# Package 'CARBayesST'

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Type Package

Title Spatio-Temporal Generalised Linear Mixed Models for Areal Unit

Data

Version 3.1

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**Description** 

Implements a class of spatio-temporal generalised linear mixed models for areal unit data, with inference in a Bayesian setting using Markov chain Monte Carlo (MCMC) simulation. The response variable can be binomial, Gaussian, or Poisson, but for some models only the binomial and Poisson data likelihoods are available. The spatio-temporal autocorrelation is modelled by random effects, which are assigned conditional autoregressive (CAR) style prior distributions. A number of different random effects structures are available, including models similar to Bernardinelli et al. (1995) <doi:10.1002/sim.4780142112>, Rushworth et al. (2014) <doi:10.1016/j.sste.2014.05.001> and Lee et al. (2016) <doi:10.1214/16-AOAS941>. Full details are given in the vignette accompanying this package. The creation of this package was supported by the Engineering and Physical Sciences Research Council (EPSRC) grant EP/J017442/1 and the Medical Research Council (MRC) grant MR/L022184/1.

License GPL (>= 2)

**Depends** MASS, R (>= 3.0.0), Rcpp (>= 0.11.5)

**Imports** CARBayesdata, coda, dplyr, GGally, ggplot2, gridExtra, gtools, leaflet, matrixcalc, matrixStats, rgdal, sp, spam, spdep, stats, testthat, truncdist, truncnorm, utils

LinkingTo Rcpp
LazyLoad yes

ByteCompile yes

URL http://github.com/duncanplee/CARBayesST

BugReports http://github.com/duncanplee/CARBayesST/issues

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# **R** topics documented:

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# **Description**

Implements a class of spatio-temporal generalised linear mixed models for areal unit data, with inference in a Bayesian setting using Markov chain Monte Carlo (MCMC) simulation. The response variable can be binomial, Gaussian or Poisson, but for some models only the binomial and Poisson data likelihoods are available. The spatio-temporal autocorrelation is modelled by random effects, which are assigned conditional autoregressive (CAR) style prior distributions. A number of different random effects structures are available, and full details are given in the vignette accompanying this package and the references below. The creation of this package was supported by the Engineering and Physical Sciences Research Council (EPSRC) grant EP/J017442/1 and the Medical Research Council (MRC) grant MR/L022184/1.

# **Details**

Package: CARBayesST Type: Package Version: 3.1 Date: 2020-03-09

Date: 2020-03-09 License: GPL (>= 2) coef.CARBayesST 3

#### Author(s)

Author: Duncan Lee, Alastair Rushworth and Gary Napier Maintainer: Duncan Lee <Duncan.Lee@glasgow.ac.uk>

#### References

Bernardinelli, L., D. Clayton, C.Pascuto, C.Montomoli, M.Ghislandi, and M. Songini (1995). Bayesian analysis of space-time variation in disease risk. Statistics in Medicine, 14, 2433-2443.

Knorr-Held, L. (2000). Bayesian modelling of inseparable space-time variation in disease risk. Statistics in Medicine, 19, 2555-2567.

Lee, D and Lawson, C (2016). Quantifying the spatial inequality and temporal trends in maternal smoking rates in Glasgow, Annals of Applied Statistics, 10, 1427-1446.

Lee, D and Rushworth, A and Napier, G (2018). Spatio-Temporal Areal Unit Modeling in R with Conditional Autoregressive Priors Using the CARBayesST Package, Journal of Statistical Software, 84, 9, 1-39.

Napier, G, D. Lee, C. Robertson, A. Lawson, and K. Pollock (2016). A model to estimate the impact of changes in MMR vaccination uptake on inequalities in measles susceptibility in Scotland, Statistical Methods in Medical Research, 25, 1185-1200.

Napier, G., Lee, D., Robertson, C., and Lawson, A. (2019). A Bayesian space-time model for clustering areal units based on their disease trends, Biostatistics, 20, 681-697.

Rushworth, A., D. Lee, and R. Mitchell (2014). A spatio-temporal model for estimating the long-term effects of air pollution on respiratory hospital admissions in Greater London. Spatial and Spatio-temporal Epidemiology 10, 29-38.

Rushworth, A., Lee, D., and Sarran, C (2017). An adaptive spatio-temporal smoothing model for estimating trends and step changes in disease risk. Journal of the Royal Statistical Society Series C, 66, 141-157.

# **Examples**

## See the examples in the function specific help files and in the vignette
## accompanying this package.

coef.CARBayesST

Extract the regression coefficients from a model.

## **Description**

This function takes a CARBayesST object and returns the vector of estimated regression coefficients (posterior medians).

#### Usage

```
## S3 method for class 'CARBayesST'
coef(object, ...)
```

# **Arguments**

object A CARBayesST fitted model object.

... Ignored.

## Author(s)

Duncan Lee

 ${\tt fitted.CARBayesST}$ 

Extract the fitted values from a model.

# **Description**

This function takes a CARBayesST object and returns the vector of fitted values (posterior means).

# Usage

```
## S3 method for class 'CARBayesST'
fitted(object, ...)
```

# Arguments

object A CARBayesST fitted model object.

... Ignored.

# Author(s)

Duncan Lee

logLik.CARBayesST

Extract the estimated loglikelihood from a fitted model.

# **Description**

This function takes a CARBayesST object and returns the estimated loglikelihood (posterior means).

## Usage

```
## S3 method for class 'CARBayesST'
logLik(object, ...)
```

# Arguments

object A CARBayesST fitted model object.

... Ignored.

# Author(s)

Duncan Lee

```
model.matrix.CARBayesST
```

Extract the model (design) matrix from a model.

# Description

This function takes a CARBayesST object and returns the design matrix.

# Usage

```
## S3 method for class 'CARBayesST'
model.matrix(object, ...)
```

# **Arguments**

```
object A CARBayesST fitted model object.
... Ignored.
```

# Author(s)

Duncan Lee

print.CARBayesST

Print a summary of the fitted model to the screen.

# **Description**

This function takes a CARBayesST object and returns a summary of the fitted model. The summary includes, for selected parameters, posterior medians and 95 percent credible intervals, the effective number of independent samples and the Geweke convergence diagnostic in the form of a Z-score.

## Usage

```
## S3 method for class 'CARBayesST'
print(x, ...)
```

# **Arguments**

```
x A CARBayesST fitted model object.
... Ignored.
```

# Author(s)

Duncan Lee

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residuals.CARBayesST Extract the residuals from a model.

## Description

This function takes a CARBayesST object and returns a set of residuals. The allowable types of residual are "response" (raw), and "pearson" (the default). In each case the fitted values are based on posterior means.

