# Overview of the package BuyseTest

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This vignette describes the main functionalities of the **BuyseTest** package. This package implements the Generalized Pairwise Comparisons (GPC) as defined in Buyse (2010) for complete observations, and extended in Péron et al. (2018) to deal with right-censoring. It is assumed that the reader is familar with the GPC terminology <sup>1</sup>, e.g. prioritized endpoints, pair, net benefit, win ratio, threshold of clinical relevance, ..., since this vignette focuses on the software aspect of the **BuyseTest** package (not on the underlying statistical model).

The **BuyseTest** package contains three main functions:

- the function BuyseTest is the main function of the package. It performs the GPC, estimates the net benefit/win ratio, and output a *BuyseRes* object. The user can interact with *BuyseRes* objects using:
  - summary to obtain a nice display of the results
  - coef to extract the estimates.
  - confint to extract estimates, confidence intervals, and p.values.
  - getIid to extract the iid decomposition of the estimator.
  - getPairScore to extract the contribution of each pair to the net benefit/win ratio.
  - getSurvival to extract the estimates of the survival (only relevant for right-censored endpoints).
- the powerBuyseTest function performs simulation studies, e.g. to estimate the statistical power or assess the bias / type 1 error rate of a test for a specific design.
- the BuyseTest.options function enables the user to display the default values used in the BuyseTest package (essentially used by the BuyseTest function). function. The function can also change the default values to better match the user needs.

<sup>&</sup>lt;sup>1</sup> if not, Buyse (2010) is a good place to start.

Before going further we need to load the **BuyseTest** package in the R session:

library(BuyseTest)
library(data.table)

To illustrate the functionalities of the package, we will used the **veteran** dataset from the **survival** package:

```
data(veteran,package="survival")
head(veteran)
```

	trt	celltype	time	status	karno	diagtime	age	prior
1	1	squamous	72	1	60	7	69	0
2	1	squamous	411	1	70	5	64	10
3	1	squamous	228	1	60	3	38	0
4	1	squamous	126	1	60	9	63	10
5	1	squamous	118	1	70	11	65	10
6	1	squamous	10	1	20	5	49	0

See ?veteran for a presentation of the database.

<u>Note:</u> the **BuyseTest** package is under active development. Newer package versions may include additional functionalities and fix previous bugs. The version of the package that is being is:

utils::packageVersion("BuyseTest")

#### [1] '2.0.0'

For completness, the details of the R session used to generate this document are:

sessionInfo()

```
R version 3.5.1 (2018-07-02)
Platform: x86_64-pc-linux-gnu (64-bit)
Running under: Ubuntu 16.04.5 LTS
Matrix products: default
BLAS: /usr/lib/libblas/libblas.so.3.6.0
LAPACK: /usr/lib/lapack/liblapack.so.3.6.0
locale:
 [1] LC_CTYPE=fr_FR.UTF-8
                                LC_NUMERIC=C
                                                            LC_TIME=da_DK.UTF-8
 [4] LC_COLLATE=fr_FR.UTF-8
                                                            LC_MESSAGES=fr_FR.UTF-8
                                LC_MONETARY=da_DK.UTF-8
 [7] LC_PAPER=da_DK.UTF-8
                                LC_NAME=C
                                                            LC_ADDRESS=C
                                LC_MEASUREMENT=da_DK.UTF-8 LC_IDENTIFICATION=C
[10] LC_TELEPHONE=C
attached base packages:
```

other attached packages: [1] data.table\_1.12.8 BuyseTest\_2.0.0 Rcpp\_1.0.4

 loaded via a namespace (and not attached):
 [1] compiler\_3.5.1
 Matrix\_1.2-14
 tools\_3.5.1
 parallel\_3.5.1

 [5] survival\_2.44-1.1
 prodlim\_2019.11.13
 splines\_3.5.1
 grid\_3.5.1

 [9] lava\_1.6.7
 stats4\_3.5.1
 lattice\_0.20-35

# 1 Performing generalized pairwise comparisons (GPC) using the BuyseTest function

To perform generalized pairwise comparisons, the BuyseTest function needs:

• where the data are stored	- argument data
• the name of the endpoints	- argument endpoint
• the type of each endpoint	- argument type
• the variable defining the two treatment groups	- argument treatment
The BuyseTest function has many optional arguments to specify for example:	
• the threshold of clinical relevance associated to each endpoint	- argument threshold
• the censoring associated to each endpoint (for time to event endpoints)	- argument status

There are two equivalent ways to define the GPC:

• using a separate argument for each element<sup>2</sup>:

```
BT <- BuyseTest(data = veteran,
endpoint = "time",
type = "timeToEvent",
treatment = "trt",
status = "status",
threshold = 20)
```

Generalized Pairwise Comparisons

# Settings - 2 groups : Control = 1 and Treatment = 2 - 1 endpoint: priority endpoint type operator threshold event 1 time time to event higher is favorable 20 status (0 1) - right-censored pairs: probabilistic score based on the survival curves Point estimation and calculation of the iid decomposition Estimation of the estimator's distribution - method: moments of the U-statistic Gather the results in a S4BuyseTest object

 $<sup>^{2}</sup>$  the argument method.inference is set to "none" to diseable the computation of p-values and confidence intervals. This makes the execution of BuyseTest much faster.

