

Package ‘MortalityTables’

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Title A Framework for Various Types of Mortality / Life Tables

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URL <https://gitlab.open-tools.net/R/r-mortality-tables>

Depends ggplot2, methods, scales, utils

Suggests lifecontingencies, knitr, rmarkdown

Description Classes to implement and plot cohort life tables for actuarial calculations. In particular, birth-year dependent mortality tables using a yearly trend to extrapolate from a base year are implemented, as well as period life table, cohort life tables using an age shift, and merged life tables.

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Collate 'mortalityTable.R' 'mortalityTable.period.R'
'mortalityTable.ageShift.R' 'ageShift.R'
'mortalityTable.observed.R' 'mortalityTable.joined.R'
'mortalityTable.mixed.R' 'ages.R' 'baseTable.R' 'baseYear.R'
'fillAges.R' 'pensionTable.R' 'commutationNumbers.R'
'mortalityTable.improvementFactors.R'
'mortalityTable.trendProjection.R' 'deathProbabilities.R'
'getCohortTable.R' 'getOmega.R' 'getPeriodTable.R'
'lifeTable.R' 'makeQxDataFrame.R' 'mortalityComparisonTable.R'
'mortalityImprovement.R' 'mortalityTable.MakehamGompertz.R'
'mortalityTable.Weibull.R' 'mortalityTable.deMoivre.R'
'periodDeathProbabilities.R' 'mortalityTable.jointLives.R'
'mortalityTables.list.R' 'mortalityTables.load.R'
'plot.mortalityTable.R' 'plotMortalityTableComparisons.R'
'plotMortalityTables.R' 'plotMortalityTrend.R' 'setLoading.R'
'setModification.R' 'undampenTrend.R'
'whittaker.mortalityTable.R'

VignetteBuilder knitr

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| | |
|---|----|
| MortalityTables-package | 3 |
| ages | 3 |
| ageShift | 4 |
| baseTable | 5 |
| baseYear | 6 |
| calculateImprovements | 7 |
| commutationNumbers | 8 |
| deathProbabilities | 9 |
| deathProbabilitiesIndividual | 10 |
| fillAges | 11 |
| generateAgeShift | 12 |
| getCohortTable | 12 |
| getOmega | 13 |
| getPeriodTable | 14 |
| lifeTable | 14 |
| makeQxDataFrame | 15 |
| mortalityComparisonTable | 16 |
| mortalityImprovement | 17 |
| mortalityTable-class | 18 |
| mortalityTable.ageShift-class | 18 |
| mortalityTable.deMoivre-class | 19 |
| mortalityTable.improvementFactors-class | 19 |
| mortalityTable.jointLives-class | 20 |
| mortalityTable.MakehamGompertz-class | 20 |
| mortalityTable.mixed-class | 21 |
| mortalityTable.once | 22 |
| mortalityTable.onceAndFuture | 22 |
| mortalityTable.period-class | 23 |
| mortalityTable.trendProjection-class | 23 |
| mortalityTable.Weibull-class | 24 |
| mortalityTable.zeroes | 25 |
| mortalityTables.list | 26 |
| mortalityTables.load | 26 |
| pensionTable-class | 27 |
| pensionTables.list | 28 |
| pensionTables.load | 29 |
| periodDeathProbabilities | 29 |
| periodDeathProbabilitiesIndividual | 31 |
| periodTransitionProbabilities | 31 |
| plot.mortalityTable | 33 |

| | |
|---|----|
| plotMortalityTableComparisons | 34 |
| plotMortalityTables | 35 |
| plotMortalityTrend | 36 |
| setLoading | 38 |
| setModification | 38 |
| transitionProbabilities | 39 |
| undampenTrend | 40 |
| whittaker.mortalityTable | 41 |

Index 44

MortalityTables-package

Provide life table classes for life insurance purposes

Description

Provide life table classes for life insurance purposes

Author(s)

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See Also

Useful links:

- <https://gitlab.open-tools.net/R/r-mortality-tables>
-

ages

Return the defined ages of the life table

Description

Return the defined ages of the life table

Usage

```
ages(object, ...)
```

```
## S4 method for signature 'mortalityTable.period'
```

```
ages(object, ...)
```

```
## S4 method for signature 'mortalityTable.mixed'
```

```
ages(object, ...)
```

```
## S4 method for signature 'mortalityTable.jointLives'
```

```
ages(object, ...)
```

Arguments

| | |
|--------|--|
| object | A life table object (instance of a mortalityTable class) |
| ... | Currently unused |

Methods (by class)

- `mortalityTable.period`: Return the defined ages of the period life table
- `mortalityTable.mixed`: Return the defined ages of the mixed life table
- `mortalityTable.jointLives`: Return the defined ages of the joint lives mortality table (returns the ages of the first table used for joint lives)

Examples

```
mortalityTables.load("Austria_*")
ages(AV0e2005R.male)
ages(AV0e1996R.male)
ages(mort.AT.census.2011.male)
```

| | |
|----------|--|
| ageShift | <i>Return the age shift of the age-shifted life table given the birth year</i> |
|----------|--|

Description

Return the age shift of the age-shifted life table given the birth year

Usage

```
ageShift(object, YOB = 1975, ...)
```

S4 method for signature 'mortalityTable'

```
ageShift(object, YOB = 1975, ...)
```

S4 method for signature 'mortalityTable.ageShift'

```
ageShift(object, YOB = 1975, ...)
```

Arguments

| | |
|--------|---|
| object | The life table object (class inherited from <code>mortalityTable</code>) |
| YOB | The birth year for which the age shift should be determined. |
| ... | Other parameters (currently unused) |

Methods (by class)

- `mortalityTable`: Age shifts apply only to `mortalityTable.ageShift`, so all other tables return NA.
- `mortalityTable.ageShift`: Return the age shift of the age-shifted life table given the birth year

Examples

```
mortalityTables.load("Austria_Annuities")
ageShift(AV0e2005R.male.av, YOB=1910)
ageShift(AV0e2005R.male.av, YOB=1955)
ageShift(AV0e2005R.male.av, YOB=2010)
# A table with trend does NOT have any age shift, so NA is returned:
ageShift(AV0e2005R.male, YOB=1910)
```

| | |
|-----------|--|
| baseTable | <i>Return the base table of the life table</i> |
|-----------|--|

Description

Return the base table of the life table

Usage

```
baseTable(object, ...)

## S4 method for signature 'mortalityTable'
baseTable(object, ...)

## S4 method for signature 'mortalityTable.period'
baseTable(object, ...)

## S4 method for signature 'mortalityTable.jointLives'
baseTable(object, ...)
```

Arguments

| | |
|--------|---|
| object | The life table object (class inherited from mortalityTable) |
| ... | Other parameters (currently unused) |

Methods (by class)

- mortalityTable: Return the base table of the life table
- mortalityTable.period: Return the base table of the life table
- mortalityTable.jointLives: Return the base table of the joint lives mortality table (returns the base table of the first table used for joint lives)

Examples

```
mortalityTables.load("Austria_Annuities")
baseTable(AV0e2005R.male)
```

| | |
|----------|---|
| baseYear | <i>Return the base year of the life table</i> |
|----------|---|

Description

Return the base year of the life table

Usage

```
baseYear(object, ...)
```

```
## S4 method for signature 'mortalityTable'
```

```
baseYear(object, ...)
```

```
## S4 method for signature 'mortalityTable.mixed'
```

```
baseYear(object, ...)
```

```
## S4 method for signature 'mortalityTable.jointLives'
```

```
baseYear(object, ...)
```

Arguments

object The life table object (class inherited from mortalityTable)

... Other parameters (currently unused)

Methods (by class)

- mortalityTable: Return the base year of the life table
- mortalityTable.mixed: Return the base year of the life table
- mortalityTable.jointLives: Return the base year of the life table

Examples

```
mortalityTables.load("Austria-Annuities")  
baseYear(AV0e2005R.male)
```

calculateImprovements *Calculate the improvement factors for the given birth-year and the `mortalityTable.improvementFactors` object*

Description

Calculate the improvement factors for the given birth-year and the `mortalityTable.improvementFactors` object

Usage

```
calculateImprovements(object, ...)
```

```
## S4 method for signature 'mortalityTable.improvementFactors'  
calculateImprovements(object, ...,  
  Period = NULL, YOB = 1982)
```

Arguments

| | |
|--------|---|
| object | A pension table object (instance of a <code>mortalityTable.improvementFactors</code> class) |
| ... | Currently unused |
| Period | Observation period (either Period or YOB should be given) |
| YOB | Year of birth (either Period or YOB should be given) |

Methods (by class)

- `mortalityTable.improvementFactors`: Calculate the total mortality improvement factors relative to the base year for the given birth-year and the `mortalityTable.improvementFactors` object