#### Usage

```
## S3 method for class 'CARBayesST'
residuals(object, type, ...)
```

# Arguments

object A CARBayesST fitted model object.

type A text string and one of c("response", "pearson"). If this argument is omitted

the default is "pearson".

... Ignored.

#### Author(s)

Duncan Lee

ST. CARadaptive Fit a spatio-temporal generalised linear mixed model to data, with a

spatio-temporal autoregressive process that has an adaptive autocor-

relation stucture.

# Description

Fit a spatio-temporal generalised linear mixed model to areal unit data, where the response variable can be binomial, Gaussian or Poisson. The linear predictor is modelled by known covariates and a vector of random effects. The latter follows a multivariate first order autoregressive time series process, where spatial autocorrelation is modelled via the precision matrix, which is based on a CAR type structure and a neighbourhood (adjacency) matrix W. The non-zero elements of W associated with each pair of geographically adjacent areal units are treated as random variables with ranges in the unit interval, which allows step changes to be identified in the random effects surface between geographically adjacent regions. The model is similar to that proposed by Rushworth et al. (2017). Further details are given in the vignette accompanying this package. Inference is conducted in a Bayesian setting using Markov chain Monte Carlo (MCMC) simulation.

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# Usage

ST.CARadaptive(formula, family, data=NULL, trials=NULL, W, burnin, n.sample, thin=1, prior.mean.beta=NULL, prior.var.beta=NULL, prior.nu2=NULL, prior.tau2=NULL, rho = NULL, epsilon = 0, MALA=FALSE, verbose=TRUE)

#### **Arguments**

formula A formula for the covariate part of the model using the syntax of the lm() func-

tion. Offsets can be included here using the offset() function. The response and each covariate should be vectors of length (KN)\*1, where K is the number of spatial units and N is the number of time periods. Each vector should be ordered so that the first K data points are the set of all K spatial locations at time 1, the next K are the set of spatial locations for time 2 and so on. The response must

NOT contain missing (NA) values.

family One of either "binomial", "gaussian", or "poisson", which respectively specify

a binomial likelihood model with a logistic link function, a Gaussian likelihood model with an identity link function, or a Poisson likelihood model with a log

link function.

data An optional data frame containing the variables in the formula.

trials A vector the same length and in the same order as the response containing

the total number of trials for each area and time period. Only used if fam-

ily="binomial".

W A non-negative K by K neighbourhood matrix (where K is the number of spatial

units). Typically a binary specification is used, where the jkth element equals one if areas (j, k) are spatially close (e.g. share a common border) and is zero

otherwise. For this model the matrix must be binary.

burnin The number of MCMC samples to discard as the burn-in period.

n.sample The number of MCMC samples to generate.

thin The level of thinning to apply to the MCMC samples to reduce their temporal

autocorrelation. Defaults to 1 (no thinning).

prior.mean.beta

A vector of prior means for the regression parameters beta (Gaussian priors are

assumed). Defaults to a vector of zeros.

prior.var.beta A vector of prior variances for the regression parameters beta (Gaussian priors

are assumed). Defaults to a vector with values 100000.

prior.nu2 The prior shape and scale in the form of c(shape, scale) for an Inverse-Gamma(shape,

scale) prior for nu2. Defaults to c(1, 0.01) and only used if family="Gaussian".

prior.tau2 The prior shape and scale in the form of c(shape, scale) for an Inverse-Gamma(shape,

scale) prior for tau2. Defaults to c(1, 0.01).

rho The value in the interval [0, 1] that the spatial dependence parameter rho is fixed

at if it should not be estimated. If this arugment is NULL then rho is estimated in the model. Setting rho=1, reduces the random effects prior to the intrinsic

CAR model but does require epsilon>0.

epsilon Diagonal ridge parameter to add to the random effects prior precision matrix,

only required when rho = 1, and the prior precision is improper. Defaults to 0.

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MALA Logical, should the function use Metropolis adjusted Langevin algorithm (MALA)

updates (TRUE) or simple random walk (FALSE, default) updates for the random effects and the regression parameters. Not applicable if family="gaussian".

verbose Logical, should the function update the user on its progress.

#### Value

summary.results

A summary table of the parameters.

samples A list containing the MCMC samples from the model. fitted.values A vector of fitted values for each area and time period.

residuals A matrix with 2 columns where each column is a type of residual and each

row relates to an area and time period. The types are "response" (raw), and

"pearson".

modelfit Model fit criteria including the Deviance Information Criterion (DIC) and its

corresponding estimated effective number of parameters (p.d), the Log Marginal Predictive Likelihood (LMPL), the Watanabe-Akaike Information Criterion (WAIC) and its corresponding estimated number of effective parameters (p.w), and the

loglikelihood.

accept The acceptance probabilities for the parameters.

localised.structure

A list with 2 K\*K matrices, Wmedian and W99 summarising the estimated adjacency relationships. Wmedian contains the posterior median for each w\_ij element estimated in the model for adjacent areal units, while W99 contains binary indicator variables for whether Prob(w\_ij < 0.5|data)>0.99. For both matrices,

elements corresponding to non-adjacent pairs of areas have NA values.

formula The formula (as a text string) for the response, covariate and offset parts of the

model.

model A text string describing the model fit.

X The design matrix of covariates.

## Author(s)

Alastair Rushworth

#### References

Rushworth, A., Lee, D., and Sarran, C (2017). An adaptive spatio-temporal smoothing model for estimating trends and step changes in disease risk. Journal of the Royal Statistical Society Series C, 66, 141-157.

# Examples

```
x.easting <- 1:10
x.northing <- 1:10
Grid <- expand.grid(x.easting, x.northing)</pre>
K <- nrow(Grid)</pre>
N <- 10
N.all \leftarrow N * K
#### set up spatial neighbourhood matrix W
distance <- as.matrix(dist(Grid))</pre>
W \leftarrow array(0, c(K,K))
W[distance==1] <-1
#### Simulate the elements in the linear predictor and the data
Q.W \leftarrow 0.99 * (diag(apply(W, 2, sum)) - W) + 0.01 * diag(rep(1,K))
Q.W.inv <- solve(Q.W)
phi.temp <- mvrnorm(n=1, mu=rep(0,K), Sigma=(0.1 * Q.W.inv))</pre>
phi <- phi.temp</pre>
    for(i in 2:N)
    phi.temp2 <- mvrnorm(n=1, mu=(0.8 * phi.temp), Sigma=(0.1 * Q.W.inv))</pre>
    phi.temp <- phi.temp2</pre>
    phi <- c(phi, phi.temp)</pre>
jump <- \text{rep}(c(\text{rep}(2, 70), \text{rep}(4, 30)), N)
LP <- jump + phi
fitted <- exp(LP)
Y <- rpois(n=N.all, lambda=fitted)
#### Run the model
## Not run: model <- ST.CARadaptive(formula=Y~1, family="poisson", W=W, burnin=10000,
n.sample=50000)
## End(Not run)
#### Toy example for checking
model <- ST.CARadaptive(formula=Y~1, family="poisson", W=W, burnin=10,</pre>
n.sample=50)
```

ST.CARanova

Fit a spatio-temporal generalised linear mixed model to data, with spatial and temporal main effects and a spatio-temporal interaction.

