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License GPL (>= 2)

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R topics documented:

BART-package 3

abart	 	 •••	 	 	 		 •			 3
ACTG175	 	 	 	 	 		 •			 8
alligator	 	 • • •	 	 	 		 •	•		 10
arq	 	 	 	 	 		 •	•		 12
bartModelMatrix	 	 	 	 	 		 •			 13
bladder	 	 	 	 	 		 •			 14
crisk.bart	 	 	 	 	 		 •			 16
crisk.pre.bart	 	 	 	 	 		 •			 22
crisk2.bart										24
draw_lambda_i										
gbart	 	 	 	 	 					 32
gbmm	 	 	 	 	 		 •			 37
gewekediag	 	 	 	 	 		 •			 42
lbart	 	 	 	 	 					 44
leukemia	 	 	 	 	 					 50
lung	 	 	 	 	 					 52
mbart										
mbart2										
mc.cores.openmp	 	 	 	 	 					 62
mc.crisk.pwbart										
mc.crisk2.pwbart										
mc.lbart										
mc.pbart										
mc.surv.pwbart										
mc.wbart										
mc.wbart.gse										
pbart										
predict.crisk2bart										
predict.criskbart										
predict.lbart										
predict.mbart										
predict.pbart										
predict.recurbart										
predict.survbart										
predict.wbart										
pwbart										
recur.bart										
recur.pre.bart										
rs.pbart										
rtgamma										
rtnorm										
spectrum0ar										
srstepwise										
stratrs										
surv.bart										
surv.pre.bart										
transplant										
wbart										
woalt	 	 	 	 	 	 •	 •	•		 14/

BART-package

.dm20.test	. 151
.dm20.train	. 152
/dm20.train	. 154

Index

BART-package

Bayesian Additive Regression Trees

Description

Bayesian Additive Regression Trees (BART) provide flexible nonparametric modeling of covariates for continuous, binary and time-to-event outcomes. For more information on BART, see Chipman, George and McCulloch (2010) <doi:10.1214/09-AOAS285> and Sparapani, Logan, McCulloch and Laud (2016) <doi:10.1002/sim.6893>.

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abart

AFT BART for time-to-event outcomes

Description

BART is a Bayesian "sum-of-trees" model. For a numeric response y, we have $y = f(x) + \epsilon$, where $\epsilon \sim N(0, \sigma^2)$.

f is the sum of many tree models. The goal is to have very flexible inference for the uknown function f.

In the spirit of "ensemble models", each tree is constrained by a prior to be a weak learner so that it contributes a small amount to the overall fit.

156

abart

Usage

```
abart(
     x.train, times, delta,
     x.test=matrix(0,0,0), K=100,
     type='abart', ntype=1,
     sparse=FALSE, theta=0, omega=1,
     a=0.5, b=1, augment=FALSE, rho=NULL,
     xinfo=matrix(0,0,0), usequants=FALSE,
     rm.const=TRUE,
     sigest=NA, sigdf=3, sigquant=0.90,
     k=2, power=2, base=0.95,
     lambda=NA, tau.num=c(NA, 3, 6)[ntype],
     offset=NULL, w=rep(1, length(times)),
     ntree=c(200L, 50L, 50L)[ntype], numcut=100L,
     ndpost=1000L, nskip=100L,
     keepevery=c(1L, 10L, 10L)[ntype],
     printevery=100L, transposed=FALSE,
     mc.cores = 1L, ## mc.abart only
     nice = 19L, ## mc.abart only
     seed = 99L
                   ## mc.abart only
)
mc.abart(
         x.train, times, delta,
        x.test=matrix(0,0,0), K=100,
         type='abart', ntype=1,
         sparse=FALSE, theta=0, omega=1,
         a=0.5, b=1, augment=FALSE, rho=NULL,
         xinfo=matrix(0,0,0), usequants=FALSE,
         rm.const=TRUE,
         sigest=NA, sigdf=3, sigquant=0.90,
         k=2, power=2, base=0.95,
         lambda=NA, tau.num=c(NA, 3, 6)[ntype],
         offset=NULL, w=rep(1, length(times)),
         ntree=c(200L, 50L, 50L)[ntype], numcut=100L,
         ndpost=1000L, nskip=100L,
         keepevery=c(1L, 10L, 10L)[ntype],
         printevery=100L, transposed=FALSE,
         mc.cores = 2L, nice = 19L, seed = 99L
)
```

abart

Arguments

x.train	 Explanatory variables for training (in sample) data. May be a matrix or a data frame, with (as usual) rows corresponding to observations and columns to variables. If a variable is a factor in a data frame, it is replaced with dummies. Note that q dummies are created if q > 2 and one dummy created if q = 2 where q is the number of levels of the factor. abart will generate draws of f(x) for each x which is a row of x.train.
times	The time of event or right-censoring. If y.train is NULL, then times (and delta) must be provided.
delta	The event indicator: 1 is an event while 0 is censored. If y.train is NULL, then delta (and times) must be provided.
x.test	Explanatory variables for test (out of sample) data. Should have same structure as x.train. abart will generate draws of $f(x)$ for each x which is a row of x.test.
К	If provided, then coarsen times per the quantiles $1/K, 2/K,, K/K$.
type	You can use this argument to specify the type of fit. 'abart' for AFT BART.
ntype	The integer equivalent of type where 'abart' is 1.
sparse	Whether to perform variable selection based on a sparse Dirichlet prior rather than simply uniform; see Linero 2016.
theta	Set <i>theta</i> parameter; zero means random.
omega	Set <i>omega</i> parameter; zero means random.
а	Sparse parameter for $Beta(a, b)$ prior: $0.5 <= a <= 1$ where lower values inducing more sparsity.
b	Sparse parameter for $Beta(a, b)$ prior; typically, $b = 1$.
rho	Sparse parameter: typically $rho = p$ where p is the number of covariates under consideration.
augment	Whether data augmentation is to be performed in sparse variable selection.
xinfo	You can provide the cutpoints to BART or let BART choose them for you. To provide them, use the xinfo argument to specify a list (matrix) where the items (rows) are the covariates and the contents of the items (columns) are the cutpoints.
usequants	If usequants=FALSE, then the cutpoints in xinfo are generated uniformly; oth- erwise, if TRUE, uniform quantiles are used for the cutpoints.
rm.const	Whether or not to remove constant variables.
sigest	The prior for the error variance $(sigma^2)$ is inverted chi-squared (the standard conditionally conjugate prior). The prior is specified by choosing the degrees of freedom, a rough estimate of the corresponding standard deviation and a quantile to put this rough estimate at. If sigest=NA then the rough estimate will be the usual least squares estimator. Otherwise the supplied value will be used. Not used if y is binary.
sigdf	Degrees of freedom for error variance prior. Not used if y is binary.

sigquant	The quantile of the prior that the rough estimate (see sigest) is placed at. The closer the quantile is to 1, the more aggresive the fit will be as you are putting more prior weight on error standard deviations ($sigma$) less than the rough estimate. Not used if y is binary.
k	For numeric y, k is the number of prior standard deviations $E(Y x) = f(x)$ is away from +/-0.5. The response, codey.train, is internally scaled to range from -0.5 to 0.5. For binary y, k is the number of prior standard deviations $f(x)$ is away from +/-3. The bigger k is, the more conservative the fitting will be.
power	Power parameter for tree prior.
base	Base parameter for tree prior.
lambda	The scale of the prior for the variance. Not used if y is binary.
tau.num	The numerator in the tau definition, i.e., tau=tau.num/(k*sqrt(ntree)).
offset	Continuus BART operates on y.train centered by offset which defaults to mean(y.train). With binary BART, the centering is $P(Y = 1 x) = F(f(x) + offset)$ where offset defaults to F^{-1}(mean(y.train)). You can use the offset parameter to over-ride these defaults.
W	Vector of weights which multiply the standard deviation. Not used if y is binary.
ntree	The number of trees in the sum.
numcut	The number of possible values of c (see usequants). If a single number if given, this is used for all variables. Otherwise a vector with length equal to ncol(x.train) is required, where the i^{th} element gives the number of c used for the i^{th} variable in x.train. If usequants is false, numcut equally spaced cutoffs are used covering the range of values in the corresponding column of x.train. If usequants is true, then $min(numcut, thenumberofunique values in the corresponding column of 1)$ values are used.
ndpost	The number of posterior draws returned.
nskip	Number of MCMC iterations to be treated as burn in.
printevery	As the MCMC runs, a message is printed every printevery draws.
keepevery	Every keepevery draw is kept to be returned to the user.
transposed	When running abart in parallel, it is more memory-efficient to transpose x.train and x.test, if any, prior to calling mc.abart.
seed	Setting the seed required for reproducible MCMC.
mc.cores	Number of cores to employ in parallel.
nice	Set the job niceness. The default niceness is 19: niceness goes from 0 (highest) to 19 (lowest).

Details

BART is a Bayesian MCMC method. At each MCMC interation, we produce a draw from the joint posterior $(f, \sigma)|(x, y)$ in the numeric y case and just f in the binary y case.

Thus, unlike a lot of other modelling methods in R, we do not produce a single model object from which fits and summaries may be extracted. The output consists of values $f^*(x)$ (and σ^* in the numeric case) where * denotes a particular draw. The x is either a row from the training data, x.train or the test data, x.test.

abart

Value

abart returns an object of type abart which is essentially a list. In the numeric y case, the list has components:

yhat.train	A matrix with ndpost rows and nrow(x.train) columns. Each row corresponds to a draw f^* from the posterior of f and each column corresponds to a row of x.train. The (i, j) value is $f^*(x)$ for the i^{th} kept draw of f and the j^{th} row of x.train. Burn-in is dropped.
yhat.test	Same as yhat.train but now the x's are the rows of the test data.
yhat.train.mear	1
	train data fits = mean of yhat.train columns.
yhat.test.mean	test data fits = mean of yhat.test columns.
sigma	post burn in draws of sigma, length = ndpost.
first.sigma	burn-in draws of sigma.
varcount	a matrix with ndpost rows and nrow(x.train) columns. Each row is for a draw. For each variable (corresponding to the columns), the total count of the number of times that variable is used in a tree decision rule (over all trees) is given.
sigest	The rough error standard deviation (σ) used in the prior.

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References

Chipman, H., George, E., and McCulloch R. (2010) Bayesian Additive Regression Trees. *The Annals of Applied Statistics*, **4**,**1**, 266-298 <doi:10.1214/09-AOAS285>.

Chipman, H., George, E., and McCulloch R. (2006) Bayesian Ensemble Learning. Advances in Neural Information Processing Systems 19, Scholkopf, Platt and Hoffman, Eds., MIT Press, Cambridge, MA, 265-272.

Friedman, J.H. (1991) Multivariate adaptive regression splines. The Annals of Statistics, 19, 1–67.

Linero, A.R. (2018) Bayesian regression trees for high dimensional prediction and variable selection. *JASA*, **113**, 626–36.

See Also

wbart

Examples

```
set.seed(12)
x.train=matrix(runif(N*P, -2, 2), N, P)
mu = x.train[, 1]^3
y=rnorm(N, mu)
offset=mean(y)
T=exp(y)
C=rexp(N, 0.05)
delta=(T<C)*1</pre>
table(delta)/N
times=(T*delta+C*(1-delta))
##test BART with token run to ensure installation works
set.seed(99)
post1 = abart(x.train, times, delta, nskip=5, ndpost=10)
## Not run:
post1 = mc.abart(x.train, times, delta,
                 mc.cores=M, seed=99)
post2 = mc.abart(x.train, times, delta, offset=offset,
                 mc.cores=M, seed=99)
Z=8
plot(mu, post1$yhat.train.mean, asp=1,
     xlim=c(-Z, Z), ylim=c(-Z, Z))
abline(a=0, b=1)
plot(mu, post2$yhat.train.mean, asp=1,
     xlim=c(-Z, Z), ylim=c(-Z, Z))
abline(a=0, b=1)
plot(post1$yhat.train.mean, post2$yhat.train.mean, asp=1,
     xlim=c(-Z, Z), ylim=c(-Z, Z))
abline(a=0, b=1)
## End(Not run)
```

ACTG175

AIDS Clinical Trials Group Study 175

Description

ACTG 175 was a randomized clinical trial to compare monotherapy with zidovudine or didanosine with combination therapy with zidovudine and didanosine or zidovudine and zalcitabine in adults infected with the human immunodeficiency virus type I whose CD4 T cell counts were between 200 and 500 per cubic millimeter.

8

ACTG175

Usage

data(ACTG175)

Format

A data frame with 2139 observations on the following 27 variables:

pidnum patient's ID number age age in years at baseline wtkg weight in kg at baseline hemo hemophilia (0=no, 1=yes) homo homosexual activity (0=no, 1=yes) drugs history of intravenous drug use (0=no, 1=yes) karnof Karnofsky score (on a scale of 0-100) oprior non-zidovudine antiretroviral therapy prior to initiation of study treatment (0=no, 1=yes) z30 zidovudine use in the 30 days prior to treatment initiation (0=no, 1=yes) zprior zidovudine use prior to treatment initiation (0=no, 1=yes) preanti number of days of previously received antiretroviral therapy race race (0=white, 1=non-white) gender gender (0=female, 1=male) str2 antiretroviral history (0=naive, 1=experienced) strat antiretroviral history stratification (1='antiretroviral naive', 2='> 1 but \leq 52 weeks of prior antiretroviral therapy', 3='> 52 weeks') symptom symptomatic indicator (0=asymptomatic, 1=symptomatic) treat treatment indicator (0=zidovudine only, 1=other therapies) offtrt indicator of off-treatment before 96 ± 5 weeks (0=no,1=yes) cd40 CD4 T cell count at baseline cd420 CD4 T cell count at 20+5 weeks cd496 CD4 T cell count at 96 \pm 5 weeks (=NA if missing) r missing CD4 T cell count at 96±5 weeks (0=missing, 1=observed) cd80 CD8 T cell count at baseline cd820 CD8 T cell count at 20 ± 5 weeks cens indicator of observing the event in days days number of days until the first occurrence of: (i) a decline in CD4 T cell count of at least 50 (ii) an event indicating progression to AIDS, or (iii) death.

arms treatment arm (0=zidovudine, 1=zidovudine and didanosine, 2=zidovudine and zalcitabine, 3=didanosine).

Details

The variable days contains right-censored time-to-event observations. The data set includes the following post-randomization covariates: CD4 and CD8 T cell count at 20 ± 5 weeks and the indicator of whether or not the patient was taken off-treatment before 96 ± 5 weeks.

References

Hammer SM, et al. (1996), "A trial comparing nucleoside monotherapy with combination therapy in HIV-infected adults with CD4 cell counts from 200 to 500 per cubic millimeter.", *New England Journal of Medicine*, 335:1081–1090.

alligator

American alligator Food Choice

Description

In 1985, American alligators were harvested by hunters from August 26 to September 30 in peninsular Florida from lakes Oklawaha (Putnam County), George (Putnam and Volusia counties), Hancock (Polk County) and Trafford (Collier County). Lake, length and sex were recorded for each alligator. Stomachs from a sample of alligators 1.09-3.89m long were frozen prior to analysis. After thawing, stomach contents were removed and separated and food items were identified and tallied. Volumes were determined by water displacement. The stomach contents of 219 alligators were classified into five categories of primary food choice: Fish (the most common primary food choice), Invertebrate (snails, insects, crayfish, etc.), Reptile (turtles, alligators), Bird, and Other (amphibians, plants, household pets, stones, and other debris).

Usage

data(alligator)

Format

A data frame with 80 observations on the following 5 variables.

lake a factor with levels George Hancock Oklawaha Trafford

sex a factor with levels female male

size alligator size, a factor with levels large (>2.3m) small (<=2.3m)

food primary food choice, a factor with levels bird fish invert other reptile

count cell frequency, a numeric vector

Details

The table contains a fair number of 0 counts. food is the response variable. fish is the most frequent choice, and often taken as a baseline category in multinomial response models.

Source

Agresti, A. (2002). Categorical Data Analysis, New York: Wiley, 2nd Ed., Table 7.1

References

Delany MF, Linda SB, Moore CT (1999). "Diet and condition of American alligators in 4 Florida lakes." In *Proceedings of the Annual Conference of the Southeastern Association of Fish and Wildlife Agencies*, **53**, 375–389.

alligator

Examples

```
data(alligator)
## nnet::multinom Multinomial logit model fit with neural nets
fit <- multinom(food ~ lake+size+sex, data=alligator, weights=count)</pre>
summary(fit$fitted.values)
## 1=bird, 2=fish, 3=invert, 4=other, 5=reptile
(L=length(alligator$count))
(N=sum(alligator$count))
y.train=integer(N)
x.train=matrix(nrow=N, ncol=3)
x.test=matrix(nrow=L, ncol=3)
k=1
for(i in 1:L) {
    x.test[i, ]=as.integer(
        c(alligator$lake[i], alligator$size[i], alligator$sex[i]))
    if(alligator$count[i]>0)
        for(j in 1:alligator$count[i]) {
            y.train[k]=as.integer(alligator$food[i])
            x.train[k, ]=as.integer(
                c(alligator$lake[i], alligator$size[i], alligator$sex[i]))
            k=k+1
        }
}
table(y.train)
##test mbart with token run to ensure installation works
set.seed(99)
check = mbart(x.train, y.train, nskip=1, ndpost=1)
## Not run:
set.seed(99)
check = mbart(x.train, y.train, nskip=1, ndpost=1)
post=mbart(x.train, y.train, x.test)
##post=mc.mbart(x.train, y.train, x.test, mc.cores=8, seed=99)
##check=predict(post, x.test, mc.cores=8)
##print(cor(post$prob.test.mean, check$prob.test.mean)^2)
par(mfrow=c(3, 2))
K=5
for(j in 1:5) {
   h=seq(j, L*K, K)
    print(cor(fit$fitted.values[ , j], post$prob.test.mean[h])^2)
    plot(fit$fitted.values[ , j], post$prob.test.mean[h],
         xlim=0:1, ylim=0:1,
         xlab=paste0('NN: Est. Prob. j=', j),
         ylab=paste0('BART: Est. Prob. j=', j))
    abline(a=0, b=1)
}
```

arq

12

```
par(mfrow=c(1, 1))
L=16
x.test=matrix(nrow=L, ncol=3)
k=1
for(size in 1:2)
    for(sex in 1:2)
        for(lake in 1:4) {
            x.test[k, ]=c(lake, size, sex)
            k=k+1
        }
x.test
## two sizes: 1=large: >2.3m, 2=small: <=2.3m</pre>
pred=predict(post, x.test)
##pred=predict(post, x.test, mc.cores=8)
ndpost=nrow(pred$prob.test)
size.test=matrix(nrow=ndpost, ncol=K*2)
for(i in 1:K) {
    j=seq(i, L*K/2, K) ## large
    size.test[ , i]=apply(pred$prob.test[ , j], 1, mean)
    j=j+L*K/2 ## small
    size.test[ , i+K]=apply(pred$prob.test[ , j], 1, mean)
}
size.test.mean=apply(size.test, 2, mean)
size.test.025=apply(size.test, 2, quantile, probs=0.025)
size.test.975=apply(size.test, 2, quantile, probs=0.975)
plot(factor(1:K, labels=c('bird', 'fish', 'invert', 'other', 'reptile')),
     rep(1, K), col=1:K, type='n', lwd=1, lty=0,
             xlim=c(1, K), ylim=c(0, 0.5), ylab='Prob.',
     sub="Multinomial BART\nFriedman's partial dependence function")
points(1:K, size.test.mean[1:K+K], col=1)
lines(1:K, size.test.025[1:K+K], col=1, lty=2)
lines(1:K, size.test.975[1:K+K], col=1, lty=2)
points(1:K, size.test.mean[1:K], col=2)
lines(1:K, size.test.025[1:K], col=2, lty=2)
lines(1:K, size.test.975[1:K], col=2, lty=2)
## legend('topright', legend=c('Small', 'Large'),
##
          pch=1, col=1:2)
```

End(Not run)

NHANES 2009-2010 Arthritis Questionnaire

arq

bartModelMatrix

Description

This data set was created from the National Health and Nutrition Examination Survey (NHANES) 2009-2010 Arthritis Questionnaire.

Usage

data(arq)

Details

We have two outcomes of interest. Chronic neck pain: Yes arq010a=1 vs. No arq010a=0. Chronic lower-back/buttock pain: Yes arq010de=1 vs. No arq010de=0. seqn is a unique survey respondent identifier. wtint2yr is the survey sampling weight. riagendr is gender: 1 for males, 2 for females. ridageyr is age in years. There are several anthropometric measurements: bmxwt, weight in kg; bmxht, height in cm; bmxbmi, body mass index in kg/m²; and bmxwaist, waist circumference in cm. The data was subsetted to ensure non-missing values of these variables.

References

National Health and Nutrition Examination Survey (NHANES) 2009-2010 Arthritis Questionnaire. https://wwwn.cdc.gov/nchs/nhanes/2009-2010/ARQ_F.htm

bartModelMatrix Create a matrix out of a vector or data.frame

Description

The external BART functions operate on matrices in memory. Therefore, if the user submits a vector or data.frame, then this function converts it to a matrix. Also, it determines the number of cutpoints necessary for each column when asked to do so.

Usage

Arguments

Х	A vector or data.frame to create the matrix from.
numcut	The maximum number of cutpoints to consider. If numcut=0, then just return a matrix; otherwise, return a list containing a matrix X, a vector numcut and a list xinfo.
usequants	If usequants is FALSE, then the cutpoints in xinfo are generated uniformly; otherwise, if TRUE, then quantiles are used for the cutpoints.
type	Determines which quantile algorithm is employed.
rm.const	Whether or not to remove constant variables.

cont	Whether or not to assume all variables are continuous.
xinfo	You can provide the cutpoints to BART or let BART choose them for you. To provide them, use the xinfo argument to specify a list (matrix) where the items (rows) are the covariates and the contents of the items (columns) are the cutpoints.

See Also

class.ind

Examples

```
set.seed(99)
a <- rbinom(10, 4, 0.4)
table(a)
x <- runif(10)
df <- data.frame(a=factor(a), x=x)
b <- bartModelMatrix(df)
b
b <- bartModelMatrix(df, numcut=9)
b
b <- bartModelMatrix(df, numcut=9, usequants=TRUE)
b
## Not run:
    f <- bartModelMatrix(as.character(a))
## End(Not run)</pre>
```

bladder

Bladder Cancer Recurrences

Description

This interesting example is from a clinical trial conducted by the Veterans Administration Cooperative Urological Research Group. This data on recurrence of bladder cancer has been used by many to demonstrate methodology for recurrent events modelling. In this study, all patients had superficial bladder tumors when they entered the trial. These tumors were removed transurethrally

bladder

and patients were randomly assigned to one of three treatments: placebo, thiotepa or pyridoxine (vitamin B6). Many patients had multiple recurrences of tumors during the study and new tumors were removed at each visit. For each patient, their recurrence time, if any, was measured from the beginning of treatment.

bladder is the data set that appears most commonly in the literature. It uses only the 85 subjects with nonzero follow-up who were assigned to either thiotepa or placebo and only the first four recurrences for any patient. The status variable is 1 for recurrence and 0 for everything else (including death for any reason). The data set is laid out in the competing risks format of the paper by Wei, Lin, and Weissfeld (WLW).

bladder1 is the full data set from the study. It contains all three treatment arms and all recurrences for 118 subjects; the maximum observed number of recurrences is 9.

bladder2 uses the same subset of subjects as bladder, but formated in the (start, stop] or Anderson-Gill (AG) style. Note that in transforming from the WLW to the AG style data set there is a quite common programming mistake that leads to extra follow-up time for 12 subjects: all those with follow-up beyond their fourth recurrence. Over this extended time these subjects are by definition not at risk for another event in the WLW data set.

Format

bladder

id:	Patient id
rx:	Treatment 1=placebo 2=thiotepa
number:	Initial number of tumours (8=8 or more)
size:	size (cm) of largest initial tumour
stop:	recurrence or censoring time
enum:	which recurrence (up to 4)

bladder1

id:	Patient id
treatment:	Placebo, pyridoxine (vitamin B6), or thiotepa
number:	Initial number of tumours (8=8 or more)
size:	Size (cm) of largest initial tumour
recur:	Number of recurrences
start,stop:	The start and end time of each time interval
status:	End of interval code, 0=censored, 1=recurrence,
	2=death from bladder disease, 3=death other/unknown cause
rtumor:	Number of tumors found at the time of a recurrence
rsize:	Size of largest tumor at a recurrence
enum:	Event number (observation number within patient)

bladder2

id:	Patient id
rx:	Treatment 1=placebo 2=thiotepa

number:	Initial number of tumours (8=8 or more)
size:	size (cm) of largest initial tumour
start:	start of interval (0 or previous recurrence time)
stop:	recurrence or censoring time
enum:	which recurrence (up to 4)

References

Byar, DP (1980), "The Veterans Administration Study of Chemoprophylaxis for Recurrent Stage I Bladder Tumors: Comparisons of Placebo, Pyridoxine, and Topical Thiotepa," in *Bladder Tumors and Other Topics in Urological Oncology*, eds. M Pavone-Macaluso, PH Smith, and F Edsmyn, New York: Plenum, pp. 363-370.

Andrews DF, Hertzberg AM (1985), DATA: A Collection of Problems from Many Fields for the Student and Research Worker, New York: Springer-Verlag.

LJ Wei, DY Lin, L Weissfeld (1989), Regression analysis of multivariate incomplete failure time data by modeling marginal distributions. *Journal of the American Statistical Association*, **84**.

Examples

data(bladder)

crisk.bart

BART for competing risks

Description

Here we have implemented a simple and direct approach to utilize BART for competing risks that is very flexible, and is akin to discrete-time survival analysis. Following the capabilities of BART, we allow for maximum flexibility in modeling the dependence of competing failure times on covariates. In particular, we do not impose proportional hazards.

To elaborate, consider data in the form: (s_i, δ_i, x_i) where s_i is the event time; δ_i is an indicator distinguishing events, $\delta_i = h$ due to cause hin1, 2, from right-censoring, $\delta_i = 0$; x_i is a vector of covariates; and i = 1, ..., N indexes subjects.

We denote the K distinct event/censoring times by $0 < t_{(1)} < ... < t_{(K)} < \infty$ thus taking $t_{(j)}$ to be the j^{th} order statistic among distinct observation times and, for convenience, $t_{(0)} = 0$. Now consider event indicators for cause h: y_{hij} for each subject i at each distinct time $t_{(j)}$ up to and including the subject's last observation time $s_i = t_{(n_i)}$ with $n_i = \arg \max_j [t_{(j)} \le s_i]$ for cause 1, but only up to $n_i - y_{1ij}$ for cause 2.