Examples

```
pensionTables.load("USA_PensionPlan_RP2014")  
calculateImprovements(RP2014.male@qx, YOB = 2017)
```

| | |
|--------------------|---|
| commutationNumbers | <i>Calculate the commutation numbers for the given parameters, using the mortality table and an interest rate</i> |
|--------------------|---|

Description

Calculate the commutation numbers for the given parameters, using the mortality table and an interest rate

Usage

```
commutationNumbers(object, ..., ages = NULL, i = 0.03)
```

```
## S4 method for signature 'mortalityTable'
commutationNumbers(object, ..., ages = NULL,
  i = 0.03)
```

```
## S4 method for signature 'numeric'
commutationNumbers(object, ages, i = 0.03)
```

```
## S4 method for signature 'pensionTable'
commutationNumbers(object, ..., ages = NULL,
  i = 0.03)
```

Arguments

| | |
|--------|---|
| object | The life table object (class inherited from mortalityTable) |
| ... | Other parameters to be passed to the deathProbabilities call (e.g. YOB) |
| ages | Vector of ages for which the probabilities should be extracted and commutation numbers calculates |
| i | Interest rate used for the calculation of the commutation numbers |

Methods (by class)

- `mortalityTable`: Calculate the commutation numbers for the given parameters, using the mortality table and an interest rate
- `numeric`: Calculate the commutation numbers for the given death probabilities (passed as a numeric vector with argument name "object"), ages and an interest rate Return value is a list of data frames
- `pensionTable`: Calculate the commutation numbers for the given parameters, using the pension table and an interest rate Return value is a list of data frames

Examples

```
mortalityTables.load("Austria-Annuities")
commutationNumbers(AV0e2005R.male, i = 0.03, YOB = 1975)
```

deathProbabilities *Return the (cohort) death probabilities of the life table given the birth year (if needed)*

Description

Return the (cohort) death probabilities of the life table given the birth year (if needed)

Usage

```
deathProbabilities(object, ..., ages = NULL, YOB = 1975)

## S4 method for signature 'mortalityTable.period'
deathProbabilities(object, ..., ages = NULL,
  YOB = 1975)

## S4 method for signature 'mortalityTable.ageShift'
deathProbabilities(object, ...,
  ages = NULL, YOB = 1975)

## S4 method for signature 'mortalityTable.trendProjection'
deathProbabilities(object, ...,
  ages = NULL, YOB = 1975)

## S4 method for signature 'mortalityTable.improvementFactors'
deathProbabilities(object, ...,
  ages = NULL, YOB = 1975)

## S4 method for signature 'mortalityTable.mixed'
deathProbabilities(object, ..., ages = NULL,
  YOB = 1975)

## S4 method for signature 'mortalityTable.jointLives'
deathProbabilities(object, ...,
  ageDifferences = c(), ages = NULL, YOB = 1975)
```

Arguments

| | |
|----------------|---|
| object | The life table object (class inherited from mortalityTable) |
| ... | Other parameters (currently unused) |
| ages | Desired age range (if NULL, the probabilities of the age range provided by the table will be returned), missing ages will be filled with NA |
| YOB | The birth year for which the death probabilities should be calculated |
| ageDifferences | A vector of age differences of all joint lives. |

Methods (by class)

- `mortalityTable.period`: Return the (cohort) death probabilities of the life table given the birth year (if needed)
- `mortalityTable.ageShift`: Return the (cohort) death probabilities of the life table given the birth year (if needed)
- `mortalityTable.trendProjection`: Return the (cohort) death probabilities of the life table given the birth year (if needed)
- `mortalityTable.improvementFactors`: Return the (cohort) death probabilities of the life table given the birth year (if needed)
- `mortalityTable.mixed`: Return the (cohort) death probabilities of the life table given the birth year (if needed)
- `mortalityTable.jointLives`: Return the (cohort) death probabilities of the life table given the birth year (if needed)

Examples

```

mortalityTables.load("Austria_Annuities")
deathProbabilities(AV0e2005R.male, YOB = 1975)
deathProbabilities(AV0e2005R.male, YOB = 2017)

mortalityTables.load("Germany_Census")
table.JL = mortalityTable.jointLives(
  name = "ADSt 24/26 auf verbundene Leben",
  table = mort.DE.census.1924.26.male
)
deathProbabilities(table.JL, YOB = 1977, ageDifferences = c(1, 5, -5, 16))
deathProbabilities(table.JL, YOB = 1977, ageDifferences = c(0))
deathProbabilities(table.JL, YOB = 1977, ageDifferences = c(1, 5, 16))

```

deathProbabilitiesIndividual

Return a matrix of the persons' individual death probabilities of a joint-life table (instance of `mortalityTable.jointLives`)

Description

Return a matrix of the persons' individual death probabilities of a joint-life table (instance of `mortalityTable.jointLives`)

Usage

```
deathProbabilitiesIndividual(tables, YOB, ageDifferences)
```

Arguments

| | |
|----------------|---|
| tables | List of life table objects (object inherited from <code>mortalityTable</code>) |
| YOB | The birth year for the first person |
| ageDifferences | The age differences to the first person |

Examples

```
mortalityTables.load("Germany_Census")
deathProbabilitiesIndividual(list(mort.DE.census.1924.26.male), 1977, c(0, 0))
deathProbabilitiesIndividual(list(mort.DE.census.1924.26.male), 1977, c(0, -5, 13))
```

| | |
|----------|---|
| fillAges | <i>Fill the given probabilities with NA to match the desired age range.</i> |
|----------|---|

Description

Fill the given probabilities with NA to match the desired age range.

Usage

```
fillAges(probs = c(), givenAges = c(), neededAges = NULL,
         fill = NA_real_)
```

Arguments

| | |
|------------|--|
| probs | Numeric vector |
| givenAges | ages assigned to the given vector |
| neededAges | desired age range for output |
| fill | If set, missing values will be replaced with this value. Default is to fill with NA. |

Examples

```
# Ages 20-70 have linearly increasing death probabilities. Fill with 0 for the whole age range 0-120
fillAges(probs = c(0:50/50), givenAges = 20:70, neededAges = 0:120, fill = 0)
```

| | |
|------------------|--|
| generateAgeShift | <i>Generate data.frame containing age shifts for each birth year</i> |
|------------------|--|

Description

Generate a dataframe suitable to be passed to the mortalityTable.ageShift class.

Usage

```
generateAgeShift(initial = 0, YOBS = c(1900, 2100), step = -1)
```

Arguments

| | |
|---------|--|
| initial | Age shift for the first birth year given in the YOBS vector |
| YOBS | Vector of birth years in which the age shift changes by step. The last entry gives the first birth year that does not have any shift defined any more. |
| step | How much the age shift changes in each year given in the YOBS vector |

Examples

```
generateAgeShift(initial = 1, YOBS = c(1922, 1944, 1958, 1973, 1989, 2006, 2023, 2041, 2056))
```

| | |
|----------------|---|
| getCohortTable | <i>Return the cohort life table as a mortalityTable.period object</i> |
|----------------|---|

Description

Return the cohort life table as a mortalityTable.period object

Usage

```
getCohortTable(object, YOB, ...)

## S4 method for signature 'mortalityTable'
getCohortTable(object, YOB, ...)
```

Arguments

| | |
|--------|--|
| object | The life table object (class inherited from mortalityTable) |
| YOB | The birth year for which the life table should be calculated |
| ... | Other parameters (currently unused) |

Methods (by class)

- mortalityTable: Return the cohort life table as a mortalityTable.period object

Examples

```
mortalityTables.load("Austria_Annuities")
tb75 = getCohortTable(AV0e2005R.male, YOB = 1975)
# The tb75 is a fixed table with no trend any more
plot(AV0e2005R.male, tb75, Period = 2017)
```

| | |
|----------|---|
| getOmega | <i>Return the maximum age of the life table</i> |
|----------|---|

Description

Return the maximum age of the life table

Usage

```
getOmega(object)

## S4 method for signature 'mortalityTable.period'
getOmega(object)

## S4 method for signature 'mortalityTable.mixed'
getOmega(object)

## S4 method for signature 'mortalityTable.jointLives'
getOmega(object)
```

Arguments

object A life table object (instance of a mortalityTable class)

Methods (by class)

- mortalityTable.period: Return the maximum age of the period life table
- mortalityTable.mixed: Return the maximum age of the mixed life table
- mortalityTable.jointLives: Return the maximum age of the joint lives mortality table (returns the maximum age of the first table used for joint lives, as the ages of the joint lives are now known to the function)

Examples

```
mortalityTables.load("Austria_Annuities")
getOmega(AV0e2005R.male)
getOmega(mortalityTable.deMoivre(omega = 100))
```

| | |
|----------------|---|
| getPeriodTable | <i>Return the period life table as a mortalityTable.period object</i> |
|----------------|---|