# **Description**

Fit a spatio-temporal generalised linear mixed model to areal unit data, where the response variable can be binomial, Gaussian or Poisson. The linear predictor is modelled by known covariates and three vectors of random effects. The latter include spatial and temporal main effects and a

spatio-temporal interaction. The spatial and temporal main effects are modelled by the conditional autoregressive (CAR) prior proposed by Leroux et al. (2000), while the spatio-temporal interaction random effects are independent. Due to the lack of identifiability between the interactions and the Gaussian errors, only main effects are allowed in the Gaussian model. Missing values are allowed in the response in this model, and are sampled from in the model using data augmentation. The model is similar to that proposed by Knorr-Held (2000), and further details are given in the vignette accompanying this package. Inference is conducted in a Bayesian setting using Markov chain Monte Carlo (MCMC) simulation.

## Usage

ST.CARanova(formula, family, data=NULL, trials=NULL, W, interaction=TRUE, burnin, n.sample, thin=1, prior.mean.beta=NULL, prior.var.beta=NULL, prior.nu2=NULL, prior.tau2=NULL, rho.S=NULL, rho.T=NULL, MALA=FALSE, verbose=TRUE)

# **Arguments**

formula A formula for the covariate part of the model using the syntax of the lm() func-

tion. Offsets can be included here using the offset() function. The response and each covariate should be vectors of length (KN)\*1, where K is the number of spatial units and N is the number of time periods. Each vector should be ordered so that the first K data points are the set of all K spatial locations at time 1, the next K are the set of spatial locations for time 2 and so on. The response can

contain missing (NA) values.

family One of either "binomial", "gaussian" or "poisson", which respectively specify a

binomial likelihood model with a logistic link function, a Gaussian likelihood model with an identity link function, or a Poisson likelihood model with a log

link function.

data An optional data.frame containing the variables in the formula.

trials A vector the same length and in the same order as the response containing

the total number of trials for each area and time period. Only used if fam-

ily="binomial".

W A non-negative K by K neighbourhood matrix (where K is the number of spatial

units). Typically a binary specification is used, where the jkth element equals one if areas (j, k) are spatially close (e.g. share a common border) and is zero otherwise. The matrix can be non-binary, but each row must contain at least one

non-zero entry.

interaction TRUE or FALSE indicating whether the spatio-temporal interaction random ef-

fects should be included. Defaults to TRUE unless family="gaussian" in which

case interactions are not allowed.

burnin The number of MCMC samples to discard as the burn-in period.

n. sample The number of MCMC samples to generate.

thin The level of thinning to apply to the MCMC samples to reduce their temporal

autocorrelation. Defaults to 1 (no thinning).

prior.mean.beta

A vector of prior means for the regression parameters beta (Gaussian priors are

assumed). Defaults to a vector of zeros.

prior.var.beta A vector of prior variances for the regression parameters beta (Gaussian priors are assumed). Defaults to a vector with values 100000. prior.nu2 The prior shape and scale in the form of c(shape, scale) for an Inverse-Gamma(shape, scale) prior for nu2. Defaults to c(1, 0.01) and only used if family="Gaussian". prior.tau2 The prior shape and scale in the form of c(shape, scale) for an Inverse-Gamma(shape, scale) prior for tau2. Defaults to c(1, 0.01). rho.S The value in the interval [0, 1] that the spatial dependence parameter rho.S is fixed at if it should not be estimated. If this arugment is NULL then rho.S is estimated in the model. rho.T The value in the interval [0, 1] that the temporal dependence parameter rho.T is fixed at if it should not be estimated. If this arugment is NULL then rho.T is estimated in the model. Logical, should the function use Metropolis adjusted Langevin algorithm (MALA) MALA updates (TRUE) or simple random walk (FALSE, default) updates for the random effects and the regression parameters. Not applicable if family="gaussian". Logical, should the function update the user on its progress. verbose

## Value

summary.results

A summary table of the parameters.

samples A list containing the MCMC samples from the model. fitted.values A vector of fitted values for each area and time period.

residuals A matrix with 2 columns where each column is a type of residual and each

row relates to an area and time period. The types are "response" (raw), and

"pearson".

modelfit Model fit criteria including the Deviance Information Criterion (DIC) and its

corresponding estimated effective number of parameters (p.d), the Log Marginal Predictive Likelihood (LMPL), the Watanabe-Akaike Information Criterion (WAIC) and its corresponding estimated number of effective parameters (p.w), and the

loglikelihood.

accept The acceptance probabilities for the parameters.

localised.structure

NULL, for compatability with the other models.

formula The formula (as a text string) for the response, covariate and offset parts of the

model.

model A text string describing the model fit.

X The design matrix of covariates.

#### Author(s)

Duncan Lee

## References

Knorr-Held, L. (2000). Bayesian modelling of inseparable space-time variation in disease risk. Statistics in Medicine, 19, 2555-2567.

Leroux, B., X. Lei, and N. Breslow (2000). Estimation of disease rates in small areas: A new mixed model for spatial dependence, Chapter Statistical Models in Epidemiology, the Environment and Clinical Trials, Halloran, M and Berry, D (eds), pp. 135-178. Springer-Verlag, New York.

```
#### Run the model on simulated data on a lattice
#### set up the regular lattice
x.easting <- 1:10
x.northing <- 1:10
Grid <- expand.grid(x.easting, x.northing)</pre>
K <- nrow(Grid)</pre>
N < -10
N.all \leftarrow N * K
#### set up spatial (W) and temporal (D) neighbourhood matrices
distance <- as.matrix(dist(Grid))</pre>
W \leftarrow array(0, c(K,K))
W[distance==1] <-1
D <-array(0, c(N,N))</pre>
for(i in 1:N)
    for(j in 1:N)
        if(abs((i-j))==1) D[i,j] <- 1
}
#### Simulate the elements in the linear predictor and the data
gamma <- rnorm(n=N.all, mean=0, sd=0.001)</pre>
x <- rnorm(n=N.all, mean=0, sd=1)
beta <- 0.1
Q.W \leftarrow 0.99 * (diag(apply(W, 2, sum)) - W) + 0.01 * diag(rep(1,K))
Q.W.inv <- solve(Q.W)
phi <- mvrnorm(n=1, mu=rep(0,K), Sigma=(0.01 * Q.W.inv))</pre>
Q.D \leftarrow 0.99 * (diag(apply(D, 2, sum)) - D) + 0.01 * diag(rep(1,N))
Q.D.inv <- solve(Q.D)
delta <- mvrnorm(n=1, mu=rep(0,N), Sigma=(0.01 * Q.D.inv))</pre>
phi.long <- rep(phi, N)</pre>
delta.long <- kronecker(delta, rep(1,K))</pre>
```