We then denote by p_{hij} the probability of an event at time $t_{(j)}$ conditional on no previous event. We now write the model for y_{hij} as a nonparametric probit (or logistic) regression of y_{hij} on the time $t_{(j)}$ and the covariates x_{hi} , and then utilize BART for binary responses. Specifically, $y_{hij} = I[\delta_i =$ $h]I[s_i = t_{(j)}], j = 1, ..., n_i - I[h = 2]y_{1ij}$. Therefore, we have $p_{hij} = F(mu_{hij}), mu_{hij} =$ $mu_h + f_h(t_{(j)}, x_{hi})$ where F denotes the Normal (or Logistic) cdf. As in the binary response case, f_h is the sum of many tree models. Finally, based on these probabilities, p_{hij} , we can construct targets of inference such as the cumulative incidence functions.

crisk.bart

Usage

```
crisk.bart(x.train=matrix(0,0,0), y.train=NULL,
           x.train2=x.train, y.train2=NULL,
           times=NULL, delta=NULL, K=NULL,
           x.test=matrix(0,0,0), x.test2=x.test, cond=NULL,
           sparse=FALSE, theta=0, omega=1,
           a=0.5, b=1, augment=FALSE,
           rho=NULL, rho2=NULL,
           xinfo=matrix(0,0,0), xinfo2=matrix(0,0,0),
           usequants=FALSE,
           rm.const=TRUE, type='pbart',
           ntype=as.integer(
               factor(type, levels=c('wbart', 'pbart', 'lbart'))),
           k=2, power=2, base=0.95,
           offset=NULL, offset2=NULL,
           tau.num=c(NA, 3, 6)[ntype],
           ntree=50, numcut=100, ndpost=1000, nskip=250,
           keepevery = 10L,
           printevery=100L,
           id=NULL.
                       ## crisk.bart only
           seed=99,
                     ## mc.crisk.bart only
           mc.cores=2, ## mc.crisk.bart only
           nice=19L ## mc.crisk.bart only
          )
mc.crisk.bart(x.train=matrix(0,0,0), y.train=NULL,
              x.train2=x.train, y.train2=NULL,
              times=NULL, delta=NULL, K=NULL,
              x.test=matrix(0,0,0), x.test2=x.test, cond=NULL,
              sparse=FALSE, theta=0, omega=1,
              a=0.5, b=1, augment=FALSE,
              rho=NULL, rho2=NULL,
              xinfo=matrix(0,0,0), xinfo2=matrix(0,0,0),
              usequants=FALSE,
              rm.const=TRUE, type='pbart',
              ntype=as.integer(
                  factor(type, levels=c('wbart', 'pbart', 'lbart'))),
              k=2, power=2, base=0.95,
              offset=NULL, offset2=NULL,
              tau.num=c(NA, 3, 6)[ntype],
              ntree=50, numcut=100, ndpost=1000, nskip=250,
```

```
keepevery = 10L,
```

printevery=100L,

```
id=NULL, ## crisk.bart only
seed=99, ## mc.crisk.bart only
mc.cores=2, ## mc.crisk.bart only
nice=19L ## mc.crisk.bart only
)
```

Arguments

x.train	Covariates for training (in sample) data of cause 1. Must be a data.frame or a matrix with rows corresponding to observations and columns to variables. crisk.bart will generate draws of $f_1(t, x)$ for each x which is a row of x.train (note that the definition of x.train is dependent on whether y.train has been specified; see below).
y.train	Cause 1 binary response for training (in sample) data. If y.train is NULL, then y.train (x.train and x.test, if specified) are gen- erated by a call to crisk.pre.bart (which require that times and delta be provided: see below); otherwise, y.train (x.train and x.test, if specified) are utilized as given assuming that the data construction has already been per- formed.
x.train2	Covariates for training (in sample) data of cause 2. Similar to x.train above.
y.train2	Cause 2 binary response for training (in sample) data, i.e., failure from any cause besides the cause of interest which is cause 1. Similar to y.train above.
times	The time of event or right-censoring, s_i . If y.train is NULL, then times (and delta) must be provided.
delta	The event indicator: 1 for cause 1, 2 for cause 2 and 0 is censored. If y.train is NULL, then delta (and times) must be provided.
К	If provided, then coarsen times per the quantiles $1/K, 2/K,, K/K$.
x.test	Covariates for test (out of sample) data of cause 1. Must be a data.frame or a matrix and have the same structure as x.train. crisk.bart will generate draws of $f_1(t, x)$ for each x which is a row of x.test.
x.test2	Covariates for test (out of sample) data of cause 2. Similar to x.test above.
cond	A vector of indices for y.train2 indicating subjects who did not suffer a cause 1 event and, therefore, are eligible for cause 2.
sparse	Whether to perform variable selection based on a sparse Dirichlet prior; see Linero 2016.
theta	Set <i>theta</i> parameter; zero means random.
omega	Set omega parameter; zero means random.

inducing more sparsity.bSparse parameter for $Beta(a, b)$ pior; typically, b=1.rhoSparse parameter: typically rho2=p where p is the number of covariates in x.train.rho2Sparse parameter: typically rho2=p where p is the number of covariates in x.train2.augmentWhether data augmentation is to be performed in sparse variable selection.xinfoYou can provide the cutpoints to BART or let BART choose them for you. To provide them, use the xinfo argument to specify a list (matrix) where the items (rows) are the covariates and the contents of the items (columns) are the cutpoints.xinfo2Cause 2 cutpoints.usequantsIf usequants=FALSE, then the cutpoints in xinfo are generated uniformly; otherwise.rm.constWhether or not to remove constant variables.typeWhether to employ probit BART via Albert-Chib, 'pbart', or logistic BART by Holmes-Held, 'lbart'.ntypeThe integer equivalent of type where 'wbart' is 1, 'pbart' is 2 and 'lbart' is 3.kk is the number of prior standard deviations $f_h(t, x)$ is away from +/-3. The bigger k is, the more conservative the fitting will be.powerPower parameter for tree prior.offset2Cause 1 binary offset.tau.numThe number of possible values of cutpoints (see usequants). If a single number of rolos in the sum.numcutThe number of tree sin de sum.numcutThe number of the iter variable in x.train. If usequants is FALSE, numcut equally spaced cutoffs are used covering the range of values in the corresponding columns of x.train -1) cutpoint values are used.ndpostThe number of MCMC iterations to be treated as burn in.keepever	а	Sparse parameter for $Beta(a, b)$ prior: $0.5 <= a <= 1$ where lower values
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ntreeThe number of trees in the sum.numcutThe number of possible values of cutpoints (see usequants). If a single number if given, this is used for all variables. Otherwise a vector with length equal to ncol(x.train) is required, where the i th element gives the number of cutpoints used for the i th variable in x.train. If usequants is FALSE, numcut equally spaced cutoffs are used covering the range of values in the corresponding column of x.train. If usequants is TRUE, then min(numcut, the number of unique values in the corresponding columns of x.train -1) cutpoint values are used.ndpostThe number of posterior draws returned.nskipNumber of MCMC iterations to be treated as burn in.keepeveryEvery keepevery draw is kept to be returned to the user.printeveryAs the MCMC runs, a message is printed every printevery draws.idcrisk.bart only: seed required for reproducible MCMC.mc.coresmc.crisk.bart only: seet required for reproducible MCMC.mc.crisk.bart only: set the job niceness. The default niceness is 19: niceness	offset2	Cause 2 binary offset.
numcutThe number of possible values of cutpoints (see usequants). If a single number if given, this is used for all variables. Otherwise a vector with length equal to ncol(x.train) is required, where the i^{th} element gives the number of cutpoints used for the i^{th} variable in x.train. If usequants is FALSE, numcut equally spaced cutoffs are used covering the range of values in the corresponding column of x.train. If usequants is TRUE, then min(numcut, the number of unique values in the corresponding columns of x.train -1) cutpoint values are used.ndpostThe number of posterior draws returned.nskipNumber of MCMC iterations to be treated as burn in.keepeveryEvery keepevery draw is kept to be returned to the user.printeveryAs the MCMC runs, a message is printed every printevery draws.idcrisk.bart only: unique identifier added to returned list.seedmc.crisk.bart only: seed required for reproducible MCMC.mc.coresmc.crisk.bart only: set the job niceness. The default niceness is 19: niceness	tau.num	The numerator in the tau definition.
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nskipNumber of MCMC iterations to be treated as burn in.keepeveryEvery keepevery draw is kept to be returned to the user.printeveryAs the MCMC runs, a message is printed every printevery draws.idcrisk.bart only: unique identifier added to returned list.seedmc.crisk.bart only: seed required for reproducible MCMC.mc.coresmc.crisk.bart only: number of cores to employ in parallel.nicemc.crisk.bart only: set the job niceness. The default niceness is 19: niceness	numcut	ber if given, this is used for all variables. Otherwise a vector with length equal to $ncol(x.train)$ is required, where the i^{th} element gives the number of cutpoints used for the i^{th} variable in x.train. If usequants is FALSE, numcut equally spaced cutoffs are used covering the range of values in the corresponding column of x.train. If usequants is TRUE, then min(numcut, the number of unique values in the corresponding columns of x.train -1) cutpoint values.
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printeveryAs the MCMC runs, a message is printed every printevery draws.idcrisk.bart only: unique identifier added to returned list.seedmc.crisk.bart only: seed required for reproducible MCMC.mc.coresmc.crisk.bart only: number of cores to employ in parallel.nicemc.crisk.bart only: set the job niceness. The default niceness is 19: niceness	nskip	Number of MCMC iterations to be treated as burn in.
idcrisk.bart only: unique identifier added to returned list.seedmc.crisk.bart only: seed required for reproducible MCMC.mc.coresmc.crisk.bart only: number of cores to employ in parallel.nicemc.crisk.bart only: set the job niceness. The default niceness is 19: niceness	keepevery	Every keepevery draw is kept to be returned to the user.
seedmc.crisk.bart only: seed required for reproducible MCMC.mc.coresmc.crisk.bart only: number of cores to employ in parallel.nicemc.crisk.bart only: set the job niceness. The default niceness is 19: niceness	printevery	As the MCMC runs, a message is printed every printevery draws.
mc.coresmc.crisk.bart only: number of cores to employ in parallel.nicemc.crisk.bart only: set the job niceness. The default niceness is 19: niceness	id	crisk.bart only: unique identifier added to returned list.
nice mc.crisk.bart only: set the job niceness. The default niceness is 19: niceness	seed	mc.crisk.bart only: seed required for reproducible MCMC.
	mc.cores	mc.crisk.bart only: number of cores to employ in parallel.
	nice	

crisk.bart returns an object of type criskbart which is essentially a list. Besides the items listed below, the list has offset, offset2, times which are the unique times, K which is the number of unique times, tx.train and tx.test, if any.

yhat.train	A matrix with ndpost rows and nrow(x.train) columns. Each row corresponds to a draw f_1^* from the posterior of f_1 and each column corresponds to a row of x.train. The (i, j) value is $f_1^*(t, x)$ for the i^{th} kept draw of f_1 and the j^{th} row of x.train. Burn-in is dropped.	
yhat.test	Same as yhat.train but now the x's are the rows of the test data.	
surv.test	test data fits for the survival function, $S(t, x)$.	
surv.test.mean	mean of surv.test over the posterior samples.	
prob.test	The probability of suffering cause 1.	
prob.test2	The probability of suffering cause 2.	
cif.test	The cumulative incidence function of cause 1, $F_1(t, x)$.	
cif.test2	The cumulative incidence function of cause 2, $F_2(t, x)$.	
cif.test.mean	mean of cif.test columns for cause 1.	
cif.test2.mean	mean of cif.test2 columns for cause 2.	
varcount	a matrix with ndpost rows and nrow(x.train) columns. Each row is for a draw. For each variable (corresponding to the columns), the total count of the number of times this variable is used for cause 1 in a tree decision rule (over all trees) is given.	
varcount2	For each variable the total count of the number of times this variable is used for cause 2 in a tree decision rule is given.	

Author(s)

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References

Chipman, H., George, E., and McCulloch R. (2010) Bayesian Additive Regression Trees. *The Annals of Applied Statistics*, **4**,**1**, 266-298 <doi: 10.1214/09-AOAS285>.

Friedman, J.H. (1991) Multivariate adaptive regression splines. The Annals of Statistics, 19, 1-67.

Gramacy, RB and Polson, NG (2012) Simulation-based regularized logistic regression. *Bayesian Analysis*, **7**, 567–590.

Holmes, C and Held, L (2006) Bayesian auxiliary variable models for binary and multinomial regression. *Bayesian Analysis*, **1**, 145–68.

Linero, A.R. (2018) Bayesian regression trees for high dimensional prediction and variable selection. *JASA*, **113**, 626–36.

Sparapani, Logan, McCulloch, Laud (2018) Nonparametric competing risks analysis using Bayesian Additive Regression Trees (BART). arXiv preprint arXiv:1806.11237

crisk.bart

See Also

crisk.pre.bart, predict.criskbart, mc.crisk.pwbart, crisk2.bart

Examples

```
data(transplant)
pfit <- survfit(Surv(futime, event) ~ abo, transplant)</pre>
# competing risks for type 0
plot(pfit[4,], xscale=7, xmax=735, col=1:3, lwd=2, ylim=c(0, 1),
       xlab='t (weeks)', ylab='Aalen-Johansen (AJ) CI(t)')
    legend(450, .4, c("Death", "Transplant", "Withdrawal"), col=1:3, lwd=2)
## plot(pfit[4,], xscale=30.5, xmax=735, col=1:3, lwd=2, ylim=c(0, 1),
##
          xlab='t (months)', ylab='Aalen-Johansen (AJ) CI(t)')
       legend(450, .4, c("Death", "Transplant", "Withdrawal"), col=1:3, lwd=2)
##
delta <- (as.numeric(transplant$event)-1)</pre>
## recode so that delta=1 is cause of interest; delta=2 otherwise
delta[delta==1] <- 4</pre>
delta[delta==2] <- 1</pre>
delta[delta>1] <- 2</pre>
table(delta, transplant$event)
times <- pmax(1, ceiling(transplant$futime/7)) ## weeks</pre>
##times <- pmax(1, ceiling(transplant$futime/30.5)) ## months</pre>
table(times)
type0 <- 1*(transplant$abo=='0')</pre>
typeA <- 1*(transplant$abo=='A')</pre>
typeB <- 1*(transplant$abo=='B')</pre>
typeAB <- 1*(transplant$abo=='AB')</pre>
table(typeA, type0)
x.train <- cbind(type0, typeA, typeB, typeAB)</pre>
x.test <- cbind(1, 0, 0, 0)
dimnames(x.test)[[2]] <- dimnames(x.train)[[2]]</pre>
##test BART with token run to ensure installation works
set.seed(99)
post <- crisk.bart(x.train=x.train, times=times, delta=delta,</pre>
                    x.test=x.test, nskip=1, ndpost=1, keepevery=1)
## Not run:
## run one long MCMC chain in one process
## set.seed(99)
## post <- crisk.bart(x.train=x.train, times=times, delta=delta, x.test=x.test)</pre>
## in the interest of time, consider speeding it up by parallel processing
```

```
## run "mc.cores" number of shorter MCMC chains in parallel processes
post <- mc.crisk.bart(x.train=x.train, times=times, delta=delta,</pre>
                      x.test=x.test, seed=99, mc.cores=8)
K <- post$K
typeO.cif.mean <- apply(post$cif.test, 2, mean)</pre>
type0.cif.025 <- apply(post$cif.test, 2, quantile, probs=0.025)</pre>
type0.cif.975 <- apply(post$cif.test, 2, quantile, probs=0.975)</pre>
plot(pfit[4,], xscale=7, xmax=735, col=1:3, lwd=2, ylim=c(0, 0.8),
       xlab='t (weeks)', ylab='CI(t)')
points(c(0, post$times)*7, c(0, type0.cif.mean), col=4, type='s', lwd=2)
points(c(0, post$times)*7, c(0, type0.cif.025), col=4, type='s', lwd=2, lty=2)
points(c(0, post$times)*7, c(0, type0.cif.975), col=4, type='s', lwd=2, lty=2)
     legend(450, .4, c("Transplant(BART)", "Transplant(AJ)",
                        "Death(AJ)", "Withdrawal(AJ)"),
            col=c(4, 2, 1, 3), lwd=2)
##dev.copy2pdf(file='../vignettes/figures/liver-BART.pdf')
## plot(pfit[4,], xscale=30.5, xmax=735, col=1:3, lwd=2, ylim=c(0, 0.8),
##
          xlab='t (months)', ylab='CI(t)')
## points(c(0, post$times)*30.5, c(0, type0.cif.mean), col=4, type='s', lwd=2)
## points(c(0, post$times)*30.5, c(0, type0.cif.025), col=4, type='s', lwd=2, lty=2)
## points(c(0, post$times)*30.5, c(0, type0.cif.975), col=4, type='s', lwd=2, lty=2)
        legend(450, .4, c("Transplant(BART)", "Transplant(AJ)",
##
                          "Death(AJ)", "Withdrawal(AJ)"),
##
               col=c(4, 2, 1, 3), lwd=2)
##
```

End(Not run)

crisk.pre.bart Data construction for competing risks with BART

Description

Competing risks contained in (t, δ, x) must be translated to data suitable for the BART competing risks model; see crisk.bart for more details.

Usage

Arguments

times	The time of event or right-censoring.
delta	The event indicator: 1 is a cause 1 event, 2 a cause 2 while 0 is censored.

x.train	Explanatory variables for training (in sample) data of cause 1. If provided, must be a matrix with (as usual) rows corresponding to observations and columns to variables.
x.test	Explanatory variables for test (out of sample) data of cause 1. If provided, must be a matrix and have the same structure as x.train.
x.train2	Explanatory variables for training (in sample) data of cause 2. If provided, must be a matrix with (as usual) rows corresponding to observations and columns to variables.
x.test2	Explanatory variables for test (out of sample) data of cause 2. If provided, must be a matrix and have the same structure as x.train.
К	If provided, then coarsen times per the quantiles $1/K, 2/K,, K/K$.

Value

surv.pre.bart returns a list. Besides the items listed below, the list has a times component giving the unique times and K which is the number of unique times.

y.train	A vector of binary responses for cause 1.
y.train2	A vector of binary responses for cause 2.
cond	A vector of indices of y.train indicating censored subjects.
binaryOffset	The binary offset for y.train.
binaryOffset2	The binary offset for y.train2.
tx.train	A matrix with rows consisting of time and the covariates of the training data for cause 1.
tx.train2	A matrix with rows consisting of time and the covariates of the training data for cause 2.
tx.test	A matrix with rows consisting of time and the covariates of the test data, if any, for cause 1.
tx.test2	A matrix with rows consisting of time and the covariates of the test data, if any, for cause 2.

Author(s)

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References

Sparapani, R., Logan, B., McCulloch, R., and Laud, P. (2016) Nonparametric survival analysis using Bayesian Additive Regression Trees (BART). *Statistics in Medicine*, **16:2741-53** <doi:10.1002/sim.6893>.

See Also

crisk.bart

Examples

```
data(transplant)
delta <- (as.numeric(transplant$event)-1)</pre>
delta[delta==1] <- 4
delta[delta==2] <- 1</pre>
delta[delta>1] <- 2</pre>
table(delta, transplant$event)
table(1+floor(transplant$futime/30.5)) ## months
times <- 1+floor(transplant$futime/30.5)</pre>
type0 <- 1*(transplant$abo=='0')</pre>
typeA <- 1*(transplant$abo=='A')</pre>
typeB <- 1*(transplant$abo=='B')</pre>
typeAB <- 1*(transplant$abo=='AB')</pre>
table(typeA, type0)
x.train <- cbind(type0, typeA, typeB, typeAB)</pre>
N <- nrow(x.train)</pre>
x.test <- x.train</pre>
x.test[1:N, 1:4] <- matrix(c(1, 0, 0, 0), nrow=N, ncol=4, byrow=TRUE)</pre>
pre <- crisk.pre.bart(x.train=x.train, times=times, delta=delta, x.test=x.test)</pre>
```

crisk2.bart BART for competing risks

Description

Here we have implemented another approach to utilize BART for competing risks that is very flexible, and is akin to discrete-time survival analysis. Following the capabilities of BART, we allow for maximum flexibility in modeling the dependence of competing failure times on covariates. In particular, we do not impose proportional hazards.

Similar to crisk.bart, we utilize two BART models, yet they are two different BART models than previously considered. First, given an event of either cause occurred, we employ a typical binary BART model to discriminate between cause 1 and 2. Next, we proceed as if it were a typical survival analysis with BART for an absorbing event from either cause.

To elaborate, consider data in the form: (s_i, δ_i, x_i) where s_i is the event time; δ_i is an indicator distinguishing events, $\delta_i = h$ due to cause hin1, 2, from right-censoring, $\delta_i = 0$; x_i is a vector of covariates; and i = 1, ..., N indexes subjects. We denote the K distinct event/censoring times by

24

crisk2.bart

 $0 < t_{(1)} < ... < t_{(K)} < \infty$ thus taking $t_{(j)}$ to be the j^{th} order statistic among distinct observation times and, for convenience, $t_{(0)} = 0$.

First, consider event indicators for an event from either cause: y_{1ij} for each subject i at each distinct time $t_{(j)}$ up to and including the subject's last observation time $s_i = t_{(n_i)}$ with $n_i = \arg \max_j [t_{(j)} \leq s_i]$. We denote by p_{1ij} the probability of an event at time $t_{(j)}$ conditional on no previous event. We now write the model for y_{1ij} as a nonparametric probit (or logistic) regression of y_{1ij} on the time $t_{(j)}$ and the covariates x_{1i} , and then utilize BART for binary responses. Specifically, $y_{1ij} = I[\delta_i > 0]I[s_i = t_{(j)}], j = 1, ..., n_i$. Therefore, we have $p_{1ij} = F(mu_{1ij}), mu_{1ij} = mu_1 + f_1(t_{(j)}, x_{1i})$ where F denotes the Normal (or Logistic) cdf.

Next, we denote by p_{2i} the probability of a cause 1 event at time s_i conditional on an event having occurred. We now write the model for y_{2i} as a nonparametric probit (or logistic) regression of y_{2i} on the time s_i and the covariates x_{2i} , via BART for binary responses. Specifically, $y_{2i} = I[\delta_i = 1]$. Therefore, we have $p_{2i} = F(mu_{2i})$, $mu_{2i} = mu_2 + f_2(s_i, x_{2i})$ where F denotes the Normal (or Logistic) cdf. Although, we modeled p_{2i} at the time of an event, s_i , we can estimate this probability at any other time points on the grid via $p(t_{(j)}, x_2) = F(mu_2 + f_2(t_{(j)}, x_2))$. Finally, based on these probabilities, p_{hij} , we can construct targets of inference such as the cumulative incidence functions.

Usage

```
crisk2.bart(x.train=matrix(0,0,0), y.train=NULL,
           x.train2=x.train, y.train2=NULL,
           times=NULL, delta=NULL, K=NULL,
           x.test=matrix(0,0,0), x.test2=x.test,
           sparse=FALSE, theta=0, omega=1,
           a=0.5, b=1, augment=FALSE,
           rho=NULL, rho2=NULL,
           xinfo=matrix(0,0,0), xinfo2=matrix(0,0,0),
           usequants=FALSE,
           rm.const=TRUE, type='pbart',
           ntype=as.integer(
               factor(type, levels=c('wbart', 'pbart', 'lbart'))),
           k=2, power=2, base=0.95,
           offset=NULL, offset2=NULL,
           tau.num=c(NA, 3, 6)[ntype],
           ntree=50, numcut=100, ndpost=1000, nskip=250,
           keepevery = 10L,
           printevery=100L.
           id=NULL.
                       ## crisk2.bart only
           seed=99,
                       ## mc.crisk2.bart only
           mc.cores=2, ## mc.crisk2.bart only
           nice=19L ## mc.crisk2.bart only
```

```
mc.crisk2.bart(x.train=matrix(0,0,0), y.train=NULL,
              x.train2=x.train, y.train2=NULL,
              times=NULL, delta=NULL, K=NULL,
              x.test=matrix(0,0,0), x.test2=x.test,
              sparse=FALSE, theta=0, omega=1,
              a=0.5, b=1, augment=FALSE,
              rho=NULL, rho2=NULL,
              xinfo=matrix(0,0,0), xinfo2=matrix(0,0,0),
              usequants=FALSE,
              rm.const=TRUE, type='pbart',
              ntype=as.integer(
                  factor(type, levels=c('wbart', 'pbart', 'lbart'))),
              k=2, power=2, base=0.95,
              offset=NULL, offset2=NULL,
              tau.num=c(NA, 3, 6)[ntype],
              ntree=50, numcut=100, ndpost=1000, nskip=250,
              keepevery = 10L,
              printevery=100L,
```

```
id=NULL, ## crisk2.bart only
seed=99, ## mc.crisk2.bart only
mc.cores=2, ## mc.crisk2.bart only
nice=19L ## mc.crisk2.bart only
)
```

Arguments

x.train	Covariates for training (in sample) data for an event. Must be a data.frame or a matrix with rows corresponding to observations and columns to variables. crisk2.bart will generate draws of $f_1(t,x)$ for each x which is a row of x.train (note that the definition of x.train is dependent on whether y.train has been specified; see below).
y.train	Event binary response for training (in sample) data. If y.train is NULL, then y.train (x.train and x.test, if specified) are gen- erated by a call to surv.pre.bart (which require that times and delta be provided: see below); otherwise, y.train (x.train and x.test, if specified) are utilized as given assuming that the data construction has already been per- formed.
x.train2	Covariates for training (in sample) data of for a cause 1 event. Similar to x.train above.

)

y.train2	Cause 1 event binary response for training (in sample) data. Similar to y.train above.
times	The time of event or right-censoring, s_i . If y.train is NULL, then times (and delta) must be provided.
delta	The event indicator: 1 for cause 1, 2 for cause 2 and 0 is censored. If y.train is NULL, then delta (and times) must be provided.
К	If provided, then coarsen times per the quantiles $1/K, 2/K,, K/K$.
x.test	Covariates for test (out of sample) data of an event. Must be a data.frame or a matrix and have the same structure as x.train. crisk2.bart will generate draws of $f_1(t, x)$ for each x which is a row of x.test.
x.test2	Covariates for test (out of sample) data of a cause 1 event. Similar to x.test above.
sparse	Whether to perform variable selection based on a sparse Dirichlet prior; see Linero 2016.
theta	Set <i>theta</i> parameter; zero means random.
omega	Set <i>omega</i> parameter; zero means random.
а	Sparse parameter for $Beta(a, b)$ prior: $0.5 <= a <= 1$ where lower values inducing more sparsity.
b	Sparse parameter for $Beta(a, b)$ prior; typically, b=1.
rho	Sparse parameter: typically rho=p where p is the number of covariates in x.train.
rho2	Sparse parameter: typically rho2=p where p is the number of covariates in x.train2.
augment	Whether data augmentation is to be performed in sparse variable selection.
xinfo	You can provide the cutpoints to BART or let BART choose them for you. To provide them, use the xinfo argument to specify a list (matrix) where the items (rows) are the covariates and the contents of the items (columns) are the cutpoints.
xinfo2	Cause 2 cutpoints.
usequants	If usequants=FALSE, then the cutpoints in xinfo are generated uniformly; oth- erwise, if TRUE, uniform quantiles are used for the cutpoints.
rm.const	Whether or not to remove constant variables.
type	Whether to employ probit BART via Albert-Chib, 'pbart', or logistic BART by Holmes-Held, 'lbart'.
ntype	The integer equivalent of type where 'wbart' is 1, 'pbart' is 2 and 'lbart' is 3.
k	k is the number of prior standard deviations $f_h(t, x)$ is away from +/-3. The bigger k is, the more conservative the fitting will be.
power	Power parameter for tree prior.
base	Base parameter for tree prior.
offset	Cause 1 binary offset.

offset2	Cause 2 binary offset.
tau.num	The numerator in the tau definition.
ntree	The number of trees in the sum.
numcut	The number of possible values of cutpoints (see usequants). If a single number if given, this is used for all variables. Otherwise a vector with length equal to $ncol(x.train)$ is required, where the i^{th} element gives the number of cutpoints used for the i^{th} variable in x.train. If usequants is FALSE, numcut equally spaced cutoffs are used covering the range of values in the corresponding column of x.train. If usequants is TRUE, then min(numcut, the number of unique values in the corresponding columns of x.train-1) cutpoint values are used.
ndpost	The number of posterior draws returned.
nskip	Number of MCMC iterations to be treated as burn in.
keepevery	Every keepevery draw is kept to be returned to the user.
printevery	As the MCMC runs, a message is printed every printevery draws.
id	crisk2.bart only: unique identifier added to returned list.
seed	mc.crisk2.bart only: seed required for reproducible MCMC.
mc.cores	mc.crisk2.bart only: number of cores to employ in parallel.
nice	mc.crisk2.bart only: set the job niceness. The default niceness is 19: niceness goes from 0 (highest priority) to 19 (lowest priority).

Value

crisk2.bart returns an object of type crisk2bart which is essentially a list. Besides the items listed below, the list has offset, offset2, times which are the unique times, K which is the number of unique times, tx.train and tx.test, if any.

yhat.train	A matrix with ndpost rows and nrow(x.train) columns. Each row corresponds to a draw f_1^* from the posterior of f_1 and each column corresponds to a row of x.train. The (i, j) value is $f_1^*(t, x)$ for the i^{th} kept draw of f_1 and the j^{th} row of x.train. Burn-in is dropped.
yhat.test	Same as yhat.train but now the x's are the rows of the test data.
surv.test	test data fits for the survival function, $S(t, x)$.
<pre>surv.test.mean</pre>	mean of surv.test over the posterior samples.
prob.test	The probability of suffering an event.
prob.test2	The probability of suffering a cause 1 event.
cif.test	The cumulative incidence function of cause 1, $F_1(t, x)$.
cif.test2	The cumulative incidence function of cause 2, $F_2(t, x)$.
cif.test.mean	mean of cif.test columns for cause 1.
cif.test2.mean	mean of cif.test2 columns for cause 2.

varcount	a matrix with ndpost rows and nrow(x.train) columns. Each row is for a
	draw. For each variable (corresponding to the columns), the total count of the
	number of times this variable is used for an event in a tree decision rule (over all trees) is given.
varcount2	For each variable the total count of the number of times this variable is used for a cause 1 event in a tree decision rule is given.