Description

Return the period life table as a mortalityTable.period object

Usage

```
getPeriodTable(object, Period, ...)

## S4 method for signature 'mortalityTable'
getPeriodTable(object, Period, ...)
```

Arguments

| | |
|--------|--|
| object | The life table object (class inherited from mortalityTable) |
| Period | The observation year, for which the death probabilities should be determined |
| ... | Other parameters (currently unused) |

Methods (by class)

- mortalityTable: Return the period life table as a mortalityTable.period object

Examples

```
mortalityTables.load("Austria_Annuities")
tb17 = getPeriodTable(AV0e2005R.male, Period = 2017)
# The tb17 is a fixed table with no trend any more
plot(AV0e2005R.male, tb17, YOB = 1975)
```

| | |
|-----------|--|
| lifeTable | <i>Return the lifetable object (package lifecontingencies) for the cohort life table</i> |
|-----------|--|

Description

Return the lifetable object (package lifecontingencies) for the cohort life table

Usage

```
lifeTable(object, ...)

## S4 method for signature 'mortalityTable'
lifeTable(object, ...)
```

Arguments

object The life table object (class inherited from mortalityTable)
 ... Parameters to be passed to the deathProbabilities method of the life table

Methods (by class)

- mortalityTable: Return the lifetable object (package lifecontingencies) for the cohort life table

Examples

```
library("lifecontingencies")
mortalityTables.load("Austria-Annuities")
lifeTable(AV0e2005R.male, YOB = 2017)
axn(lifeTable(AV0e2005R.male, YOB = 1975), x = 65, i = 0.03)
axn(lifeTable(AV0e2005R.male, YOB = 2017), x = 65, i = 0.03)
```

| | |
|-----------------|---|
| makeQxDataFrame | <i>Converts one or multiple mortality table objects to a data frame that can be plotted by plotMortalityTables or plotMortalityTableComparisons</i> |
|-----------------|---|

Description

It is not required to call this function manually, plotMortalityTables will automatically do it if object derived from class mortalityTable are passed.

Usage

```
makeQxDataFrame(..., YOB = 1972, Period = NA, reference = NULL)
```

Arguments

... Life tables (objects of classes derived from mortalityTable)
 YOB desired year of birth to be plotted as cohort life table (default: 1972)
 Period desired observation year to be plotted (default: NA). If both YOB and Period are given, a period comparison is generated.
 reference Reference life table, used to show relative death probabilities (i.e. the q_x for all ages are divided by the corresponding probabilities of the reference table)

Examples

```
mortalityTables.load("Austria-Annuities")
makeQxDataFrame(AV0e2005R.male, AV0e2005R.female, YOB = 1975)
```

mortalityComparisonTable

Calculate relative mortalities for age bands and birth years

Description

Calculate relative mortalities for age bands and birth years

Usage

```
mortalityComparisonTable(table1, table2, years, ages, binsize = 5, ...)
```

Arguments

| | |
|----------------|--|
| table1, table2 | The mortalityTable objects to compare (mortalities of table1 relative to table2) |
| years | Vector of birth years to include in the comparisons. |
| ages | Vector of ages to include in the comparisons |
| binsize | How many ages to combine into one age band |
| ... | Other parameters (currently unused) |

Examples

```
mortalityTables.load("Austria_Annuities")
# Compare mortality of Austrian male and female annuitants born 1930 to 2030
mortalityComparisonTable(
  AVOe2005R.male, AVOe2005R.female,
  years = seq(1930, 2030, by = 10),
  ages = 0:119)

# Compare the two Austrian male annuity tables AVOe 2005-R and AVOe 1996-R,
# combining ages 10-19, 20-29, etc.
mortalityComparisonTable(
  AVOe2005R.male, AVOe1996R.male,
  years = seq(1930, 2030, by = 10),
  ages = 0:109, binsize=10)
```

mortalityImprovement *Return the mortality trend (yearly log-death-probability improvement) of the given period or the given generation.*

Description

Return the mortality trend (yearly log-death-probability improvement) of the given period or the given generation.

Usage

```
mortalityImprovement(object, ..., Period = NULL, YOB = 1975)
```

```
## S4 method for signature 'mortalityTable'
mortalityImprovement(object, ..., Period = NULL,
  YOB = 1975)
```

Arguments

| | |
|--------|--|
| object | The life table object (class inherited from mortalityTable) |
| ... | Other parameters (currently unused) |
| Period | The observation year for which the mortality improvement should be calculated. If both YOB and Period are given, YOB is ignored. |
| YOB | The birth year for which the mortality improvement should be calculated |

Methods (by class)

- mortalityTable: Return the yearly log-mortality improvement of the life table given the birth or observation year

Examples

```
mortalityTables.load("Austria-Annuities")
# AV0e 2005R includes a trend decline by default, compare the exact table
# with the table without decline:
mortalityImprovement(AV0e2005R.male, Period = 2017)
mortalityImprovement(AV0e2005R.male.nodamping, Period = 2017)
```

mortalityTable-class *Class mortalityTable*

Description

Class mortalityTable is the (virtual) base class for all mortality tables. It contains the name and some general values applying to all types of tables, but does not contain any data itself. Use a child class to create actual mortality tables.

Slots

name The human-readable name of the mortality table
baseYear The base year of the mortality table (e.g. for tables with trend projection)
modification A function that will be called with the final death probabilities to give the user a way to modify the final probabilities
loading Additional security loading on the resulting table (single numeric value, e.g. 0.05 adds 5% security margin to the probabilities)

mortalityTable.ageShift-class
 Class mortalityTable.ageShift - Cohort life tables generated by age-shift

Description

A cohort life table, obtained by age-shifting from a given base table (death probabilities)

Slots

ageShifts A data.frame with columns YOB and shifts giving the age shifts for each birth year

Examples

```
mortalityTables.load("Austria_Annuities_AV0e2005R")
tb = mortalityTable.ageShift(
  ages = ages(AV0e2005R.male),
  deathProbs = deathProbabilities(AV0e2005R.male, YOB = 1992),
  ageShifts = generateAgeShift(1, c(1962, 1985, 2000, 2015, 2040, 2070)))
# The cohort tables for different birth years are just the base probabilities with modified ages
plot(getCohortTable(tb, YOB = 1963), getCohortTable(tb, YOB = 2017))
```

 mortalityTable.deMoivre-class

Class mortalityTable.deMoivre - Mortality table with de Moivre's law

Description

A period life table with maximum age ω and the time of death identically distributed on the interval $[0, \omega]$. The only required slot is the maximum age ω , all probabilities are calculated from it. Optionally, a name and loading can be passed (inherited from [mortalityTable](#)).

Slots

`omega` Maximum age

Examples

```
mm = mortalityTable.deMoivre(100)
plot(mm,
      mortalityTable.deMoivre(90),
      mortalityTable.deMoivre(50))
```

 mortalityTable.improvementFactors-class

Class mortalityTable.improvementFactors - Cohort life table with improvement factors

Description

A cohort life table, obtained by an improvement factor projection from a given base table (PODs for a given observation year).

Slots

`baseYear` The base year for the improvements (`baseTable` describes the death probabilities in this year)

`improvement` Yearly improvement factors per age

Examples

```
mortalityTables.load("Austria_Annuities_AV0e2005R")
# AV0e 2005R base table with yearly improvements of 3% for age 0, linearly
# decreasing to 0% for age 120.
tb = mortalityTable.improvementFactors(
  ages = ages(AV0e2005R.male),
  deathProbs = periodDeathProbabilities(AV0e2005R.male, Period = 2002),
```

```

    baseYear = 2002,
    improvement = 0.03 * (1 - ages(AV0e2005R.male)/121),
    name = "AV0e 2005R base with linearly falling improvements (DEMO)"
  )
# Yearly trend is declining:
plotMortalityTrend(tb, AV0e2005R.male, Period = 2017, title = "Mortality Trend")
# The cohort tables for different birth years:
plot(getCohortTable(tb, YOB = 1963), getCohortTable(tb, YOB = 2017))

```

mortalityTable.jointLives-class

Class mortalityTable.jointLives - Life table for multiple joint lives

Description

A cohort life table obtained by calculating joint death probabilities for multiple lives, each possibly using a different mortality table.