- or via a formula interface. In the formula interface endpoint are wrapped by parentheses. The parentheses must be preceded by their type:
  - binary (b, bin, or binary)
  - continuous (c, cont, or continuous)
  - time to event (t, tte, or timetoevent)

Here we set in addition the argument trace to 0 to force the function to be silent (i.e. no display in the terminal). We can check that the two approaches are equivalent:

testthat::expect\_equal(BT.f,BT)

#### 1.1 Displaying the results

The results of the GPC can be displayed using the summary method:

summary(BT)

```
Generalized pairwise comparisons with 1 endpoint
> statistic
                  : net benefit (delta: endpoint specific, Delta: global)
> null hypothesis : Delta == 0
> confidence level: 0.95
                  : H-projection of order 1
> inference
> treatment groups: 1 (control) vs. 2 (treatment)
> right-censored pairs: probabilistic score based on the survival curves
> results
endpoint threshold total(%) favorable(%) unfavorable(%) neutral(%) uninf(%)
                                                                               delta
                                                                                       Delta
   time
                20
                        100
                                   37.78
                                                  46.54
                                                              15.68
                                                                           0 -0.0877 -0.0877
CI [2.5%; 97.5%] p.value
 [-0.2735;0.1045] 0.37161
```

To display the number of pairs instead of the percentage of pairs that are favorable/unfavorable/neutral/uniformative, set the argument percentage to FALSE:

summary(BT, percentage = FALSE)

```
Generalized pairwise comparisons with 1 endpoint
> statistic
                  : net benefit (delta: endpoint specific, Delta: global)
> null hypothesis : Delta == 0
> confidence level: 0.95
> inference
                  : H-projection of order 1
> treatment groups: 1 (control) vs. 2 (treatment)
> right-censored pairs: probabilistic score based on the survival curves
> results
endpoint threshold total favorable unfavorable neutral uninf
                                                               delta
                                                                       Delta
   time
                20 4692
                           1772.59
                                       2183.89 735.52
                                                           0 -0.0877 -0.0877
CI [2.5%; 97.5%] p.value
 [-0.2735;0.1045] 0.37161
```

By default summary displays results relative to the net benefit. To get results for the win ratio set the argument statistic to "winRatio":

summary(BT, statistic = "winRatio")

```
Generalized pairwise comparisons with 1 endpoint
> statistic
                  : win ratio (delta: endpoint specific, Delta: global)
> null hypothesis : Delta == 1
> confidence level: 0.95
                : H-projection of order 1
> inference
> treatment groups: 1 (control) vs. 2 (treatment)
> right-censored pairs: probabilistic score based on the survival curves
> results
endpoint threshold total(%) favorable(%) unfavorable(%) neutral(%) uninf(%) delta Delta
                                   37.78
                                                  46.54
   time
                20
                        100
                                                             15.68
                                                                          0 0.8117 0.8117
CI [2.5%; 97.5%] p.value
  [0.5134;1.2832] 0.37194
```

See help(BuyseRes-summary) for more detailed explanations about the summary method and its output.

#### 1.2 Using multiple endpoints

More than one endpoint can be considered by indicating a vector of endpoints, types, and thresholds. In the formula interface, the different endpoints must be separated with a "+" on the right hand side of the formula:

```
ff2 <- trt \sim tte(time, threshold = 20, status = "status") + cont(karno, threshold = 0)
BT.H <- BuyseTest(ff2, data = veteran, trace = 0)
summary(BT.H)
```

```
Generalized pairwise comparisons with 2 prioritized endpoints
```

```
: net benefit (delta: endpoint specific, Delta: global)
> statistic
> null hypothesis : Delta == 0
> confidence level: 0.95
> inference
                  : H-projection of order 1
> treatment groups: 1 (control) vs. 2 (treatment)
> right-censored pairs: probabilistic score based on the survival curves
> neutral pairs : re-analyzed using lower priority endpoints
> results
endpoint threshold total(%) favorable(%) unfavorable(%) neutral(%) uninf(%)
                                                                               delta
                                                                                       Delta
                     100.00
                                   37.78
                20
                                                   46.54
                                                              15.68
                                                                           0 -0.0877 -0.0877
    time
             1e-12
                      15.68
                                    5.78
                                                    7.11
                                                               2.78
                                                                           0 -0.0133 -0.1009
  karno
CI [2.5%; 97.5%] p.value
 [-0.2735;0.1045] 0.37161
 [-0.2901;0.0959] 0.31477
```