Author(s)

Rodney Sparapani: <rsparapa@mcw.edu>

References

Chipman, H., George, E., and McCulloch R. (2010) Bayesian Additive Regression Trees. *The Annals of Applied Statistics*, **4**,**1**, 266-298 <doi: 10.1214/09-AOAS285>.

Friedman, J.H. (1991) Multivariate adaptive regression splines. The Annals of Statistics, 19, 1–67.

Gramacy, RB and Polson, NG (2012) Simulation-based regularized logistic regression. *Bayesian Analysis*, **7**, 567–590.

Holmes, C and Held, L (2006) Bayesian auxiliary variable models for binary and multinomial regression. *Bayesian Analysis*, **1**, 145–68.

Linero, A.R. (2018) Bayesian regression trees for high dimensional prediction and variable selection. *JASA*, **113**, 626–36.

Sparapani, Logan, McCulloch, Laud (2018) Nonparametric competing risks analysis using Bayesian Additive Regression Trees (BART). arXiv preprint arXiv:1806.11237

See Also

surv.pre.bart, predict.crisk2bart, mc.crisk2.pwbart, crisk.bart

Examples

```
data(transplant)
pfit <- survfit(Surv(futime, event) ~ abo, transplant)</pre>
# competing risks for type 0
plot(pfit[4,], xscale=7, xmax=735, col=1:3, lwd=2, ylim=c(0, 1),
       xlab='t (weeks)', ylab='Aalen-Johansen (AJ) CI(t)')
    legend(450, .4, c("Death", "Transplant", "Withdrawal"), col=1:3, lwd=2)
## plot(pfit[4,], xscale=30.5, xmax=735, col=1:3, lwd=2, ylim=c(0, 1),
          xlab='t (months)', ylab='Aalen-Johansen (AJ) CI(t)')
##
       legend(450, .4, c("Death", "Transplant", "Withdrawal"), col=1:3, lwd=2)
##
delta <- (as.numeric(transplant$event)-1)</pre>
## recode so that delta=1 is cause of interest; delta=2 otherwise
delta[delta==1] <- 4
delta[delta==2] <- 1</pre>
delta[delta>1] <- 2</pre>
```

```
table(delta, transplant$event)
times <- pmax(1, ceiling(transplant$futime/7)) ## weeks</pre>
##times <- pmax(1, ceiling(transplant$futime/30.5)) ## months</pre>
table(times)
type0 <- 1*(transplant$abo=='0')</pre>
typeA <- 1*(transplant$abo=='A')</pre>
typeB <- 1*(transplant$abo=='B')</pre>
typeAB <- 1*(transplant$abo=='AB')</pre>
table(typeA, type0)
x.train <- cbind(type0, typeA, typeB, typeAB)</pre>
x.test <- cbind(1, 0, 0, 0)
dimnames(x.test)[[2]] <- dimnames(x.train)[[2]]</pre>
##test BART with token run to ensure installation works
set.seed(99)
post <- crisk2.bart(x.train=x.train, times=times, delta=delta,</pre>
                   x.test=x.test, nskip=1, ndpost=1, keepevery=1)
## Not run:
## run one long MCMC chain in one process
## set.seed(99)
## post <- crisk2.bart(x.train=x.train, times=times, delta=delta, x.test=x.test)</pre>
## in the interest of time, consider speeding it up by parallel processing
## run "mc.cores" number of shorter MCMC chains in parallel processes
post <- mc.crisk2.bart(x.train=x.train, times=times, delta=delta,</pre>
                      x.test=x.test, seed=99, mc.cores=8)
K <- post$K
typeO.cif.mean <- apply(post$cif.test, 2, mean)</pre>
type0.cif.025 <- apply(post$cif.test, 2, quantile, probs=0.025)</pre>
type0.cif.975 <- apply(post$cif.test, 2, quantile, probs=0.975)</pre>
plot(pfit[4,], xscale=7, xmax=735, col=1:3, lwd=2, ylim=c(0, 0.8),
       xlab='t (weeks)', ylab='CI(t)')
points(c(0, post$times)*7, c(0, type0.cif.mean), col=4, type='s', lwd=2)
points(c(0, post$times)*7, c(0, type0.cif.025), col=4, type='s', lwd=2, lty=2)
points(c(0, post$times)*7, c(0, type0.cif.975), col=4, type='s', lwd=2, lty=2)
     legend(450, .4, c("Transplant(BART)", "Transplant(AJ)",
                        "Death(AJ)", "Withdrawal(AJ)"),
            col=c(4, 2, 1, 3), lwd=2)
##dev.copy2pdf(file='../vignettes/figures/liver-BART.pdf')
## plot(pfit[4,], xscale=30.5, xmax=735, col=1:3, lwd=2, ylim=c(0, 0.8),
##
          xlab='t (months)', ylab='CI(t)')
## points(c(0, post$times)*30.5, c(0, type0.cif.mean), col=4, type='s', lwd=2)
## points(c(0, post$times)*30.5, c(0, type0.cif.025), col=4, type='s', lwd=2, lty=2)
## points(c(0, post$times)*30.5, c(0, type0.cif.975), col=4, type='s', lwd=2, lty=2)
```

30

```
## legend(450, .4, c("Transplant(BART)", "Transplant(AJ)",
## "Death(AJ)", "Withdrawal(AJ)"),
## col=c(4, 2, 1, 3), lwd=2)
```

```
## End(Not run)
```

draw_lambda_i Testing truncated Normal sampling

Description

Truncated Normal latents with non-unit variance are necessary for logistic BART.

Usage

draw_lambda_i(lambda, mean, kmax=1000, thin=1)

Arguments

lambda	Previous value of lambda.
mean	Mean of truncated Normal.
kmax	The number of terms in the mixture.
thin	The thinning parameter.

Value

Returns the variance for a truncated Normal, i.e., N(mean, lambda)I(tau, infinity).

Author(s)

Robert McCulloch: <robert.e.mcculloch@gmail.com>, Rodney Sparapani: <rsparapa@mcw.edu> , Robert Gramacy: <rbg@vt.edu>.

See Also

rtnorm,lbart

Examples

```
set.seed(12)
```

```
draw_lambda_i(1, 2)
rtnorm(1, 2, sqrt(6.773462), 6)
draw_lambda_i(6.773462, 2)
```

Description

BART is a Bayesian "sum-of-trees" model. For a numeric response y, we have $y = f(x) + \epsilon$, where $\epsilon \sim N(0, \sigma^2)$.

f is the sum of many tree models. The goal is to have very flexible inference for the uknown function f.

In the spirit of "ensemble models", each tree is constrained by a prior to be a weak learner so that it contributes a small amount to the overall fit.

Usage

```
gbart(
      x.train, y.train,
      x.test=matrix(0,0,0), type='wbart',
      ntype=as.integer(
          factor(type, levels=c('wbart', 'pbart', 'lbart'))),
      sparse=FALSE, theta=0, omega=1,
      a=0.5, b=1, augment=FALSE, rho=NULL,
      xinfo=matrix(0,0,0), usequants=FALSE,
      rm.const=TRUE,
      sigest=NA, sigdf=3, sigquant=0.90,
      k=2, power=2, base=0.95,
      lambda=NA, tau.num=c(NA, 3, 6)[ntype],
      offset=NULL, w=rep(1, length(y.train)),
      ntree=c(200L, 50L, 50L)[ntype], numcut=100L,
      ndpost=1000L, nskip=100L,
      keepevery=c(1L, 10L, 10L)[ntype],
      printevery=100L, transposed=FALSE,
      hostname=FALSE,
      mc.cores = 1L, ## mc.gbart only
      nice = 19L, ## mc.gbart only
      seed = 99L
                   ## mc.gbart only
)
mc.gbart(
         x.train, y.train,
         x.test=matrix(0,0,0), type='wbart',
         ntype=as.integer(
             factor(type, levels=c('wbart', 'pbart', 'lbart'))),
         sparse=FALSE, theta=0, omega=1,
```

gbart

```
a=0.5, b=1, augment=FALSE, rho=NULL,
xinfo=matrix(0,0,0), usequants=FALSE,
rm.const=TRUE,
sigest=NA, sigdf=3, sigquant=0.90,
k=2, power=2, base=0.95,
lambda=NA, tau.num=c(NA, 3, 6)[ntype],
offset=NULL, w=rep(1, length(y.train)),
ntree=c(200L, 50L, 50L)[ntype], numcut=100L,
ndpost=1000L, nskip=100L,
keepevery=c(1L, 10L, 10L)[ntype],
printevery=100L, transposed=FALSE,
hostname=FALSE,
mc.cores = 2L, nice = 19L, seed = 99L
```

Arguments

)

x.train	Explanatory variables for training (in sample) data. May be a matrix or a data frame, with (as usual) rows corresponding to observations and columns to variables. If a variable is a factor in a data frame, it is replaced with dummies. Note that q dummies are created if $q > 2$ and one dummy created if $q = 2$ where q is the number of levels of the factor. gbart will generate draws of $f(x)$ for each x which is a row of x.train.
y.train	Continuous or binary dependent variable for training (in sample) data. If y is numeric, then a continuous BART model is fit (Normal errors). If y is binary (has only 0's and 1's), then a binary BART model with a probit link is fit by default: you can over-ride the default via the argument type to specify a logit BART model.
x.test	Explanatory variables for test (out of sample) data. Should have same structure as x.train. gbart will generate draws of $f(x)$ for each x which is a row of x.test.
type	You can use this argument to specify the type of fit. 'wbart' for continuous BART, 'pbart' for probit BART or 'lbart' for logit BART.
ntype	The integer equivalent of type where 'wbart' is 1, 'pbart' is 2 and 'lbart' is 3.
sparse	Whether to perform variable selection based on a sparse Dirichlet prior rather than simply uniform; see Linero 2016.
theta	Set <i>theta</i> parameter; zero means random.
omega	Set omega parameter; zero means random.
а	Sparse parameter for $Beta(a,b)$ prior: $0.5 <= a <= 1$ where lower values inducing more sparsity.
b	Sparse parameter for $Beta(a, b)$ prior; typically, $b = 1$.

rho	Sparse parameter: typically $rho = p$ where p is the number of covariates under consideration.
augment	Whether data augmentation is to be performed in sparse variable selection.
xinfo	You can provide the cutpoints to BART or let BART choose them for you. To provide them, use the xinfo argument to specify a list (matrix) where the items (rows) are the covariates and the contents of the items (columns) are the cutpoints.
usequants	If usequants=FALSE, then the cutpoints in xinfo are generated uniformly; oth- erwise, if TRUE, uniform quantiles are used for the cutpoints.
rm.const	Whether or not to remove constant variables.
sigest	The prior for the error variance $(sigma^2)$ is inverted chi-squared (the standard conditionally conjugate prior). The prior is specified by choosing the degrees of freedom, a rough estimate of the corresponding standard deviation and a quantile to put this rough estimate at. If sigest=NA then the rough estimate will be the usual least squares estimator. Otherwise the supplied value will be used. Not used if y is binary.
sigdf	Degrees of freedom for error variance prior. Not used if y is binary.
sigquant	The quantile of the prior that the rough estimate (see sigest) is placed at. The closer the quantile is to 1, the more aggresive the fit will be as you are putting more prior weight on error standard deviations $(sigma)$ less than the rough estimate. Not used if y is binary.
k	For numeric y, k is the number of prior standard deviations $E(Y x) = f(x)$ is away from +/-0.5. The response, codey.train, is internally scaled to range from -0.5 to 0.5. For binary y, k is the number of prior standard deviations $f(x)$ is away from +/-3. The bigger k is, the more conservative the fitting will be.
power	Power parameter for tree prior.
base	Base parameter for tree prior.
lambda	The scale of the prior for the variance. If lambda is zero, then the variance is to be considered fixed and known at the given value of sigest. Not used if y is binary.
tau.num	The numerator in the tau definition, i.e., tau=tau.num/(k*sqrt(ntree)).
offset	Continous BART operates on y.train centered by offset which defaults to mean(y.train). With binary BART, the centering is $P(Y = 1 x) = F(f(x) + offset)$ where offset defaults to F^{-1}(mean(y.train)). You can use the offset parameter to over-ride these defaults.
W	Vector of weights which multiply the standard deviation. Not used if y is binary.
ntree	The number of trees in the sum.
numcut	The number of possible values of c (see usequants). If a single number if given, this is used for all variables. Otherwise a vector with length equal to ncol(x.train) is required, where the i^{th} element gives the number of c used for the i^{th} variable in x.train. If usequants is false, numcut equally spaced cutoffs are used covering the range of values in the corresponding column of x.train. If usequants is true, then $min(numcut, thenumberofuniquevaluesinthecorresponding column 1)$ values are used.

gbart

ndpost	The number of posterior draws returned.
nskip	Number of MCMC iterations to be treated as burn in.
printevery	As the MCMC runs, a message is printed every printevery draws.
keepevery	Every keepevery draw is kept to be returned to the user.
transposed	When running gbart in parallel, it is more memory-efficient to transpose x.train and x.test, if any, prior to calling mc.gbart.
hostname	When running on a cluster occasionally it is useful to track on which node each chain is running; to do so set this argument to TRUE.
seed	Setting the seed required for reproducible MCMC.
mc.cores	Number of cores to employ in parallel.
nice	Set the job niceness. The default niceness is 19: niceness goes from 0 (highest) to 19 (lowest).

Details

BART is a Bayesian MCMC method. At each MCMC interation, we produce a draw from the joint posterior $(f, \sigma)|(x, y)$ in the numeric y case and just f in the binary y case.

Thus, unlike a lot of other modelling methods in R, we do not produce a single model object from which fits and summaries may be extracted. The output consists of values $f^*(x)$ (and σ^* in the numeric case) where * denotes a particular draw. The x is either a row from the training data, x.train or the test data, x.test.

For x.train/x.test with missing data elements, gbart will singly impute them with hot decking. For one or more missing covariates, record-level hot-decking imputation *deWaPann11* is employed that is biased towards the null, i.e., nonmissing values from another record are randomly selected regardless of the outcome. Since mc.gbart runs multiple gbart threads in parallel, mc.gbart performs multiple imputation with hot decking, i.e., a separate imputation for each thread. This record-level hot-decking imputation is biased towards the null, i.e., nonmissing values from another record are randomly selected regardless of y.train.

Value

gbart returns an object of type gbart which is essentially a list. In the numeric y case, the list has components:

yhat.train	A matrix with ndpost rows and nrow(x.train) columns. Each row corresponds to a draw f^* from the posterior of f and each column corresponds to a row of x.train. The (i, j) value is $f^*(x)$ for the i^{th} kept draw of f and the j^{th} row of x.train. Burn-in is dropped.	
yhat.test	Same as yhat.train but now the x's are the rows of the test data.	
yhat.train.mean		
	train data fits = mean of yhat.train columns.	
yhat.test.mean	test data fits = mean of yhat.test columns.	
sigma	post burn in draws of sigma, length = ndpost.	

first.sigma	burn-in draws of sigma.
varcount	a matrix with ndpost rows and nrow(x.train) columns. Each row is for a draw. For each variable (corresponding to the columns), the total count of the number of times that variable is used in a tree decision rule (over all trees) is given.
sigest	The rough error standard deviation (σ) used in the prior.

Author(s)

Robert McCulloch: <robert.e.mcculloch@gmail.com>, Rodney Sparapani: <rsparapa@mcw.edu>.

References

Chipman, H., George, E., and McCulloch R. (2010) Bayesian Additive Regression Trees. *The Annals of Applied Statistics*, **4**,**1**, 266-298 <doi:10.1214/09-AOAS285>.

Chipman, H., George, E., and McCulloch R. (2006) Bayesian Ensemble Learning. Advances in Neural Information Processing Systems 19, Scholkopf, Platt and Hoffman, Eds., MIT Press, Cambridge, MA, 265-272.

De Waal, T., Pannekoek, J. and Scholtus, S. (2011) Handbook of statistical data editing and imputation. John Wiley & Sons, Hoboken, NJ.

Friedman, J.H. (1991) Multivariate adaptive regression splines. The Annals of Statistics, 19, 1–67.

Gramacy, RB and Polson, NG (2012) Simulation-based regularized logistic regression. *Bayesian Analysis*, **7**, 567–590.

Holmes, C and Held, L (2006) Bayesian auxiliary variable models for binary and multinomial regression. *Bayesian Analysis*, **1**, 145–68.

Linero, A.R. (2016) Bayesian regression trees for high dimensional prediction and variable selection. *JASA*, http://dx.doi.org/10.1080/01621459.2016.1264957

See Also

pbart

Examples

```
##simulate data (example from Friedman MARS paper)
f = function(x){
10*sin(pi*x[,1]*x[,2]) + 20*(x[,3]-.5)^2+10*x[,4]+5*x[,5]
}
sigma = 1.0 #y = f(x) + sigma*z , z~N(0,1)
n = 100 #number of observations
set.seed(99)
x=matrix(runif(n*10),n,10) #10 variables, only first 5 matter
Ey = f(x)
y=Ey+sigma*rnorm(n)
lmFit = lm(y~.,data.frame(x,y)) #compare lm fit to BART later
##test BART with token run to ensure installation works
set.seed(99)
```

gbmm

```
bartFit = wbart(x,y,nskip=5,ndpost=5)
## Not run:
##run BART
set.seed(99)
bartFit = wbart(x,y)
##compare BART fit to linear matter and truth = Ey
fitmat = cbind(y,Ey,lmFit$fitted,bartFit$yhat.train.mean)
colnames(fitmat) = c('y','Ey','lm','bart')
print(cor(fitmat))
```

```
## End(Not run)
```

gbmm

Generalized BART Mixed Model for continuous and binary outcomes

Description

BART is a Bayesian "sum-of-trees" model. For a numeric response y, we have $y = f(x) + \epsilon$, where $\epsilon \sim N(0, \sigma^2)$.

f is the sum of many tree models. The goal is to have very flexible inference for the uknown function f.

In the spirit of "ensemble models", each tree is constrained by a prior to be a weak learner so that it contributes a small amount to the overall fit.

Usage

```
gbmm(
      x.train, y.train,
      x.test=matrix(0,0,0), type='wbart',
      u.train=NULL, B=NULL,
      ntype=as.integer(
          factor(type, levels=c('wbart', 'pbart'))),
      sparse=FALSE, theta=0, omega=1,
      a=0.5, b=1, augment=FALSE, rho=NULL,
      xinfo=matrix(0,0,0), usequants=FALSE,
      rm.const=TRUE,
      sigest=NA, sigdf=3, sigquant=0.90,
      k=2, power=2, base=0.95,
      lambda=NA, tau.num=c(NA, 3, 6)[ntype],
      offset=NULL,
      ntree=c(200L, 50L, 50L)[ntype], numcut=100L,
      ndpost=1000L, nskip=100L,
      keepevery=c(1L, 10L, 10L)[ntype],
      printevery=100L, transposed=FALSE,
```

```
hostname=FALSE,
      mc.cores = 1L, ## mc.gbmm only
      nice = 19L, ## mc.gbmm only
      seed = 99L
                   ## mc.gbmm only
)
mc.gbmm(
         x.train, y.train,
         x.test=matrix(0,0,0), type='wbart',
         u.train=NULL, B=NULL,
         ntype=as.integer(
             factor(type, levels=c('wbart', 'pbart'))),
         sparse=FALSE, theta=0, omega=1,
         a=0.5, b=1, augment=FALSE, rho=NULL,
         xinfo=matrix(0,0,0), usequants=FALSE,
         rm.const=TRUE,
         sigest=NA, sigdf=3, sigquant=0.90,
         k=2, power=2, base=0.95,
         lambda=NA, tau.num=c(NA, 3, 6)[ntype],
         offset=NULL,
         ntree=c(200L, 50L, 50L)[ntype], numcut=100L,
         ndpost=1000L, nskip=100L,
         keepevery=c(1L, 10L, 10L)[ntype],
         printevery=100L, transposed=FALSE,
         hostname=FALSE,
         mc.cores = 2L, nice = 19L, seed = 99L
```

```
)
```

Arguments

x.train	Explanatory variables for training (in sample) data.
	May be a matrix or a data frame, with (as usual) rows corresponding to obser-
	vations and columns to variables.
	If a variable is a factor in a data frame, it is replaced with dummies. Note that q dummies are created if $q > 2$ and one dummy created if $q = 2$ where q is
	the number of levels of the factor. gbmm will generate draws of $f(\boldsymbol{x})$ for each \boldsymbol{x} which is a row of x.train.
y.train	Continuous or binary dependent variable for training (in sample) data.
-	If y is numeric, then a continuous BART model is fit (Normal errors).
	If y is binary (has only 0's and 1's), then a binary BART model with a probit link
	is fit by default: you can over-ride the default via the argument type to specify a logit BART model.
x.test	Explanatory variables for test (out of sample) data. Should have same structure as x.train. gbmm will generate draws of $f(x)$ for each x which is a row of x.test.
u.train	Integer indices specifying the random effects.
В	The prior for the standard deviation of the random effects is $U(0, B)$.

gbmm

type	You can use this argument to specify the type of fit. 'wbart' for continuous BART or 'pbart' for probit BART.
ntype	The integer equivalent of type where 'wbart' is 1 and 'pbart' is 2.
sparse	Whether to perform variable selection based on a sparse Dirichlet prior rather than simply uniform; see Linero 2016.
theta	Set <i>theta</i> parameter; zero means random.
omega	Set <i>omega</i> parameter; zero means random.
а	Sparse parameter for $Beta(a, b)$ prior: $0.5 <= a <= 1$ where lower values inducing more sparsity.
b	Sparse parameter for $Beta(a, b)$ prior; typically, $b = 1$.
rho	Sparse parameter: typically $rho = p$ where p is the number of covariates under consideration.
augment	Whether data augmentation is to be performed in sparse variable selection.
xinfo	You can provide the cutpoints to BART or let BART choose them for you. To provide them, use the xinfo argument to specify a list (matrix) where the items (rows) are the covariates and the contents of the items (columns) are the cutpoints.
usequants	If usequants=FALSE, then the cutpoints in xinfo are generated uniformly; oth- erwise, if TRUE, uniform quantiles are used for the cutpoints.
rm.const	Whether or not to remove constant variables.
sigest	The prior for the error variance $(sigma^2)$ is inverted chi-squared (the standard conditionally conjugate prior). The prior is specified by choosing the degrees of freedom, a rough estimate of the corresponding standard deviation and a quantile to put this rough estimate at. If sigest=NA then the rough estimate will be the usual least squares estimator. Otherwise the supplied value will be used. Not used if y is binary.
sigdf	Degrees of freedom for error variance prior. Not used if y is binary.
sigquant	The quantile of the prior that the rough estimate (see sigest) is placed at. The closer the quantile is to 1, the more aggresive the fit will be as you are putting more prior weight on error standard deviations $(sigma)$ less than the rough estimate. Not used if y is binary.
k	For numeric y , k is the number of prior standard deviations $E(Y x) = f(x)$ is away from +/-0.5. The response, codey.train, is internally scaled to range from -0.5 to 0.5. For binary y , k is the number of prior standard deviations $f(x)$ is away from +/-3. The bigger k is, the more conservative the fitting will be.
power	Power parameter for tree prior.
base	Base parameter for tree prior.
lambda	The scale of the prior for the variance. If lambda is zero, then the variance is to be considered fixed and known at the given value of sigest. Not used if y is binary.
tau.num	The numerator in the tau definition, i.e., tau=tau.num/(k*sqrt(ntree)).

offset	Continous BART operates on y.train centered by offset which defaults to mean(y.train). With binary BART, the centering is $P(Y = 1 x) = F(f(x) + offset)$ where offset defaults to F^{-1}(mean(y.train)). You can use the offset parameter to over-ride these defaults.
ntree	The number of trees in the sum.
numcut	The number of possible values of c (see usequants). If a single number if given, this is used for all variables. Otherwise a vector with length equal to ncol(x.train) is required, where the i^{th} element gives the number of c used for the i^{th} variable in x.train. If usequants is false, numcut equally spaced cutoffs are used covering the range of values in the corresponding column of x.train. If usequants is true, then $min(numcut, thenumberofuniquevalues in the corresponding column 1)$ values are used.
ndpost	The number of posterior draws returned.
nskip	Number of MCMC iterations to be treated as burn in.
printevery	As the MCMC runs, a message is printed every printevery draws.
keepevery	Every keepevery draw is kept to be returned to the user.
transposed	When running gbmm in parallel, it is more memory-efficient to transpose x.train and x.test, if any, prior to calling mc.gbmm.
hostname	When running on a cluster occasionally it is useful to track on which node each chain is running; to do so set this argument to TRUE.
seed	Setting the seed required for reproducible MCMC.
mc.cores	Number of cores to employ in parallel.
nice	Set the job niceness. The default niceness is 19: niceness goes from 0 (highest) to 19 (lowest).

Details

BART is a Bayesian MCMC method. At each MCMC interation, we produce a draw from the joint posterior $(f, \sigma)|(x, y)$ in the numeric y case and just f in the binary y case.

Thus, unlike a lot of other modelling methods in R, we do not produce a single model object from which fits and summaries may be extracted. The output consists of values $f^*(x)$ (and σ^* in the numeric case) where * denotes a particular draw. The x is either a row from the training data, x.train or the test data, x.test.

For x.train/x.test with missing data elements, gbmm will singly impute them with hot decking. For one or more missing covariates, record-level hot-decking imputation *deWaPann11* is employed that is biased towards the null, i.e., nonmissing values from another record are randomly selected regardless of the outcome. Since mc.gbmm runs multiple gbmm threads in parallel, mc.gbmm performs multiple imputation with hot decking, i.e., a separate imputation for each thread. This record-level hot-decking imputation is biased towards the null, i.e., nonmissing values from another record are randomly selected regardless of y.train.

gbmm

Value

gbmm returns an object of type gbmm which is essentially a list. In the numeric y case, the list has components:

yhat.train	A matrix with ndpost rows and nrow(x.train) columns. Each row corresponds to a draw f^* from the posterior of f and each column corresponds to a row of x.train. The (i, j) value is $f^*(x)$ for the i^{th} kept draw of f and the j^{th} row of x.train. Burn-in is dropped.
yhat.test	Same as yhat.train but now the x's are the rows of the test data.
yhat.train.mear	1
	train data fits = mean of yhat.train columns.
yhat.test.mean	test data fits = mean of yhat.test columns.
sigma	post burn in draws of sigma, length = ndpost.
first.sigma	burn-in draws of sigma.
varcount	a matrix with ndpost rows and nrow(x.train) columns. Each row is for a draw. For each variable (corresponding to the columns), the total count of the number of times that variable is used in a tree decision rule (over all trees) is given.
sigest	The rough error standard deviation (σ) used in the prior.

Author(s)

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References

Chipman, H., George, E., and McCulloch R. (2010) Bayesian Additive Regression Trees. *The Annals of Applied Statistics*, **4**,**1**, 266-298 <doi:10.1214/09-AOAS285>.

Chipman, H., George, E., and McCulloch R. (2006) Bayesian Ensemble Learning. Advances in Neural Information Processing Systems 19, Scholkopf, Platt and Hoffman, Eds., MIT Press, Cambridge, MA, 265-272.

De Waal, T., Pannekoek, J. and Scholtus, S. (2011) Handbook of statistical data editing and imputation. John Wiley & Sons, Hoboken, NJ.

Friedman, J.H. (1991) Multivariate adaptive regression splines. The Annals of Statistics, 19, 1-67.

Linero, A.R. (2018) Bayesian regression trees for high dimensional prediction and variable selection. *JASA*, **113(522)**, 626–636.