Slots

table The mortalityTable object for all lives (vector if different tables should be used for the different persons)

Examples

```

mortalityTables.load("Germany_Census")
table.JL = mortalityTable.jointLives(
  name = "ADSt 24/26 auf verbundene Leben",
  table = mort.DE.census.1924.26.male
)
deathProbabilities(table.JL, YOB = 1977, ageDifferences = c(1, 5, -5, 16))
deathProbabilities(table.JL, YOB = 1977, ageDifferences = c(0))
deathProbabilities(table.JL, YOB = 1977, ageDifferences = c(1, 5, 16))

```

mortalityTable.MakehamGompertz-class

Class mortalityTable.MakehamGompertz - Mortality table with Makeham-Gompertz's law

Description

A period life table following Makeham and Gompertz's law of a mortality rate μ increasing exponentially with age x ($\mu_{x+t} = A + Bc^{(x+t)}$). The only required slots are the parameters A , B and c , all probabilities are calculated from them, for technical reasons a maximum age of 120 is technically assumed. Optionally, a name and loading can be passed (inherited from [mortalityTable](#)).

Slots

A Parameter A of the Makeham-Gompertz distribution
 B Parameter B of the Makeham-Gompertz distribution
 c Parameter c of the Makeham-Gompertz distribution
 omega Maximum age (default: 150)

Examples

```
# A Gompertz mortality, roughly approximating the Austrian annuitants 2017
gmp = mortalityTable.MakehamGompertz(A = 0, B = 0.00001, c = 1.11)
mortalityTables.load("Austria_Annuities_AVOe2005R")
plot(gmp, AVOe2005R.male, Period=2017)

# A Makeham-Gompertz mortality, approximating the Austrian annuitants 2017
mg = mortalityTable.MakehamGompertz(A = 0.0002, B = 0.00001, c = 1.11)
plot(mg, gmp, AVOe2005R.male, Period=2017)
```

mortalityTable.mixed-class

Class mortalityTable.mixed - Life table as a mix of two life tables

Description

A cohort life table obtained by mixing two life tables with the given weights. Typically, when only gender-specific tables are available, unisex tables are generated by mixing the two gender-specific tables for males and for females with a pre-defined, constant proportion (e.g. 60:30 or 40:60, depending on the portfolio and on the security margins).

Slots

table1 The first mortalityTable
 table2 The second mortalityTable
 weight1 The weight of the first mortality table
 weight2 The weight of the second mortality table
 loading Additional security loading

Examples

```
mortalityTables.load("Austria_Annuities_AVOe2005R")
# Generate a unisex table with mixing relation 60:40 from male + female tables
AVOe2005R.myUnisex = mortalityTable.mixed(
  table1 = AVOe2005R.male, table2 = AVOe2005R.female,
  weight1 = 0.6, weight2 = 0.4,
  name = "My custom AVOe 2005R unisex (60:40)")
plot(AVOe2005R.myUnisex, AVOe2005R.male, AVOe2005R.female, Period = 2017)
```

mortalityTable.once *Generate a (deterministic) mortality table with only one probability set to 1 (for the given age)*

Description

Generate a (deterministic) mortality table with only one probability set to 1 (for the given age)

Usage

```
mortalityTable.once(transitionAge, name = "Deterministic mortality table",
  ages = 0:99)
```

Arguments

| | |
|---------------|---|
| transitionAge | The age where the deterministic transition occurs |
| name | The name of the table |
| ages | The ages of the table |

mortalityTable.onceAndFuture
 Generate a (deterministic) mortality table with all probabilities starting at a given age set to 1

Description

Generate a (deterministic) mortality table with all probabilities starting at a given age set to 1

Usage

```
mortalityTable.onceAndFuture(transitionAge,
  name = "Deterministic mortality table", ages = 0:99)
```

Arguments

| | |
|---------------|---|
| transitionAge | The age where the deterministic transition occurs |
| name | The name of the table |
| ages | The ages of the table |

 mortalityTable.period-class

Class mortalityTable.period - Period life tables

Description

A period life table, giving death probabilities for each age, up to maximum age omega. The baseYear slot can be used to hold information about the period.

Slots

ages The ages corresponding to the entries of the deathProbs

deathProbs The one-year death probabilities for the ages

exposures (Optional) exposures used to determine death probabilities (can be used as weights for smoothing, for variances, etc.)

Examples

```
linTable = mortalityTable.period(name="linear mortality", ages = 0:50, deathProbs = 0:50/50)
constTable = mortalityTable.period(name="const. mortality", ages = 0:50,
                                   deathProbs = c(rep(0.1, 50), 1))
plot(linTable, constTable, title="Comparison of linear and constant death probabilities")

# A sample observation table with exposures and raw probabilities
obsTable = mortalityTable.period(
  name = "trivial observed table",
  ages = 0:15,
  deathProbs = c(
    0.0072, 0.00212, 0.00081, 0.0005, 0.0013,
    0.001, 0.00122, 0.00142, 0.007, 0.0043,
    0.0058, 0.0067, 0.0082, 0.0091, 0.0075, 0.01),
  exposures = c(
    150, 222, 350, 362, 542,
    682, 1022, 1053, 1103, 1037,
    968, 736, 822, 701, 653, 438))
plot(obsTable, title = "Observed death probabilities")
```

 mortalityTable.trendProjection-class

Class mortalityTable.trendProjection - Cohort mortality table with age-specific trend

Description

A cohort mortality table, obtained by a trend projection from a given base table (PODs for a given observation year). Typically, the trend is obtained by the Lee-Carter method or some other trend estimation. The dampingFunction can be used to modify the cumulative years (e.g. $G(\tau+x)$ instead of $\tau+x$) If trend2 is given, the $G(\tau+x)$ gives the weight of the first trend, $1-G(\tau+x)$ the weight of the second trend

Slots

baseYear The base year of the trend projection (baseTable describes the death probabilities in this year)

trend The yearly improvements of the log-death probabilities (per age)

dampingFunction A possible damping of the trend. This is a function damping(delta_years) that gets a vector of years from the baseYear and should return the dampened values.

trend2 The alternate trend. If given, the damping function interpolates between trend and trend2, otherwise the dumping function simply modifies the coefficients of trend.

Examples

```
obsTable = mortalityTable.trendProjection(
  name = "Const. table with trend",
  baseYear = 2018,
  ages = 0:15,
  deathProbs = rep(0.02, 16),
  trend = c(
    0.045, 0.04, 0.03, 0.04, 0.042, 0.041, 0.038, 0.035,
    0.032, 0.031, 0.028, 0.020, 0.015, 0.01, 0.005, 0))
# In 2018 the flat mortality can be seen
plotMortalityTables(obsTable, Period = 2018, title = "Period death probabilities 2018")
# In 2038, the age-specific trend affected the probabilities differently for 20 years:
plotMortalityTables(obsTable, Period = 2038, title = "Period death probabilities 2038")
# Consequently, a person born 2018 will also not have constand death probabilities
plotMortalityTables(obsTable, YOB = 2018, title = "Cohort death probabilities, YOB 2018")

plotMortalityTables(
  lapply(2018:2033, function(y) getCohortTable(obsTable, YOB = y)),
  title = "Cohort tables for different YOBs", legend.position = c(0.99, 0.01))
plotMortalityTables(
  lapply(2018:2033, function(y) getPeriodTable(obsTable, Period = y)),
  title = "Period tables for different years", legend.position = c(0.99, 0.01))
```

mortalityTable.Weibull-class

Class mortalityTable.Weibull - Mortality table with Weibull's law

Description

A period life table following Weibull's law of a mortality rate μ increasing as a power of t :

$$\mu_{x+t} = k * (x + t)^n$$

The only required slots are the parameters $k > 0$ and $n > 0$, all probabilities are calculated from them, for technical reasons a maximum age of 150 is technically assumed. Optionally, a name and loading can be passed (inherited from `mortalityTable`).

Slots

k Parameter k of the Weibull distribution

n Parameter n of the Weibull distribution

omega Maximum age (default: 120)

Examples

```
# A Weibull mortality
wbl = mortalityTable.Weibull(k = 0.0000000001, n = 4.8)
mortalityTables.load("Austria_Annuities_AV0e2005R")
plot(wbl, AV0e2005R.male, Period=2017, ylim = c(0.00005, 1))
```

mortalityTable.zeroes *Generate a mortality table with all probabilities set to zero.*

Description

Generate a mortality table with all probabilities set to zero.

Usage

```
mortalityTable.zeroes(name = "Zero mortality table", ages = 0:99)
```

Arguments

name The name of the table

ages The ages of the table

`mortalityTables.list` *List all available sets of life tables provided by the [MortalityTables-package](#) package. An existing life table can then be loaded with [mortalityTables.load](#).*

Description

List all available sets of life tables provided by the [MortalityTables-package](#) package. An existing life table can then be loaded with [mortalityTables.load](#).