The hierarchy of the endpoint is defined from left (most important endpoint, here time) to right (least important endpoint, here karno). It is also possible to perform the comparisons on all endpoints setting the argument hierarchical to FALSE:

```
BT.nH <- BuyseTest(ff2, hierarchical = FALSE, data = veteran, trace = 0)
summary(BT.nH)</pre>
```

Generalized pairwise comparisons with 2 endpoints > statistic : net benefit (delta: endpoint specific, Delta: global) > null hypothesis : Delta == 0 > confidence level: 0.95 > inference : H-projection of order 1 > treatment groups: 1 (control) vs. 2 (treatment) > right-censored pairs: probabilistic score based on the survival curves > neutral pairs : re-analyzed using lower priority endpoints > results endpoint threshold weight total(%) favorable(%) unfavorable(%) neutral(%) uninf(%) time 20 1 100 37.78 46.54 15.68 karno 1e-12 1 100 41.82 44.95 13.24 Delta CI [2.5%; 97.5%] p.value -0.0877 [-0.2735;0.1045] 0.37161

```
-0.1190 [-0.4346;0.2226] 0.49821
```

delta

0 -0.0877

0 -0.0313

In that case the score of a pair is the weighted sum of the score relative to each endpoint. By default the weights are all set to 1 but this behavior can be changed by setting the argument weight when calling BuyseTest, e.g.:

```
ff2w <- trt ~ tte(time, threshold = 20, status = "status", weight = 0.8)
ff2w <- update.formula(ff2w, . ~ . + cont(karno, threshold = 0, weight = 0.2))
BT.nHw <- BuyseTest(ff2w, hierarchical = FALSE, data = veteran, trace = 0)
summary(BT.nHw)</pre>
```

Generalized pairwise comparisons with 2 endpoints > statistic : net benefit (delta: endpoint specific, Delta: global) > null hypothesis : Delta == 0 > confidence level: 0.95 : H-projection of order 1 > inference > treatment groups: 1 (control) vs. 2 (treatment) > right-censored pairs: probabilistic score based on the survival curves > neutral pairs : re-analyzed using lower priority endpoints > results endpoint threshold weight total(%) favorable(%) unfavorable(%) neutral(%) uninf(%) delta 37.78 time 20 0.8 100 46.54 15.68 0 -0.0877 1e-12 0.2 41.82 44.95 0 -0.0313 karno 100 13.24 Delta CI [2.5%; 97.5%] p.value -0.0701 [-0.2204;0.0834] 0.37072 -0.0764 [-0.2504;0.1024] 0.40268

This has been referred as the O'Brien test in the litterature (Verbeeck et al. (2019), section 3.2).

#### **1.3** What if smaller is better?

By default BuyseTest will always assume that higher values of an endpoint are favorable. This behavior can be changed by specifying operator = "<0" for an endpoint:

```
endpoint threshold delta Delta
time 20 0.0844 0.0844
```

Internally BuyseTest will multiply by -1 the values of the endpoint to ensure that lower values are considered as favorable. A direct consequence is that BuyseTest will not accept an endpoint with different operators:

Error in (function (name.call, status, correction.uninf, cpus, data, endpoint, : Cannot have different operator for the same endpoint used at different priorities.

#### 1.4 Stratified GPC

GPC can be performed for subgroups of a categorical variable - argument strata

For instance, the celltype may have huge influence on the survival time and the investigator would like to only compare patients that have the same celltype. In the formula interface this is achieved by adding a single variable in the right hand side of the formula:

The fact the it is not wrapped by **bin**, **cont** or **tte** indicates differentiate it from endpoint variables.

When doing a stratified analysis, the summary method displays the global results as well as the results within each strata<sup>3</sup>:

```
Generalized pairwise comparisons with 2 prioritized endpoints and 4 strata
> statistic
                  : net benefit (delta: endpoint specific, Delta: global)
> null hypothesis : Delta == 0
> treatment groups: 1 (control) vs. 2 (treatment)
> right-censored pairs: probabilistic score based on the survival curves
                 : re-analyzed using lower priority endpoints
> neutral pairs
> uninformative pairs: no contribution at the current endpoint, analyzed at later endpoints
> results
endpoint threshold
                      strata total(%) favorable(%) unfavorable(%)
                                                                      delta
                                                                              Delta
                20
                                100.00
                                                              45.77 -0.0971 -0.0971
    time
                      global
                                              36.06
                                 25.38
                                              14.33
                                                               8.77 0.2193
                    squamous
                   smallcell
                                 45.69
                                              12.69
                                                              20.88 -0.1792
                       adeno
                                13.71
                                               4.74
                                                               6.15 -0.1034
                       large
                                                               9.97 -0.3722
                                 15.23
                                               4.30
  karno
             1e-12
                      global
                                 18.17
                                               6.72
                                                               8.07 -0.0135 -0.1106
                                  2.28
                                               0.76
                                                               0.94 -0.0071
                    squamous
                   smallcell
                                 12.12
                                               4.33
                                                               5.75 -0.0311
                                                               0.85 0.0448
                       adeno
                                  2.81
                                               1.46
                                  0.96
                                                               0.54 -0.0241
                                               0.17
                       large
```