See Also

wbart, pbart

Examples

```
##simulate data (example from Friedman MARS paper)
f = function(x){
10*sin(pi*x[,1]*x[,2]) + 20*(x[,3]-.5)^2+10*x[,4]+5*x[,5]
}
sigma = 1.0 \#y = f(x) + sigma * z, z \sim N(0,1)
n = 100
             #number of observations
set.seed(99)
x=matrix(runif(n*10),n,10) #10 variables, only first 5 matter
Ey = f(x)
y=Ey+sigma*rnorm(n)
lmFit = lm(y^{-}, data.frame(x, y)) #compare lm fit to BART later
##test BART with token run to ensure installation works
set.seed(99)
bartFit = wbart(x,y,nskip=5,ndpost=5)
## Not run:
##run BART
set.seed(99)
bartFit = wbart(x,y)
##compare BART fit to linear matter and truth = Ey
fitmat = cbind(y,Ey,lmFit$fitted,bartFit$yhat.train.mean)
colnames(fitmat) = c('y', 'Ey', 'lm', 'bart')
print(cor(fitmat))
## End(Not run)
```

gewekediag

Geweke's convergence diagnostic

Description

Geweke (1992) proposed a convergence diagnostic for Markov chains based on a test for equality of the means of the first and last part of a Markov chain (by default the first 10% and the last 50%). If the samples are drawn from the stationary distribution of the chain, the two means are equal and Geweke's statistic has an asymptotically standard normal distribution.

The test statistic is a standard Z-score: the difference between the two sample means divided by its estimated standard error. The standard error is estimated from the spectral density at zero and so takes into account any autocorrelation.

The Z-score is calculated under the assumption that the two parts of the chain are asymptotically independent, which requires that the sum of frac1 and frac2 be strictly less than 1.

Adapted from the geweke.diag function of the coda package which passes mcmc objects as arguments rather than matrices.

Usage

```
gewekediag(x, frac1=0.1, frac2=0.5)
```

42

gewekediag

Arguments

X	Matrix of MCMC chains: the rows are the samples and the columns are different "parameters". For BART, generally, the columns are estimates of f . For pbart, they are different subjects. For surv.bart, they are different subjects at a grid of times.
frac1	fraction to use from beginning of chain
frac2	fraction to use from end of chain

Value

Z-scores for a test of equality of means between the first and last parts of the chain. A separate statistic is calculated for each variable in each chain.

References

Geweke, J. Evaluating the accuracy of sampling-based approaches to calculating posterior moments. In *Bayesian Statistics 4* (ed JM Bernado, JO Berger, AP Dawid and AFM Smith). Clarendon Press, Oxford, UK.

Martyn Plummer, Nicky Best, Kate Cowles and Karen Vines (2006). CODA: Convergence Diagnosis and Output Analysis for MCMC, R News, vol 6, 7-11.

See Also

spectrum0ar.

Examples

load survival package for the advanced lung cancer example
data(lung)

```
group <- -which(is.na(lung[, 7])) ## remove missing row for ph.karno
times <- lung[group, 2] ##lung$time
delta <- lung[group, 3]-1 ##lung$status: 1=censored, 2=dead
##delta: 0=censored, 1=dead
```

this study reports time in days rather than months like other studies
coarsening from days to months will reduce the computational burden
times <- ceiling(times/30)</pre>

```
summary(times)
table(delta)
```

x.train <- as.matrix(lung[group, c(4, 5, 7)]) ## matrix of observed covariates</pre>

## lung\$age:	Age in years
<pre>## lung\$sex:</pre>	Male=1 Female=2
<pre>## lung\$ph.karno:</pre>	<pre>Karnofsky performance score (dead=0:normal=100:by=10)</pre>
##	rated by physician

```
dimnames(x.train)[[2]] <- c('age(yr)', 'M(1):F(2)', 'ph.karno(0:100:10)')</pre>
summary(x.train[ , 1])
table(x.train[ , 2])
table(x.train[ , 3])
x.test <- matrix(nrow=84, ncol=3) ## matrix of covariate scenarios</pre>
dimnames(x.test)[[2]] <- dimnames(x.train)[[2]]</pre>
i <- 1
for(age in 5*(9:15)) for(sex in 1:2) for(ph.karno in 10*(5:10)) {
    x.test[i, ] <- c(age, sex, ph.karno)</pre>
    i <- i+1
}
## Not run:
    set.seed(99)
    post <- surv.bart(x.train=x.train, times=times, delta=delta, x.test=x.test)</pre>
    ## in the interest of time, consider speeding it up by parallel processing
    ## run "mc.cores" number of shorter MCMC chains in parallel processes
    ## post <- mc.surv.bart(x.train=x.train, times=times, delta=delta,</pre>
    ##
                             x.test=x.test, mc.cores=8, seed=99)
    N <- nrow(x.test)</pre>
    K <- post$K
    ## select 10 lung cancer patients uniformly spread out over the data set
    h <- seq(1, N*K, floor(N/10)*K)</pre>
    for(i in h) {
        post.mcmc <- post$yhat.test[ , (i-1)+1:K]</pre>
        z <- gewekediag(post.mcmc)$z</pre>
        y <- max(c(4, abs(z)))</pre>
        ## plot the z scores vs. time for each patient
        if(i==1) plot(post$times, z, ylim=c(-y, y), type='l',
                       xlab='t', ylab='z')
        else lines(post$times, z, type='l')
    }
    ## add two-sided alpha=0.05 critical value lines
    lines(post$times, rep(-1.96, K), type='l', lty=2)
    lines(post$times, rep( 1.96, K), type='l', lty=2)
```

End(Not run)

lbart

Logit BART for dichotomous outcomes with Logistic latents

lbart

Description

BART is a Bayesian "sum-of-trees" model.

For numeric response y, we have $y = f(x) + \epsilon$, where $\epsilon \sim Log(0, 1)$.

For a binary response y, P(Y = 1|x) = F(f(x)), where F denotes the standard Logistic CDF (logit link).

In both cases, f is the sum of many tree models. The goal is to have very flexible inference for the uknown function f.

In the spirit of "ensemble models", each tree is constrained by a prior to be a weak learner so that it contributes a small amount to the overall fit.

Usage

```
lbart(
    x.train, y.train, x.test=matrix(0.0,0,0),
    sparse=FALSE, a=0.5, b=1, augment=FALSE, rho=NULL,
    xinfo=matrix(0.0,0,0), usequants=FALSE,
    cont=FALSE, rm.const=TRUE, tau.interval=0.95,
    k=2.0, power=2.0, base=.95,
    binaryOffset=NULL,
    ntree=200L, numcut=100L,
    ndpost=1000L, nskip=100L,
    keepevery=1L,
    nkeeptrain=ndpost, nkeeptest=ndpost,
    nkeeptreedraws=ndpost,
    printevery=100L, transposed=FALSE
```

```
)
```

Arguments

x.train	Explanatory variables for training (in sample) data.
	May be a matrix or a data frame, with (as usual) rows corresponding to obser-
	vations and columns to variables.
	If a variable is a factor in a data frame, it is replaced with dummies. Note that q dummies are created if $q>2$ and one dummy is created if $q=2$, where q is the number of levels of the factor. 1bart will generate draws of $f(x)$ for each x which is a row of x train.
	which is a low of x.train.
y.train	Binary dependent variable for training (in sample) data.
x.test	Explanatory variables for test (out of sample) data.
	Should have same structure as x.train.
	lbart will generate draws of $f(x)$ for each x which is a row of x.test.
sparse	Whether to perform variable selection based on a sparse Dirichlet prior rather than simply uniform; see Linero 2016.
а	Sparse parameter for $Beta(a,b)$ prior: $0.5 <= a <= 1$ where lower values inducing more sparsity.

h	Sparce peremeter for $P_{ota}(a, b)$ prior typically $b = 1$
b	Sparse parameter for $Beta(a, b)$ prior; typically, $b = 1$.
rho	Sparse parameter: typically $rho = p$ where p is the number of covariates under consideration.
augment	Whether data augmentation is to be performed in sparse variable selection.
xinfo	You can provide the cutpoints to BART or let BART choose them for you. To provide them, use the xinfo argument to specify a list (matrix) where the items (rows) are the covariates and the contents of the items (columns) are the cutpoints.
usequants	If usequants=FALSE, then the cutpoints in xinfo are generated uniformly; otherwise, if TRUE, uniform quantiles are used for the cutpoints.
cont	Whether or not to assume all variables are continuous.
rm.const	Whether or not to remove constant variables.
tau.interval	The width of the interval to scale the variance for the terminal leaf values.
k	For numeric y, k is the number of prior standard deviations $E(Y x) = f(x)$ is away from +/5. The response (y.train) is internally scaled to range from5 to .5. For binary y, k is the number of prior standard deviations $f(x)$ is away from +/-3. In both cases, the bigger k is, the more conservative the fitting will be.
power	Power parameter for tree prior.
base	Base parameter for tree prior.
binaryOffset	Used for binary y. The model is $P(Y = 1 x) = F(f(x) + binaryOffset)$.
ntree	The number of trees in the sum.
numcut	The number of possible values of c (see usequants). If a single number if given, this is used for all variables. Otherwise a vector with length equal to $ncol(x.train)$ is required, where the i^{th} element gives the number of c used for the i^{th} variable in x.train. If usequants is false, numcut equally spaced cutoffs are used covering the range of values in the corresponding column of x.train. If usequants is true, then min(numcut, the number of unique values in the corresponding columns of x.train - 1) c values are used.
ndpost	The number of posterior draws returned.
nskip	Number of MCMC iterations to be treated as burn in.
nkeeptrain	Number of MCMC iterations to be returned for train data.
nkeeptest	Number of MCMC iterations to be returned for test data.
nkeeptreedraws	Number of MCMC iterations to be returned for tree draws.
keepevery	Every keepevery draw is kept to be returned to the user.
printevery	As the MCMC runs, a message is printed every printevery draws.
transposed	When running lbart in parallel, it is more memory-efficient to transpose x.train and x.test, if any, prior to calling mc.lbart.

lbart

Details

BART is an Bayesian MCMC method. At each MCMC interation, we produce a draw from the joint posterior f|(x, y) in the numeric y case and just f in the binary y case.

Thus, unlike a lot of other modelling methods in R, we do not produce a single model object from which fits and summaries may be extracted. The output consists of values $f^*(x)$

where * denotes a particular draw. The x is either a row from the training data (x.train) or the test data (x.test).

Value

lbart returns an object of type lbart which is essentially a list.

yhat.train	A matrix with ndpost rows and nrow(x.train) columns. Each row corresponds to a draw f^* from the posterior of f and each column corresponds to a row of x.train. The (i, j) value is $f^*(x)$ for the i^{th} kept draw of f and the j^{th} row of x.train. Burn-in is dropped.	
yhat.test	Same as yhat.train but now the x's are the rows of the test data.	
yhat.train.mean		
	train data fits = mean of yhat.train columns.	
yhat.test.mean	test data fits = mean of yhat.test columns.	
varcount	a matrix with ndpost rows and nrow(x.train) columns. Each row is for a draw. For each variable (corresponding to the columns), the total count of the number of times that variable is used in a tree decision rule (over all trees) is given.	

In addition, the list has a binaryOffset giving the value used.

Note that in the binary y, case yhat.train and yhat.test are f(x) + binaryOffset. If you want draws of the probability P(Y = 1|x) you need to apply the Logistic CDF (plogis) to these values.

Author(s)

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References

Chipman, H., George, E., and McCulloch R. (2010) Bayesian Additive Regression Trees. *The Annals of Applied Statistics*, **4**,**1**, 266-298 <doi: 10.1214/09-AOAS285>.

Chipman, H., George, E., and McCulloch R. (2006) Bayesian Ensemble Learning. Advances in Neural Information Processing Systems 19, Scholkopf, Platt and Hoffman, Eds., MIT Press, Cambridge, MA, 265-272.

Friedman, J.H. (1991) Multivariate adaptive regression splines. The Annals of Statistics, 19, 1-67.

Gramacy, RB and Polson, NG (2012) Simulation-based regularized logistic regression. *Bayesian Analysis*, **7**, 567–590.

Holmes, C and Held, L (2006) Bayesian auxiliary variable models for binary and multinomial regression. *Bayesian Analysis*, **1**, 145–68.

Linero, A.R. (2018) Bayesian regression trees for high dimensional prediction and variable selection. *JASA*, **113**, 626–36.

See Also

wbart

data(ACTG175)

Examples

```
## exclude those who do not have CD4 count at 96 weeks
ex <- is.na(ACTG175$cd496)</pre>
table(ex)
## inclusion criteria are CD4 counts between 200 and 500
ACTG175$cd40 <- min(500, max(250, ACTG175$cd40))
## calculate relative CD4 decline
y <- ((ACTG175$cd496-ACTG175$cd40)/ACTG175$cd40)[!ex]</pre>
summary(y)
## 0=failure, 1=success
y < -1*(y > -0.5)
## summarize CD4 outcomes
table(y, ACTG175$arms[!ex])
table(y, ACTG175$arms[!ex])/
   matrix(table(ACTG175$arms[!ex]), nrow=2, ncol=4, byrow=TRUE)
## drop unneeded and unwanted variables
## 1: 'pidnum' patient ID number
##14: 'str2' which will be handled by strat1 below
##15: 'strat' which will be handled by strat1-strat3 below
##17: 'treat' handled by arm0-arm3 below
##18: 'offtrt' indicator of off-treatment before 96 weeks
##20: 'cd420' CD4 T cell count at 20 weeks
##21: 'cd496' CD4 T cell count at 96 weeks
##22: 'r' missing CD4 T cell count at 96 weeks
##24: 'cd820' CD8 T cell count at 20 weeks
##25: 'cens' indicator of observing the event in days
##26: 'days' number of days until the primary endpoint
##27: 'arms' handled by arm0-arm3 below
train <- as.matrix(ACTG175)[!ex, -c(1, 14:15, 17, 18, 20:22, 24:27)]
train <- cbind(1*(ACTG175$strat[!ex]==1), 1*(ACTG175$strat[!ex]==2),</pre>
               1*(ACTG175$strat[!ex]==3), train)
dimnames(train)[[2]][1:3] <- paste0('strat', 1:3)</pre>
train <- cbind(1*(ACTG175$arms[!ex]==0), 1*(ACTG175$arms[!ex]==1),</pre>
```

```
1*(ACTG175$arms[!ex]==2), 1*(ACTG175$arms[!ex]==3), train)
dimnames(train)[[2]][1:4] <- paste0('arm', 0:3)</pre>
N <- nrow(train)</pre>
test0 <- train; test0[ , 1:4] <- 0; test0[ , 1] <- 1
test1 <- train; test1[ , 1:4] <- 0; test1[ , 2] <- 1
test2 <- train; test2[ , 1:4] <- 0; test2[ , 3] <- 1
test3 <- train; test3[ , 1:4] <- 0; test3[ , 4] <- 1
test <- rbind(test0, test1, test2, test3)</pre>
##test BART with token run to ensure installation works
## set.seed(21)
## post <- lbart(train, y, test, nskip=5, ndpost=5)</pre>
## Not run:
set.seed(21)
post <- lbart(train, y, test)</pre>
## turn z-scores into probabilities
post$prob.test <- plogis(post$yhat.test)</pre>
## average over the posterior samples
post$prob.test.mean <- apply(post$prob.test, 2, mean)</pre>
## place estimates for arms 0-3 next to each other for convenience
itr <- cbind(post$prob.test.mean[(1:N)], post$prob.test.mean[N+(1:N)],</pre>
             post$prob.test.mean[2*N+(1:N)], post$prob.test.mean[3*N+(1:N)])
## find the BART ITR for each patient
itr.pick <- integer(N)</pre>
for(i in 1:N) itr.pick[i] <- which(itr[i, ]==max(itr[i, ]))-1</pre>
## arms 0 and 3 (monotherapy) are never chosen
table(itr.pick)
## do arms 1 and 2 show treatment heterogeneity?
diff. <- apply(post$prob.test[ , 2*N+(1:N)]-post$prob.test[ , N+(1:N)], 2, mean)
plot(sort(diff.), type='h', main='ACTG175 trial: 50% CD4 decline from baseline at 96 weeks',
     xlab='Arm 2 (1) Preferable to the Right (Left)', ylab='Prob.Diff.: Arms 2 - 1')
library(rpart)
library(rpart.plot)
## make data frame for nicer names in the plot
var <- as.data.frame(train[ , -(1:4)])</pre>
dss <- rpart(diff. ~ var$age+var$gender+var$race+var$wtkg+var$cd40+var$cd80+</pre>
                   var$karnof+var$symptom+var$hemo+var$homo+var$drugs+var$z30+
                    var$zprior+var$oprior+var$strat1+var$strat2+var$strat3,
               method='anova', control=rpart.control(cp=0.1))
rpart.plot(dss, type=3, extra=101)
```

```
## if strat1==1 (antiretroviral naive), then arm 2 is better
## otherwise, arm 1
print(dss)
all0 <- apply(post$prob.test[ , (1:N)], 1, mean)</pre>
all1 <- apply(post$prob.test[ , N+(1:N)], 1, mean)</pre>
all2 <- apply(post$prob.test[ , 2*N+(1:N)], 1, mean)</pre>
all3 <- apply(post$prob.test[ , 3*N+(1:N)], 1, mean)
## BART ITR
BART.itr <- apply(post$prob.test[, c(N+which(itr.pick==1), 2*N+which(itr.pick==2))], 1, mean)
test <- train
test[ , 1:4] <- 0
test[test[ , 5]==0, 2] <- 1
test[test[ , 5]==1, 3] <- 1
## BART ITR simple
BART.itr.simp <- pwbart(test, post$treedraws)</pre>
BART.itr.simp <- apply(plogis(BART.itr.simp), 1, mean)</pre>
plot(density(BART.itr), xlab='Value', xlim=c(0.475, 0.775), lwd=2,
     main='ACTG175 trial: 50% CD4 decline from baseline at 96 weeks')
lines(density(BART.itr.simp), col='brown', lwd=2)
lines(density(all0), col='green', lwd=2)
lines(density(all1), col='red', lwd=2)
lines(density(all2), col='blue', lwd=2)
lines(density(all3), col='yellow', lwd=2)
legend('topleft', legend=c('All Arm 0 (ZDV only)', 'All Arm 1 (ZDV+DDI)',
                            'All Arm 2 (ZDV+DDC)', 'All Arm 3 (DDI only)',
                            'BART ITR simple', 'BART ITR'),
       col=c('green', 'red', 'blue', 'yellow', 'brown', 'black'), lty=1, lwd=2)
```

End(Not run)

leukemia

Bone marrow transplantation for leukemia and multi-state models

Description

137 patients with acute myelocytic leukemia (AML) and acute lymphoblastic leukemia (ALL) were given oral busulfan (Bu) 4 mg/kg on each of 4 days and intravenous cyclophosphamide (Cy) 60 mg/kg on each of 2 days (BuCy2) followed by allogeneic bone marrow transplantation from an HLA-identical or one antigen disparate sibling.

Usage

data(leukemia)

50

leukemia

Format

A data frame with 137 subjects on the following 22 variables.

- G Disease Group (1=ALL, 2=AML Low Risk in first remission, 3=AML High Risk not in first remission)
- TD Time To Death Or On Study Time
- TB Disease Free Survival Time (Time To Relapse, Death Or End Of Study)
- D Death Indicator (0=Alive, 1=Dead)
- R Relapse Indicator (0=Disease Free, 1=Relapsed)
- B Disease Free Survival Indicator (0=Alive and Disease Free, 1=Dead or Relapsed)
- TA Time To Acute Graft-Versus-Host Disease (GVHD)
- A Acute GVHD Indicator (0=Never Developed Acute GVHD, 1=Developed Acute GVHD)
- TC Time To Chronic Graft-Versus-Host Disease (GVHD)
- C Chronic GVHD Indicator (0=Never Developed Chronic GVHD, 1=Developed Chronic GVHD)
- TP Time of Platelets Returning to Normal Levels
- P Platelet Recovery Indicator (0=Platelets Never Returned to Normal, 1=Platelets Returned To Normal)
- X1 Patient Age In Years
- X2 Donor Age In Years
- X3 Patient Gender (0=female, 1=male)
- X4 Donor Gender (0=female, 1=male)
- X5 Patient Cytomegalovirus (CMV) Immune Status (0=CMV Negative, 1=CMV Positive)
- X6 Donor Cytomegalovirus (CMV) Immune Status (0=CMV Negative, 1=CMV Positive)
- X7 Waiting Time to Transplant In Days
- X8 AML Patients with Elevated Risk By French-American-British (FAB) Classification (0=Not AML/Elevated, 1=FAB M4 Or M5 with AML)
- X9 Hospital (1=The Ohio State University in Columbus, 2=Alfred in Melbourne, 3=St. Vincent in Sydney, 4=Hahnemann University in Philadelphia)
- X10 Methotrexate Used as a Graft-Versus-Host Disease Prophylactic (0=No, 1=Yes)

Source

Klein, J. and Moeschberger, M.L. (2003). *Survival Analysis: Techniques for Censored and Truncated Data*, New York: Springer-Verlag, 2nd Ed., Section 1.3. https://www.mcw.edu/-/media/ MCW/Departments/Biostatistics/datafromsection13.txt

References

Copelan, E.A., Biggs, J.C., Thompson, J.M., Crilley, P., Szer, J., Klein, J.P., Kapoor, N., Avalos, B.R., Cunningham, I. and Atkinson, K. (1991). "Treatment for acute myelocytic leukemia with allogeneic bone marrow transplantation following preparation with BuCy2". *Blood*, **78**(**3**), pp.838-843.

lung

Description

Survival in patients with advanced lung cancer from the North Central Cancer Treatment Group. Performance scores rate how well the patient can perform usual daily activities.

Format

inst:	Institution code
time:	Survival time in days
status:	censoring status 1=censored, 2=dead
age:	Age in years
sex:	Male=1 Female=2
ph.ecog:	ECOG performance score (0=good 5=dead)
ph.karno:	Karnofsky performance score (bad=0-good=100) rated by physician
pat.karno:	Karnofsky performance score as rated by patient
meal.cal:	Calories consumed at meals
wt.loss:	Weight loss in last six months

Source

Terry Therneau

References

Loprinzi CL. Laurie JA. Wieand HS. Krook JE. Novotny PJ. Kugler JW. Bartel J. Law M. Bateman M. Klatt NE. et al. Prospective evaluation of prognostic variables from patient-completed questionnaires. North Central Cancer Treatment Group. Journal of Clinical Oncology. 12(3):601-7, 1994.

Examples

data(lung)

mbart

Multinomial BART for categorical outcomes with fewer categories

Description

BART is a Bayesian "sum-of-trees" model.

For numeric response y, we have $y = f(x) + \epsilon y = f(x) + \epsilon$, where $\epsilon \sim N(0, 1)$.

For a multinomial response y, P(Y = y|x) = F(f(x)), where F denotes the standard Normal CDF (probit link) or the standard Logistic CDF (logit link).

In both cases, f is the sum of many tree models. The goal is to have very flexible inference for the uknown function f.

In the spirit of "ensemble models", each tree is constrained by a prior to be a weak learner so that it contributes a small amount to the overall fit.

Usage

```
mbart(
      x.train, y.train,
      x.test=matrix(0,0,0), type='pbart',
      ntype=as.integer(
          factor(type,
                 levels=c('wbart', 'pbart', 'lbart'))),
      sparse=FALSE, theta=0, omega=1,
      a=0.5, b=1, augment=FALSE, rho=NULL,
      xinfo=matrix(0,0,0), usequants=FALSE,
      rm.const=TRUE,
      k=2, power=2, base=0.95,
      tau.num=c(NA, 3, 6)[ntype],
      offset=NULL,
      ntree=c(200L, 50L, 50L)[ntype], numcut=100L,
      ndpost=1000L, nskip=100L,
      keepevery=c(1L, 10L, 10L)[ntype],
      printevery=100L, transposed=FALSE,
      hostname=FALSE,
      mc.cores = 2L, ## mc.bart only
      nice = 19L, ## mc.bart only
      seed = 99L ## mc.bart only
     )
mc.mbart(
         x.train, y.train,
         x.test=matrix(0,0,0), type='pbart',
         ntype=as.integer(
             factor(type,
                    levels=c('wbart', 'pbart', 'lbart'))),
         sparse=FALSE, theta=0, omega=1,
         a=0.5, b=1, augment=FALSE, rho=NULL,
         xinfo=matrix(0,0,0), usequants=FALSE,
         rm.const=TRUE,
         k=2, power=2, base=0.95,
         tau.num=c(NA, 3, 6)[ntype],
         offset=NULL,
```

```
ntree=c(200L, 50L, 50L)[ntype], numcut=100L,
ndpost=1000L, nskip=100L,
keepevery=c(1L, 10L, 10L)[ntype],
printevery=100L, transposed=FALSE,
hostname=FALSE,
mc.cores = 2L, ## mc.bart only
nice = 19L, ## mc.bart only
seed = 99L ## mc.bart only
)
```

Arguments

x.train	Explanatory variables for training (in sample) data. May be a matrix or a data frame, with (as usual) rows corresponding to observations and columns to variables. If a variable is a factor in a data frame, it is replaced with dummies. Note that q dummies are created if $q>2$ and one dummy is created if $q=2$, where q is the number of levels of the factor. mbart will generate draws of $f(x)$ for each x which is a row of x.train.
y.train	Categorical dependent variable for training (in sample) data.
x.test	Explanatory variables for test (out of sample) data. Should have same structure as x.train. mbart will generate draws of $f(x)$ for each x which is a row of x.test.
type	You can use this argument to specify the type of fit. 'pbart' for probit BART or 'lbart' for logit BART.
ntype	The integer equivalent of type where 'pbart' is 2 and 'lbart' is 3.
sparse	Whether to perform variable selection based on a sparse Dirichlet prior rather than simply uniform; see Linero 2016.
theta	Set <i>theta</i> parameter; zero means random.
omega	Set <i>omega</i> parameter; zero means random.
а	Sparse parameter for $Beta(a,b)$ prior: $0.5 <= a <= 1$ where lower values inducing more sparsity.
b	Sparse parameter for $Beta(a, b)$ prior; typically, $b = 1$.
rho	Sparse parameter: typically $rho = p$ where p is the number of covariates under consideration.
augment	Whether data augmentation is to be performed in sparse variable selection.
xinfo	You can provide the cutpoints to BART or let BART choose them for you. To provide them, use the xinfo argument to specify a list (matrix) where the items (rows) are the covariates and the contents of the items (columns) are the cutpoints.
usequants	If usequants=FALSE, then the cutpoints in xinfo are generated uniformly; otherwise, if TRUE, uniform quantiles are used for the cutpoints.
rm.const	Whether or not to remove constant variables.

k	For categorical y.train, k is the number of prior standard deviations $f(x)$ is away from +/-3.	
power	Power parameter for tree prior.	
base	Base parameter for tree prior.	
tau.num	The numerator in the tau definition, i.e., tau=tau.num/(k*sqrt(ntree)).	
offset	With Multinomial BART, the centering is $P(yj = 1 x) = F(fj(x) + offset[j])$ where offset defaults to F^{-1}(mean(y.train)). You can use the offset parameter to over-ride these defaults.	
ntree	The number of trees in the sum.	
numcut	The number of possible values of c (see usequants). If a single number if given, this is used for all variables. Otherwise a vector with length equal to $ncol(x.train)$ is required, where the i^{th} element gives the number of c used for the i^{th} variable in x.train. If usequants is false, numcut equally spaced cutoffs are used covering the range of values in the corresponding column of x.train. If usequants is true, then min(numcut, the number of unique values in the corresponding columns of x.train - 1) c values are used.	
ndpost	The number of posterior draws returned.	
nskip	Number of MCMC iterations to be treated as burn in.	
keepevery	Every keepevery draw is kept to be returned to the user.	
printevery	As the MCMC runs, a message is printed every printevery draws.	
transposed	When running mbart in parallel, it is more memory-efficient to transpose x.train and x.test, if any, prior to calling mc.mbart.	
hostname	When running on a cluster occasionally it is useful to track on which node each chain is running; to do so set this argument to TRUE.	
seed	Setting the seed required for reproducible MCMC.	
mc.cores	Number of cores to employ in parallel.	
nice	Set the job niceness. The default niceness is 19: niceness goes from 0 (highest) to 19 (lowest).	

Details

BART is an Bayesian MCMC method. At each MCMC interation, we produce a draw from

f in the categorical y case.