Usage

```
mortalityTables.list(pattern = "*", package = c("MortalityTables",
  "MortalityTablesPrivate"), prefix = "MortalityTables")
```

Arguments

| | |
|---------|---|
| pattern | Restrict the results only to life table sets that match the pattern (default: "*" to show all sets) |
| package | The package that contains the desired dataset in its extdata/ directory. Defaults to the "MortalityTables" package. Multiple packages can be given as a vector. |
| prefix | The file prefix, defaults to MortalityTables. Can be overridden to list other types of files, like "PensionTables" |

Examples

```
mortalityTables.list()
mortalityTables.list("Austria_*")
mortalityTables.list("*Annuities")
mortalityTables.list(package = c("MyCustomPackage"))
```

`mortalityTables.load` *Load a named set of mortality tables provided by the [MortalityTables](#) package*

Description

Load a named set of mortality tables provided by the [MortalityTables](#) package

Usage

```
mortalityTables.load(dataset, package = c("MortalityTables",
  "MortalityTablesPrivate"), prefix = "MortalityTables")
```

Arguments

| | |
|---------|--|
| dataset | The set(s) of life tables to be loaded. A list of all available data sets is provided by the function <code>mortalityTables.list</code> . Wildcards (*) are allowed to match and load multiple datasets. |
| package | The package that contains the dataset in its <code>extdata/</code> directory. Defaults to the "MortalityTables" package. Multiple packages can be given as a vector. |
| prefix | The prefix for the data sets (default is "MortalityTables"). |

Examples

```
mortalityTables.list()
mortalityTables.load("Austria_Annuities_*")
mortalityTables.load("Austria_Annuities_AV0e2005R")
mortalityTables.load("*Annuities")
mortalityTables.load("MyCustomTable", package = c("MyCustomPackage"))
```

pensionTable-class *Class pensionTable*

Description

Class `pensionTable` is the (virtual) base class for all pensions tables. It contains the name and some general values applying to all types of tables. In particular, it holds individual tables for each of the transition probabilities. Possible states are:

- active: healty, no pension, typically paying some kin of premium
- incapacity: disability pension, in most cases permanent, not working, early pension
- retirement: old age pension, usually starting with a fixed age
- dead
 - Widow/widower pension

Correspondingly, the following transition probabilities can be given:

qxaa death probability of actives (active -> dead)

ix invalidity probability (active -> incapacity)

qix death probability of invalid (invalid -> dead)

rx reactivation probability (incapacity -> active)

apx retirement probability (active -> retirement), typically 1 for a fixed age

qpx death probability of retired (retired -> dead)

hx probability of a widow at moment of death (dead -> widow), $y(x)$ age difference

qxw death probability of widows/widowers

qgx death probability of total group (irrespective of state)

invalids.retire Flag to indicate whether invalid persons retire like active (one death probability for all retirees) or whether they stay invalid until death with death probabilities specific to invalids.

Slots

qx Death probability table of actives (derived from mortalityTable)
 ix Invalidation probability of actives (derived from mortalityTable)
 qix Death probability table of invalids (derived from mortalityTable)
 rx Reactivation probability of invalids (derived from mortalityTable)
 apx Retirement probability of actives (derived from mortalityTable)
 qpx Death probability of old age pensioners (derived from mortalityTable)
 hx Probability of a widow at the moment of death (derived from mortalityTable)
 qwy Death probability of widow(er)s (derived from mortality Table)
 yx Age difference of the widow to the deceased
 qgx Death probability of whole group (derived from mortalityTable), irrespective of state
 invalids.retire Whether invalids retire like actives or stay invalid until death

pensionTables.list *List all available sets of pension tables provided by the [MortalityTables-package](#) package. An existing pension table can then be loaded with [pensionTables.load](#).*

Description

List all available sets of pension tables provided by the [MortalityTables-package](#) package. An existing pension table can then be loaded with [pensionTables.load](#).

Usage

```
pensionTables.list(pattern = "*", package = c("MortalityTables",
      "MortalityTablesPrivate"))
```

Arguments

| | |
|---------|---|
| pattern | Restrict the results only to pension table sets that match the pattern (default: "*" to show all sets) |
| package | The package that contains the desired dataset in its extdata/ directory. Defaults to the "MortalityTables" package. Multiple packages can be given as a vector. |

Examples

```

pensionTables.list()
pensionTables.list("USA_*")
pensionTables.list(package = c("MyCustomPackage"))

```

pensionTables.load *Load a named set of pension tables provided by the [MortalityTables](#) package*

Description

Load a named set of pension tables provided by the [MortalityTables](#) package

Usage

```
pensionTables.load(dataset, package = c("MortalityTables",
  "MortalityTablesPrivate"))
```

Arguments

| | |
|---------|---|
| dataset | The set of lifpensione tables to be loaded. A list of all available data sets is provided by the function pensionTables.list . Wildcards (*) are allowed to match and load multiple datasets. |
| package | The package that contains the dataset in its extdata/ directory. Defaults to the "MortalityTables" package. Multiple packages can be given as a vector. <p>pensionTables.list() pensionTables.load("*") pensionTables.load("USA_PensionPlan_RP2014")</p> |

periodDeathProbabilities

Return the (period) death probabilities of the life table for a given observation year

Description

Return the (period) death probabilities of the life table for a given observation year

Usage

```
periodDeathProbabilities(object, ..., ages = NULL, Period = 1975)

## S4 method for signature 'mortalityTable.period'
periodDeathProbabilities(object, ...,
  ages = NULL, Period = 1975)

## S4 method for signature 'mortalityTable.ageShift'
periodDeathProbabilities(object, ...,
  ages = NULL, Period = 1975)

## S4 method for signature 'mortalityTable.trendProjection'
periodDeathProbabilities(object, ...,
```

```

ages = NULL, Period = 1975)

## S4 method for signature 'mortalityTable.improvementFactors'
periodDeathProbabilities(object,
  ..., ages = NULL, Period = 1975)

## S4 method for signature 'mortalityTable.mixed'
periodDeathProbabilities(object, ...,
  ages = NULL, Period = 1975)

## S4 method for signature 'mortalityTable.jointLives'
periodDeathProbabilities(object, ...,
  ageDifferences = c(), ages = NULL, Period = 1975)

```

Arguments

| | |
|-----------------------------|--|
| <code>object</code> | The life table object (class inherited from <code>mortalityTable</code>) |
| <code>...</code> | Other parameters (currently unused) |
| <code>ages</code> | Desired age range (if <code>NULL</code> , the probabilities of the age range provided by the table will be returned), missing ages will be filled with <code>NA</code> |
| <code>Period</code> | The observation year for which the period death probabilities should be determined |
| <code>ageDifferences</code> | A vector of age differences of all joint lives. |

Methods (by class)

- `mortalityTable.period`: Return the (period) death probabilities of the life table for a given observation year
- `mortalityTable.ageShift`: Return the (period) death probabilities of the life table for a given observation year
- `mortalityTable.trendProjection`: Return the (period) death probabilities of the life table for a given observation year
- `mortalityTable.improvementFactors`: Return the (period) death probabilities of the life table for a given observation year
- `mortalityTable.mixed`: Return the (period) death probabilities of the life table for a given observation year
- `mortalityTable.jointLives`: Return the (period) death probabilities of the joint lives mortality table for a given observation year

Examples

```

mortalityTables.load("Austria_Annuities")
periodDeathProbabilities(AVOe2005R.male, Period = 1975)
periodDeathProbabilities(AVOe2005R.male, Period = 2017)

mortalityTables.load("Germany_Census")
table.JL = mortalityTable.jointLives(

```

```

    name = "ADSt 24/26 auf verbundene Leben",
    table = mort.DE.census.1924.26.male
  )
periodDeathProbabilities(table.JL, Period = 2017, ageDifferences = c(1, 5, -5, 16))
periodDeathProbabilities(table.JL, Period = 2017, ageDifferences = c(0))
periodDeathProbabilities(table.JL, Period = 2017, ageDifferences = c(1, 5, 16))

```

periodDeathProbabilitiesIndividual

Return a matrix of the persons' individual period death probabilities of a joint-life table (instance of [mortalityTable.jointLives](#))

Description

Return a matrix of the persons' individual period death probabilities of a joint-life table (instance of [mortalityTable.jointLives](#))

Usage

```
periodDeathProbabilitiesIndividual(tables, period, ageDifferences)
```

Arguments

| | |
|----------------|--|
| tables | List of life table objects (object inherited from mortalityTable) |
| period | The observation period |
| ageDifferences | The age differences to the first person |

Examples

```

mortalityTables.load("Germany_Census")
periodDeathProbabilitiesIndividual(list(mort.DE.census.1924.26.male), 1977, c(0, 0))
periodDeathProbabilitiesIndividual(list(mort.DE.census.1924.26.male), 1977, c(0, -5, 13))