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```
LP <- 4 + x * beta + phi.long + delta.long + gamma
mean <- exp(LP)
Y <- rpois(n=N.all, lambda=mean)

##### Run the model
## Not run: model <- ST.CARanova(formula=Y~x, family="poisson", interaction=TRUE,
W=W, burnin=10000, n.sample=50000)
## End(Not run)

#### Toy example for checking
model <- ST.CARanova(formula=Y~x, family="poisson", interaction=TRUE,
W=W, burnin=10, n.sample=50)</pre>
```

ST.CARar

Fit a spatio-temporal generalised linear mixed model to data, with a spatio-temporal autoregressive process.

# **Description**

Fit a spatio-temporal generalised linear mixed model to areal unit data, where the response variable can be binomial, Gaussian or Poisson. The linear predictor is modelled by known covariates and a vector of random effects. The latter follows a multivariate first order autoregressive time series process, where spatial autocorrelation is modelled via the precision matrix. This precision matrix comes from the conditional autoregressive (CAR) prior proposed by Leroux et al. (2000), and the full model was proposed by Rushworth et al. (2014). Missing values are allowed in the response in this model, and are sampled from in the model using data augmentation.. Further details are given in the vignette accompanying this package. Inference is conducted in a Bayesian setting using Markov chain Monte Carlo (MCMC) simulation.

## Usage

```
ST.CARar(formula, family, data=NULL, trials=NULL, W, burnin, n.sample, thin=1, prior.mean.beta=NULL, prior.var.beta=NULL, prior.nu2=NULL, prior.tau2=NULL, rho.S=NULL, rho.T=NULL, MALA=FALSE, verbose=TRUE)
```

#### **Arguments**

formula

A formula for the covariate part of the model using the syntax of the lm() function. Offsets can be included here using the offset() function. The response and each covariate should be vectors of length (KN)\*1, where K is the number of spatial units and N is the number of time periods. Each vector should be ordered so that the first K data points are the set of all K spatial locations at time 1, the next K are the set of spatial locations for time 2 and so on. The response can contain missing (NA) values.

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family	One of either "binomial", "gaussian" or "poisson", which respectively specify a binomial likelihood model with a logistic link function, a Gaussian likelihood model with an identity link function, or a Poisson likelihood model with a log link function.					
data	An optional data frame containing the variables in the formula.					
trials	A vector the same length and in the same order as the response containing the total number of trials for each area and time period. Only used if family="binomial".					
W	A non-negative K by K neighbourhood matrix (where K is the number of spatial units). Typically a binary specification is used, where the jkth element equals one if areas (j, k) are spatially close (e.g. share a common border) and is zero otherwise. The matrix can be non-binary, but each row must contain at least one non-zero entry.					
burnin	The number of MCMC samples to discard as the burn-in period.					
n.sample	The number of MCMC samples to generate.					
thin	The level of thinning to apply to the MCMC samples to reduce their temporal autocorrelation. Defaults to 1 (no thinning).					
prior.mean.beta						
	A vector of prior means for the regression parameters beta (Gaussian priors are assumed). Defaults to a vector of zeros.					
prior.var.beta	A vector of prior variances for the regression parameters beta (Gaussian priors are assumed). Defaults to a vector with values 100000.					
prior.nu2	The prior shape and scale in the form of $c(shape, scale)$ for an Inverse-Gamma(shape, scale) prior for nu2. Defaults to $c(1, 0.01)$ and only used if family="Gaussian".					
prior.tau2	The prior shape and scale in the form of $c(shape, scale)$ for an Inverse-Gamma(shape, scale) prior for tau2. Defaults to $c(1, 0.01)$ .					
rho.S	The value in the interval [0, 1] that the spatial dependence parameter rho.S is fixed at if it should not be estimated. If this arugment is NULL then rho.S is estimated in the model.					
rho.T	The value in the interval [0, 1] that the temporal dependence parameter rho.T is fixed at if it should not be estimated. If this arugment is NULL then rho.T is estimated in the model.					
MALA	Logical, should the function use Metropolis adjusted Langevin algorithm (MALA) updates (TRUE) or simple random walk (FALSE, default) updates for the random effects and the regression parameters. Not applicable if family="gaussian".					
verbose	Logical, should the function update the user on its progress.					

# Value

 $\verb|summary.results||$ 

A summary table of the parameters.

samples A list containing the MCMC samples from the model. fitted.values A vector of fitted values for each area and time period.

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residuals A matrix with 2 columns where each column is a type of residual and each

row relates to an area and time period. The types are "response" (raw), and

"pearson".

modelfit Model fit criteria including the Deviance Information Criterion (DIC) and its

corresponding estimated effective number of parameters (p.d), the Log Marginal Predictive Likelihood (LMPL), the Watanabe-Akaike Information Criterion (WAIC) and its corresponding estimated number of effective parameters (p.w), and the

loglikelihood.

accept The acceptance probabilities for the parameters.

localised.structure

NULL, for compatability with the other models.

formula The formula (as a text string) for the response, covariate and offset parts of the

model.

model A text string describing the model fit.

X The design matrix of covariates.

## Author(s)

Duncan Lee

#### References

Rushworth, A., D. Lee, and R. Mitchell (2014). A spatio-temporal model for estimating the long-term effects of air pollution on respiratory hospital admissions in Greater London. Spatial and Spatio-temporal Epidemiology 10, 29-38.