Thus, unlike a lot of other modelling methods in R, we do not produce a single model object from which fits and summaries may be extracted. The output consists of values $f^*(x)$

where * denotes a particular draw. The x is either a row from the training data (x.train).

Value

mbart returns an object of type mbart which is essentially a list.

yhat.train	A matrix with ndpost rows and nrow(x.train)*K columns. Each row corresponds to a draw f^* from the posterior of f and each column corresponds to an estimate for a row of x.train. For the ith row of x.train, we provide the corresponding (i-1)*K+jth column of yhat.train where j=1,,K indexes the categories. Burn-in is dropped.
yhat.train.mean	
	train data fits = mean of yhat.train columns.
varcount	a matrix with ndpost rows and nrow(x.train) columns. Each row is for a draw. For each variable (corresponding to the columns), the total count of the number of times that variable is used in a tree decision rule (over all trees) is given.

In addition, the list has a offset vector giving the value used.

Note that in the multinomial y case yhat.train is f(x) + offset[j].

Author(s)

Robert McCulloch: <robert.e.mcculloch@gmail.com>,
Rodney Sparapani: <rsparapa@mcw.edu>,
Robert Gramacy: <rbg@vt.edu>.

References

Chipman, H., George, E., and McCulloch R. (2010) Bayesian Additive Regression Trees. *The Annals of Applied Statistics*, **4**,**1**, 266-298 <doi: 10.1214/09-AOAS285>.

Friedman, J.H. (1991) Multivariate adaptive regression splines. The Annals of Statistics, 19, 1-67.

Gramacy, RB and Polson, NG (2012) Simulation-based regularized logistic regression. *Bayesian Analysis*, **7**, 567–590.

Holmes, C and Held, L (2006) Bayesian auxiliary variable models for binary and multinomial regression. *Bayesian Analysis*, **1**, 145–68.

Linero, A.R. (2018) Bayesian regression trees for high dimensional prediction and variable selection. *JASA*, **113**, 626–36.

See Also

gbart, alligator

Examples

```
N=500
set.seed(12)
x1=runif(N)
x2=runif(N, max=1-x1)
x3=1-x1-x2
x.train=cbind(x1, x2, x3)
y.train=0
```

```
for(i in 1:N)
    y.train[i]=sum((1:3)*rmultinom(1, 1, x.train[i, ]))
table(y.train)/N
##test mbart with token run to ensure installation works
set.seed(99)
post = mbart(x.train, y.train, nskip=1, ndpost=1)
## Not run:
set.seed(99)
post=mbart(x.train, y.train, x.train)
##mc.post=mbart(x.train, y.train, x.test, mc.cores=8, seed=99)
K=3
i=seq(1, N*K, K)-1
for(j in 1:K)
    print(cor(x.train[, j], post$prob.test.mean[i+j])^2)
```

End(Not run)

mbart2

Multinomial BART for categorical outcomes with more categories

Description

BART is a Bayesian "sum-of-trees" model.

For numeric response y, we have $y = f(x) + \epsilon$ y = f(x) + e, where $\epsilon \sim N(0, 1)$. For a multinomial response y, P(Y = y|x) = F(f(x)), where F denotes the standard Normal CDF (probit link) or the standard Logistic CDF (logit link).

In both cases, f is the sum of many tree models. The goal is to have very flexible inference for the uknown function f.

In the spirit of "ensemble models", each tree is constrained by a prior to be a weak learner so that it contributes a small amount to the overall fit.

Usage

```
mbart2(
    x.train, y.train,
    x.test=matrix(0,0,0), type='lbart',
    ntype=as.integer(
        factor(type,
            levels=c('wbart', 'pbart', 'lbart'))),
    sparse=FALSE, theta=0, omega=1,
    a=0.5, b=1, augment=FALSE, rho=NULL,
    xinfo=matrix(0,0,0), usequants=FALSE,
    rm.const=TRUE,
    k=2, power=2, base=0.95,
```

```
tau.num=c(NA, 3, 6)[ntype],
      offset=NULL,
      ntree=c(200L, 50L, 50L)[ntype], numcut=100L,
      ndpost=1000L, nskip=100L,
      keepevery=c(1L, 10L, 10L)[ntype],
      printevery=100L, transposed=FALSE,
      hostname=FALSE,
      mc.cores = 2L, ## mc.bart only
      nice = 19L, ## mc.bart only
      seed = 99L ## mc.bart only
     )
mc.mbart2(
         x.train, y.train,
         x.test=matrix(0,0,0), type='lbart',
         ntype=as.integer(
             factor(type,
                    levels=c('wbart', 'pbart', 'lbart'))),
         sparse=FALSE, theta=0, omega=1,
         a=0.5, b=1, augment=FALSE, rho=NULL,
         xinfo=matrix(0,0,0), usequants=FALSE,
         rm.const=TRUE,
         k=2, power=2, base=0.95,
         tau.num=c(NA, 3, 6)[ntype],
         offset=NULL,
         ntree=c(200L, 50L, 50L)[ntype], numcut=100L,
         ndpost=1000L, nskip=100L,
         keepevery=c(1L, 10L, 10L)[ntype],
         printevery=100L, transposed=FALSE,
         hostname=FALSE,
        mc.cores = 2L, ## mc.bart only
        nice = 19L, ## mc.bart only
         seed = 99L
                      ## mc.bart only
        )
```

Arguments

x.train	Explanatory variables for training (in sample) data. May be a matrix or a data frame, with (as usual) rows corresponding to observations and columns to variables. If a variable is a factor in a data frame, it is replaced with dummies. Note that q dummies are created if $q>2$ and one dummy is created if $q=2$, where q is the number of levels of the factor. mbart2 will generate draws of $f(x)$ for each x which is a row of x.train.
y.train	Categorical dependent variable for training (in sample) data.
x.test	Explanatory variables for test (out of sample) data.

	Should have same structure as x.train. mbart2 will generate draws of $f(x)$ for each x which is a row of x.test.
type	You can use this argument to specify the type of fit. 'pbart' for probit BART or 'lbart' for logit BART.
ntype	The integer equivalent of type where 'pbart' is 2 and 'lbart' is 3.
sparse	Whether to perform variable selection based on a sparse Dirichlet prior rather than simply uniform; see Linero 2016.
theta	Set <i>theta</i> parameter; zero means random.
omega	Set omega parameter; zero means random.
а	Sparse parameter for $Beta(a,b)$ prior: $0.5 <= a <= 1$ where lower values inducing more sparsity.
b	Sparse parameter for $Beta(a, b)$ prior; typically, $b = 1$.
rho	Sparse parameter: typically $rho = p$ where p is the number of covariates under consideration.
augment	Whether data augmentation is to be performed in sparse variable selection.
xinfo	You can provide the cutpoints to BART or let BART choose them for you. To provide them, use the xinfo argument to specify a list (matrix) where the items (rows) are the covariates and the contents of the items (columns) are the cutpoints.
usequants	If usequants=FALSE, then the cutpoints in xinfo are generated uniformly; oth- erwise, if TRUE, uniform quantiles are used for the cutpoints.
rm.const	Whether or not to remove constant variables.
k	For categorical y.train, k is the number of prior standard deviations $f(x)$ is away from +/-3.
power	Power parameter for tree prior.
base	Base parameter for tree prior.
tau.num	The numerator in the tau definition, i.e., tau=tau.num/(k*sqrt(ntree)).
offset	With Multinomial BART, the centering is $P(yj = 1 x) = F(fj(x)+offset[j])$ where offset defaults to F^{-1}(mean(y.train)). You can use the offset parameter to over-ride these defaults.
ntree	The number of trees in the sum.
numcut	The number of possible values of c (see usequants). If a single number if given, this is used for all variables. Otherwise a vector with length equal to $ncol(x.train)$ is required, where the i^{th} element gives the number of c used for the i^{th} variable in x.train. If usequants is false, numcut equally spaced cutoffs are used covering the range of values in the corresponding column of x.train. If usequants is true, then min(numcut, the number of unique values in the corresponding columns of x.train - 1) c values are used.
ndpost	The number of posterior draws returned.
nskip	Number of MCMC iterations to be treated as burn in.
keepevery	Every keepevery draw is kept to be returned to the user.

printevery	As the MCMC runs, a message is printed every printevery draws.
transposed	When running mbart2 in parallel, it is more memory-efficient to transpose x.train and x.test, if any, prior to calling mc.mbart2.
hostname	When running on a cluster occasionally it is useful to track on which node each chain is running; to do so set this argument to TRUE.
seed	Setting the seed required for reproducible MCMC.
mc.cores	Number of cores to employ in parallel.
nice	Set the job niceness. The default niceness is 19: niceness goes from 0 (highest) to 19 (lowest).

Details

BART is an Bayesian MCMC method. At each MCMC interation, we produce a draw from

f in the categorical y case.

Thus, unlike a lot of other modelling methods in R, we do not produce a single model object from which fits and summaries may be extracted. The output consists of values $f^*(x)$

where * denotes a particular draw. The x is either a row from the training data (x.train).

Value

mbart2 returns an object of type mbart2 which is essentially a list.

yhat.train	A matrix with ndpost rows and nrow(x.train)*K columns. Each row corresponds to a draw f^* from the posterior of f and each column corresponds to an estimate for a row of x.train. For the ith row of x.train, we provide the corresponding (i-1)*K+jth column of yhat.train where j=1,,K indexes the categories. Burn-in is dropped.	
yhat.train.mean		
	train data fits = mean of yhat.train columns.	
varcount	a matrix with ndpost rows and $nrow(x.train)$ columns. Each row is for a draw. For each variable (corresponding to the columns), the total count of the number of times that variable is used in a tree decision rule (over all trees) is given.	

In addition, the list has a offset vector giving the value used.

Note that in the multinomial y case yhat.train is f(x) + offset[j].

Author(s)

Robert McCulloch: <robert.e.mcculloch@gmail.com>,
Rodney Sparapani: <rsparapa@mcw.edu>,
Robert Gramacy: <rbg@vt.edu>.

References

Chipman, H., George, E., and McCulloch R. (2010) Bayesian Additive Regression Trees. *The Annals of Applied Statistics*, **4**,**1**, 266-298 <doi: 10.1214/09-AOAS285>.

Friedman, J.H. (1991) Multivariate adaptive regression splines. The Annals of Statistics, 19, 1–67.

Gramacy, RB and Polson, NG (2012) Simulation-based regularized logistic regression. *Bayesian Analysis*, **7**, 567–590.

Holmes, C and Held, L (2006) Bayesian auxiliary variable models for binary and multinomial regression. *Bayesian Analysis*, **1**, 145–68.

Linero, A.R. (2018) Bayesian regression trees for high dimensional prediction and variable selection. *JASA*, **113**, 626–36.

See Also

gbart, alligator

Examples

```
N=500
set.seed(12)
x1=runif(N)
x2=runif(N, max=1-x1)
x3=1-x1-x2
x.train=cbind(x1, x2, x3)
y.train=0
for(i in 1:N)
    y.train[i]=sum((1:3)*rmultinom(1, 1, x.train[i, ]))
table(y.train)/N
##test mbart2 with token run to ensure installation works
set.seed(99)
post = mbart2(x.train, y.train, nskip=1, ndpost=1)
## Not run:
set.seed(99)
post=mbart2(x.train, y.train, x.train)
##mc.post=mbart2(x.train, y.train, x.test, mc.cores=8, seed=99)
K=3
i=seq(1, N*K, K)-1
for(j in 1:K)
    print(cor(x.train[ , j], post$prob.test.mean[i+j])^2)
```

End(Not run)

mc.cores.openmp

Description

This package was designed for OpenMP. For example, the pwbart function can use OpenMP or the parallel R package for multi-threading. On UNIX/Unix-like systems, OpenMP, if available, is discovered at install time; for the details, see the configure.ac file which can be found in the source version of this package. However, we know of no GPL licensed code available to detect OpenMP on Windows (for Artistic licensed OpenMP detection code on Windows, see the Bioconductor R package rGADEM). To determine whether OpenMP is available at run time, we provide the function documented here.

Usage

mc.cores.openmp()

Value

Returns a zero when OpenMP is not available, otherwise, an integer greater than zero when OpenMP is available (returns one unless you are running in a multi-threaded process).

Author(s)

Robert McCulloch: <robert.e.mcculloch@gmail.com>, Rodney Sparapani: <rsparapa@mcw.edu>.

See Also

pwbart

Examples

mc.cores.openmp()

mc.crisk.pwbart

Predicting new observations with a previously fitted BART model

Description

BART is a Bayesian "sum-of-trees" model. For a numeric response y, we have $y = f(x) + \epsilon$, where $\epsilon \sim N(0, \sigma^2)$.

f is the sum of many tree models. The goal is to have very flexible inference for the uknown function f.

In the spirit of "ensemble models", each tree is constrained by a prior to be a weak learner so that it contributes a small amount to the overall fit.

Usage

Arguments

x.test	Matrix of covariates to predict y for cause 1.
x.test2	Matrix of covariates to predict y for cause 2.
treedraws	<pre>\$treedraws for cause 1.</pre>
treedraws2	<pre>\$treedraws for cause 2.</pre>
binaryOffset	Mean to add on to y prediction for cause 1.
binaryOffset2	Mean to add on to y prediction for cause 2.
mc.cores	Number of threads to utilize.
type	Whether to employ Albert-Chib, 'pbart', or Holmes-Held, 'lbart'.
transposed	When running pwbart or mc.pwbart in parallel, it is more memory-efficient to transpose x.test prior to calling the internal versions of these functions.
nice	Set the job niceness. The default niceness is 19: niceness goes from 0 (highest) to 19 (lowest).

Details

BART is an Bayesian MCMC method. At each MCMC interation, we produce a draw from the joint posterior $(f, \sigma)|(x, y)$ in the numeric y case and just f in the binary y case.

Thus, unlike a lot of other modelling methods in R, we do not produce a single model object from which fits and summaries may be extracted. The output consists of values $f^*(x)$ (and σ^* in the numeric case) where * denotes a particular draw. The x is either a row from the training data (x.train) or the test data (x.test).

Returns an object of type criskbart which is essentially a list with components:

yhat.test	A matrix with ndpost rows and nrow(x.test) columns. Each row corresponds to a draw f^* from the posterior of f and each column corresponds to a row of x.train. The (i, j) value is $f^*(x)$ for the i^{th} kept draw of f and the j^{th} row of x.train. Burn-in is dropped.
surv.test	test data fits for survival probability.
<pre>surv.test.mean</pre>	mean of surv.test over the posterior samples.
prob.test	The probability of suffering cause 1 which is occasionally useful, e.g., in calculating the concordance.
prob.test2	The probability of suffering cause 2 which is occasionally useful, e.g., in calculating the concordance.
cif.test	The cumulative incidence function of cause 1, $F_1(t, x)$, where x's are the rows of the test data.
cif.test2	The cumulative incidence function of cause 2, $F_2(t, x)$, where x's are the rows of the test data.
yhat.test.mean	test data fits = mean of yhat.test columns.
cif.test.mean	mean of cif.test columns for cause 1.
cif.test2.mean	mean of cif.test2 columns for cause 2.

Author(s)

Robert McCulloch: <robert.e.mcculloch@gmail.com>,
Rodney Sparapani: <rsparapa@mcw.edu>.

References

Sparapani, R., Logan, B., McCulloch, R., and Laud, P. (2016) Nonparametric survival analysis using Bayesian Additive Regression Trees (BART). *Statistics in Medicine*, **16:2741-53** <doi:10.1002/sim.6893>.

See Also

pwbart, crisk.bart, mc.crisk.bart

Examples

```
data(transplant)
```

```
delta <- (as.numeric(transplant$event)-1)
## recode so that delta=1 is cause of interest; delta=2 otherwise
delta[delta==1] <- 4
delta[delta==2] <- 1
delta[delta>1] <- 2</pre>
```

```
table(delta, transplant$event)
times <- pmax(1, ceiling(transplant$futime/7)) ## weeks</pre>
##times <- pmax(1, ceiling(transplant$futime/30.5)) ## months</pre>
table(times)
type0 <- 1*(transplant$abo=='0')</pre>
typeA <- 1*(transplant$abo=='A')</pre>
typeB <- 1*(transplant$abo=='B')</pre>
typeAB <- 1*(transplant$abo=='AB')</pre>
table(typeA, type0)
x.train <- cbind(type0, typeA, typeB, typeAB)</pre>
x.test <- cbind(1, 0, 0, 0)
dimnames(x.test)[[2]] <- dimnames(x.train)[[2]]</pre>
## parallel::mcparallel/mccollect do not exist on windows
if(.Platform$OS.type=='unix') {
##test BART with token run to ensure installation works
        post <- mc.crisk.bart(x.train=x.train, times=times, delta=delta,</pre>
                                 seed=99, mc.cores=2, nskip=5, ndpost=5,
                                 keepevery=1)
        pre <- surv.pre.bart(x.train=x.train, x.test=x.test,</pre>
                              times=times, delta=delta)
        K <- post$K
        pred <- mc.crisk.pwbart(pre$tx.test, pre$tx.test,</pre>
                                  post$treedraws, post$treedraws2,
                                  post$binaryOffset, post$binaryOffset2)
}
## Not run:
## run one long MCMC chain in one process
## set.seed(99)
## post <- crisk.bart(x.train=x.train, times=times, delta=delta, x.test=x.test)</pre>
## in the interest of time, consider speeding it up by parallel processing
## run "mc.cores" number of shorter MCMC chains in parallel processes
post <- mc.crisk.bart(x.train=x.train,</pre>
                        times=times, delta=delta,
                        x.test=x.test, seed=99, mc.cores=8)
check <- mc.crisk.pwbart(post$tx.test, post$tx.test,</pre>
                           post$treedraws, post$treedraws2,
                           post$binaryOffset,
                           post$binaryOffset2, mc.cores=8)
## check <- predict(post, newdata=post$tx.test, newdata2=post$tx.test2,</pre>
##
                     mc.cores=8)
```

```
print(c(post$surv.test.mean[1], check$surv.test.mean[1],
        post$surv.test.mean[1]-check$surv.test.mean[1]), digits=22)
print(all(round(post$surv.test.mean, digits=9)==
        round(check$surv.test.mean[1], check$cif.test.mean[1],
        post$cif.test.mean[1]-check$cif.test.mean[1]), digits=22)
print(all(round(post$cif.test.mean, digits=9)==
        round(check$cif.test2.mean[1], check$cif.test2.mean[1],
        post$cif.test2.mean[1], check$cif.test2.mean[1],
        post$cif.test2.mean[1]-check$cif.test2.mean[1],
        post$cif.test2.mean[1]-check$cif.test2.mean[1],
        post$cif.test2.mean[1]-check$cif.test2.mean[1],
        post$cif.test2.mean[1]-check$cif.test2.mean[1],
        post$cif.test2.mean[1]-check$cif.test2.mean[1],
        post$cif.test2.mean[1]-check$cif.test2.mean[1]], digits=22)
print(all(round(post$cif.test2.mean, digits=9)==
        round(check$cif.test2.mean, digits=9)])
## End(Not run)
```

mc.crisk2.pwbart Predicting new observations with a previously fitted BART model

Description

BART is a Bayesian "sum-of-trees" model. For a numeric response y, we have $y = f(x) + \epsilon$, where $\epsilon \sim N(0, \sigma^2)$.

f is the sum of many tree models. The goal is to have very flexible inference for the uknown function f.

In the spirit of "ensemble models", each tree is constrained by a prior to be a weak learner so that it contributes a small amount to the overall fit.

Usage

Arguments

x.test	Matrix of covariates to predict y for cause 1.
x.test2	Matrix of covariates to predict y for cause 2.
treedraws	\$treedraws for cause 1.

treedraws2	<pre>\$treedraws for cause 2.</pre>
binaryOffset	Mean to add on to y prediction for cause 1.
binaryOffset2	Mean to add on to y prediction for cause 2.
mc.cores	Number of threads to utilize.
type	Whether to employ Albert-Chib, 'pbart', or Holmes-Held, 'lbart'.
transposed	When running pwbart or mc.pwbart in parallel, it is more memory-efficient to transpose x.test prior to calling the internal versions of these functions.
nice	Set the job niceness. The default niceness is 19: niceness goes from 0 (highest) to 19 (lowest).

Details

BART is an Bayesian MCMC method. At each MCMC interation, we produce a draw from the joint posterior $(f, \sigma)|(x, y)$ in the numeric y case and just f in the binary y case.

Thus, unlike a lot of other modelling methods in R, we do not produce a single model object from which fits and summaries may be extracted. The output consists of values $f^*(x)$ (and σ^* in the numeric case) where * denotes a particular draw. The x is either a row from the training data (x.train) or the test data (x.test).

Value

Returns an object of type crisk2bart which is essentially a list with components:

yhat.test	A matrix with ndpost rows and nrow(x.test) columns. Each row corresponds to a draw f^* from the posterior of f and each column corresponds to a row of x.train. The (i, j) value is $f^*(x)$ for the i^{th} kept draw of f and the j^{th} row of x.train. Burn-in is dropped.
surv.test	test data fits for survival probability.
<pre>surv.test.mean</pre>	mean of surv.test over the posterior samples.
prob.test	The probability of suffering cause 1 which is occasionally useful, e.g., in calculating the concordance.
prob.test2	The probability of suffering cause 2 which is occasionally useful, e.g., in calculating the concordance.
cif.test	The cumulative incidence function of cause 1, $F_1(t, x)$, where x's are the rows of the test data.
cif.test2	The cumulative incidence function of cause 2, $F_2(t, x)$, where x's are the rows of the test data.
yhat.test.mean	test data fits = mean of yhat.test columns.
cif.test.mean	mean of cif.test columns for cause 1.
cif.test2.mean	mean of cif.test2 columns for cause 2.

Author(s)

Robert McCulloch: <robert.e.mcculloch@gmail.com>,
Rodney Sparapani: <rsparapa@mcw.edu>.

References

Sparapani, R., Logan, B., McCulloch, R., and Laud, P. (2016) Nonparametric survival analysis using Bayesian Additive Regression Trees (BART). *Statistics in Medicine*, **16:2741-53** <doi:10.1002/sim.6893>.

See Also

pwbart, crisk2.bart, mc.crisk2.bart

Examples

```
data(transplant)
```

```
delta <- (as.numeric(transplant$event)-1)</pre>
## recode so that delta=1 is cause of interest; delta=2 otherwise
delta[delta==1] <- 4</pre>
delta[delta==2] <- 1</pre>
delta[delta>1] <- 2</pre>
table(delta, transplant$event)
times <- pmax(1, ceiling(transplant$futime/7)) ## weeks</pre>
##times <- pmax(1, ceiling(transplant$futime/30.5)) ## months</pre>
table(times)
type0 <- 1*(transplant$abo=='0')</pre>
typeA <- 1*(transplant$abo=='A')</pre>
typeB <- 1*(transplant$abo=='B')</pre>
typeAB <- 1*(transplant$abo=='AB')</pre>
table(typeA, type0)
x.train <- cbind(type0, typeA, typeB, typeAB)</pre>
x.test <- cbind(1, 0, 0, 0)
dimnames(x.test)[[2]] <- dimnames(x.train)[[2]]</pre>
## parallel::mcparallel/mccollect do not exist on windows
if(.Platform$0S.type=='unix') {
##test BART with token run to ensure installation works
        post <- mc.crisk2.bart(x.train=x.train, times=times, delta=delta,</pre>
                                  seed=99, mc.cores=2, nskip=5, ndpost=5,
                                  keepevery=1)
        pre <- surv.pre.bart(x.train=x.train, x.test=x.test,</pre>
                                times=times, delta=delta)
```

K <- post\$K

```
pred <- mc.crisk2.pwbart(pre$tx.test, pre$tx.test,</pre>
                                 post$treedraws, post$treedraws2,
                                 post$binaryOffset, post$binaryOffset2)
}
## Not run:
## run one long MCMC chain in one process
## set.seed(99)
## post <- crisk2.bart(x.train=x.train, times=times, delta=delta, x.test=x.test)</pre>
## in the interest of time, consider speeding it up by parallel processing
## run "mc.cores" number of shorter MCMC chains in parallel processes
post <- mc.crisk2.bart(x.train=x.train,</pre>
                       times=times, delta=delta,
                       x.test=x.test, seed=99, mc.cores=8)
check <- mc.crisk2.pwbart(post$tx.test, post$tx.test,</pre>
                           post$treedraws, post$treedraws2,
                           post$binaryOffset,
                           post$binaryOffset2, mc.cores=8)
## check <- predict(post, newdata=post$tx.test, newdata2=post$tx.test2,</pre>
##
                    mc.cores=8)
print(c(post$surv.test.mean[1], check$surv.test.mean[1],
        post$surv.test.mean[1]-check$surv.test.mean[1]), digits=22)
print(all(round(post$surv.test.mean, digits=9)==
    round(check$surv.test.mean, digits=9)))
print(c(post$cif.test.mean[1], check$cif.test.mean[1],
        post$cif.test.mean[1]-check$cif.test.mean[1]), digits=22)
print(all(round(post$cif.test.mean, digits=9)==
    round(check$cif.test.mean, digits=9)))
print(c(post$cif.test2.mean[1], check$cif.test2.mean[1],
        post$cif.test2.mean[1]-check$cif.test2.mean[1]), digits=22)
print(all(round(post$cif.test2.mean, digits=9)==
    round(check$cif.test2.mean, digits=9)))
```

End(Not run)

mc.lbart

Logit BART for dichotomous outcomes with Logistic latents and parallel computation

Description

BART is a Bayesian "sum-of-trees" model.

For numeric response y, we have $y = f(x) + \epsilon$, where $\epsilon \sim Log(0, 1)$.

For a binary response y, P(Y = 1|x) = F(f(x)), where F denotes the standard Logistic CDF (logit link).

In both cases, f is the sum of many tree models. The goal is to have very flexible inference for the uknown function f.

In the spirit of "ensemble models", each tree is constrained by a prior to be a weak learner so that it contributes a small amount to the overall fit.

Usage

```
mc.lbart(
    x.train, y.train, x.test=matrix(0.0,0,0),
    sparse=FALSE, a=0.5, b=1, augment=FALSE, rho=NULL,
    xinfo=matrix(0.0,0,0), usequants=FALSE,
    cont=FALSE, rm.const=TRUE, tau.interval=0.95,
    k=2.0, power=2.0, base=.95,
    binaryOffset=NULL,
    ntree=50L, numcut=100L,
    ndpost=1000L, nskip=100L,
    keepevery=1L, printevery=100,
    keeptrainfits=TRUE, transposed=FALSE,
    mc.cores = 2L, nice = 19L,
    seed = 99L
```

```
)
```

Arguments

x.train	Explanatory variables for training (in sample) data.
	May be a matrix or a data frame, with (as usual) rows corresponding to obser-
	vations and columns to variables.
	If a variable is a factor in a data frame, it is replaced with dummies. Note that q dummies are created if $q>2$ and one dummy is created if $q=2$, where q is the number of levels of the factor. lbart will generate draws of $f(x)$ for each x which is a row of x.train.
y.train	Dependent variable for training (in sample) data. If y is numeric a continous response model is fit (normal errors).
	If y is a factor (or just has values 0 and 1) then a binary response model with a logit link is fit.
x.test	Explanatory variables for test (out of sample) data. Should have same structure as x.train.
	lbart will generate draws of $f(x)$ for each x which is a row of x.test.
sparse	Whether to perform variable selection based on a sparse Dirichlet prior rather than simply uniform; see Linero 2016.