```

periodTransitionProbabilities

Return all period transition probabilities of the pension table

Description

Return all period transition probabilities of the pension table

Usage

```

periodTransitionProbabilities(object, ...)

## S4 method for signature 'pensionTable'
periodTransitionProbabilities(object, Period = 2017,
  ..., ages = NULL, OverallMortality = FALSE, retirement = NULL,
  invalids.retire = object@invalids.retire, as.data.frame = TRUE)

```

Arguments

| | |
|-------------------------------|--|
| <code>object</code> | A pension table object (instance of a pensionTable class) |
| <code>...</code> | Currently unused |
| <code>Period</code> | Observation year |
| <code>ages</code> | Desired age range (if NULL, the probabilities of the age range provided by the table will be returned), missing ages will be filled with NA |
| <code>OverallMortality</code> | Whether the overall mortality should be returned for actives, or the active mortality |
| <code>retirement</code> | Override the retirement transition probabilities of the pension table. Possible values are: <ul style="list-style-type: none"> • Single age (describing a deterministic retirement at the given age) • <code>mortalityTable</code> object: transition probabilities for retirement |
| <code>invalids.retire</code> | Override the pensionTable 's <code>invalids.retire</code> flag, which indicates whether invalids retire like actives (i.e. same death probabilities after retirement) or stay invalid until death. |
| <code>as.data.frame</code> | Whether the return value should be a <code>data.frame</code> or an array containing transition matrices |

Methods (by class)

- `pensionTable`: Return all transition probabilities of the pension table for the period `Period`

Examples

```

pensionTables.load("USA_PensionPlans")
# transitionProbabilities internally calls periodTransitionProbabilities
# if a Period is given:
transitionProbabilities(RP2014.male, Period = 1955)
periodTransitionProbabilities(RP2014.male, Period = 1955)
periodTransitionProbabilities(RP2014.male, Period = 2025)

```

plot.mortalityTable *Plot multiple mortality tables (life tables) in one plot*

Description

plot.mortalityTable displays multiple life tables (objects of child classes of mortalityTable) in one plot, with a legend showing the names of the tables. If the argument reference not given, all mortality rates are plotted on a log-linear scale for comparison. If the argument reference is given and is a valid life table, then all death probabilities are scaled by the given reference table and the y-axis shows the death rates as percentage of the reference table.

Usage

```
## S3 method for class 'mortalityTable'
plot(x, ..., reference = NULL, trend = FALSE)
```

Arguments

| | |
|-----------|--|
| x | First life table to be plotted. Must be a mortalityTable object for the dispatcher to call this function |
| ... | Additional life tables to be plotted (mortalityTable objects) as well as any of the following parameters (which are passed on to plotMortalityTables or plotMortalityTableComparisons): xlim,ylim Axes limitation (as a two-element vectors) xlab,ylab Axes labels (default for x-axis: "Alter", default for y-axis: "Sterbewahrscheinlichkeit q_x") title The plot title legend.position The position of the legend (default is c(0.9, 0.1)) legend.key.width The keywidth of the lines in the legend (default is unit(25, "mm")) |
| reference | The reference table that determines the 100% values. If not given, the absolute mortality values are compared and plotted on a log-linear scale. |
| trend | If set to TRUE, the function plotMortalityTrend is used to plot the trends of the given tables. |

See Also

[plotMortalityTables](#) and [plotMortalityTableComparisons](#)

Examples

```
# Load the Austrian census data
mortalityTables.load("Austria_Census")

# Plot some select census tables in a log-linear plot
plot(mort.AT.census.1869.male, mort.AT.census.1869.female,
      mort.AT.census.1971.male, mort.AT.census.1971.female,
```

```

mort.AT.census.2011.male, mort.AT.census.2011.female,
title="Austrian census tables",
ylab=expression(q[x]), xlab="Age",
xlim=c(0,90),
legend.position=c(0.95,0.05))

# Compare some census tables with the mortality of 2011 Austrian males
plot(mort.AT.census.1869.male, mort.AT.census.1869.female,
mort.AT.census.1971.male, mort.AT.census.1971.female,
mort.AT.census.2011.male, mort.AT.census.2011.female,
title="Austrian Census tables, relative to 2011 males",
reference=mort.AT.census.2011.male)

```

plotMortalityTableComparisons

Plot multiple mortality tables (life tables) in one plot, relative to a given reference table

Description

plotMortalityTableComparisons prints multiple life tables (objects of child classes of mortalityTable) in one plot and scales each by the given reference table, so that the relative mortality can be easily seen. A legend is added showing the names of the tables.

Usage

```

plotMortalityTableComparisons(data, ..., ages = NULL, xlim = NULL,
ylim = NULL, xlab = NULL, ylab = NULL, title = "",
legend.position = c(0.9, 0.1), legend.justification = c(1, 0),
legend.key.width = unit(25, "mm"), reference = NULL)

```

Arguments

| | |
|-----------------|---|
| data | First life table to be plotted. Either a data.frame generated by makeQxDataFrame or a mortalityTable object |
| ... | Additional life tables to be plotted (if data is a mortalityTable object) |
| ages | Plot only the given ages |
| xlim | X-axis limitation (as a two-element vector) |
| ylim | Y-axis limitation (as a two-element vector) |
| xlab | X-axis label (default: "Alter") |
| ylab | Y-axis label (default: "Sterbewahrscheinlichkeit q_x relativ zu") |
| title | The plot title |
| legend.position | The position of the legend (default is c(0.9, 0.1)) |

| | |
|----------------------|---|
| legend.justification | The justification of the legend (default is <code>c(1,)</code>) |
| legend.key.width | The keywidth of the lines in the legend (default is <code>unit(25, "mm")</code>) |
| reference | The reference table that determines the 100% values. If not given, the first argument of data is used as reference table. |

Examples

```
# Load the Austrian census data
mortalityTables.load("Austria_Census")

# Compare some census tables with the mortality of 2011 Austrian males
# plot with the reference argument is the same as calling plotMortalityTableComparisons
plot(mort.AT.census.1869.male, mort.AT.census.1869.female,
     mort.AT.census.1971.male, mort.AT.census.1971.female,
     mort.AT.census.2011.male, mort.AT.census.2011.female,
     title = "Austrian Census tables, relative to 1971 males",
     reference = mort.AT.census.1971.male)
plotMortalityTableComparisons(mort.AT.census.1869.male, mort.AT.census.1869.female,
                              mort.AT.census.1971.male, mort.AT.census.1971.female,
                              mort.AT.census.2011.male, mort.AT.census.2011.female,
                              title = "Austrian Census tables, relative to 1971 males",
                              reference = mort.AT.census.1971.male)
```

`plotMortalityTables` *Plot multiple mortality tables (life tables) in one plot*

Description

`plotMortalityTables` prints multiple life tables (objects of child classes of `mortalityTable`) in one log-linear plot, with a legend showing the names of the tables.

Usage

```
plotMortalityTables(data, ..., ages = NULL, legend.title = "Sterbetafel",
                   xlim = NULL, ylim = NULL, xlab = NULL, ylab = NULL, title = "",
                   legend.position = c(0.9, 0.1), legend.justification = c(1, 0),
                   legend.key.width = unit(25, "mm"))
```

Arguments

| | |
|-------------------|--|
| <code>data</code> | First life table to be plotted. Either a <code>data.frame</code> generated by <code>makeQxDataFrame</code> or a <code>mortalityTable</code> object |
| <code>...</code> | Additional life tables to be plotted (if <code>data</code> is a <code>mortalityTable</code> object) |
| <code>ages</code> | Plot only the given ages |

| | |
|----------------------|---|
| legend.title | Title of the legend |
| xlim | X-axis limitation (as a two-element vector) |
| ylim | Y-axis limitation (as a two-element vector) |
| xlab | X-axis label (default: "Alter") |
| ylab | Y-axis label (default: "Sterbewahrscheinlichkeit q_x relativ zu") |
| title | The plot title |
| legend.position | The position of the legend (default is <code>c(0.9, 0.1)</code>) |
| legend.justification | The justification of the legend (default is <code>c(1,)</code>) |
| legend.key.width | The keywidth of the lines in the legend (default is <code>unit(25, "mm")</code>) |

Examples

```
# Load the Austrian census data
mortalityTables.load("Austria_Annuities")
mortalityTables.load("Austria_Census")

# Plot some select census tables in a log-linear plot (plot called
# with mortalityTable objects is equal to calling plotMortalityTables directly)
plot(mort.AT.census.1869.male, mort.AT.census.1869.female,
     mort.AT.census.1971.male, mort.AT.census.1971.female,
     mort.AT.census.2011.male, mort.AT.census.2011.female,
     title="Austrian census tables",
     ylab=expression(q[x]), xlab="Age",
     xlim=c(0,90),
     legend.position=c(0.95,0.05))

# To compare period or cohort life tables, use the YOB and Period arguments:
plot(AVOe2005R.male, AVOe2005R.female, AVOe1996R.male, AVOe1996R.female,
     Period = 2018, title = "Austrian Annuity Tables, Period 2018")
plot(AVOe2005R.male, AVOe2005R.female, AVOe1996R.male, AVOe1996R.female,
     YOB = 2000, title = "Austrian Annuity Tables for cohort YOB=2000")
```

plotMortalityTrend *Plot the trends of multiple mortality tables (life tables) in one chart*

Description

plotMortalityTrend prints the trends of multiple life tables (objects of child classes of mortalityTable) in one plot, with a legend showing the names of the tables.