Note that here the numbers in the total/favorable/unfavorable/ columns are relative to the overall sample while the delta is only relative to the strata. The global delta is a sum of the strata specific delta weighted by the empirical proportion of pairs for each strata.

#### **1.5** Stopping comparison for neutral pairs

In presence of neutral pairs, BuyseTest will, by default, continue the comparison on the endpoints with lower priority. For instance let consider a dataset with one observation in each treatment arm:

```
Id treatment tumor size
1: 1 Yes Yes 15
2: 2 No Yes 20
```

<sup>&</sup>lt;sup>3</sup>the strata-specific results can be removed by setting the argument strata to "global" when calling summary.

If we use the GPC with tumor as the first endpoint and size as the second endpoint:

#### Generalized pairwise comparisons with 2 prioritized endpoints

```
: net benefit (delta: endpoint specific, Delta: global)
> statistic
> null hypothesis : Delta == 0
> treatment groups: 0 (control) vs. 1 (treatment)
> neutral pairs : re-analyzed using lower priority endpoints
> results
endpoint threshold total(%) favorable(%) unfavorable(%) neutral(%) uninf(%) delta Delta
               0.5
                        100
                                       0
                                                       0
                                                                100
                                                                           0
                                                                                 0
                                                                                       0
  tumor
                                                       0
                                                                  0
                                     100
                                                                           0
             1e-12
                        100
                                                                                 1
                                                                                       1
    size
```

the outcome of the comparison is neutral for the first priority, but favorable for the second priority. If we set the argument neutral.as.uninf to FALSE, BuyseTest will stop the comparison when a pair is classified as neutral:

#### Generalized pairwise comparisons with 2 prioritized endpoints

> statisti	с :	net bene	efit (delta: d	endpoint specif:	ic, Delta: g	global)					
> null hyp	> null hypothesis : Delta == 0										
> treatment groups: 0 (control) vs. 1 (treatment)											
> neutral pairs : ignored at lower priority endpoints											
> results											
endpoint t	hreshold	total(%)	<pre>favorable(%)</pre>	unfavorable(%)	neutral(%)	uninf(%)	delta	Delta			
tumor	0.5	100	0	0	100	0	0	0			
size	1e-12	0	0	0	0	0	0	0			

So in this case no pair is analyzed at second priority.

#### 1.6 What about p-value and confidence intervals?

Several methods are available in **BuyseTest** to perform statistical inference:

• permutation test setting the argument method.inference to "permutation". Assuming exchangeability under the null hypothesis, this approach gives valid p-values (regardless to the sample size) for testing the absence of a difference between the groups.

Generalized pairwise comparisons with 1 endpoint

```
> statistic
                  : net benefit (delta: endpoint specific, Delta: global)
> null hypothesis : Delta == 0
> confidence level: 0.95
> inference
                  : permutation test with 1000 samples
                    p-value computed using the permutation distribution
> treatment groups: 1 (control) vs. 2 (treatment)
> right-censored pairs: probabilistic score based on the survival curves
> results
endpoint threshold total(%) favorable(%) unfavorable(%) neutral(%) uninf(%)
                                                                               delta
                                                                                       Delta
                20
                        100
                                   37.78
                                                  46.54
                                                              15.68
                                                                           0 -0.0877 -0.0877
    time
p.value
  0.355
```

• bootstrap resampling setting the argument method.inference to "bootstrap". In large enough samples, this approach gives valid p-values and confidence intervals.

Generalized pairwise comparisons with 1 endpoint

```
endpoint threshold total(%) favorable(%) unfavorable(%) neutral(%) uninf(%) delta Delta
   time 20 100 37.78 46.54 15.68 0 -0.0877 -0.0877
CI [2.5%; 97.5%] p.value
[-0.2922;0.1013] 0.393
```

• asymptotic distribution setting the argument method.inference to "u-statistic". In large enough samples, this approach gives valid p-values and confidence intervals.