```
#### Run the model on simulated data on a lattice
#### set up the regular lattice
x.easting <- 1:10
x.northing <- 1:10
Grid <- expand.grid(x.easting, x.northing)</pre>
K <- nrow(Grid)</pre>
N <- 10
N.all \leftarrow N * K
#### set up spatial neighbourhood matrix W
distance <- as.matrix(dist(Grid))</pre>
W \leftarrow array(0, c(K,K))
W[distance==1] <-1
#### Simulate the elements in the linear predictor and the data
gamma <- rnorm(n=N.all, mean=0, sd=0.001)</pre>
x <- rnorm(n=N.all, mean=0, sd=1)
```

```
beta <- 0.1
Q.W < -0.99 * (diag(apply(W, 2, sum)) - W) + 0.01 * diag(rep(1,K))
Q.W.inv <- solve(Q.W)
phi.temp <- mvrnorm(n=1, mu=rep(0,K), Sigma=(0.1 * Q.W.inv))
phi <- phi.temp</pre>
    for(i in 2:N)
   phi.temp2 <- mvrnorm(n=1, mu=(0.8 * phi.temp), Sigma=(0.1 * Q.W.inv))</pre>
   phi.temp <- phi.temp2</pre>
   phi <- c(phi, phi.temp)</pre>
LP <- 3 + x * beta + phi
mean <- exp(LP)
Y <- rpois(n=N.all, lambda=mean)
#### Run the model
## Not run: model <- ST.CARar(formula=Y~x, family="poisson", W=W, burnin=10000,
    n.sample=50000)
## End(Not run)
#### Toy example for checking
model <- ST.CARar(formula=Y~x, family="poisson", W=W, burnin=10,</pre>
    n.sample=50)
```

ST.CARclustrends

Fit a spatio-temporal generalised linear mixed model to data, with a clustering of temporal trend functions and a temporally common spatial surface.

# Description

Fit a spatio-temporal generalised linear mixed model to areal unit data, where the response variable can be binomial or Poisson. The linear predictor is modelled by known covariates, a temoporally common spatial surface, and a mixture of temporal trend functions. The spatial component is modelled by the conditional autoregressive (CAR) prior proposed by Leroux et al. (2000). The temporal trend functions are user-specified and are fixed parametric forms (e.g. linear, step-change) or constrained shapes (e.g. monotonically increasing). Further details are given in Napier et al. (2018) and in the vignette accompanying this package. Inference is conducted in a Bayesian setting using Metropolis coupled Markov chain Monte Carlo (MCMCMC) simulation.

## Usage

```
ST.CARclustrends(formula, family, data=NULL, trials=NULL, W, burnin, n.sample, thin=1, trends=NULL, changepoint=NULL, knots=NULL, prior.mean.beta=NULL, prior.var.beta=NULL, prior.mean.gamma=NULL, prior.var.gamma=NULL, prior.lambda=NULL, prior.tau2=NULL, Nchains=4, verbose=TRUE)
```

#### **Arguments**

formula

A formula using the syntax of the lm() function. However, due to identifiability issues covariates are not allowed. So the only elements allowed on the right side of the formula are an intercept term and an offset term using the offset() function. The response variable and the offset (if specified) should be vectors of length (KN)\*1, where K is the number of spatial units and N is the number of time periods. Each vector should be ordered so that the first K data points are the set of all K spatial locations at time 1, the next K are the set of spatial locations for time 2 and so on.

family

One of either "binomial" or "poisson", which respectively specify a binomial likelihood model with a logistic link function, or a Poisson likelihood model with a log link function.

data

An optional data.frame containing the variables in the formula.

trials

A vector the same length and in the same order as the response containing the total number of trials for each area and time period. Only used if family="binomial".

W

A non-negative K by K neighbourhood matrix (where K is the number of spatial units). Typically a binary specification is used, where the jkth element equals one if areas (j, k) are spatially close (e.g. share a common border) and is zero otherwise. The matrix can be non-binary, but each row must contain at least one non-zero entry.

burnin

The number of MCMC samples to discard as the burn-in period.

n.sample

The number of MCMC samples to generate.

thin

The level of thinning to apply to the MCMC samples to reduce their temporal autocorrelation. Defaults to 1 (no thinning).

trends

A vector containing the temporal trend functions to include in the model, which include: constant ("Constant""); linear decreasing ("LD"); linear increasing ("LI"); Known change point, where the trend can increase towards the change point before subsequently decreasing ("CP"); or decrease towards the change point before subsequently increasing ("CT"); and monotonic cubic splines which are decreasing ("MD") or increasing ("MI"). At least two trends have to be selected, with the constant trend always included. To avoid identifiability problems only one of "LI" or "MI" can be included at a given time (similarily for "LD" and "MD").

changepoint

A scalar indicating the position of the change point should one of the change point trend functions be included in the trends vector, i.e. if "CP" or "CT" is specified.

knots

A scalar indicating the number of knots to use should one of the monotonic cubic splines trend functions be included in the trends vector, i.e. if "MD" or "MI" is specified.

prior.mean.beta

A vector of prior means for the regression parameters beta (Gaussian priors are assumed). Defaults to a vector of zeros.

prior.var.beta A vector of prior variances for the regression parameters beta (Gaussian priors are assumed). Defaults to a vector with values 100000.

prior.mean.gamma

A vector of prior means for the temporal trend parameters (Gaussian priors are assumed). Defaults to a vector of zeros.

prior.var.gamma

A vector of prior variances for the temporal trend parameters (Gaussian priors

are assumed). Defaults to a vector with values 100000.

prior.lambda A vector of prior samples sizes for the Dirichlet prior controlling the probabili-

ties that each trend function is chosen. The vector should be the same length as

the trends vector and defaults to a vector of ones.

prior.tau2 The prior shape and scale in the form of c(shape, scale) for an Inverse-Gamma(shape,

scale) prior for the random effect variances tau2. Defaults to c(1, 0.01).

Nchains The number of parallel Markov chains to be used in the Metropolis coupled

Markov chain Monte Carlo (MCMCMC) simulations. Defaults to 4.

verbose Logical, should the function update the user on its progress.

#### Value

summary.results

residuals

A summary table of the parameters.

samples A list containing the MCMC samples from the model.

fitted.values A vector of fitted values for each area and time period.

A matrix with 2 columns where each column is a type of residual and each row relates to an area and time period. The types are "response" (raw), and

"pearson".

modelfit Model fit criteria including the Deviance Information Criterion (DIC) and its

corresponding estimated effective number of parameters (p.d), the Log Marginal Predictive Likelihood (LMPL), the Watanabe-Akaike Information Criterion (WAIC) and its corresponding estimated number of effective parameters (p.w), and the

loglikelihood.

accept The acceptance probabilities for the parameters.

localised.structure

A list containing two elements. The first is "trends", which is a vector the same length and in the same order as the number of areas. The kth element specifies which trend area k has been allocated to based on the posterior mode. The second element is "trend.probs", which is a matrix containing the probabilities

associated with each trend for each areal unit.

formula The formula (as a text string) for the response, covariate and offset parts of the

model.

model A text string describing the model fit.

X The design matrix of covariates.

#### Author(s)

Gary Napier

#### References

Leroux, B., Lei, X., and Breslow, N. (2000). Estimation of disease rates in small areas: A new mixed model for spatial dependence, Chapter Statistical Models in Epidemiology, the Environment and Clinical Trials, Halloran, M and Berry, D (eds), pp. 135-178. Springer-Verlag, New York.

Napier, G., Lee, D., Robertson, C., and Lawson, A. (2019). A Bayesian space-time model for clustering areal units based on their disease trends, Biostatistics, 20, 681-697.