Usage

```
plotMortalityTrend(data, ..., xlim = NULL, ylim = NULL, xlab = NULL,
  ylab = NULL, title = "", legend.position = c(0.9, 0.9),
  legend.key.width = unit(25, "mm"))
```

Arguments

| | |
|------------------|---|
| data | First life table to be plotted. Either a data.frame generated by makeQxDataFrame or a mortalityTable object |
| ... | Additional life tables to be plotted (if data is a mortalityTable object) |
| xlim | X-axis limitation (as a two-element vector) |
| ylim | Y-axis limitation (as a two-element vector) |
| xlab | X-axis label (default: "Alter") |
| ylab | Y-axis label (default: "Sterbewahrscheinlichkeit q_x relativ zu") |
| title | The plot title |
| legend.position | The position of the legend (default is c(0.9, 0.1)) |
| legend.key.width | The keywidth of the lines in the legend (default is unit(25, "mm")) |

Examples

```
# Load the Austrian annuity data
mortalityTables.load("Austria-Annuities")

# Compare the trends of these tables
plotMortalityTrend(AV0e2005R.male, AV0e2005R.female, AV0e1996R.male, AV0e1996R.female,
  Period = 2002, title = "Trends of Austrian Annuity Tables")
# For tables with a non-constant trend, the Period and YOB can be used to compare
# the age-specific trends that apply to the death probabilities during a given
# period or for a given birth year
plotMortalityTrend(AV0e2005R.male, AV0e2005R.female, AV0e1996R.male, AV0e1996R.female,
  YOB = 1950, title = "Trends of Austrian Annuity Tables for cohort YOB=1950")
plotMortalityTrend(AV0e2005R.male, AV0e2005R.female, AV0e1996R.male, AV0e1996R.female,
  YOB = 2000, title = "Trends of Austrian Annuity Tables for cohort YOB=2000")
plotMortalityTrend(AV0e2005R.male, AV0e2005R.female, AV0e1996R.male, AV0e1996R.female,
  Period = 1999, title = "Trends of Austrian Annuity Tables for Period 2002")
plotMortalityTrend(AV0e2005R.male, AV0e2005R.female, AV0e1996R.male, AV0e1996R.female,
  Period = 2030, title = "Trends of Austrian Annuity Tables for Period 2030")
#' @import scales
```

| | |
|------------|--|
| setLoading | <i>Return a copy of the table with an additional loading added</i> |
|------------|--|

Description

Return a copy of the table with an additional loading added

Usage

```
setLoading(object, loading = 0)

## S4 method for signature 'mortalityTable'
setLoading(object, loading = 0)
```

Arguments

| | |
|---------|---|
| object | A life table object (instance of a mortalityTable class) |
| loading | The additional (security) loading to be added to the table. |

Methods (by class)

- mortalityTable: Return the life table with the given loading set

Examples

```
mortalityTables.load("Austria_Census")
# Austrian census mortality 2011 reduced by 30%
setLoading(mort.AT.census.2011.male, loading = -0.3)
```

| | |
|-----------------|--|
| setModification | <i>Return a copy of the table with the given modification function added</i> |
|-----------------|--|

Description

Return a copy of the table with the given modification function added

Usage

```
setModification(object, modification = 0)

## S4 method for signature 'mortalityTable'
setModification(object, modification = 0)
```

Arguments

object A life table object (instance of a mortalityTable class)
 modification The postprocessing modification function (for example, to enforce a lower bound).

Methods (by class)

- mortalityTable: Return the life table with the given modification set

Examples

```
mortalityTables.load("Austria_Census")
# Austrian census mortality 2011, with a lower floor of 0.1% death probability
at11.mod1perm = setModification(mort.AT.census.2011.male,
  modification = function(qx) {pmax(qx, 0.001)})
at11.mod1perm@name = paste(at11.mod1perm@name, "at least 0.1%")
# Austrian census mortality 2011, modified with 40% selection for ages
# below 60, vanishing linearly to age 80
at11.modSelection = setModification(mort.AT.census.2011.male,
  modification = function(qx) {
    qx * c(rep(0.6, 60), 0.6 + 0.4 * (0:20)/20, rep(1, length(qx)-81))
  })
at11.modSelection@name = paste(at11.modSelection@name, " 40% selection below 60")

plot(mort.AT.census.2011.male, at11.mod1perm, at11.modSelection,
  title = "Austrian census mortality with modifications", legend.position = c(0.99, 0.01))
```

transitionProbabilities

Return all transition probabilities of the pension table (generational probabilities)

Description

Return all transition probabilities of the pension table (generational probabilities)

Usage

```
transitionProbabilities(object, ...)
```

S4 method for signature 'pensionTable'

```
transitionProbabilities(object, YOB = 1982, ...,
  ages = NULL, OverallMortality = FALSE, Period = NULL,
  retirement = NULL, invalids.retire = object@invalids.retire,
  as.data.frame = TRUE)
```

Arguments

| | |
|------------------|---|
| object | A pension table object (instance of a <code>pensionTable</code> class) |
| ... | Currently unused |
| YOB | Year of birth |
| ages | Desired age range (if NULL, the probabilities of the age range provided by the table will be returned), missing ages will be filled with NA |
| OverallMortality | Whether the overall mortality should be returned for actives, or the active mortality |
| Period | Observation year to calculate period transition probabilities. If given, this argument overrides the YOB parameter and this function returns period transition probabilities. If this argument is not given or is null, then this function returns generational transition probabilities. |
| retirement | Override the retirement transition probabilities of the pension table. Possible values are: <ul style="list-style-type: none"> • Single age (describing a deterministic retirement at the given age) • mortalityTable object: transition probabilities for retirement |
| invalids.retire | Override the <code>pensionTable</code> 's <code>invalids.retire</code> flag, which indicates whether invalids retire like actives (i.e. same death probabilities after retirement) or stay invalid until death. |
| as.data.frame | Whether the return value should be a data.frame or an array containing transition matrices |

Methods (by class)

- `pensionTable`: Return all transition probabilities of the pension table for the generation YOB

Examples

```
pensionTables.load("USA_PensionPlans")
transitionProbabilities(RP2014.male, YOB = 1962)
transitionProbabilities(RP2014.male, Period = 1955)
transitionProbabilities(RP2014.male, Period = 2025)
```

| | |
|---------------|---|
| undampenTrend | <i>Return a mortalityTable.trendProjection object with the trend damping removed.</i> |
|---------------|---|

Description

Return a `mortalityTable.trendProjection` object with the trend damping removed.

Usage

```
undampenTrend(object)

## S4 method for signature 'mortalityTable.trendProjection'
undampenTrend(object)
```

Arguments

object The life table object (class inherited from mortalityTable)

Methods (by class)

- mortalityTable.trendProjection: Return a mortalityTable.trendProjection object with the trend damping removed.

Examples

```
mortalityTables.load("Austria_Annuities")
AV0e2005R.male.undamped = undampenTrend(AV0e2005R.male)
AV0e2005R.male.undamped@name = paste(AV0e2005R.male.undamped@name, "no trend dampening")

plot(AV0e2005R.male, AV0e2005R.male.undamped,
     title = "AV0e 2005R with trend dampening and without", YOB = 2000)
```

whittaker.mortalityTable

Smooth a life table using the Whittaker-Henderson method, interpolation possibly missing values

Description

whittaker.mortalityTable uses the Whittaker-Henderson graduation method to smooth a table of raw observed death probabilities, optionally using the exposures stored in the table as weights (if no exposures are given, equal weights are applied). The weights (either explicitly given, implicitly taken from the exposures or implicit equal weights) will be normalized to sum 1. The parameter lambda indicates the importance of smoothness. A lower value of lambda will put more emphasis on reproducing the observation as good as possible at the cost of less smoothness. In turn, a higher value of lambda will force the smoothed result to be as smooth as possible with possibly larger deviation from the input data. All ages with a death probability of NA will be interpolated in the Whittaker-Henderson method (see e.g. Lowrie)

Usage

```
whittaker.mortalityTable(table, lambda = 10, d = 2,
  name.postfix = ", smoothed", ..., weights = NULL)
```

