Package 'Pade'

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Type Package Title Padé Approximant Coefficients Version 1.0.1 Date 2020-06-02 Description Given a vector of Taylor series coefficients of sufficient length as input, the function returns the numerator and denominator coefficients for the Padé approximant of appropriate order (Baker, 1975) < ISBN:9780120748556>. License GPL (>= 2) | BSD_2_clause + file LICENSE Imports utils Suggests testthat, covr URL https://github.com/aadler/Pade BugReports https://github.com/aadler/Pade/issues **Encoding** UTF-8 NeedsCompilation no Author Avraham Adler [aut, cph, cre] (<https://orcid.org/0000-0002-3039-0703>) Maintainer Avraham Adler <Avraham. Adler@gmail.com> **Repository** CRAN

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Pade-package

Description

Given a vector of Taylor series coefficients of sufficient length as input, the function returns the numerator and denominator coefficients for the Padé approximant of appropriate order (Baker, 1975) <ISBN:9780120748556>.

Details

The DESCRIPTION file:

Package:	Pade
Type:	Package
Title:	Padé Approximant Coefficients
Version:	1.0.1
Date:	2020-06-02
Authors@R:	c(person(given="Avraham", family="Adler", role=c("aut", "cph", "cre"), email="Avraham.Adler@gmailer.com", compared to the second s
Description:	Given a vector of Taylor series coefficients of sufficient length as input, the function returns the numerat
License:	GPL (>= 2) BSD_2_clause + file LICENSE
Imports:	utils
Suggests:	testthat, covr
URL:	https://github.com/aadler/Pade
BugReports:	https://github.com/aadler/Pade/issues
Encoding:	UTF-8
NeedsCompilation:	no
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Author(s)

NA

Maintainer: NA

Description

Given Taylor series coefficients a_n from n = 0 up to n = T, the function will calculate the Padé [L/M] approximant coefficients so long as $L + M \leq T$.

Usage

Pade(L, M, A)

Arguments

L	Order of Padé numerator
М	Order of Padé denominator
A	vector of Taylor series coefficients, starting at x^0

Details

As the Taylor series expansion is the "best" polynomial approximation to a function, the Padé approximants are the "best" rational function approximations to the original function. The Padé approximant often has a wider radius of convergence than the corresponding Taylor series, and can even converge where the Taylor series does not, which makes it very suitable for computer-based numerical analysis.

The [L/M] Padé approximant to a Taylor series A(x) is the quotient

$$\frac{P_L(x)}{Q_M(x)}$$

where where $P_L(x)$ is of order L and $Q_M(x)$ is of order M. In this case:

$$A(x) - \frac{P_L(x)}{Q_M(x)} = \mathcal{O}\left(x^{L+M+1}\right)$$

When q_0 is defined to be 1, there is a unique solution to the system of linear equations which can be used to calculate the coefficients.

The function accepts a vector A of length T + 1, composed of the a_n of the of truncated Taylor series

$$A(x) = \sum_{j=0}^{T} a_j x^j$$

and returns a list of two elements, Px and Qx, the Padé numerator and denominator coefficients respectively, as long as $L + M \leq T$.

Value

Pade returns a list with two entries:

Px	Coefficients of the numerator polynomial starting at x^0.
Qx	Coefficients of the denominator polynomial starting at x^0.

Author(s)

Avraham Adler <Avraham.Adler@gmail.com>

References

Baker, George Allen (1975) Essentials of Padé Approximants Academic Press. ISBN 978-0-120-74855-6

See Also

This package provides similar functionality to the pade function in the **pracma** package. However, it does not allow computation of coefficients beyond the supplied Taylor coefficients and it expects its input and provides its output in ascending, instead of descending, order.

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