```
#### Run the model on simulated data on a lattice
#### Load the libraries required
library(truncdist)
library(gtools)
#### set up the regular lattice
x.easting <- 1:10
x.northing <- 1:10
Grid <- expand.grid(x.easting, x.northing)</pre>
K <- nrow(Grid)</pre>
N < -10
N.all \leftarrow N * K
#### set up spatial neighbourhood matrix W
distance <- as.matrix(dist(Grid))</pre>
W \leftarrow array(0, c(K,K))
W[distance==1] <-1
#### Create the spatial covariance matrix
Q.W \leftarrow 0.99 * (diag(apply(W, 2, sum)) - W) + 0.01 * diag(rep(1,K))
Q.W.inv <- solve(Q.W)
#### Simulate the elements in the linear predictor and the data
beta <- 0.01
gamma <- 0.7
phi <- mvrnorm(n=1, mu=rep(0,K), Sigma=(0.01 * Q.W.inv))</pre>
lambda \leftarrow rep(1/2, 2)
w <- t(rmultinom(K, 1, lambda))</pre>
Y <- matrix(NA, nrow = K, ncol = N)
for (i in 1:N)
{
 LP \leftarrow beta + w[, 2] * (gamma * i) + phi
 mean <- exp(LP)</pre>
 Y[, i] <- rpois(n=K, lambda=mean)
 }
```

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```
#### Run the model
## Not run: model <- ST.CARclustrends(formula=Y~1, family="poisson", W=W, burnin=10000,
n.sample=50000, trends=c("Constant", "LI"))
## End(Not run)

#### Toy example for checking
model <- ST.CARclustrends(formula=Y~1, family="poisson", W=W, burnin=10,
n.sample=50, trends=c("Constant", "LI"))</pre>
```

ST.CARlinear

Fit a spatio-temporal generalised linear mixed model to data, where the spatial units have linear time trends with spatially varying intercepts and slopes.

## **Description**

Fit a spatio-temporal generalised linear mixed model to areal unit data, where the response variable can be binomial, Gaussian or Poisson. The linear predictor is modelled by known covariates and an area specific linear time trend. The area specific intercepts and slopes are spatially autocorrelated and modelled by the conditional autoregressive (CAR) prior proposed by Leroux et al. (2000). The model is similar to that proposed by Bernardinelli et al. (1995) and further details are given in the vignette accompanying this package. Missing values are allowed in the response in this model, and are sampled from in the model using data augmentation. Inference is conducted in a Bayesian setting using Markov chain Monte Carlo (MCMC) simulation.

## Usage

```
ST.CARlinear(formula, family, data=NULL, trials=NULL, W, burnin, n.sample, thin=1, prior.mean.beta=NULL, prior.var.beta=NULL, prior.mean.alpha=NULL, prior.var.alpha=NULL, prior.nu2=NULL, prior.tau2=NULL, rho.slo=NULL, rho.int=NULL, MALA=FALSE, verbose=TRUE)
```

#### Arguments

formula

A formula for the covariate part of the model using the syntax of the lm() function. Offsets can be included here using the offset() function. The response and each covariate should be vectors of length (KN)\*1, where K is the number of spatial units and N is the number of time periods. Each vector should be ordered so that the first K data points are the set of all K spatial locations at time 1, the next K are the set of spatial locations for time 2 and so on. The response can contain missing (NA) values.

family

One of either "binomial", "gaussian" or "poisson", which respectively specify a binomial likelihood model with a logistic link function, a Gaussian likelihood model with an identity link function, or a Poisson likelihood model with a log link function.

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data An optional data.frame containing the variables in the formula. trials A vector the same length and in the same order as the response containing the total number of trials for each area and time period. Only used if family="binomial". A non-negative K by K neighbourhood matrix (where K is the number of spatial units). Typically a binary specification is used, where the jkth element equals one if areas (j, k) are spatially close (e.g. share a common border) and is zero otherwise. The matrix can be non-binary, but each row must contain at least one non-zero entry. burnin The number of MCMC samples to discard as the burn-in period. The number of MCMC samples to generate. n.sample thin The level of thinning to apply to the MCMC samples to reduce their temporal autocorrelation. Defaults to 1 (no thinning). prior.mean.beta A vector of prior means for the regression parameters beta (Gaussian priors are assumed). Defaults to a vector of zeros. prior.var.beta A vector of prior variances for the regression parameters beta (Gaussian priors are assumed). Defaults to a vector with values 100000. prior.mean.alpha The prior mean for the average slope of the linear time trend alpha (a Gaussian prior is assumed). Defaults to zero. prior.var.alpha The prior variance for the average slope of the linear time trend alpha (a Gaussian prior is assumed). Defaults to 100000. prior.nu2 The prior shape and scale in the form of c(shape, scale) for an Inverse-Gamma(shape, scale) prior for nu2. Defaults to c(1, 0.01) and only used if family="Gaussian". The prior shape and scale in the form of c(shape, scale) for an Inverse-Gamma(shape, prior.tau2 scale) prior for tau2. Defaults to c(1, 0.01). rho.slo The value in the interval [0, 1] that the spatial dependence parameter for the slope of the linear time trend, rho.slo, is fixed at if it should not be estimated. If this arugment is NULL then rho.slo is estimated in the model. rho.int The value in the interval [0, 1] that the spatial dependence parameter for the intercept of the linear time trend, rho.int, is fixed at if it should not be estimated. If this arugment is NULL then rho.int is estimated in the model. Logical, should the function use Metropolis adjusted Langevin algorithm (MALA) MALA updates (TRUE) or simple random walk (FALSE, default) updates for the random effects and the regression parameters. Not applicable if family="gaussian".

Logical, should the function update the user on its progress.

## Value

summary.results

verbose

A summary table of the parameters.

samples A list containing the MCMC samples from the model.

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fitted.values A vector of fitted values for each area and time period.

residuals A matrix with 2 columns where each column is a type of residual and each

row relates to an area and time period. The types are "response" (raw), and

"pearson".

modelfit Model fit criteria including the Deviance Information Criterion (DIC) and its

corresponding estimated effective number of parameters (p.d), the Log Marginal Predictive Likelihood (LMPL), the Watanabe-Akaike Information Criterion (WAIC) and its corresponding estimated number of effective parameters (p.w), and the

loglikelihood.

accept The acceptance probabilities for the parameters.

localised.structure

NULL, for compatability with the other models.

formula The formula (as a text string) for the response, covariate and offset parts of the

model.

model A text string describing the model fit.

X The design matrix of covariates.

## Author(s)

Duncan Lee

#### References

Bernardinelli, L., D. Clayton, C.Pascuto, C.Montomoli, M.Ghislandi, and M. Songini (1995). Bayesian analysis of space-time variation in disease risk. Statistics in Medicine, 14, 2433-2443.