#### Generalized pairwise comparisons with 1 endpoint

```
: net benefit (delta: endpoint specific, Delta: global)
> statistic
> null hypothesis : Delta == 0
> confidence level: 0.95
                  : H-projection of order 1
> inference
> treatment groups: 1 (control) vs. 2 (treatment)
> right-censored pairs: probabilistic score based on the survival curves
> results
endpoint threshold total(%) favorable(%) unfavorable(%) neutral(%) uninf(%)
                                                                                delta
                                                                                        Delta
                20
                        100
                                   37.78
                                                   46.54
                                                              15.68
                                                                            0 -0.0877 -0.0877
    time
CI [2.5%; 97.5%] p.value
 [-0.2735;0.1045] 0.37161
```

The first two approaches require simulating a large number of samples and applying the GPC to each of these samples. The number of samples is set using the arugment n.resampling and it should large enough to limit the Monte Carlo error when estimating the p-value. Typically should be at least 10000 to get, roughtly, 2-digit precision, as examplified below:

```
set.seed(10)
sapply(1:10, function(i){mean(rbinom(1e4, size = 1, prob = 0.05))})
```

#### [1] 0.0511 0.0491 0.0489 0.0454 0.0516 0.0522 0.0468 0.0483 0.0491 0.0508

Indeed, here we get a reasonnable approximation of 0.05 (if we round and only keep 2 digits). Note that to get 3 digits precision we would need more samples. The last method does not rely on resampling but on the computation of the influence function of the estimator. Fortunately, when using the Gehan's scoring rule, this does not really involve any extra-calculations and this is therefore very fast to perform. When using the Peron's scoring rule, more serious extra-calculations are involved so the computation time is expected to increase by a factor 5 to 10 compared to the point estimate alone (i.e. method.inference equal to "none").

# 2 Getting additional inside: looking at the pair level

So far we have looked at the overall score and probabilities. But it is also possible to extract the score relative to each pair, as well as to "manually" compute this score. This can give further inside on what the software is actually doing and what is the contribution of each individual on the evaluation of the treatment.

#### 2.1 Extracting the contribution of each pair to the statistic

The net benefit or the win ratio statistics can be expressed as a sum of a score over all pairs of patients. The argument keep.pairScore enables to export the score relative to each pair in the output of BuyseTest:

The method getPairScore can then be used to extract the contribution of each pair. For instance the following code extracts the contribution for the first endpoint:

getPairScore(BT.keep, endpoint = 1)

	index.1	index.2	favorable	unfavorable	neutral	uninf	weight
1:	1	70	1	0	0	0	1
2:	2	70	1	0	0	0	1
3:	3	70	1	0	0	0	1
4:	4	70	1	0	0	0	1
5:	5	70	1	0	0	0	1
4688:	65	137	0	1	0	0	1
4689:	66	137	0	1	0	0	1
4690:	67	137	0	1	0	0	1
4691:	68	137	0	1	0	0	1
4692:	69	137	0	1	0	0	1

Each line corresponds to different comparison between a pair from the control arm and the treatment arm. The column strata store to which strata the pair belongs (first, second, ...). The columns favorable, unfavorable, neutral, uninformative contains the result of the comparison, e.g. the first pair was classified as favorable while the last was classified as favorable with a weight of 1. The second and third columns indicates the rows in the original dataset corresponding to the pair:

veteran[c(70,1),]

	trt	celltype	time	status	karno	diagtime	age	prior
70	2	squamous	999	1	90	12	54	10
1	1	squamous	72	1	60	7	69	0

For the first pair, the event was observed for both observations and since 999 > 72 + 20 the pair is rated favorable. Substracting the average probability of the pair being favorable minus the average probability of the pair being unfavorable:

getPairScore(BT.keep, endpoint = 1)[, mean(favorable) - mean(unfavorable)]

[1] -0.08765836

gives the net benefit in favor of the treatment for the first endpoint:

BT.keep

```
endpoint threshold delta Delta
time 20 -0.0877 -0.0877
karno 1e-12 -0.0133 -0.1009
```

More examples and explanation can be found in the documentation of the method getPairScore.

#### 2.2 Extracting the survival probabilities

When using scoring.rule equals "Peron", survival probabilities at event time, and event times +/threshold in the control and treatment arms are used to score the pair. Setting keep.survival to TRUE in BuyseTest.options enables to export the survival probabilities in the output of BuyseTest:

