed phenotype, adjusting for the model matrix X.

DINT

Usage

```
DINT(y, G, X = NULL, k = 3/8, test = "Score", simple = FALSE,
    parallel = FALSE)
```

Arguments

У	Numeric phenotype vector.
G	Obs by snp genotype matrix.
X	Model matrix of covariates and structure adjustments. Should include an intercept. Omit to perform marginal tests of association.
k	Offset applied during rank-normalization. See rankNorm.
test	Either Score or Wald.
simple	Return the p-values only?
parallel	Logical indicating whether to run in parallel. Must register parallel backend first.

Value

If simple=T, returns a vector of p-values, one for each column of G. If simple=F, returns a numeric matrix, including the Wald or Score statistic, its standard error, the Z-score, and the p-value.

See Also

Basic association test BAT, indirect INT IINT, omnibus INT OINT.

Examples

```
## Not run:
set.seed(100);
# Design matrix
X = cbind(1,rnorm(1e3));
# Genotypes
G = replicate(1e3,rbinom(n=1e3,size=2,prob=0.25));
storage.mode(G) = "numeric";
# Phenotype
y = exp(as.numeric(X%*%c(1,1))+rnorm(1e3));
# Association test
p = DINT(y=y,G=G,X=X,simple=T);
## End(Not run)
```

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fit0LS

Univariate OLS model.

Description

Fits the standard OLS model.

Usage

```
fitOLS(y, X)
```

Arguments

y Numeric vector.

X Numeric matrix.

Value

List containing the following:

Beta Regression coefficient.

V Outcome variance.

Ibb Information matrix for beta.

Resid Outcome residuals.

IINT Indirect-INT

Description

Two-stage association testing procedure. In the first stage, phenotype y and genotype G are each regressed on the model matrix X to obtain residuals. The phenotypic residuals are transformed using rankNorm. In the next stage, the INT-transformed residuals are regressed on the genotypic residuals.

Usage

```
IINT(y, G, X = NULL, k = 3/8, simple = FALSE, parallel = FALSE)
```

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Arguments

У	Numeric phenotype vector.
G	Obs by snp genotype matrix.
X	Model matrix of covariates and structure adjustments. Should include an intercept. Omit to perform marginal tests of association.
k	Offset applied during rank-normalization. See rankNorm.
simple	Return the p-values only?
parallel	Logical indicating whether to run in parallel. Must register parallel backend first.

Value

If simple=T, returns a vector of p-values, one for each column of G. If simple=F, returns a numeric matrix, including the Wald or Score statistic, its standard error, the Z-score, and the p-value.

See Also

Basic association test BAT, direct INT DINT, omnibus INT OINT.

Examples

```
## Not run:
set.seed(100);
# Design matrix
X = cbind(1,rnorm(1e3));
# Genotypes
G = replicate(1e3,rbinom(n=1e3,size=2,prob=0.25));
storage.mode(G) = "numeric";
# Phenotype
y = exp(as.numeric(X%*%c(1,1))+rnorm(1e3));
# Association test
p = IINT(y=y,G=G,X=X,simple=T);
## End(Not run);
```

 ${\tt matInv}$

Matrix Inverse

Description

```
Calcualtes A^{-1}.
```

Usage

```
matInv(A)
```

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Arguments

A Numeric matrix.

Value

A numeric matrix.

matIP

Matrix Inner Product

Description

Calculates the inner product A'B.

Usage

matIP(A, B)

Arguments

A Numeric matrix.

B Numeric matrix.

Value

Numeric matrix.

OINT

Omnibus-INT

Description

Association test that synthesizes the DINT and IINT tests. The first approach is most powerful for traits that could have arisen from a rank-preserving transformation of a latent normal trait. The second approach is most powerful for traits that are linear in covariates, yet have skewed or kurtotic residual distributions. During the omnibus test, the direct and indirect tests are separately applied then

Usage

```
OINT(y, G, X = NULL, k = 3/8, simple = FALSE, parallel = FALSE)
```

OINTp

Arguments

у	Numeric phenotype vector.
G	Obs by locus genotype matrix.
Χ	Model matrix of covariates and structure adjustments. Should include an intercept. Omit to perform marginal tests of association.
k	Offset applied during rank-normalization. See rankNorm.
simple	Return the OINT p-values only?
parallel	Logical indicating whether to run in parallel. Must register parallel backend first.

Value

A numeric matrix of p-values, three for each column of G.

See Also

Basic association test BAT, direct INT DINT, indirect INT IINT.

Examples

```
## Not run:
set.seed(100);
# Design matrix
X = cbind(1,rnorm(1e3));
# Genotypes
G = replicate(1e3,rbinom(n=1e3,size=2,prob=0.25));
storage.mode(G) = "numeric";
# Phenotype
y = exp(as.numeric(X%*%c(1,1))+rnorm(1e3));
# Omnibus
p = OINT(y=y,G=G,X=X,simple=T);
## End(Not run)
```

OINTp

Omnibus p-value

Description

Omnibus p-value

Usage

OINTp(p)

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Arguments

p Vector of p-values

Value

OINT p-value.

rankNorm

Rank-Normalize

Description

Applies the rank based inverse normal transform (INT) to a numeric vector. The INT can be broken down into a two-step procedure. In the first, the observations are transformed onto the probability scale using the empirical cumulative distribution function (ECDF). In the second, the observations are transformed onto the real line, as Z-scores, using the probit function.

Usage

```
rankNorm(u, k = 3/8)
```

Arguments

u Numeric vector.

k Offset. Defaults to (3/8), correspond to the Blom transform.

Value

Numeric vector of rank normalized measurements.

See Also

Direct INT DINT, indirect INT IINT, omnibus INT OINT.

Examples

```
## Not run:
# Draw from chi-1 distribution
y = rchisq(n=1e3,df=1);
# Rank normalize
z = rankNorm(y);
# Plot density of transformed measurement
plot(density(z));
## End(Not run)
```

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RNOmni-help

RNOmni: Rank-Normal Omnibus Association Testing

Description

Implementation of genetic association tests that incorporate the rank-based inverse normal transformation (INT) rankNorm. The direct-INT DINT test directly transforms the outcome, whereas the indirect-INT IINT test forms residuals prior to transformation. The omnibus INT OINT test adaptively combines the D-INT and I-INT tests into a single robust and statistically powerful procedure.

Author(s)

Zachary R. McCaw

SchurC

Schur complement

Description

Calculates the efficient information $I_{bb} - I_{ba}I_{aa}^{-1}I_{ab}$.

Usage

```
SchurC(Ibb, Iaa, Iba)
```

Arguments

Ibb Information of target parameter

Iaa Information of nuisance parameter

Iba Cross information between target and nuisance parameters

Value

Numeric matrix.

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