а	Sparse parameter for $Beta(a, b)$ prior: $0.5 <= a <= 1$ where lower values inducing more sparsity.
b	Sparse parameter for $Beta(a, b)$ prior; typically, $b = 1$.
rho	Sparse parameter: typically $rho = p$ where p is the number of covariates under consideration.
augment	Whether data augmentation is to be performed in sparse variable selection.
xinfo	You can provide the cutpoints to BART or let BART choose them for you. To provide them, use the xinfo argument to specify a list (matrix) where the items (rows) are the covariates and the contents of the items (columns) are the cutpoints.
usequants	If usequants=FALSE, then the cutpoints in xinfo are generated uniformly; oth- erwise, if TRUE, uniform quantiles are used for the cutpoints.
cont	Whether or not to assume all variables are continuous.
rm.const	Whether or not to remove constant variables.
tau.interval	The width of the interval to scale the variance for the terminal leaf values.
k	For numeric y, k is the number of prior standard deviations $E(Y x) = f(x)$ is away from +/5. The response (y.train) is internally scaled to range from5 to .5. For binary y, k is the number of prior standard deviations $f(x)$ is away from +/-3. In both cases, the bigger k is, the more conservative the fitting will be.
power	Power parameter for tree prior.
base	Base parameter for tree prior.
binaryOffset	Used for binary y. The model is $P(Y = 1 x) = F(f(x) + binaryOffset)$.
ntree	The number of trees in the sum.
numcut	The number of possible values of c (see usequants). If a single number if given, this is used for all variables. Otherwise a vector with length equal to $ncol(x.train)$ is required, where the i^{th} element gives the number of c used for the i^{th} variable in x.train. If usequants is false, numcut equally spaced cutoffs are used covering the range of values in the corresponding column of x.train. If usequants is true, then min(numcut, the number of unique values in the corresponding columns of x.train - 1) c values are used.
ndpost	The number of posterior draws returned.
nskip	Number of MCMC iterations to be treated as burn in.
keepevery	Every keepevery draw is kept to be returned to the user.
printevery	As the MCMC runs, a message is printed every printevery draws.
keeptrainfits	Whether to keep yhat.train or not.
transposed	When running lbart in parallel, it is more memory-efficient to transpose x.train and x.test, if any, prior to calling mc.lbart.
seed	Setting the seed required for reproducible MCMC.
mc.cores	Number of cores to employ in parallel.
nice	Set the job niceness. The default niceness is 19: niceness goes from 0 (highest) to 19 (lowest).

Details

BART is an Bayesian MCMC method. At each MCMC interation, we produce a draw from the joint posterior $(f, \sigma)|(x, y)$ in the numeric y case and just f in the binary y case.

Thus, unlike a lot of other modelling methods in R, we do not produce a single model object from which fits and summaries may be extracted. The output consists of values $f^*(x)$ (and σ^* in the numeric case) where * denotes a particular draw. The x is either a row from the training data (x.train) or the test data (x.test).

Value

mc.lbart returns an object of type lbart which is essentially a list.

yhat.train	A matrix with ndpost rows and nrow(x.train) columns. Each row corresponds to a draw f^* from the posterior of f and each column corresponds to a row of x.train. The (i, j) value is $f^*(x)$ for the i^{th} kept draw of f and the j^{th} row of x.train. Burn-in is dropped.
yhat.test	Same as yhat.train but now the x's are the rows of the test data.
yhat.train.mean	
	train data fits = mean of yhat.train columns.
<pre>yhat.test.mean</pre>	test data fits = mean of yhat.test columns.
varcount	a matrix with ndpost rows and nrow(x.train) columns. Each row is for a draw. For each variable (corresponding to the columns), the total count of the number of times that variable is used in a tree decision rule (over all trees) is given.

In addition, the list has a binaryOffset giving the value used.

Note that in the binary y, case yhat.train and yhat.test are f(x) + binaryOffset. If you want draws of the probability P(Y = 1|x) you need to apply the Logistic cdf (plogis) to these values.

Author(s)

Robert McCulloch: <robert.e.mcculloch@gmail.com>,
Rodney Sparapani: <rsparapa@mcw.edu>.

References

Chipman, H., George, E., and McCulloch R. (2010) Bayesian Additive Regression Trees. *The Annals of Applied Statistics*, **4**,**1**, 266-298 <doi: 10.1214/09-AOAS285>.

Friedman, J.H. (1991) Multivariate adaptive regression splines. The Annals of Statistics, 19, 1–67.

Gramacy, RB and Polson, NG (2012) Simulation-based regularized logistic regression. *Bayesian Analysis*, **7**, 567–590.

Holmes, C and Held, L (2006) Bayesian auxiliary variable models for binary and multinomial regression. *Bayesian Analysis*, **1**, 145–68.

Linero, A.R. (2018) Bayesian regression trees for high dimensional prediction and variable selection. *JASA*, **113**, 626–36.

mc.lbart

See Also

lbart

```
set.seed(99)
n=5000
x = sort(-2+4*runif(n))
X=matrix(x,ncol=1)
f = function(x) \{return((1/2)*x^3)\}
FL = function(x) \{return(exp(x)/(1+exp(x)))\}
pv = FL(f(x))
y = rbinom(n, 1, pv)
np=100
xp=-2+4*(1:np)/np
Xp=matrix(xp,ncol=1)
## parallel::mcparallel/mccollect do not exist on windows
## if(.Platform$OS.type=='unix') {
## ##test BART with token run to ensure installation works
##
       mf = mc.lbart(X, y, nskip=5, ndpost=5, mc.cores=1, seed=99)
## }
## Not run:
set.seed(99)
pf = lbart(X,y,Xp)
plot(f(Xp), pf$yhat.test.mean, xlim=c(-4, 4), ylim=c(-4, 4),
     xlab='True f(x)', ylab='BART f(x)')
lines(c(-4, 4), c(-4, 4))
mf = mc.lbart(X,y,Xp, mc.cores=4, seed=99)
plot(f(Xp), mf$yhat.test.mean, xlim=c(-4, 4), ylim=c(-4, 4),
     xlab='True f(x)', ylab='BART f(x)')
lines(c(-4, 4), c(-4, 4))
par(mfrow=c(2,2))
plot(range(xp), range(pf$yhat.test), xlab='x', ylab='f(x)', type='n')
lines(x,f(x),col='blue',lwd=2)
lines(xp,apply(pf$yhat.test,2,mean),col='red')
qpl = apply(pf$yhat.test,2,quantile,probs=c(.025,.975))
lines(xp,qpl[1,],col='green',lty=1)
lines(xp,qpl[2,],col='green',lty=1)
title(main='BART::lbart f(x) with 0.95 intervals')
plot(range(xp),range(mf$yhat.test),xlab='x',ylab='f(x)',type='n')
lines(x,f(x),col='blue',lwd=2)
lines(xp,apply(mf$yhat.test,2,mean),col='red')
qpl = apply(mf$yhat.test,2,quantile,probs=c(.025,.975))
lines(xp,qpl[1,],col='green',lty=1)
```

```
lines(xp,qpl[2,],col='green',lty=1)
title(main='BART::mc.lbart f(x) with 0.95 intervals')
plot(pf$yhat.test.mean,apply(mf$yhat.test,2,mean),xlab='BART::lbart',ylab='BART::mc.lbart')
abline(0,1,col='red')
title(main="BART::lbart f(x) vs. BART::mc.lbart f(x)")
## End(Not run)
```

mc.pbart

Probit BART for dichotomous outcomes with Normal latents and parallel computation

Description

BART is a Bayesian "sum-of-trees" model.

For a binary response y, P(Y = 1|x) = F(f(x)), where F denotes the standard normal cdf (probit link).

In both cases, f is the sum of many tree models. The goal is to have very flexible inference for the uknown function f.

In the spirit of "ensemble models", each tree is constrained by a prior to be a weak learner so that it contributes a small amount to the overall fit.

Usage

```
mc.pbart(
    x.train, y.train, x.test=matrix(0.0,0,0),
    sparse=FALSE, theta=0, omega=1,
    a=0.5, b=1, augment=FALSE, rho=NULL,
    xinfo=matrix(0.0,0,0), usequants=FALSE,
    cont=FALSE, rm.const=TRUE,
    k=2.0, power=2.0, base=.95,
    binaryOffset=NULL,
    ntree=50L, numcut=100L,
    ndpost=1000L, nskip=100L,
    keepevery=1L, printevery=100,
    keeptrainfits=TRUE, transposed=FALSE,
    mc.cores = 2L, nice = 19L,
    seed = 99L
)
```

mc.pbart

Arguments

x.train	Explanatory variables for training (in sample) data. May be a matrix or a data frame, with (as usual) rows corresponding to observations and columns to variables. If a variable is a factor in a data frame, it is replaced with dummies. Note that q dummies are created if $q>2$ and one dummy is created if $q=2$, where q is the number of levels of the factor. pbart will generate draws of $f(x)$ for each x which is a row of x.train.
y.train	Binary dependent variable for training (in sample) data.
x.test	Explanatory variables for test (out of sample) data. Should have same structure as x.train. pbart will generate draws of $f(x)$ for each x which is a row of x.test.
sparse	Whether to perform variable selection based on a sparse Dirichlet prior rather than simply uniform; see Linero 2016.
theta	Set <i>theta</i> parameter; zero means random.
omega	Set <i>omega</i> parameter; zero means random.
a	Sparse parameter for $Beta(a,b)$ prior: $0.5 <= a <= 1$ where lower values inducing more sparsity.
b	Sparse parameter for $Beta(a, b)$ prior; typically, $b = 1$.
rho	Sparse parameter: typically $rho = p$ where p is the number of covariates under consideration.
augment	Whether data augmentation is to be performed in sparse variable selection.
xinfo	You can provide the cutpoints to BART or let BART choose them for you. To provide them, use the xinfo argument to specify a list (matrix) where the items (rows) are the covariates and the contents of the items (columns) are the cutpoints.
usequants	If usequants=FALSE, then the cutpoints in xinfo are generated uniformly; otherwise, if TRUE, uniform quantiles are used for the cutpoints.
cont	Whether or not to assume all variables are continuous.
rm.const	Whether or not to remove constant variables.
k	For binary y, k is the number of prior standard deviations $f(x)$ is away from +/-3.
	The bigger k is, the more conservative the fitting will be.
power	Power parameter for tree prior.
base	Base parameter for tree prior.
binaryOffset	Used for binary y. The model is $P(Y = 1 x) = F(f(x) + binaryOffset)$.
ntree	The number of trees in the sum.

numcut	The number of possible values of c (see usequants). If a single number if given, this is used for all variables. Otherwise a vector with length equal to $ncol(x.train)$ is required, where the i^{th} element gives the number of c used for the i^{th} variable in x.train. If usequants is false, numcut equally spaced cutoffs are used covering the range of values in the corresponding column of x.train. If usequants is true, then min(numcut, the number of unique values in the corresponding columns of x.train - 1) c values are used.
ndpost	The number of posterior draws returned.
nskip	Number of MCMC iterations to be treated as burn in.
keepevery	Every keepevery draw is kept to be returned to the user.
printevery	As the MCMC runs, a message is printed every printevery draws.
keeptrainfits	Whether to keep yhat.train or not.
transposed	When running pbart in parallel, it is more memory-efficient to transpose x.train and x.test, if any, prior to calling mc.pbart.
seed	Setting the seed required for reproducible MCMC.
mc.cores	Number of cores to employ in parallel.
nice	Set the job niceness. The default niceness is 19: niceness goes from 0 (highest) to 19 (lowest).

Details

BART is an Bayesian MCMC method. At each MCMC interation, we produce a draw from

f in the binary y case.

Thus, unlike a lot of other modelling methods in R, we do not produce a single model object from which fits and summaries may be extracted. The output consists of values $f^*(x)$ where * denotes a particular draw. The x is either a row from the training data (x.train) or the test data (x.test).

Value

mc.pbart returns an object of type pbart which is essentially a list.

yhat.train	A matrix with ndpost rows and nrow(x.train) columns. Each row corresponds to a draw f^* from the posterior of f and each column corresponds to a row of x.train. The (i, j) value is $f^*(x)$ for the i^{th} kept draw of f and the j^{th} row of x.train. Burn-in is dropped.
yhat.test	Same as yhat.train but now the x's are the rows of the test data.
varcount	a matrix with ndpost rows and $nrow(x.train)$ columns. Each row is for a draw. For each variable (corresponding to the columns), the total count of the number of times that variable is used in a tree decision rule (over all trees) is given.

In addition the list has a binaryOffset component giving the value used.

Note that in the binary y, case yhat.train and yhat.test are f(x) + binaryOffset. If you want draws of the probability P(Y = 1|x) you need to apply the normal cdf (pnorm) to these values.

mc.pbart

Author(s)

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References

Chipman, H., George, E., and McCulloch R. (2010) Bayesian Additive Regression Trees. *The Annals of Applied Statistics*, **4**,**1**, 266-298 <doi: 10.1214/09-AOAS285>.

Friedman, J.H. (1991) Multivariate adaptive regression splines. The Annals of Statistics, 19, 1–67.

Gramacy, RB and Polson, NG (2012) Simulation-based regularized logistic regression. *Bayesian Analysis*, **7**, 567–590.

Holmes, C and Held, L (2006) Bayesian auxiliary variable models for binary and multinomial regression. *Bayesian Analysis*, **1**, 145–68.

Linero, A.R. (2018) Bayesian regression trees for high dimensional prediction and variable selection. *JASA*, **113**, 626–36.

See Also

pbart

```
set.seed(99)
n=5000
x = sort(-2+4*runif(n))
X=matrix(x,ncol=1)
f = function(x) \{return((1/2)*x^3)\}
FL = function(x) \{return(exp(x)/(1+exp(x)))\}
pv = FL(f(x))
y = rbinom(n,1,pv)
np=100
xp=-2+4*(1:np)/np
Xp=matrix(xp,ncol=1)
## parallel::mcparallel/mccollect do not exist on windows
if(.Platform$OS.type=='unix') {
##test BART with token run to ensure installation works
    mf = mc.pbart(X, y, nskip=5, ndpost=5, mc.cores=1, seed=99)
}
## Not run:
set.seed(99)
pf = pbart(X, y, Xp)
## plot(f(Xp), pf$yhat.test.mean, xlim=c(-4, 4), ylim=c(-4, 4),
##
        xlab='True f(x)', ylab='BART f(x)')
## lines(c(-4, 4), c(-4, 4))
mf = mc.pbart(X,y,Xp, mc.cores=4, seed=99)
```

```
## plot(f(Xp), mf$yhat.test.mean, xlim=c(-4, 4), ylim=c(-4, 4),
       xlab='True f(x)', ylab='BART f(x)')
##
## lines(c(-4, 4), c(-4, 4))
par(mfrow=c(2,2))
plot(range(xp),range(pf$yhat.test),xlab='x',ylab='f(x)',type='n')
lines(x,f(x),col='blue',lwd=2)
lines(xp,apply(pf$yhat.test,2,mean),col='red')
qpl = apply(pf$yhat.test,2,quantile,probs=c(.025,.975))
lines(xp,qpl[1,],col='green',lty=1)
lines(xp,qpl[2,],col='green',lty=1)
title(main='BART::pbart f(x) with 0.95 intervals')
plot(range(xp), range(mf$yhat.test), xlab='x', ylab='f(x)', type='n')
lines(x,f(x),col='blue',lwd=2)
lines(xp,apply(mf$yhat.test,2,mean),col='red')
qpl = apply(mf$yhat.test,2,quantile,probs=c(.025,.975))
lines(xp,qpl[1,],col='green',lty=1)
lines(xp,qpl[2,],col='green',lty=1)
title(main='BART::mc.pbart f(x) with 0.95 intervals')
## plot(pf$yhat.test.mean,apply(mf$yhat.test,2,mean),xlab='BART::pbart',ylab='BART::mc.pbart')
## abline(0,1,col='red')
## title(main="BART::pbart f(x) vs. BART::mc.pbart f(x)")
## End(Not run)
```

mc.surv.pwbart Predicting new observations with a previously fitted BART model

Description

BART is a Bayesian "sum-of-trees" model. For a numeric response y, we have $y = f(x) + \epsilon$, where $\epsilon \sim N(0, \sigma^2)$.

f is the sum of many tree models. The goal is to have very flexible inference for the uknown function f.

In the spirit of "ensemble models", each tree is constrained by a prior to be a weak learner so that it contributes a small amount to the overall fit.

Usage

```
surv.pwbart(
```

```
x.test,
treedraws,
binaryOffset=0,
mc.cores=1L,
type='pbart',
```

```
transposed=FALSE, nice=19L
              )
mc.surv.pwbart(
                x.test,
                treedraws,
                binaryOffset=0,
                mc.cores=2L,
                type='pbart',
                transposed=FALSE, nice=19L
              )
mc.recur.pwbart(
                x.test,
                treedraws,
                binaryOffset=0,
                mc.cores=2L,
                type='pbart',
                 transposed=FALSE, nice=19L
               )
```

Arguments

x.test	Matrix of covariates to predict y for.
binaryOffset	Mean to add on to y prediction.
treedraws	<pre>\$treedraws returned from surv.bart, mc.surv.bart, recur.bart or mc.recur.bart</pre>
mc.cores	Number of threads to utilize.
type	Whether to employ Albert-Chib, 'pbart', or Holmes-Held, 'lbart'.
transposed	When running pwbart or mc.pwbart in parallel, it is more memory-efficient to transpose x.test prior to calling the internal versions of these functions.
nice	Set the job niceness. The default niceness is 19: niceness goes from 0 (highest) to 19 (lowest).

Details

BART is an Bayesian MCMC method. At each MCMC interation, we produce a draw from the joint posterior $(f, \sigma)|(x, y)$ in the numeric y case and just f in the binary y case.

Thus, unlike a lot of other modelling methods in R, we do not produce a single model object from which fits and summaries may be extracted. The output consists of values $f^*(x)$ (and σ^* in the numeric case) where * denotes a particular draw. The x is either a row from the training data (x.train) or the test data (x.test).

Value

Returns an object of type survbart which is essentially a list with components:

yhat.test	A matrix with ndpost rows and nrow(x.test) columns. Each row corresponds to a draw f^* from the posterior of f and each column corresponds to a row of x.train. The (i, j) value is $f^*(x)$ for the i^{th} kept draw of f and the j^{th} row of x.train. Burn-in is dropped.
surv.test	test data fits for survival probability: not available for mc.recur.pwbart.
<pre>surv.test.mean</pre>	mean of surv.test over the posterior samples: not available for mc.recur.pwbart.
haz.test	test data fits for hazard: available for mc.recur.pwbart only.
haz.test.mean	mean of haz.test over the posterior samples: available for mc.recur.pwbart only.
cum.test	test data fits for cumulative hazard: available for mc.recur.pwbart only.
cum.test.mean	mean of cum.test over the posterior samples: available for mc.recur.pwbart only.

Author(s)

Robert McCulloch: <robert.e.mcculloch@gmail.com>, Rodney Sparapani: <rsparapa@mcw.edu>.

References

Sparapani, R., Logan, B., McCulloch, R., and Laud, P. (2016) Nonparametric survival analysis using Bayesian Additive Regression Trees (BART). *Statistics in Medicine*, **16:2741-53** <doi:10.1002/sim.6893>.

See Also

pwbart

mc.surv.pwbart

```
Male=1 Female=2
## lung$sex:
                    Karnofsky performance score (dead=0:normal=100:by=10)
## lung$ph.karno:
##
                    rated by physician
dimnames(x.train)[[2]] <- c('age(yr)', 'M(1):F(2)', 'ph.karno(0:100:10)')
summary(x.train[ , 1])
table(x.train[ , 2])
table(x.train[ , 3])
x.test <- matrix(nrow=84, ncol=3) ## matrix of covariate scenarios</pre>
dimnames(x.test)[[2]] <- dimnames(x.train)[[2]]</pre>
i <- 1
for(age in 5*(9:15)) for(sex in 1:2) for(ph.karno in 10*(5:10)) {
    x.test[i, ] <- c(age, sex, ph.karno)</pre>
    i <- i+1
}
## this x.test is relatively small, but often you will want to
## predict for a large x.test matrix which may cause problems
## due to consumption of RAM so we can predict separately
## mcparallel/mccollect do not exist on windows
if(.Platform$OS.type=='unix') {
##test BART with token run to ensure installation works
    set.seed(99)
  post <- surv.bart(x.train=x.train, times=times, delta=delta, nskip=5, ndpost=5, keepevery=1)</pre>
    pre <- surv.pre.bart(x.train=x.train, times=times, delta=delta, x.test=x.test)</pre>
   pred <- mc.surv.pwbart(pre$tx.test, post$treedraws, post$binaryOffset)</pre>
}
## Not run:
## run one long MCMC chain in one process
set.seed(99)
post <- surv.bart(x.train=x.train, times=times, delta=delta)</pre>
## run "mc.cores" number of shorter MCMC chains in parallel processes
## post <- mc.surv.bart(x.train=x.train, times=times, delta=delta,</pre>
##
                        mc.cores=8, seed=99)
pre <- surv.pre.bart(x.train=x.train, times=times, delta=delta, x.test=x.test)</pre>
pred <- surv.pwbart(pre$tx.test, post$treedraws, post$binaryOffset)</pre>
## let's look at some survival curves
## first, a younger group with a healthier KPS
## age 50 with KPS=90: males and females
## males: row 17, females: row 23
```

End(Not run)

mc.wbart

BART for continuous outcomes with parallel computation

Description

BART is a Bayesian "sum-of-trees" model. For numeric response y, we have $y = f(x) + \epsilon$, where $\epsilon \sim N(0, \sigma^2)$.

In both cases, f is the sum of many tree models. The goal is to have very flexible inference for the uknown function f.

In the spirit of "ensemble models", each tree is constrained by a prior to be a weak learner so that it contributes a small amount to the overall fit.

Usage

```
mc.wbart(
   x.train, y.train, x.test=matrix(0.0,0,0),
   sparse=FALSE, theta=0, omega=1,
   a=0.5, b=1, augment=FALSE, rho=NULL,
   xinfo=matrix(0.0,0,0), usequants=FALSE,
   cont=FALSE, rm.const=TRUE,
   sigest=NA, sigdf=3, sigguant=0.90,
   k=2.0, power=2.0, base=.95,
   sigmaf=NA, lambda=NA, fmean=mean(y.train),
   w=rep(1,length(y.train)),
   ntree=200L, numcut=100L,
   ndpost=1000L, nskip=100L,
   keepevery=1L, printevery=100,
   keeptrainfits=TRUE, transposed=FALSE,
  mc.cores = 2L, nice = 19L,
   seed = 99L
)
```

mc.wbart

Arguments

x.train	Explanatory variables for training (in sample) data. May be a matrix or a data frame, with (as usual) rows corresponding to obser- vations and columns to variables. If a variable is a factor in a data frame, it is replaced with dummies. Note that
	q dummies are created if q>2 and one dummy is created if q=2, where q is the number of levels of the factor. wbart will generate draws of $f(x)$ for each x which is a row of x.train.
y.train	Dependent variable for training (in sample) data. If y is numeric a continous response model is fit (normal errors).
x.test	Explanatory variables for test (out of sample) data. Should have same structure as x.train. wbart will generate draws of $f(x)$ for each x which is a row of x.test.
sparse	Whether to perform variable selection based on a sparse Dirichlet prior rather than simply uniform; see Linero 2016.
theta	Set <i>theta</i> parameter; zero means random.
omega	Set <i>omega</i> parameter; zero means random.
a	Sparse parameter for $Beta(a, b)$ prior: $0.5 <= a <= 1$ where lower values inducing more sparsity.
b	Sparse parameter for $Beta(a, b)$ prior; typically, $b = 1$.
rho	Sparse parameter: typically $rho = p$ where p is the number of covariates under consideration.
augment	Whether data augmentation is to be performed in sparse variable selection.
xinfo	You can provide the cutpoints to BART or let BART choose them for you. To provide them, use the xinfo argument to specify a list (matrix) where the items (rows) are the covariates and the contents of the items (columns) are the cutpoints.
usequants	If usequants=FALSE, then the cutpoints in xinfo are generated uniformly; oth- erwise, if TRUE, uniform quantiles are used for the cutpoints.
cont	Whether or not to assume all variables are continuous.
rm.const	Whether or not to remove constant variables.
sigest	The prior for the error variance (σ^2) is inverted chi-squared (the standard con- ditionally conjugate prior). The prior is specified by choosing the degrees of freedom, a rough estimate of the corresponding standard deviation and a quan- tile to put this rough estimate at. If sigest=NA then the rough estimate will be the usual least squares estimator. Otherwise the supplied value will be used.
sigdf	Degrees of freedom for error variance prior.
sigquant	The quantile of the prior that the rough estimate (see sigest) is placed at. The closer the quantile is to 1, the more aggresive the fit will be as you are putting more prior weight on error standard deviations (σ) less than the rough estimate.

k	For numeric y, k is the number of prior standard deviations $E(Y x) = f(x)$ is away from +/5. The response (y.train) is internally scaled to range from5 to .5.
	The bigger k is, the more conservative the fitting will be.
power	Power parameter for tree prior.
base	Base parameter for tree prior.
sigmaf	The SD of f.
lambda	The scale of the prior for the variance.
fmean	BART operates on y.train centered by fmean.
w	Vector of weights which multiply the variance.
ntree	The number of trees in the sum.
numcut	The number of possible values of c (see usequants). If a single number if given, this is used for all variables. Otherwise a vector with length equal to $ncol(x.train)$ is required, where the i^{th} element gives the number of c used for the i^{th} variable in x.train. If usequants is false, numcut equally spaced cutoffs are used covering the range of values in the corresponding column of x.train. If usequants is true, then min(numcut, the number of unique values in the corresponding columns of x.train - 1) c values are used.
ndpost	The number of posterior draws returned.
nskip	Number of MCMC iterations to be treated as burn in.
keepevery	Every keepevery draw is kept to be returned to the user.
printevery	As the MCMC runs, a message is printed every printevery draws.
keeptrainfits	Whether to keep yhat.train or not.
transposed	When running wbart in parallel, it is more memory-efficient to transpose x.train and x.test, if any, prior to calling mc.wbart.
seed	Setting the seed required for reproducible MCMC.
mc.cores	Number of cores to employ in parallel.
nice	Set the job niceness. The default niceness is 19: niceness goes from 0 (highest) to 19 (lowest).

Details

BART is an Bayesian MCMC method. At each MCMC interation, we produce a draw from the joint posterior $(f, \sigma)|(x, y)$ in the numeric y case.

Thus, unlike a lot of other modelling methods in R, we do not produce a single model object from which fits and summaries may be extracted. The output consists of values $f^*(x)$ (and σ^* in the numeric case) where * denotes a particular draw. The x is either a row from the training data (x.train) or the test data (x.test).

mc.wbart

Value

mc.wbart returns an object of type wbart which is essentially a list.

yhat.train	A matrix with ndpost rows and nrow(x.train) columns. Each row corresponds to a draw f^* from the posterior of f and each column corresponds to a row of x.train. The (i, j) value is $f^*(x)$ for the i^{th} kept draw of f and the j^{th} row of x.train. Burn-in is dropped.	
yhat.test	Same as yhat.train but now the x's are the rows of the test data.	
yhat.train.mean		
	train data fits = mean of yhat.train columns.	
yhat.test.mean	test data fits = mean of yhat.test columns.	
varcount	a matrix with ndpost rows and nrow(x.train) columns. Each row is for a draw. For each variable (corresponding to the columns), the total count of the number of times that variable is used in a tree decision rule (over all trees) is given.	

Author(s)

Robert McCulloch: <robert.e.mcculloch@gmail.com>, Rodney Sparapani: <rsparapa@mcw.edu>.

References

Chipman, H., George, E., and McCulloch R. (2010) Bayesian Additive Regression Trees. *The Annals of Applied Statistics*, **4**,**1**, 266-298 <doi:10.1214/09-AOAS285>.

Chipman, H., George, E., and McCulloch R. (2006) Bayesian Ensemble Learning. Advances in Neural Information Processing Systems 19, Scholkopf, Platt and Hoffman, Eds., MIT Press, Cambridge, MA, 265-272.

Friedman, J.H. (1991) Multivariate adaptive regression splines. The Annals of Statistics, 19, 1–67.

Linero, A.R. (2018) Bayesian regression trees for high dimensional prediction and variable selection. *JASA*, **113**, 626–36.