The method getSurvival can then be used to extract these survival probabilities. For instance the following code extracts the survival for the first endpoint:

```
outSurv <- getSurvival(BT.keep2, endpoint = 1, strata = 1)
str(outSurv)</pre>
```

```
List of 5
 $ survTimeC: num [1:69, 1:7] 72 411 228 126 118 10 82 110 314 100 ...
  ..- attr(*, "dimnames")=List of 2
  ....$ : NULL
  ....$ : chr [1:7] "time" "SurvivalC-threshold" "SurvivalC_0" "SurvivalC+threshold" ...
 $ survTimeT: num [1:68, 1:7] 999 112 87 231 242 991 111 1 587 389 ...
  ..- attr(*, "dimnames")=List of 2
  ....$ : NULL
  ....$ : chr [1:7] "time" "SurvivalC-threshold" "SurvivalC_0" "SurvivalC+threshold" ...
 $ survJumpC: num [1:57, 1:3] 3 4 7 8 10 11 12 13 16 18 ...
  ..- attr(*, "dimnames")=List of 2
  ....$ : NULL
  ....$ : chr [1:3] "time" "survival" "dSurvival"
 $ survJumpT: num [1:51, 1:3] 1 2 7 8 13 15 18 19 20 21 ...
  ..- attr(*, "dimnames")=List of 2
  ....$ : NULL
  ....$ : chr [1:3] "time" "survival" "dSurvival"
 $ lastSurv : num [1:4] 0 0 NA NA
```

#### 2.2.1 Computation of the score with only one censored event

getPairScore(BT.keep2, endpoint = 1, rm.withinStrata = FALSE)[91]

Let's look at pair 91:

index.1 index.2 indexWithinStrata.1 indexWithinStrata.2 favorable unfavorable neutral
1: 22 71 22 2 0 0.6950827 0.3049173
uninf weight
1: 0 1

In the dataset this corresponds to:

```
veteran[c(22,71),]
```

	trt	celltype	time	status	karno	diagtime	age	prior
22	1	smallcell	97	0	60	5	67	0
71	2	squamous	112	1	80	6	60	0

The observation from the control group is censored at 97 while the observation from the treatment group has an event at 112. Since the threshold is 20, and (112-20)<97, we know that the pair is not in favor of the treatment. The formula for probability in favor of the control is  $\frac{S_c(97)}{S_c(112+20)}$ . The survival at the event time in the censoring group is stored in survTimeC. Since observation 22 is the 22th observation in the control group:

```
iSurv <- outSurv$survTimeC[22,]
iSurv</pre>
```

```
        time
        SurvivalC-threshold
        SurvivalC_0
        SurvivalC+threshold

        97.000000
        0.5615232
        0.5171924
        0.4235463

        SurvivalT-threshold
        SurvivalT_0
        SurvivalT+threshold

        0.4558824
        0.3643277
        0.2827500
```

Since we are interested in the survival in the control arm exactly at the event time:

```
Sc97 <- iSurv["SurvivalC_0"]
Sc97</pre>
```

# SurvivalC\_0

0.5171924

The survival at the event time in the treatment group is stored in survTimeC. Since observation 71 is the 2nd observation in the treatment group:

```
iSurv <- outSurv$survTimeT[2,] ## survival at time 112+20
iSurv</pre>
```

 time
 SurvivalC-threshold
 SurvivalC\_0
 SurvivalC+threshold

 112.0000000
 0.5319693
 0.4549201
 0.3594915

 SurvivalT-threshold
 SurvivalT\_0
 SurvivalT+threshold

 0.3801681
 0.2827500
 0.2827500

Since we are interested in the survival in the control arm at the event time plus threshold:

```
Sc132 <- iSurv["SurvivalC+threshold"]
Sc132</pre>
```

# SurvivalC+threshold 0.3594915

The probability in favor of the control is then:

```
Sc132/Sc97
```

SurvivalC+threshold

0.6950827

#### 2.2.2 Computation of the score with two censored events

When both observations are censored, the formula for computing the probability in favor of treatment or control involves an integral. This integral can be computed using the function calcIntegralSurv\\_cpp that takes as argument a matrix containing the survival and the jumps in survival, e.g.:

head(outSurv\$survJumpT)

	time	survival	dSurvival
[1,]	1	0.7681159	-0.02941176
[2,]	2	0.7536232	-0.01470588
[3,]	7	0.7388463	-0.02941176
[4,]	8	0.7388463	-0.02941176
[5,]	13	0.7092924	-0.01470588
[6,]	15	0.6945155	-0.02941176

and the starting time of the integration time. For instance, let's look at pair 148:

getPairScore(BT.keep2, endpoint = 1, rm.withinStrata = FALSE)[148]

```
index.1 index.2 indexWithinStrata.1 indexWithinStrata.2 favorable unfavorable neutral
1: 10 72 10 3 0.5058685 0.3770426 0.1170889
uninf weight
1: 0 1
```

which corresponds to the observations:

veteran[c(10,72),]

	trt	celltype	time	status	karno	diagtime	age	prior
10	1	squamous	100	0	70	6	70	0
72	2	squamous	87	0	80	3	48	0