Leroux, B., X. Lei, and N. Breslow (2000). Estimation of disease rates in small areas: A new mixed model for spatial dependence, Chapter Statistical Models in Epidemiology, the Environment and Clinical Trials, Halloran, M and Berry, D (eds), pp. 135-178. Springer-Verlag, New York.

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```
#### Simulate the elements in the linear predictor and the data
x <- rnorm(n=N.all, mean=0, sd=1)</pre>
beta <- 0.1
Q.W \leftarrow 0.99 * (diag(apply(W, 2, sum)) - W) + 0.01 * diag(rep(1,K))
Q.W.inv <- solve(Q.W)
phi <- mvrnorm(n=1, mu=rep(0,K), Sigma=(0.1 * Q.W.inv))</pre>
delta <- mvrnorm(n=1, mu=rep(0,K), Sigma=(0.1 * Q.W.inv))</pre>
trend <- array(NA, c(K, N))</pre>
time <-(1:N - mean(1:N))/N
    for(i in 1:K)
    trend[i, ] <- phi[i] + delta[i] * time</pre>
trend.vec <- as.numeric(trend)</pre>
LP \leftarrow 4 + x * beta + trend.vec
mean <- exp(LP)</pre>
Y <- rpois(n=N.all, lambda=mean)
#### Run the model
## Not run: model <- ST.CARlinear(formula=Y~x, family="poisson", W=W, burnin=10000,
n.sample=50000)
## End(Not run)
#### Toy example for checking
model <- ST.CARlinear(formula=Y~x, family="poisson", W=W, burnin=10,</pre>
n.sample=50)
```

ST.CARlocalised

Fit a spatio-temporal generalised linear mixed model to data, with a spatio-temporal autoregressive process and a piecewise constant intercept term.

# **Description**

Fit a spatio-temporal generalised linear mixed model to areal unit data, where the response variable can be binomial or Poisson. The linear predictor is modelled by known covariates, a vector of random effects and a piecewise constant intercept process. The random effects follow the multivariate first order autoregressive time series process proposed by Rushworth et al.(2014), which is the same as that used in the ST.CARar() function. The piecewise constant intercept component allows neighbouring areal units to have very different values if they are assigned to a different intercept component. This model allows for localised smoothness, because some pairs of neighbouring areas or time periods can have similar values (same intercept) while other neighbouring pairs have very different values (different intercepts). Furter details are given in Lee and Lawson (2016) and in the vignette accompanying this package. Inference is conducted in a Bayesian setting using Markov chain Monte Carlo (MCMC) simulation.

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## Usage

ST.CARlocalised(formula, family, data=NULL, G, trials=NULL, W, burnin, n.sample, thin=1, prior.mean.beta=NULL, prior.var.beta=NULL, prior.delta=NULL, prior.tau2=NULL, MALA=FALSE, verbose=TRUE)

#### **Arguments**

formula A formula for the covariate part of the model using the syntax of the lm() func-

tion. Offsets can be included here using the offset() function. The response and each covariate should be vectors of length (KN)\*1, where K is the number of spatial units and N is the number of time periods. Each vector should be ordered so that the first K data points are the set of all K spatial locations at time 1, the next K are the set of spatial locations for time 2 and so on. The response must

NOT contain missing (NA) values.

family One of either "binomial", or "poisson", which respectively specify a binomial

likelihood model with a logistic link function, or a Poisson likelihood model

with a log link function.

data An optional data.frame containing the variables in the formula.

G The maximum number of distinct intercept terms (clusters) to allow in the model.

trials A vector the same length and in the same order as the response containing

the total number of trials for each area and time period. Only used if fam-

ily="binomial".

W A non-negative K by K neighbourhood matrix (where K is the number of spatial

units). Typically a binary specification is used, where the jkth element equals one if areas (j, k) are spatially close (e.g. share a common border) and is zero otherwise. The matrix can be non-binary, but each row must contain at least one

non-zero entry.

burnin The number of MCMC samples to discard as the burn-in period.

n.sample The number of MCMC samples to generate.

thin The level of thinning to apply to the MCMC samples to reduce their temporal

autocorrelation. Defaults to 1 (no thinning).

prior.mean.beta

A vector of prior means for the regression parameters beta (Gaussian priors are

assumed). Defaults to a vector of zeros.

prior.var.beta A vector of prior variances for the regression parameters beta (Gaussian priors

are assumed). Defaults to a vector with values 100000.

prior.delta The prior maximum M, in a Uniform(0,M) prior, for the intercept process smooth-

ing parameter delta. Defaults to 10.

prior.tau2 The prior shape and scale in the form of c(shape, scale) for an Inverse-Gamma(shape,

scale) prior for tau2. Defaults to c(1, 0.01).

MALA Logical, should the function use Metropolis adjusted Langevin algorithm (MALA)

updates (TRUE) or simple random walk (FALSE, default) updates for the random effects and the regression parameters. Not applicable if family="gaussian".

verbose Logical, should the function update the user on its progress.

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#### Value

summary.results

A summary table of the parameters.

samples A list containing the MCMC samples from the model. fitted.values A vector of fitted values for each area and time period.

residuals A matrix with 2 columns where each column is a type of residual and each

row relates to an area and time period. The types are "response" (raw), and

"pearson".

modelfit Model fit criteria including the Deviance Information Criterion (DIC) and its

corresponding estimated effective number of parameters (p.d), the Log Marginal Predictive Likelihood (LMPL), the Watanabe-Akaike Information Criterion (WAIC) and its corresponding estimated number of effective parameters (p.w), and the

loglikelihood.

accept The acceptance probabilities for the parameters.

localised.structure

A vector giving the posterior mean of which intercept component (cluster) each

data point is in.

formula The formula (as a text string) for the response, covariate and offset parts of the

model.

model A text string describing the model fit.

X The design matrix of covariates.

## Author(s)

Duncan Lee

#### References

Lee, D and Lawson, C (2016). Quantifying the spatial inequality and temporal trends in maternal smoking rates in Glasgow, Annals of Applied Statistics, 10, 1427-1446.