See Also

wbart

```
##simulate data (example from Friedman MARS paper)
f = function(x){
10*sin(pi*x[,1]*x[,2]) + 20*(x[,3]-.5)^2+10*x[,4]+5*x[,5]
}
sigma = 1.0  #y = f(x) + sigma*z , z~N(0,1)
n = 100  #number of observations
set.seed(99)
x=matrix(runif(n*10),n,10) #10 variables, only first 5 matter
Ey = f(x)
y=Ey+sigma*rnorm(n)
```

```
lmFit = lm(y~.,data.frame(x,y)) #compare lm fit to BART later
## parallel::mcparallel/mccollect do not exist on windows
if(.Platform$OS.type=='unix') {
##test BART with token run to ensure installation works
    bartFit = mc.wbart(x,y,mc.cores=2,seed=99,nskip=5,ndpost=5)
}
## Not run:
##run BART
bartFit = mc.wbart(x,y,mc.cores=5,seed=99)
##compare BART fit to linear matter and truth = Ey
fitmat = cbind(y,Ey,lmFit$fitted,bartFit$yhat.train.mean)
colnames(fitmat) = c('y','Ey','lm','bart')
print(cor(fitmat))
## End(Not run)
```

mc.wbart.gse

Global SE variable selection for BART with parallel computation

Description

Here we implement the global SE method for variable selection in nonparametric survival analysis with BART. Unfortunately, the method is very computationally intensive so we present some tradeoffs below.

Usage

```
mc.wbart.gse( x.train, y.train,
    P=50L, R=5L, ntree=20L, numcut=100L, C=1, alpha=0.05,
    k=2.0, power=2.0, base=0.95,
    ndpost=2000L, nskip=100L,
    printevery=100L, keepevery=1L, keeptrainfits=FALSE,
    seed=99L, mc.cores=2L, nice=19L
    )
```

Arguments

x.train	Explanatory variables for training (in sample) data. Must be a matrix with (as usual) rows corresponding to observations and columns to variables. surv.bart will generate draws of $f(t, x)$ for each x which is a row of x.train.
y.train	The continuous outcome.
Р	The number of permutations: typically 50 or 100.
R	The number of replicates: typically 5 or 10.
ntree	The number of trees. In variable selection, the number of trees is smaller than what might be used for the best fit.

```
86
```

mc.wbart.gse

numcut	The number of possible values of c (see usequants). If a single number if given, this is used for all variables. Otherwise a vector with length equal to $ncol(x.train)$ is required, where the i^{th} element gives the number of c used for the i^{th} variable in x.train. If usequants is false, numcut equally spaced cutoffs are used covering the range of values in the corresponding column of x.train. If usequants is true, then min(numcut, the number of unique values in the corresponding columns of x.train - 1) c values are used.
С	The starting value for the multiple of SE. You should not need to change this except in rare circumstances.
alpha	The global SE method relies on simultaneous 1-alpha coverage across the per- mutations for all predictor variables.
k	k is the number of prior standard deviations $f(t, x)$ is away from +/-3. The bigger k is, the more conservative the fitting will be.
power	Power parameter for tree prior.
base	Base parameter for tree prior.
ndpost	The number of posterior draws after burn in. In the global SE method, generally, the method is repeated several times to establish the variable count probabilities. However, we take the alternative approach of simply running the MCMC chain longer which should result in the same stabilization of the estimates. Therefore, the number of posterior draws in variable selection should be set to a larger value than would be typically anticipated for fitting.
nskip	Number of MCMC iterations to be treated as burn in.
printevery	As the MCMC runs, a message is printed every printevery draws.
keepevery	Every keepevery draw is kept.
keeptrainfits	If TRUE the draws of $f(t, x)$ for $x = rows$ of x.train are generated.
seed	seed required for reproducible MCMC.
mc.cores	Number of cores to employ in parallel.
nice	Set the job priority. The default priority is 19: priorities go from 0 (highest) to 19 (lowest).

Value

mc.wbart.gse returns a list.

Author(s)

Rodney Sparapani: <rsparapa@mcw.edu>

References

Bleich, J., Kapelner, A., George, E.I., and Jensen, S.T. (2014). Variable selection for BART: an application to gene regulation. *The Annals of Applied Statistics*, **8:1750-81**.

See Also

mc.wbart

Examples

```
## Not run:
library(ElemStatLearn)
data(phoneme)
x.train <- matrix(NA, nrow=4509, ncol=257)
dimnames(x.train)[[2]] <- c(paste0('x.', 1:256), 'speaker')
x.train[, 257] <- as.numeric(phoneme$speaker)
for(j in 1:256) x.train[, j] <- as.numeric(phoneme[, paste0('x.', j)])
gse <- mc.wbart.gse(x.train, as.numeric(phoneme$g), mc.cores=5, seed=99)
## important variables
dimnames(x.train)[[2]][gse$which]
```

End(Not run)

pbart

Probit BART for dichotomous outcomes with Normal latents

Description

BART is a Bayesian "sum-of-trees" model.

For a binary response y, P(Y = 1|x) = F(f(x)), where F denotes the standard Normal CDF (probit link).

In both cases, f is the sum of many tree models. The goal is to have very flexible inference for the uknown function f.

In the spirit of "ensemble models", each tree is constrained by a prior to be a weak learner so that it contributes a small amount to the overall fit.

Usage

```
pbart(
    x.train, y.train, x.test=matrix(0.0,0,0),
    sparse=FALSE, theta=0, omega=1,
    a=0.5, b=1, augment=FALSE, rho=NULL,
    xinfo=matrix(0.0,0,0), usequants=FALSE,
    cont=FALSE, rm.const=TRUE,
    k=2.0, power=2.0, base=.95,
    binaryOffset=NULL,
```

pbart

```
ntree=50L, numcut=100L,
ndpost=1000L, nskip=100L, keepevery=1L,
nkeeptrain=ndpost, nkeeptest=ndpost,
nkeeptreedraws=ndpost,
printevery=100L, transposed=FALSE
```

Arguments

)

x.train	Explanatory variables for training (in sample) data. May be a matrix or a data frame, with (as usual) rows corresponding to observations and columns to variables. If a variable is a factor in a data frame, it is replaced with dummies. Note that q dummies are created if $q>2$ and one dummy is created if $q=2$, where q is the number of levels of the factor. pbart will generate draws of $f(x)$ for each x which is a row of x.train.
y.train	Binary dependent variable for training (in sample) data.
x.test	Explanatory variables for test (out of sample) data. Should have same structure as x.train. pbart will generate draws of $f(x)$ for each x which is a row of x.test.
sparse	Whether to perform variable selection based on a sparse Dirichlet prior rather than simply uniform; see Linero 2016.
theta	Set <i>theta</i> parameter; zero means random.
omega	Set <i>omega</i> parameter; zero means random.
a	Sparse parameter for $Beta(a, b)$ prior: $0.5 <= a <= 1$ where lower values inducing more sparsity.
b	Sparse parameter for $Beta(a, b)$ prior; typically, $b = 1$.
rho	Sparse parameter: typically $rho = p$ where p is the number of covariates under consideration.
augment	Whether data augmentation is to be performed in sparse variable selection.
xinfo	You can provide the cutpoints to BART or let BART choose them for you. To provide them, use the xinfo argument to specify a list (matrix) where the items (rows) are the covariates and the contents of the items (columns) are the cutpoints.
usequants	If usequants=FALSE, then the cutpoints in xinfo are generated uniformly; oth- erwise, if TRUE, uniform quantiles are used for the cutpoints.
cont	Whether or not to assume all variables are continuous.
rm.const	Whether or not to remove constant variables.
k	For binary y, k is the number of prior standard deviations $f(x)$ is away from +/-3.
	The bigger k is, the more conservative the fitting will be.
power	Power parameter for tree prior.

base	Base parameter for tree prior.
binaryOffset	Used for binary y. The model is $P(Y = 1 x) = F(f(x) + binaryOffset)$.
ntree	The number of trees in the sum.
numcut	The number of possible values of c (see usequants). If a single number if given, this is used for all variables. Otherwise a vector with length equal to $ncol(x.train)$ is required, where the i^{th} element gives the number of c used for the i^{th} variable in x.train. If usequants is false, numcut equally spaced cutoffs are used covering the range of values in the corresponding column of x.train. If usequants is true, then min(numcut, the number of unique values in the corresponding columns of x.train - 1) c values are used.
ndpost	The number of posterior draws returned.
nskip	Number of MCMC iterations to be treated as burn in.
nkeeptrain	Number of MCMC iterations to be returned for train data.
nkeeptest	Number of MCMC iterations to be returned for test data.
nkeeptreedraws	Number of MCMC iterations to be returned for tree draws.
keepevery	Every keepevery draw is kept to be returned to the user.
printevery	As the MCMC runs, a message is printed every printevery draws.
transposed	When running pbart in parallel, it is more memory-efficient to transpose x.train and x.test, if any, prior to calling mc.pbart.

Details

BART is an Bayesian MCMC method. At each MCMC interation, we produce a draw from

f in the binary y case.

Thus, unlike a lot of other modelling methods in R, we do not produce a single model object from which fits and summaries may be extracted. The output consists of values $f^*(x)$

where * denotes a particular draw. The x is either a row from the training data (x.train) or the test data (x.test).

Value

pbart returns an object of type pbart which is essentially a list.

yhat.train	A matrix with ndpost rows and nrow(x.train) columns. Each row corresponds to a draw f^* from the posterior of f and each column corresponds to a row of x.train. The (i, j) value is $f^*(x)$ for the i^{th} kept draw of f and the j^{th} row of x.train. Burn-in is dropped.
yhat.test	Same as yhat.train but now the x's are the rows of the test data.
varcount	a matrix with ndpost rows and nrow(x.train) columns. Each row is for a draw. For each variable (corresponding to the columns), the total count of the number of times that variable is used in a tree decision rule (over all trees) is given.

pbart

In addition the list has a binaryOffset component giving the value used.

Note that in the binary y, case yhat.train and yhat.test are f(x) + binaryOffset. If you want draws of the probability P(Y = 1|x) you need to apply the Normal CDF (pnorm) to these values.

Author(s)

Robert McCulloch: <robert.e.mcculloch@gmail.com>, Rodney Sparapani: <rsparapa@mcw.edu>.

References

Chipman, H., George, E., and McCulloch R. (2010) Bayesian Additive Regression Trees. *The Annals of Applied Statistics*, **4,1**, 266-298 <doi: 10.1214/09-AOAS285>.

Friedman, J.H. (1991) Multivariate adaptive regression splines. The Annals of Statistics, 19, 1-67.

Gramacy, RB and Polson, NG (2012) Simulation-based regularized logistic regression. *Bayesian Analysis*, **7**, 567–590.

Holmes, C and Held, L (2006) Bayesian auxiliary variable models for binary and multinomial regression. *Bayesian Analysis*, **1**, 145–68.

Linero, A.R. (2018) Bayesian regression trees for high dimensional prediction and variable selection. *JASA*, **113**, 626–36.

See Also

wbart

Examples

data(ACTG175)

```
## exclude those who do not have CD4 count at 96 weeks
ex <- is.na(ACTG175$cd496)
table(ex)</pre>
```

inclusion criteria are CD4 counts between 200 and 500
ACTG175\$cd40 <- min(500, max(250, ACTG175\$cd40))</pre>

```
## calculate relative CD4 decline
y <- ((ACTG175$cd496-ACTG175$cd40)/ACTG175$cd40)[!ex]
summary(y)</pre>
```

```
## 0=failure, 1=success
y <- 1*(y > -0.5)
```

```
## summarize CD4 outcomes
table(y, ACTG175$arms[!ex])
```

```
table(y, ACTG175$arms[!ex])/
matrix(table(ACTG175$arms[!ex]), nrow=2, ncol=4, byrow=TRUE)
```

```
## drop unneeded and unwanted variables
## 1: 'pidnum' patient ID number
##14: 'str2' which will be handled by strat1 below
##15: 'strat' which will be handled by strat1-strat3 below
##17: 'treat' handled by arm0-arm3 below
##18: 'offtrt' indicator of off-treatment before 96 weeks
##20: 'cd420' CD4 T cell count at 20 weeks
##21: 'cd496' CD4 T cell count at 96 weeks
##22: 'r' missing CD4 T cell count at 96 weeks
##24: 'cd820' CD8 T cell count at 20 weeks
##25: 'cens' indicator of observing the event in days
##26: 'days' number of days until the primary endpoint
##27: 'arms' handled by arm0-arm3 below
train <- as.matrix(ACTG175)[!ex, -c(1, 14:15, 17, 18, 20:22, 24:27)]
train <- cbind(1*(ACTG175$strat[!ex]==1), 1*(ACTG175$strat[!ex]==2),</pre>
               1*(ACTG175$strat[!ex]==3), train)
dimnames(train)[[2]][1:3] <- paste0('strat', 1:3)</pre>
train <- cbind(1*(ACTG175$arms[!ex]==0), 1*(ACTG175$arms[!ex]==1),</pre>
                1*(ACTG175$arms[!ex]==2), 1*(ACTG175$arms[!ex]==3), train)
dimnames(train)[[2]][1:4] <- paste0('arm', 0:3)</pre>
N <- nrow(train)</pre>
test0 <- train; test0[ , 1:4] <- 0; test0[ , 1] <- 1
test1 <- train; test1[ , 1:4] <- 0; test1[ , 2] <- 1
test2 <- train; test2[ , 1:4] <- 0; test2[ , 3] <- 1
test3 <- train; test3[ , 1:4] <- 0; test3[ , 4] <- 1
test <- rbind(test0, test1, test2, test3)</pre>
##test BART with token run to ensure installation works
set.seed(21)
post <- pbart(train, y, test, nskip=5, ndpost=5)</pre>
## Not run:
set.seed(21)
post <- pbart(train, y, test)</pre>
## turn z-scores into probabilities
post$prob.test <- pnorm(post$yhat.test)</pre>
## average over the posterior samples
post$prob.test.mean <- apply(post$prob.test, 2, mean)</pre>
## place estimates for arms 0-3 next to each other for convenience
itr <- cbind(post$prob.test.mean[(1:N)], post$prob.test.mean[N+(1:N)],</pre>
             post$prob.test.mean[2*N+(1:N)], post$prob.test.mean[3*N+(1:N)])
## find the BART ITR for each patient
itr.pick <- integer(N)</pre>
for(i in 1:N) itr.pick[i] <- which(itr[i, ]==max(itr[i, ]))-1</pre>
## arms 0 and 3 (monotherapy) are never chosen
```

pbart

```
table(itr.pick)
## do arms 1 and 2 show treatment heterogeneity?
diff. <- apply(post$prob.test[ , 2*N+(1:N)]-post$prob.test[ , N+(1:N)], 2, mean)</pre>
plot(sort(diff.), type='h', main='ACTG175 trial: 50% CD4 decline from baseline at 96 weeks',
     xlab='Arm 2 (1) Preferable to the Right (Left)', ylab='Prob.Diff.: Arms 2 - 1')
library(rpart)
library(rpart.plot)
## make data frame for nicer names in the plot
var <- as.data.frame(train[ , -(1:4)])</pre>
dss <- rpart(diff. ~ var$age+var$gender+var$race+var$wtkg+var$cd40+var$cd80+
                   var$karnof+var$symptom+var$hemo+var$homo+var$drugs+var$z30+
                   var$zprior+var$oprior+var$strat1+var$strat2+var$strat3,
               method='anova', control=rpart.control(cp=0.1))
rpart.plot(dss, type=3, extra=101)
## if strat1==1 (antiretroviral naive), then arm 2 is better
## otherwise, arm 1
print(dss)
all0 <- apply(post$prob.test[ , (1:N)], 1, mean)</pre>
all1 <- apply(post$prob.test[ , N+(1:N)], 1, mean)</pre>
all2 <- apply(post$prob.test[ , 2*N+(1:N)], 1, mean)
all3 <- apply(post$prob.test[ , 3*N+(1:N)], 1, mean)</pre>
## BART ITR
BART.itr <- apply(post$prob.test[, c(N+which(itr.pick==1), 2*N+which(itr.pick==2))], 1, mean)
test <- train
test[ , 1:4] <- 0
test[test[ , 5]==0, 2] <- 1
test[test[ , 5]==1, 3] <- 1</pre>
## BART ITR simple
BART.itr.simp <- pwbart(test, post$treedraws)</pre>
BART.itr.simp <- apply(pnorm(BART.itr.simp), 1, mean)</pre>
plot(density(BART.itr), xlab='Value', xlim=c(0.475, 0.775), lwd=2,
     main='ACTG175 trial: 50% CD4 decline from baseline at 96 weeks')
lines(density(BART.itr.simp), col='brown', lwd=2)
lines(density(all0), col='green', lwd=2)
lines(density(all1), col='red', lwd=2)
lines(density(all2), col='blue', lwd=2)
lines(density(all3), col='yellow', lwd=2)
legend('topleft', legend=c('All Arm 0 (ZDV only)', 'All Arm 1 (ZDV+DDI)',
                            'All Arm 2 (ZDV+DDC)', 'All Arm 3 (DDI only)',
                            'BART ITR simple', 'BART ITR'),
       col=c('green', 'red', 'blue', 'yellow', 'brown', 'black'), lty=1, lwd=2)
```

End(Not run)

predict.crisk2bart Predicting new observations with a previously fitted BART model

Description

BART is a Bayesian "sum-of-trees" model. For a numeric response y, we have $y = f(x) + \epsilon$, where $\epsilon \sim N(0, \sigma^2)$.

f is the sum of many tree models. The goal is to have very flexible inference for the uknown function f.

In the spirit of "ensemble models", each tree is constrained by a prior to be a weak learner so that it contributes a small amount to the overall fit.

Usage

```
## S3 method for class 'crisk2bart'
predict(object, newdata, newdata2, mc.cores=1, openmp=(mc.cores.openmp()>0), ...)
```

Arguments

object	$object\ returned\ from\ previous\ BART\ fit\ with\ \texttt{crisk2.bart}\ or\ \texttt{mc.crisk2.bart}.$
newdata	Matrix of covariates to predict the distribution of $t1$.
newdata2	Matrix of covariates to predict the distribution of $t2$.
mc.cores	Number of threads to utilize.
openmp	Logical value dictating whether OpenMP is utilized for parallel processing. Of course, this depends on whether OpenMP is available on your system which, by default, is verified with mc.cores.openmp.
	Other arguments which will be passed on to pwbart.

Details

BART is an Bayesian MCMC method. At each MCMC interation, we produce a draw from the joint posterior $(f, \sigma)|(x, y)$ in the numeric y case and just f in the binary y case.

Thus, unlike a lot of other modelling methods in R, we do not produce a single model object from which fits and summaries may be extracted. The output consists of values $f^*(x)$ (and σ^* in the numeric case) where * denotes a particular draw. The x is either a row from the training data (x.train) or the test data (x.test).

Value

Returns an object of type crisk2bart with predictions corresponding to newdata and newdata2.

predict.crisk2bart

Author(s)

Robert McCulloch: <robert.e.mcculloch@gmail.com>, Rodney Sparapani: <rsparapa@mcw.edu>.

References

Chipman, H., George, E., and McCulloch R. (2010) Bayesian Additive Regression Trees. *The Annals of Applied Statistics*, **4**,**1**, 266-298 <doi:10.1214/09-AOAS285>.

Chipman, H., George, E., and McCulloch R. (2006) Bayesian Ensemble Learning. Advances in Neural Information Processing Systems 19, Scholkopf, Platt and Hoffman, Eds., MIT Press, Cambridge, MA, 265-272.

Friedman, J.H. (1991) Multivariate adaptive regression splines. The Annals of Statistics, 19, 1–67.

See Also

crisk2.bart, mc.crisk2.bart, mc.crisk2.pwbart, mc.cores.openmp

```
data(transplant)
```

```
delta <- (as.numeric(transplant$event)-1)</pre>
## recode so that delta=1 is cause of interest; delta=2 otherwise
delta[delta==1] <- 4</pre>
delta[delta==2] <- 1</pre>
delta[delta>1] <- 2</pre>
table(delta, transplant$event)
times <- pmax(1, ceiling(transplant$futime/7)) ## weeks</pre>
##times <- pmax(1, ceiling(transplant$futime/30.5)) ## months</pre>
table(times)
type0 <- 1*(transplant$abo=='0')</pre>
typeA <- 1*(transplant$abo=='A')</pre>
typeB <- 1*(transplant$abo=='B')</pre>
typeAB <- 1*(transplant$abo=='AB')</pre>
table(typeA, type0)
x.train <- cbind(type0, typeA, typeB, typeAB)</pre>
x.test <- cbind(1, 0, 0, 0)
dimnames(x.test)[[2]] <- dimnames(x.train)[[2]]</pre>
## parallel::mcparallel/mccollect do not exist on windows
if(.Platform$OS.type=='unix') {
##test BART with token run to ensure installation works
        post <- mc.crisk2.bart(x.train=x.train, times=times, delta=delta,</pre>
                                  seed=99, mc.cores=2, nskip=5, ndpost=5,
                                  keepevery=1)
```

```
predict.criskbart
```

```
pre <- surv.pre.bart(x.train=x.train, x.test=x.test,</pre>
                             times=times, delta=delta)
        K <- post$K
        pred <- mc.crisk2.pwbart(pre$tx.test, pre$tx.test,</pre>
                                 post$treedraws, post$treedraws2,
                                 post$binaryOffset, post$binaryOffset2)
}
## Not run:
## run one long MCMC chain in one process
## set.seed(99)
## post <- crisk2.bart(x.train=x.train, times=times, delta=delta, x.test=x.test)</pre>
## in the interest of time, consider speeding it up by parallel processing
## run "mc.cores" number of shorter MCMC chains in parallel processes
post <- mc.crisk2.bart(x.train=x.train,</pre>
                       times=times, delta=delta,
                       x.test=x.test, seed=99, mc.cores=8)
## check <- mc.crisk2.pwbart(post$tx.test, post$tx.test,</pre>
##
                             post$treedraws, post$treedraws2,
##
                             post$binaryOffset,
##
                             post$binaryOffset2, mc.cores=8)
check <- predict(post, newdata=post$tx.test, newdata2=post$tx.test2,</pre>
                 mc.cores=8)
print(c(post$surv.test.mean[1], check$surv.test.mean[1],
        post$surv.test.mean[1]-check$surv.test.mean[1]), digits=22)
print(all(round(post$surv.test.mean, digits=9)==
    round(check$surv.test.mean, digits=9)))
print(c(post$cif.test.mean[1], check$cif.test.mean[1],
        post$cif.test.mean[1]-check$cif.test.mean[1]), digits=22)
print(all(round(post$cif.test.mean, digits=9)==
    round(check$cif.test.mean, digits=9)))
print(c(post$cif.test2.mean[1], check$cif.test2.mean[1],
        post$cif.test2.mean[1]-check$cif.test2.mean[1]), digits=22)
print(all(round(post$cif.test2.mean, digits=9)==
    round(check$cif.test2.mean, digits=9)))
## End(Not run)
```

predict.criskbart *Predicting new observations with a previously fitted BART model*

predict.criskbart

Description

BART is a Bayesian "sum-of-trees" model. For a numeric response y, we have $y = f(x) + \epsilon$, where $\epsilon \sim N(0, \sigma^2)$.

f is the sum of many tree models. The goal is to have very flexible inference for the uknown function f.

In the spirit of "ensemble models", each tree is constrained by a prior to be a weak learner so that it contributes a small amount to the overall fit.

Usage

```
## S3 method for class 'criskbart'
predict(object, newdata, newdata2, mc.cores=1, openmp=(mc.cores.openmp()>0), ...)
```

Arguments

object	object returned from previous BART fit with crisk.bart or mc.crisk.bart.
newdata	Matrix of covariates to predict the distribution of $t1$.
newdata2	Matrix of covariates to predict the distribution of $t2$.
mc.cores	Number of threads to utilize.
openmp	Logical value dictating whether OpenMP is utilized for parallel processing. Of course, this depends on whether OpenMP is available on your system which, by default, is verified with mc.cores.openmp.
	Other arguments which will be passed on to pwbart.

Details

BART is an Bayesian MCMC method. At each MCMC interation, we produce a draw from the joint posterior $(f, \sigma)|(x, y)$ in the numeric y case and just f in the binary y case.

Thus, unlike a lot of other modelling methods in R, we do not produce a single model object from which fits and summaries may be extracted. The output consists of values $f^*(x)$ (and σ^* in the numeric case) where * denotes a particular draw. The x is either a row from the training data (x.train) or the test data (x.test).

Value

Returns an object of type criskbart with predictions corresponding to newdata and newdata2.

Author(s)

Robert McCulloch: <robert.e.mcculloch@gmail.com>, Rodney Sparapani: <rsparapa@mcw.edu>.

References

Chipman, H., George, E., and McCulloch R. (2010) Bayesian Additive Regression Trees. *The Annals of Applied Statistics*, **4**,**1**, 266-298 <doi:10.1214/09-AOAS285>.

Chipman, H., George, E., and McCulloch R. (2006) Bayesian Ensemble Learning. Advances in Neural Information Processing Systems 19, Scholkopf, Platt and Hoffman, Eds., MIT Press, Cambridge, MA, 265-272.

Friedman, J.H. (1991) Multivariate adaptive regression splines. The Annals of Statistics, 19, 1–67.

See Also

crisk.bart,mc.crisk.bart,mc.crisk.pwbart,mc.cores.openmp

```
data(transplant)
```

```
delta <- (as.numeric(transplant$event)-1)</pre>
## recode so that delta=1 is cause of interest; delta=2 otherwise
delta[delta==1] <- 4</pre>
delta[delta==2] <- 1</pre>
delta[delta>1] <- 2</pre>
table(delta, transplant$event)
times <- pmax(1, ceiling(transplant$futime/7)) ## weeks</pre>
##times <- pmax(1, ceiling(transplant$futime/30.5)) ## months</pre>
table(times)
type0 <- 1*(transplant$abo=='0')</pre>
typeA <- 1*(transplant$abo=='A')</pre>
typeB <- 1*(transplant$abo=='B')</pre>
typeAB <- 1*(transplant$abo=='AB')</pre>
table(typeA, type0)
x.train <- cbind(type0, typeA, typeB, typeAB)</pre>
x.test <- cbind(1, 0, 0, 0)
dimnames(x.test)[[2]] <- dimnames(x.train)[[2]]</pre>
## parallel::mcparallel/mccollect do not exist on windows
if(.Platform$0S.type=='unix') {
##test BART with token run to ensure installation works
        post <- mc.crisk.bart(x.train=x.train, times=times, delta=delta,</pre>
                                  seed=99, mc.cores=2, nskip=5, ndpost=5,
                                  keepevery=1)
        pre <- surv.pre.bart(x.train=x.train, x.test=x.test,</pre>
                                times=times, delta=delta)
```

```
pred <- mc.crisk.pwbart(pre$tx.test, pre$tx.test,</pre>
                                 post$treedraws, post$treedraws2,
                                 post$binaryOffset, post$binaryOffset2)
}
## Not run:
## run one long MCMC chain in one process
## set.seed(99)
## post <- crisk.bart(x.train=x.train, times=times, delta=delta, x.test=x.test)</pre>
## in the interest of time, consider speeding it up by parallel processing
## run "mc.cores" number of shorter MCMC chains in parallel processes
post <- mc.crisk.bart(x.train=x.train,</pre>
                       times=times, delta=delta,
                       x.test=x.test, seed=99, mc.cores=8)
## check <- mc.crisk.pwbart(post$tx.test, post$tx.test,</pre>
##
                             post$treedraws, post$treedraws2,
##
                             post$binaryOffset,
##
                             post$binaryOffset2, mc.cores=8)
check <- predict(post, newdata=post$tx.test, newdata2=post$tx.test2,</pre>
                 mc.cores=8)
print(c(post$surv.test.mean[1], check$surv.test.mean[1],
        post$surv.test.mean[1]-check$surv.test.mean[1]), digits=22)
print(all(round(post$surv.test.mean, digits=9)==
    round(check$surv.test.mean, digits=9)))
print(c(post$cif.test.mean[1], check$cif.test.mean[1],
        post$cif.test.mean[1]-check$cif.test.mean[1]), digits=22)
print(all(round(post$cif.test.mean, digits=9)==
    round(check$cif.test.mean, digits=9)))
print(c(post$cif.test2.mean[1], check$cif.test2.mean[1],
        post$cif.test2.mean[1]-check$cif.test2.mean[1]), digits=22)
print(all(round(post$cif.test2.mean, digits=9)==
    round(check$cif.test2.mean, digits=9)))
## End(Not run)
```

predict.lbart

Description

BART is a Bayesian "sum-of-trees" model. For a numeric response y, we have $y = f(x) + \epsilon$, where $\epsilon \sim N(0, \sigma^2)$.

f is the sum of many tree models. The goal is to have very flexible inference for the uknown function f.