The probability in favor of the treatment  $(p_F)$  and control  $(p_{UF})$  can be computed as:

$$p_F = -\frac{1}{S_T(x)S_C(y)} \int_{t>y} S_T(t+\tau) dS_C(t)$$
$$p_{UF} = -\frac{1}{S_T(x)S_C(y)} \int_{t>x} S_C(t+\tau) dS_T(t)$$

where x = 87 and y = 100. To ease the call of calcIntegralScore\_cpp we create a warper:

```
calcInt <- function(...){ ## here we don't need to return the functionnal derivative of the
    score
    calcIntegralSurv_cpp(...,
        returnDeriv = FALSE, column = 0,
        derivSurv = matrix(0), derivSurvD = matrix(0))
}</pre>
```

and then call it to compute the probabilities:

favorable unfavorable

lowerBound 0.5058685 0.3770426 upperBound 0.5058685 0.3770426

# 3 Dealing with missing values or/and right censoring

In presence of censoring or missing values, some pairs may be classified as uninformative. This may bias the estimate of the net net benefit. Two corrections are currently proposed to correct this bias.

To illustrate the effect of these correction, we will use the following dataset:

	treatment	toxicity	eventtimeUncensored	eventtimeCensoring	eventtime	status	status1
1:	C	0	0.1588268	0.29186778	0.15882682	1	1
2:	C	1	1.7204676	0.02222436	0.02222436	0	1
3:	C	1	0.4900490	0.06386661	0.06386661	0	1
4:	C	0	0.1138545	0.16875557	0.11385446	1	1
5:	C	1	0.5191035	0.42600053	0.42600053	0	1
6:	C	0	0.9405830	0.21198508	0.21198508	0	1

where we have the uncensored event times as well as the censored event times. The percentage of censored observations is:

dt[,mean(status==0)]

#### [1] 0.658

We would like to be able to recover the net benefit estimated with the uncensored event times:

endpoint threshold delta Delta eventtimeUncensored 1 -0.2304 -0.2304

using the censored survival times:

```
endpoint threshold delta Delta
eventtime 1 -0.0022 -0.0022
```

As we can see on this example, the net benefit is shrunk toward 0.

#### 3.0.1 Inverse probability-of-censoring weights (IPCW)

With IPCW the weights of the non-informative pairs is redistributed to the informative pairs. This is only a good strategy when there are no neutral pairs or there are no lower priority endpoints. This gives an estimate much closer to the true net benefit:

Generalized pairwise comparisons with 1 endpoint

```
> statistic : net benefit (delta: endpoint specific, Delta: global)
```

```
> null hypothesis : Delta == 0
> treatment groups: C (control) vs. T (treatment)
```

```
> right-censored pairs: deterministic score or uninformative
```

> uninformative pairs: no contribution, their weight is passed to the informative pairs using IPCW > results

endpoint threshold total(%) favorable(%) unfavorable(%) neutral(%) uninf(%)deltaeventtime11001.183.1995.630 -0.0202-0.0202

We can also see that no pair is finally classified as non informative. To get some inside about the correction we can look at the scores of the pairs:

```
iScore <- getPairScore(BT, endpoint = 1)</pre>
```

To get a synthetic view, we only look at the unique favorable/unfavorable/neutral/uniformative results:

```
iScore[,.SD[1],
   .SDcols = c("favorableC","unfavorableC","neutralC","uninfC"),
   by = c("favorable","unfavorable","neutral","uninf")]
```

	favorable	unfavorable	neutral	uninf	favorableC	unfavorableC	neutralC	uninfC
1:	0	0	0	1	0.000000	0.000000	0.000000	0
2:	0	0	1	0	0.00000	0.00000	9.012582	0
3:	0	1	0	0	0.00000	9.012582	0.000000	0
4:	1	0	0	0	9.012582	0.000000	0.000000	0

We can see that the favorable/unfavorable/neutral pairs have seen their contribution multiplied by:

iScore[,1/mean(favorable + unfavorable + neutral)]

#### [1] 9.012582

i.e. the inverse probability of being informative.

#### 3.0.2 Correction at the pair level

Another possible correction is to distribute the non-informative weight of a pair to the average favorable/unfavorable/neutral probability observed on the sample:

Generalized pairwise comparisons with 1 endpoint

```
: net benefit (delta: endpoint specific, Delta: global)
> statistic
> null hypothesis : Delta == 0
> treatment groups: C (control) vs. T (treatment)
> right-censored pairs: deterministic score or uninformative
> uninformative pairs: score equals the averaged score of all informative pairs
> results
 endpoint threshold total(%) favorable(%) unfavorable(%) neutral(%) uninf(%)
                                                                                delta
                                                                                        Delta
eventtime
                  1
                         100
                                     1.18
                                                    3.19
                                                               95.63
                                                                            0 -0.0202 -0.0202
```