```
W \leftarrow (K,K)
W[distance==1] <-1
#### Simulate the elements in the linear predictor and the data
Q.W \leftarrow 0.99 * (diag(apply(W, 2, sum)) - W) + 0.01 * diag(rep(1,K))
Q.W.inv <- solve(Q.W)
phi.temp <- mvrnorm(n=1, mu=rep(0,K), Sigma=(0.1 * Q.W.inv))</pre>
phi <- phi.temp
    for(i in 2:N)
    phi.temp2 <- mvrnorm(n=1, mu=(0.8 * phi.temp), Sigma=(0.1 * Q.W.inv))</pre>
    phi.temp <- phi.temp2</pre>
    phi <- c(phi, phi.temp)</pre>
jump <- \text{rep}(c(\text{rep}(2, 70), \text{rep}(4, 30)), N)
LP <- jump + phi
fitted <- exp(LP)</pre>
Y <- rpois(n=N.all, lambda=fitted)
#### Run the model
## Not run: model <- ST.CARlocalised(formula=Y~1, family="poisson", G=3, W=W, burnin=10000,
n.sample=50000)
## End(Not run)
#### Toy example for checking
model <- ST.CARlocalised(formula=Y~1, family="poisson", G=3, W=W, burnin=10,</pre>
n.sample=50)
```

ST.CARsepspatial

Fit a spatio-temporal generalised linear mixed model to data, with a common temporal main effect and separate spatial surfaces with individual variances.

## **Description**

Fit a spatio-temporal generalised linear mixed model to areal unit data, where the response variable can be binomial or Poisson. The linear predictor is modelled by known covariates and two sets of random effects. These include a common temporal main effect, and separate time period specific spatial effects with a common spatial dependence parameter but separate variance parameters. Each component is modelled by the conditional autoregressive (CAR) prior proposed by Leroux et al. (2000). Further details are given in Napier et al. (2016) and in the vignette accompanying this package. Inference is conducted in a Bayesian setting using Markov chain Monte Carlo (MCMC) simulation.

## Usage

```
ST.CARsepspatial(formula, family, data=NULL, trials=NULL, W, burnin, n.sample,
```

thin=1, prior.mean.beta=NULL, prior.var.beta=NULL, prior.tau2=NULL, rho.S=NULL, rho.T=NULL, MALA=FALSE, verbose=TRUE)

## **Arguments**

verbose

formula A formula for the covariate part of the model using the syntax of the lm() function. Offsets can be included here using the offset() function. The response and each covariate should be vectors of length (KN)\*1, where K is the number of spatial units and N is the number of time periods. Each vector should be ordered so that the first K data points are the set of all K spatial locations at time 1, the next K are the set of spatial locations for time 2 and so on. The response must NOT contain missing (NA) values. family One of either "binomial" or "poisson", which respectively specify a binomial likelihood model with a logistic link function, or a Poisson likelihood model with a log link function. data An optional data.frame containing the variables in the formula. trials A vector the same length and in the same order as the response containing the total number of trials for each area and time period. Only used if family="binomial". W A non-negative K by K neighbourhood matrix (where K is the number of spatial units). Typically a binary specification is used, where the jkth element equals one if areas (j, k) are spatially close (e.g. share a common border) and is zero otherwise. The matrix can be non-binary, but each row must contain at least one non-zero entry. burnin The number of MCMC samples to discard as the burn-in period. n.sample The number of MCMC samples to generate. thin The level of thinning to apply to the MCMC samples to reduce their temporal autocorrelation. Defaults to 1 (no thinning). prior.mean.beta A vector of prior means for the regression parameters beta (Gaussian priors are assumed). Defaults to a vector of zeros. prior.var.beta A vector of prior variances for the regression parameters beta (Gaussian priors are assumed). Defaults to a vector with values 100000. prior.tau2 The prior shape and scale in the form of c(shape, scale) for an Inverse-Gamma(shape, scale) prior for tau2. Defaults to c(1, 0.01). rho.S The value in the interval [0, 1] that the spatial dependence parameter rho.S is fixed at if it should not be estimated. If this arugment is NULL then rho.S is estimated in the model. The value in the interval [0, 1] that the temporal dependence parameter rho.T rho.T is fixed at if it should not be estimated. If this arugment is NULL then rho.T is estimated in the model. MALA Logical, should the function use Metropolis adjusted Langevin algorithm (MALA) updates (TRUE) or simple random walk (FALSE, default) updates for the random effects and the regression parameters. Not applicable if family="gaussian".

Logical, should the function update the user on its progress.

#### Value

summary.results

A summary table of the parameters.

samples A list containing the MCMC samples from the model. fitted.values A vector of fitted values for each area and time period.

residuals A matrix with 2 columns where each column is a type of residual and each

row relates to an area and time period. The types are "response" (raw), and

"pearson".

modelfit Model fit criteria including the Deviance Information Criterion (DIC) and its

corresponding estimated effective number of parameters (p.d), the Log Marginal Predictive Likelihood (LMPL), the Watanabe-Akaike Information Criterion (WAIC) and its corresponding estimated number of effective parameters (p.w), and the

loglikelihood.

accept The acceptance probabilities for the parameters.

localised.structure

NULL, for compatability with the other models.

formula The formula (as a text string) for the response, covariate and offset parts of the

model.

model A text string describing the model fit.

X The design matrix of covariates.

#### Author(s)

Gary Napier

#### References

Napier, G, D. Lee, C. Robertson, A. Lawson, and K. Pollock (2016). A model to estimate the impact of changes in MMR vaccination uptake on inequalities in measles susceptibility in Scotland, Statistical Methods in Medical Research, 25, 1185-1200.

```
W \leftarrow array(0, c(K,K))
W[distance==1] <-1
#### Create the spatial covariance matrix
Q.W \leftarrow 0.99 * (diag(apply(W, 2, sum)) - W) + 0.01 * diag(rep(1,K))
Q.W.inv <- solve(Q.W)
#### Simulate the elements in the linear predictor and the data
x <- rnorm(n=N.all, mean=0, sd=1)
beta <- 0.1
phi1 <- mvrnorm(n=1, mu=rep(0,K), Sigma=(0.01 * Q.W.inv))
phi2 <- mvrnorm(n=1, mu=rep(0,K), Sigma=(0.01 * Q.W.inv))
phi3 <- mvrnorm(n=1, mu=rep(0,K), Sigma=(0.01 * Q.W.inv))
phi4 <- mvrnorm(n=1, mu=rep(0,K), Sigma=(0.05 * Q.W.inv))
phi5 <- mvrnorm(n=1, mu=rep(0,K), Sigma=(0.05 * Q.W.inv))
delta \leftarrow c(0, 0.5, 0, 0.5, 0)
phi.long <- c(phi1, phi2, phi3, phi4, phi5)</pre>
delta.long <- kronecker(delta, rep(1,K))</pre>
LP \leftarrow 4 + x * beta + phi.long + delta.long
mean <- exp(LP)</pre>
Y <- rpois(n=N.all, lambda=mean)
#### Run the model
## Not run: model <- ST.CARsepspatial(formula=Y~x, family="poisson", W=W, burnin=10000,
n.sample=50000)
## End(Not run)
#### Toy example for checking
model <- ST.CARsepspatial(formula=Y~x, family="poisson", W=W, burnin=10,</pre>
n.sample=50)
```

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