Arguments

| | |
|---------------------------|---|
| <code>table</code> | Mortality table to be graduated. Must be an instance of a <code>mortalityTable</code> -derived class. |
| <code>lambda</code> | Smoothing parameter (default 10) |
| <code>d</code> | order of differences (default 2) |
| <code>name.postfix</code> | Postfix appended to the name of the graduated table |
| <code>...</code> | additional arguments (currently unused) |
| <code>weights</code> | Vector of weights used for graduation. Entries with weight 0 will be interpolated. If not given, the exposures of the table or equal weights are used. Weight 0 for a certain age indicates that the observation will not be used for smoothing at all, and will rather be interpolated from the smoothing of all other values. |

References

Walter B. Lowrie: An Extension of the Whittaker-Henderson Method of Graduation, Transactions of Society of Actuaries, 1982, Vol. 34, pp. 329–372

See Also

[whittaker](#)

Examples

```
# A sample observation table with exposures and raw probabilities
obsTable = mortalityTable.period(
  name = "trivial observed table",
  ages = 0:15,
  deathProbs = c(
    0.0072, 0.00212, 0.00081, 0.0005, 0.0013,
    0.001, 0.00122, 0.00142, 0.007, 0.0043,
    0.0058, 0.0067, 0.0082, 0.0091, 0.0075, 0.01),
  exposures = c(
    150, 222, 350, 362, 542,
    682, 1022, 1053, 1103, 1037,
    968, 736, 822, 701, 653, 438))

# Effect of the different parameters
obsTable.smooth = whittaker.mortalityTable(obsTable,
  lambda = 1/10, d = 2, name.postfix = " smoothed (d=2, lambda=1/10)")
obsTable.smooth1 = whittaker.mortalityTable(obsTable,
  lambda = 1, d = 2, name.postfix = " smoothed (d=2, lambda=1)")
obsTable.smooth2 = whittaker.mortalityTable(obsTable,
  lambda = 1/10, d = 3, name.postfix = " smoothed (d=3, lambda=1/10)")
plot(obsTable, obsTable.smooth, obsTable.smooth1, obsTable.smooth2,
  title = "Observed death probabilities")

# Missing values are interpolated from the Whittaker Henderson
obsTable.missing = obsTable
obsTable.missing@deathProbs[c(6,10,11,12)] = NA_real_
```

```
obsTable.interpolated = whittaker.mortalityTable(obsTable,  
  lambda = 1/10, d = 2, name.postfix = " missing values interpolated")  
plot(obsTable.missing, obsTable.interpolated,  
  title = "Missing values are automatically interpolated") + geom_point(size = 3)
```

Index

ages, 3
ages,mortalityTable.jointLives-method
 (ages), 3
ages,mortalityTable.mixed-method
 (ages), 3
ages,mortalityTable.period-method
 (ages), 3
ageShift, 4
ageShift,mortalityTable-method
 (ageShift), 4
ageShift,mortalityTable.ageShift-method
 (ageShift), 4

baseTable, 5
baseTable,mortalityTable-method
 (baseTable), 5
baseTable,mortalityTable.jointLives-method
 (baseTable), 5
baseTable,mortalityTable.period-method
 (baseTable), 5
baseYear, 6
baseYear,mortalityTable-method
 (baseYear), 6
baseYear,mortalityTable.jointLives-method
 (baseYear), 6
baseYear,mortalityTable.mixed-method
 (baseYear), 6

calculateImprovements, 7
calculateImprovements,mortalityTable.improvementFactors-method
 (calculateImprovements), 7
commutationNumbers, 8
commutationNumbers,mortalityTable-method
 (commutationNumbers), 8
commutationNumbers,numeric-method
 (commutationNumbers), 8
commutationNumbers,pensionTable-method
 (commutationNumbers), 8

deathProbabilities, 9
deathProbabilities,mortalityTable.ageShift-method
 (deathProbabilities), 9
deathProbabilities,mortalityTable.improvementFactors-method
 (deathProbabilities), 9
deathProbabilities,mortalityTable.jointLives-method
 (deathProbabilities), 9
deathProbabilities,mortalityTable.mixed-method
 (deathProbabilities), 9
deathProbabilities,mortalityTable.period-method
 (deathProbabilities), 9
deathProbabilities,mortalityTable.trendProjection-method
 (deathProbabilities), 9
deathProbabilitiesIndividual, 10

fillAges, 11
generateAgeShift, 12
getCohortTable, 12
getCohortTable,mortalityTable-method
 (getCohortTable), 12
getOmega, 13
getOmega,mortalityTable.jointLives-method
 (getOmega), 13
getOmega,mortalityTable.mixed-method
 (getOmega), 13
getOmega,mortalityTable.period-method
 (getOmega), 13
getPeriodTable, 14
getPeriodTable,mortalityTable-method
 (getPeriodTable), 14

lifeTable, 14
lifeTable,mortalityTable-method
 (lifeTable), 14

makeQxDataFrame, 15
mortalityComparisonTable, 16
mortalityImprovement, 17
mortalityImprovement,mortalityTable-method
 (mortalityImprovement), 17

- mortalityTable, [4](#), [11](#), [16](#), [19](#), [20](#), [25](#), [31](#)
- mortalityTable (mortalityTable-class), [18](#)
- mortalityTable-class, [18](#)
- mortalityTable.ageShift (mortalityTable.ageShift-class), [18](#)
- mortalityTable.ageShift-class, [18](#)
- mortalityTable.deMoivre (mortalityTable.deMoivre-class), [19](#)
- mortalityTable.deMoivre-class, [19](#)
- mortalityTable.improvementFactors, [7](#)
- mortalityTable.improvementFactors (mortalityTable.improvementFactors-class), [19](#)
- mortalityTable.improvementFactors-class, [19](#)
- mortalityTable.jointLives, [10](#), [31](#)
- mortalityTable.jointLives (mortalityTable.jointLives-class), [20](#)
- mortalityTable.jointLives-class, [20](#)
- mortalityTable.MakehamGompertz (mortalityTable.MakehamGompertz-class), [20](#)
- mortalityTable.MakehamGompertz-class, [20](#)
- mortalityTable.mixed (mortalityTable.mixed-class), [21](#)
- mortalityTable.mixed-class, [21](#)
- mortalityTable.once, [22](#)
- mortalityTable.onceAndFuture, [22](#)
- mortalityTable.period (mortalityTable.period-class), [23](#)
- mortalityTable.period-class, [23](#)
- mortalityTable.trendProjection (mortalityTable.trendProjection-class), [23](#)
- mortalityTable.trendProjection-class, [23](#)
- mortalityTable.Weibull (mortalityTable.Weibull-class), [24](#)
- mortalityTable.Weibull-class, [24](#)
- mortalityTable.zeroes, [25](#)
- MortalityTables, [26](#), [29](#)
- MortalityTables (MortalityTables-package), [3](#)
- MortalityTables-package, [3](#), [26](#), [28](#)
- mortalityTables.list, [26](#), [27](#)
- mortalityTables.load, [26](#), [26](#)
- pensionTable, [32](#), [40](#)
- pensionTable (pensionTable-class), [27](#)
- pensionTable-class, [27](#)
- pensionTables.list, [28](#), [29](#)
- pensionTables.load, [28](#), [29](#)
- periodDeathProbabilities, [29](#)
- periodDeathProbabilities, mortalityTable.ageShift-method (periodDeathProbabilities), [29](#)
- periodDeathProbabilities, mortalityTable.improvementFactors-method (periodDeathProbabilities), [29](#)
- periodDeathProbabilities, mortalityTable.jointLives-method (periodDeathProbabilities), [29](#)
- periodDeathProbabilities, mortalityTable.mixed-method (periodDeathProbabilities), [29](#)
- periodDeathProbabilities, mortalityTable.period-method (periodDeathProbabilities), [29](#)
- periodDeathProbabilities, mortalityTable.trendProjection-method (periodDeathProbabilities), [29](#)
- periodDeathProbabilitiesIndividual, [31](#)
- periodTransitionProbabilities, [31](#)
- periodTransitionProbabilities, pensionTable-method (periodTransitionProbabilities), [31](#)
- plot.mortalityTable, [33](#)
- plotMortalityTableComparisons, [33](#), [34](#)
- plotMortalityTables, [33](#), [35](#)
- plotMortalityTrend, [33](#), [36](#)
- setLoading, [38](#)
- setLoading, mortalityTable-method (setLoading), [38](#)
- setModification, [38](#)
- setModification, mortalityTable-method (setModification), [38](#)
- transitionProbabilities, [39](#)
- transitionProbabilities, pensionTable-method (transitionProbabilities), [39](#)
- undampenTrend, [40](#)
- undampenTrend, mortalityTable.trendProjection-method (undampenTrend), [40](#)

whittaker, [42](#)

whittaker.mortalityTable, [41](#)