Looking at the scores of the pairs:

```
iScore <- getPairScore(BT, endpoint = 1)
iScore[,.SD[1],
    .SDcols = c("favorableC","unfavorableC","neutralC","uninfC"),
    by = c("favorable","unfavorable","neutral","uninf")]</pre>
```

	favorable	unfavorable	neutral	uninf	favorableC	unfavorableC	neutralC	uninfC
1:	0	0	0	1	0.01175241	0.03194059	0.956307	0
2:	0	0	1	0	0.0000000	0.0000000	1.000000	0
3:	0	1	0	0	0.0000000	1.00000000	0.000000	0
4:	1	0	0	0	1.0000000	0.0000000	0.000000	0

we can see that the corrected probability have not changed for the informative pairs, but for the non-informative they have been set to:

```
favorable unfavorable neutral
1: 0.01175241 0.03194059 0.956307
```

### 4 Simulating data using simBuyseTest

You can simulate data with the **simBuyseTest** function. For instance the following code simulates data for 5 individuals in the treatment arm and 5 individuals in the control arm:

```
set.seed(10)
simBuyseTest(n.T = 5, n.C = 5)
```

	treatment	toxicity	score	eventtime	status
1:	C	1	0.54361539	0.64461311	1
2:	C	1	-0.70762484	0.73722641	1
3:	C	1	-0.36944577	0.72134020	0
4:	C	1	-1.32197565	0.15806508	1
5:	C	1	1.28059746	0.22121166	0
6:	Т	1	0.01874617	0.14534811	0
7:	Т	1	-0.18425254	0.48556014	0
8:	Т	0	-1.37133055	0.25475046	0
9:	Т	1	-0.59916772	0.45965924	1
10:	Т	0	0.29454513	0.08948311	1

By default a categorical, continuous and time to event outcome are generated independently. You can modify their distribution via the arguments argsBin, argsCont, argsTTE. For instance the following code simulates two continuous variables with mean 5 in the treatment arm and 10 in the control arm all with variance 1:

	treatment	toxicity	tumorSize	score	eventtime	status
1:	C	1	9.010394	10.667415	0.27296196	0
2:	C	0	9.965152	11.691755	0.55624768	0
3:	C	0	10.847160	10.001261	0.37864505	1
4:	C	0	11.525498	9.257539	0.46192620	1
5:	C	1	9.932625	10.609684	0.09098929	1
6:	Т	1	5.389794	5.018746	0.17361208	1
7:	Т	1	3.791924	4.815747	0.08819698	1
8:	Т	1	4.636324	3.628669	0.71441489	1
9:	Т	0	3.373327	4.400832	0.10554670	0
10:	Т	0	4.743522	5.294545	0.51655591	1

This functionality is based on the sim function of the lava package (https://github.com/kkholst/lava)

# 5 Power calculation using powerBuyseTest

The function powerBuyseTest can be used to perform power calculation, i.e., estimate the probability of rejecting a null hypothesis under a specific generative mechanism. The user therefore need to specify:

•	the generative mecanism via a function	- argument sim
•	the null hypothesis	- argument null
•	the sample size(s) for the which the power should be computed	- argument sample.size

# 6 Modifying default options

The BuyseTest.options method enable to get and set the default options of the BuyseTest function. For instance, the default option for trace is:

```
BuyseTest.options("trace")
```

# \$trace

#### [1] 2

To change the default option to 0 (i.e. no output) use:

BuyseTest.options(trace = 0)

To change what the results output by the summary function use:

```
BuyseTest.options(summary.display = list(c("endpoint","threshold","delta","Delta","
    information(%)")))
summary(BT)
```

#### Generalized pairwise comparisons with 1 endpoint

```
> statistic : net benefit (delta: endpoint specific, Delta: global)
> null hypothesis : Delta == 0
> treatment groups: C (control) vs. T (treatment)
> right-censored pairs: deterministic score or uninformative
> uninformative pairs: score equals the averaged score of all informative pairs
> results
endpoint threshold delta Delta information(%)
eventtime 1 -0.0202 -0.0202 100
```

To restore the original default options do:

BuyseTest.options(reinitialise = TRUE)

# References

- Buyse, M. (2010). Generalized pairwise comparisons of prioritized outcomes in the two-sample problem. *Statistics in medicine*, 29(30):3245–3257.
- Péron, J., Buyse, M., Ozenne, B., Roche, L., and Roy, P. (2018). An extension of generalized pairwise comparisons for prioritized outcomes in the presence of censoring. *Statistical methods in medical research*, 27(4):1230–1239.
- Verbeeck, J., Spitzer, E., de Vries, T., van Es, G., Anderson, W., Van Mieghem, N., Leon, M., Molenberghs, G., and Tijssen, J. (2019). Generalized pairwise comparison methods to analyze (non) prioritized composite endpoints. *Statistics in medicine*.