In the spirit of "ensemble models", each tree is constrained by a prior to be a weak learner so that it contributes a small amount to the overall fit.

Usage

```
## S3 method for class 'lbart'
predict(object, newdata, mc.cores=1, openmp=(mc.cores.openmp()>0), ...)
```

Arguments

object	object returned from previous BART fit with surv.bart or mc.surv.bart.
newdata	Matrix of covariates to predict the distribution of t .
mc.cores	Number of threads to utilize.
openmp	Logical value dictating whether OpenMP is utilized for parallel processing. Of course, this depends on whether OpenMP is available on your system which, by default, is verified with mc.cores.openmp.
	Other arguments which will be passed on to pwbart.

Details

BART is an Bayesian MCMC method. At each MCMC interation, we produce a draw from the joint posterior $(f, \sigma)|(x, y)$ in the numeric y case and just f in the binary y case.

Thus, unlike a lot of other modelling methods in R, we do not produce a single model object from which fits and summaries may be extracted. The output consists of values $f^*(x)$ (and σ^* in the numeric case) where * denotes a particular draw. The x is either a row from the training data (x.train) or the test data (x.test).

Value

Returns an object of type lbart with predictions corresponding to newdata.

Author(s)

Robert McCulloch: <robert.e.mcculloch@gmail.com>, Rodney Sparapani: <rsparapa@mcw.edu>.

predict.lbart

References

Chipman, H., George, E., and McCulloch R. (2010) Bayesian Additive Regression Trees. *The Annals of Applied Statistics*, **4,1**, 266-298 <doi:10.1214/09-AOAS285>.

Chipman, H., George, E., and McCulloch R. (2006) Bayesian Ensemble Learning. Advances in Neural Information Processing Systems 19, Scholkopf, Platt and Hoffman, Eds., MIT Press, Cambridge, MA, 265-272.

Friedman, J.H. (1991) Multivariate adaptive regression splines. The Annals of Statistics, 19, 1–67.

See Also

surv.bart, mc.surv.bart, surv.pwbart, mc.surv.pwbart, mc.cores.openmp

```
## load the advanced lung cancer example
data(lung)
group <- -which(is.na(lung[ , 7])) ## remove missing row for ph.karno</pre>
times <- lung[group, 2] ##lung$time</pre>
delta <- lung[group, 3]-1 ##lung$status: 1=censored, 2=dead</pre>
                          ##delta: 0=censored, 1=dead
## this study reports time in days rather than months like other studies
## coarsening from days to months will reduce the computational burden
times <- ceiling(times/30)</pre>
summary(times)
table(delta)
x.train <- as.matrix(lung[group, c(4, 5, 7)]) ## matrix of observed covariates
## lung$age:
                    Age in years
## lung$sex:
                    Male=1 Female=2
## lung$ph.karno: Karnofsky performance score (dead=0:normal=100:by=10)
##
                    rated by physician
dimnames(x.train)[[2]] <- c('age(yr)', 'M(1):F(2)', 'ph.karno(0:100:10)')
summary(x.train[ , 1])
table(x.train[ , 2])
table(x.train[ , 3])
x.test <- matrix(nrow=84, ncol=3) ## matrix of covariate scenarios
dimnames(x.test)[[2]] <- dimnames(x.train)[[2]]</pre>
i <- 1
for(age in 5*(9:15)) for(sex in 1:2) for(ph.karno in 10*(5:10)) {
    x.test[i, ] <- c(age, sex, ph.karno)</pre>
```

```
i <- i+1
}
## this x.test is relatively small, but often you will want to
## predict for a large x.test matrix which may cause problems
## due to consumption of RAM so we can predict separately
## mcparallel/mccollect do not exist on windows
if(.Platform$OS.type=='unix') {
##test BART with token run to ensure installation works
    set.seed(99)
  post <- surv.bart(x.train=x.train, times=times, delta=delta, nskip=5, ndpost=5, keepevery=1)</pre>
   pre <- surv.pre.bart(x.train=x.train, times=times, delta=delta, x.test=x.test)</pre>
    pred <- predict(post, pre$tx.test)</pre>
    ##pred. <- surv.pwbart(pre$tx.test, post$treedraws, post$binaryOffset)</pre>
}
## Not run:
## run one long MCMC chain in one process
set.seed(99)
post <- surv.bart(x.train=x.train, times=times, delta=delta)</pre>
## run "mc.cores" number of shorter MCMC chains in parallel processes
## post <- mc.surv.bart(x.train=x.train, times=times, delta=delta,</pre>
                        mc.cores=5, seed=99)
##
pre <- surv.pre.bart(x.train=x.train, times=times, delta=delta, x.test=x.test)</pre>
pred <- predict(post, pre$tx.test)</pre>
## let's look at some survival curves
## first, a younger group with a healthier KPS
## age 50 with KPS=90: males and females
## males: row 17, females: row 23
x.test[c(17, 23), ]
low.risk.males <- 16*post$K+1:post$K ## K=unique times including censoring</pre>
low.risk.females <- 22*post$K+1:post$K</pre>
plot(post$times, pred$surv.test.mean[low.risk.males], type='s', col='blue',
     main='Age 50 with KPS=90', xlab='t', ylab='S(t)', ylim=c(0, 1))
points(post$times, pred$surv.test.mean[low.risk.females], type='s', col='red')
## End(Not run)
```

predict.mbart

Predicting new observations with a previously fitted BART model

predict.mbart

Description

BART is a Bayesian "sum-of-trees" model. For a numeric response y, we have $y = f(x) + \epsilon$, where $\epsilon \sim N(0, \sigma^2)$.

f is the sum of many tree models. The goal is to have very flexible inference for the uknown function f.

In the spirit of "ensemble models", each tree is constrained by a prior to be a weak learner so that it contributes a small amount to the overall fit.

Usage

```
## S3 method for class 'mbart'
predict(object, newdata, mc.cores=1, openmp=(mc.cores.openmp()>0), ...)
## S3 method for class 'mbart2'
predict(object, newdata, mc.cores=1, openmp=(mc.cores.openmp()>0), ...)
```

Arguments

object	object returned from previous BART fit with mbart or mbart2.
newdata	Matrix of covariates to predict the distribution of t .
mc.cores	Number of threads to utilize.
openmp	Logical value dictating whether OpenMP is utilized for parallel processing. Of course, this depends on whether OpenMP is available on your system which, by default, is verified with mc.cores.openmp.
	Other arguments which will be passed on to pwbart.

Details

BART is an Bayesian MCMC method. At each MCMC interation, we produce a draw from the joint posterior $(f, \sigma)|(x, y)$ in the numeric y case and just f in the binary y case.

Thus, unlike a lot of other modelling methods in R, we do not produce a single model object from which fits and summaries may be extracted. The output consists of values $f^*(x)$ (and σ^* in the numeric case) where * denotes a particular draw. The x is either a row from the training data (x.train) or the test data (x.test).

Value

Returns an object of type mbart with predictions corresponding to newdata.

Author(s)

Robert McCulloch: <robert.e.mcculloch@gmail.com>, Rodney Sparapani: <rsparapa@mcw.edu>.

References

Chipman, H., George, E., and McCulloch R. (2010) Bayesian Additive Regression Trees. *The Annals of Applied Statistics*, **4**,**1**, 266-298 <doi:10.1214/09-AOAS285>.

Chipman, H., George, E., and McCulloch R. (2006) Bayesian Ensemble Learning. Advances in Neural Information Processing Systems 19, Scholkopf, Platt and Hoffman, Eds., MIT Press, Cambridge, MA, 265-272.

Friedman, J.H. (1991) Multivariate adaptive regression splines. The Annals of Statistics, 19, 1-67.

See Also

mbart, mbart2

```
## load the advanced lung cancer example
data(lung)
group <- -which(is.na(lung[ , 7])) ## remove missing row for ph.karno</pre>
times <- lung[group, 2] ##lung$time</pre>
delta <- lung[group, 3]-1 ##lung$status: 1=censored, 2=dead</pre>
                          ##delta: 0=censored, 1=dead
## this study reports time in days rather than months like other studies
## coarsening from days to months will reduce the computational burden
times <- ceiling(times/30)</pre>
summary(times)
table(delta)
x.train <- as.matrix(lung[group, c(4, 5, 7)]) ## matrix of observed covariates
## lung$age:
                    Age in years
## lung$sex:
                    Male=1 Female=2
## lung$ph.karno: Karnofsky performance score (dead=0:normal=100:by=10)
##
                    rated by physician
dimnames(x.train)[[2]] <- c('age(yr)', 'M(1):F(2)', 'ph.karno(0:100:10)')
summary(x.train[ , 1])
table(x.train[ , 2])
table(x.train[ , 3])
x.test <- matrix(nrow=84, ncol=3) ## matrix of covariate scenarios
dimnames(x.test)[[2]] <- dimnames(x.train)[[2]]</pre>
i <- 1
for(age in 5*(9:15)) for(sex in 1:2) for(ph.karno in 10*(5:10)) {
    x.test[i, ] <- c(age, sex, ph.karno)</pre>
```

predict.pbart

```
i <- i+1
}
## this x.test is relatively small, but often you will want to
## predict for a large x.test matrix which may cause problems
## due to consumption of RAM so we can predict separately
## mcparallel/mccollect do not exist on windows
if(.Platform$OS.type=='unix') {
##test BART with token run to ensure installation works
    set.seed(99)
  post <- surv.bart(x.train=x.train, times=times, delta=delta, nskip=5, ndpost=5, keepevery=1)</pre>
   pre <- surv.pre.bart(x.train=x.train, times=times, delta=delta, x.test=x.test)</pre>
    pred <- predict(post, pre$tx.test)</pre>
    ##pred. <- surv.pwbart(pre$tx.test, post$treedraws, post$binaryOffset)</pre>
}
## Not run:
## run one long MCMC chain in one process
set.seed(99)
post <- surv.bart(x.train=x.train, times=times, delta=delta)</pre>
## run "mc.cores" number of shorter MCMC chains in parallel processes
## post <- mc.surv.bart(x.train=x.train, times=times, delta=delta,</pre>
                        mc.cores=5, seed=99)
##
pre <- surv.pre.bart(x.train=x.train, times=times, delta=delta, x.test=x.test)</pre>
pred <- predict(post, pre$tx.test)</pre>
## let's look at some survival curves
## first, a younger group with a healthier KPS
## age 50 with KPS=90: males and females
## males: row 17, females: row 23
x.test[c(17, 23), ]
low.risk.males <- 16*post$K+1:post$K ## K=unique times including censoring</pre>
low.risk.females <- 22*post$K+1:post$K</pre>
plot(post$times, pred$surv.test.mean[low.risk.males], type='s', col='blue',
     main='Age 50 with KPS=90', xlab='t', ylab='S(t)', ylim=c(0, 1))
points(post$times, pred$surv.test.mean[low.risk.females], type='s', col='red')
## End(Not run)
```

predict.pbart

Predicting new observations with a previously fitted BART model

Description

BART is a Bayesian "sum-of-trees" model. For a numeric response y, we have $y = f(x) + \epsilon$, where $\epsilon \sim N(0, \sigma^2)$.

f is the sum of many tree models. The goal is to have very flexible inference for the uknown function f.

In the spirit of "ensemble models", each tree is constrained by a prior to be a weak learner so that it contributes a small amount to the overall fit.

Usage

```
## S3 method for class 'pbart'
predict(object, newdata, mc.cores=1, openmp=(mc.cores.openmp()>0), ...)
```

Arguments

object	object returned from previous BART fit with surv.bart or mc.surv.bart.
newdata	Matrix of covariates to predict the distribution of t .
mc.cores	Number of threads to utilize.
openmp	Logical value dictating whether OpenMP is utilized for parallel processing. Of course, this depends on whether OpenMP is available on your system which, by default, is verified with mc.cores.openmp.
	Other arguments which will be passed on to pwbart.

Details

BART is an Bayesian MCMC method. At each MCMC interation, we produce a draw from the joint posterior $(f, \sigma)|(x, y)$ in the numeric y case and just f in the binary y case.

Thus, unlike a lot of other modelling methods in R, we do not produce a single model object from which fits and summaries may be extracted. The output consists of values $f^*(x)$ (and σ^* in the numeric case) where * denotes a particular draw. The x is either a row from the training data (x.train) or the test data (x.test).

Value

Returns an object of type pbart with predictions corresponding to newdata.

Author(s)

Robert McCulloch: <robert.e.mcculloch@gmail.com>, Rodney Sparapani: <rsparapa@mcw.edu>.

predict.pbart

References

Chipman, H., George, E., and McCulloch R. (2010) Bayesian Additive Regression Trees. *The Annals of Applied Statistics*, **4,1**, 266-298 <doi:10.1214/09-AOAS285>.

Chipman, H., George, E., and McCulloch R. (2006) Bayesian Ensemble Learning. Advances in Neural Information Processing Systems 19, Scholkopf, Platt and Hoffman, Eds., MIT Press, Cambridge, MA, 265-272.

Friedman, J.H. (1991) Multivariate adaptive regression splines. The Annals of Statistics, 19, 1–67.

See Also

surv.bart, mc.surv.bart, surv.pwbart, mc.surv.pwbart, mc.cores.openmp

```
## load the advanced lung cancer example
data(lung)
group <- -which(is.na(lung[ , 7])) ## remove missing row for ph.karno</pre>
times <- lung[group, 2] ##lung$time</pre>
delta <- lung[group, 3]-1 ##lung$status: 1=censored, 2=dead</pre>
                          ##delta: 0=censored, 1=dead
## this study reports time in days rather than months like other studies
## coarsening from days to months will reduce the computational burden
times <- ceiling(times/30)</pre>
summary(times)
table(delta)
x.train <- as.matrix(lung[group, c(4, 5, 7)]) ## matrix of observed covariates
## lung$age:
                    Age in years
## lung$sex:
                    Male=1 Female=2
## lung$ph.karno: Karnofsky performance score (dead=0:normal=100:by=10)
##
                    rated by physician
dimnames(x.train)[[2]] <- c('age(yr)', 'M(1):F(2)', 'ph.karno(0:100:10)')
summary(x.train[ , 1])
table(x.train[ , 2])
table(x.train[ , 3])
x.test <- matrix(nrow=84, ncol=3) ## matrix of covariate scenarios
dimnames(x.test)[[2]] <- dimnames(x.train)[[2]]</pre>
i <- 1
for(age in 5*(9:15)) for(sex in 1:2) for(ph.karno in 10*(5:10)) {
    x.test[i, ] <- c(age, sex, ph.karno)</pre>
```

```
i <- i+1
}
## this x.test is relatively small, but often you will want to
## predict for a large x.test matrix which may cause problems
## due to consumption of RAM so we can predict separately
## mcparallel/mccollect do not exist on windows
if(.Platform$OS.type=='unix') {
##test BART with token run to ensure installation works
    set.seed(99)
  post <- surv.bart(x.train=x.train, times=times, delta=delta, nskip=5, ndpost=5, keepevery=1)</pre>
   pre <- surv.pre.bart(x.train=x.train, times=times, delta=delta, x.test=x.test)</pre>
    pred <- predict(post, pre$tx.test)</pre>
    ##pred. <- surv.pwbart(pre$tx.test, post$treedraws, post$binaryOffset)</pre>
}
## Not run:
## run one long MCMC chain in one process
set.seed(99)
post <- surv.bart(x.train=x.train, times=times, delta=delta)</pre>
## run "mc.cores" number of shorter MCMC chains in parallel processes
## post <- mc.surv.bart(x.train=x.train, times=times, delta=delta,</pre>
                        mc.cores=5, seed=99)
##
pre <- surv.pre.bart(x.train=x.train, times=times, delta=delta, x.test=x.test)</pre>
pred <- predict(post, pre$tx.test)</pre>
## let's look at some survival curves
## first, a younger group with a healthier KPS
## age 50 with KPS=90: males and females
## males: row 17, females: row 23
x.test[c(17, 23), ]
low.risk.males <- 16*post$K+1:post$K ## K=unique times including censoring</pre>
low.risk.females <- 22*post$K+1:post$K</pre>
plot(post$times, pred$surv.test.mean[low.risk.males], type='s', col='blue',
     main='Age 50 with KPS=90', xlab='t', ylab='S(t)', ylim=c(0, 1))
points(post$times, pred$surv.test.mean[low.risk.females], type='s', col='red')
## End(Not run)
```

predict.recurbart *Predicting new observations with a previously fitted BART model*

predict.recurbart

Description

BART is a Bayesian "sum-of-trees" model. For a numeric response y, we have $y = f(x) + \epsilon$, where $\epsilon \sim N(0, \sigma^2)$.

f is the sum of many tree models. The goal is to have very flexible inference for the uknown function f.

In the spirit of "ensemble models", each tree is constrained by a prior to be a weak learner so that it contributes a small amount to the overall fit.

Usage

```
## S3 method for class 'recurbart'
predict(object, newdata, mc.cores=1, openmp=(mc.cores.openmp()>0), ...)
```

Arguments

object	object returned from previous BART fit with recur.bart or mc.recur.bart.
newdata	Matrix of covariates to predict the distribution of t .
mc.cores	Number of threads to utilize.
openmp	Logical value dictating whether OpenMP is utilized for parallel processing. Of course, this depends on whether OpenMP is available on your system which, by default, is verified with mc.cores.openmp.
	Other arguments which will be passed on to pwbart.

Details

BART is an Bayesian MCMC method. At each MCMC interation, we produce a draw from the joint posterior $(f, \sigma)|(x, y)$ in the numeric y case and just f in the binary y case.

Thus, unlike a lot of other modelling methods in R, we do not produce a single model object from which fits and summaries may be extracted. The output consists of values $f^*(x)$ (and σ^* in the numeric case) where * denotes a particular draw. The x is either a row from the training data (x.train) or the test data (x.test).

Value

Returns an object of type recurbart with predictions corresponding to newdata.

Author(s)

Robert McCulloch: <robert.e.mcculloch@gmail.com>, Rodney Sparapani: <rsparapa@mcw.edu>.

References

Chipman, H., George, E., and McCulloch R. (2010) Bayesian Additive Regression Trees. *The Annals of Applied Statistics*, **4**,**1**, 266-298 <doi:10.1214/09-AOAS285>.

Chipman, H., George, E., and McCulloch R. (2006) Bayesian Ensemble Learning. Advances in Neural Information Processing Systems 19, Scholkopf, Platt and Hoffman, Eds., MIT Press, Cambridge, MA, 265-272.

Friedman, J.H. (1991) Multivariate adaptive regression splines. The Annals of Statistics, 19, 1–67.

See Also

recur.bart, mc.recur.bart, recur.pwbart, mc.recur.pwbart, mc.cores.openmp

Examples

```
## load 20 percent random sample
data(xdm20.train)
data(xdm20.test)
data(ydm20.train)
##test BART with token run to ensure installation works
## with current technology even a token run will violate CRAN policy
## set.seed(99)
## post <- recur.bart(x.train=xdm20.train, y.train=ydm20.train,</pre>
##
                      nskip=1, ndpost=1, keepevery=1)
## Not run:
set.seed(99)
post <- recur.bart(x.train=xdm20.train, y.train=ydm20.train)</pre>
## larger data sets can take some time so, if parallel processing
## is available, submit this statement instead
## post <- mc.recur.bart(x.train=xdm20.train, y.train=ydm20.train,</pre>
##
                        mc.cores=8, seed=99)
require(rpart)
require(rpart.plot)
dss <- rpart(post$yhat.train.mean~xdm20.train)</pre>
rpart.plot(dss)
## for the 20 percent sample, notice that the top splits
## involve cci_pvd and n
## for the full data set, notice that all splits
## involve ca, cci_pud, cci_pvd, ins270 and n
## (except one at the bottom involving a small group)
## compare patients treated with insulin (ins270=1) vs
## not treated with insulin (ins270=0)
N.train <- 50
N.test <- 50
K <- post$K ## 798 unique time points</pre>
```

```
## only testing set, i.e., remove training set
xdm20.test. <- xdm20.test[N.train*K+(1:(N.test*K)), ]</pre>
xdm20.test. <- rbind(xdm20.test., xdm20.test.)</pre>
xdm20.test.[ , 'ins270'] <- rep(0:1, each=N.test*K)</pre>
## multiple threads will be utilized if available
pred <- predict(post, xdm20.test., mc.cores=8)</pre>
## create Friedman's partial dependence function for the
## intensity/hazard by time and ins270
NK.test <- N.test*K
M <- nrow(pred$haz.test) ## number of MCMC samples, typically 1000</pre>
RI <- matrix(0, M, K)
for(i in 1:N.test)
    RI <- RI+(pred$haz.test[ , (N.test+i-1)*K+1:K]/</pre>
              pred$haz.test[ , (i-1)*K+1:K])/N.test
RI.lo <- apply(RI, 2, quantile, probs=0.025)
RI.mu <- apply(RI, 2, mean)</pre>
RI.hi <- apply(RI, 2, quantile, probs=0.975)</pre>
plot(post$times, RI.hi, type='l', lty=2, log='y',
     ylim=c(min(RI.lo, 1/RI.hi), max(1/RI.lo, RI.hi)),
     xlab='t', ylab='RI(t, x)',
     sub='insulin(ins270=1) vs. no insulin(ins270=0)',
     main='Relative intensity of hospital admissions for diabetics')
lines(post$times, RI.mu)
lines(post$times, RI.lo, lty=2)
lines(post$times, rep(1, K), col='darkgray')
## RI for insulin therapy seems fairly constant with time
mean(RI.mu)
## End(Not run)
```

predict.survbart *Predicting new observations with a previously fitted BART model*

Description

BART is a Bayesian "sum-of-trees" model. For a numeric response y, we have $y = f(x) + \epsilon$, where $\epsilon \sim N(0, \sigma^2)$.

f is the sum of many tree models. The goal is to have very flexible inference for the uknown function f.

In the spirit of "ensemble models", each tree is constrained by a prior to be a weak learner so that it contributes a small amount to the overall fit.

Usage

```
## S3 method for class 'survbart'
predict(object, newdata, mc.cores=1, openmp=(mc.cores.openmp()>0), ...)
```

Arguments

object	object returned from previous BART fit with $surv.bart or mc.surv.bart$.
newdata	Matrix of covariates to predict the distribution of t .
mc.cores	Number of threads to utilize.
openmp	Logical value dictating whether OpenMP is utilized for parallel processing. Of course, this depends on whether OpenMP is available on your system which, by default, is verified with mc.cores.openmp.
	Other arguments which will be passed on to pwbart.

Details

BART is an Bayesian MCMC method. At each MCMC interation, we produce a draw from the joint posterior $(f, \sigma)|(x, y)$ in the numeric y case and just f in the binary y case.

Thus, unlike a lot of other modelling methods in R, we do not produce a single model object from which fits and summaries may be extracted. The output consists of values $f^*(x)$ (and σ^* in the numeric case) where * denotes a particular draw. The x is either a row from the training data (x.train) or the test data (x.test).

Value

Returns an object of type survbart with predictions corresponding to newdata.

Author(s)

Robert McCulloch: <robert.e.mcculloch@gmail.com>, Rodney Sparapani: <rsparapa@mcw.edu>.

References

Chipman, H., George, E., and McCulloch R. (2010) Bayesian Additive Regression Trees. *The Annals of Applied Statistics*, **4**,**1**, 266-298 <doi:10.1214/09-AOAS285>.

Chipman, H., George, E., and McCulloch R. (2006) Bayesian Ensemble Learning. Advances in Neural Information Processing Systems 19, Scholkopf, Platt and Hoffman, Eds., MIT Press, Cambridge, MA, 265-272.

Friedman, J.H. (1991) Multivariate adaptive regression splines. The Annals of Statistics, 19, 1-67.

See Also

surv.bart, mc.surv.bart, surv.pwbart, mc.surv.pwbart, mc.cores.openmp

predict.survbart

Examples

```
## load the advanced lung cancer example
data(lung)
group <- -which(is.na(lung[ , 7])) ## remove missing row for ph.karno</pre>
times <- lung[group, 2] ##lung$time</pre>
delta <- lung[group, 3]-1 ##lung$status: 1=censored, 2=dead</pre>
                           ##delta: 0=censored, 1=dead
## this study reports time in days rather than months like other studies
## coarsening from days to months will reduce the computational burden
times <- ceiling(times/30)</pre>
summary(times)
table(delta)
x.train <- as.matrix(lung[group, c(4, 5, 7)]) ## matrix of observed covariates
## lung$age:
                    Age in years
## lung$sex:
                    Male=1 Female=2
## lung$ph.karno: Karnofsky performance score (dead=0:normal=100:by=10)
##
                    rated by physician
dimnames(x.train)[[2]] <- c('age(yr)', 'M(1):F(2)', 'ph.karno(0:100:10)')</pre>
summary(x.train[ , 1])
table(x.train[ , 2])
table(x.train[ , 3])
x.test <- matrix(nrow=84, ncol=3) ## matrix of covariate scenarios</pre>
dimnames(x.test)[[2]] <- dimnames(x.train)[[2]]</pre>
i <- 1
for(age in 5*(9:15)) for(sex in 1:2) for(ph.karno in 10*(5:10)) {
    x.test[i, ] <- c(age, sex, ph.karno)</pre>
    i <- i+1
}
## this x.test is relatively small, but often you will want to
## predict for a large x.test matrix which may cause problems
## due to consumption of RAM so we can predict separately
## mcparallel/mccollect do not exist on windows
if(.Platform$OS.type=='unix') {
##test BART with token run to ensure installation works
    set.seed(99)
  post <- surv.bart(x.train=x.train, times=times, delta=delta, nskip=5, ndpost=5, keepevery=1)</pre>
    pre <- surv.pre.bart(x.train=x.train, times=times, delta=delta, x.test=x.test)</pre>
```

predict.wbart

```
pred <- predict(post, pre$tx.test)</pre>
    ##pred. <- surv.pwbart(pre$tx.test, post$treedraws, post$binaryOffset)</pre>
}
## Not run:
## run one long MCMC chain in one process
set.seed(99)
post <- surv.bart(x.train=x.train, times=times, delta=delta)</pre>
## run "mc.cores" number of shorter MCMC chains in parallel processes
## post <- mc.surv.bart(x.train=x.train, times=times, delta=delta,</pre>
##
                         mc.cores=5, seed=99)
pre <- surv.pre.bart(x.train=x.train, times=times, delta=delta, x.test=x.test)</pre>
pred <- predict(post, pre$tx.test)</pre>
## let's look at some survival curves
## first, a younger group with a healthier KPS
## age 50 with KPS=90: males and females
## males: row 17, females: row 23
x.test[c(17, 23), ]
low.risk.males <- 16*post$K+1:post$K ## K=unique times including censoring
low.risk.females <- 22*post$K+1:post$K</pre>
plot(post$times, pred$surv.test.mean[low.risk.males], type='s', col='blue',
     main='Age 50 with KPS=90', xlab='t', ylab='S(t)', ylim=c(0, 1))
points(post$times, pred$surv.test.mean[low.risk.females], type='s', col='red')
## End(Not run)
```

predict.wbart Predicting new observations with a previously fitted BART model

Description

BART is a Bayesian "sum-of-trees" model. For a numeric response y, we have $y = f(x) + \epsilon$, where $\epsilon \sim N(0, \sigma^2)$.

f is the sum of many tree models. The goal is to have very flexible inference for the uknown function f.

In the spirit of "ensemble models", each tree is constrained by a prior to be a weak learner so that it contributes a small amount to the overall fit.

predict.wbart

Usage

```
## S3 method for class 'wbart'
predict(object, newdata, mc.cores=1, openmp=(mc.cores.openmp()>0), ...)
```

Arguments

object	object returned from previous BART fit.
newdata	Matrix of covariates to predict y for.
mc.cores	Number of threads to utilize.
openmp	Logical value dictating whether OpenMP is utilized for parallel processing. Of course, this depends on whether OpenMP is available on your system which, by default, is verified with mc.cores.openmp.
	Other arguments which will be passed on to pwbart.

Details

BART is an Bayesian MCMC method. At each MCMC interation, we produce a draw from the joint posterior $(f, \sigma)|(x, y)$ in the numeric y case and just f in the binary y case.

Thus, unlike a lot of other modelling methods in R, we do not produce a single model object from which fits and summaries may be extracted. The output consists of values $f^*(x)$ (and σ^* in the numeric case) where * denotes a particular draw. The x is either a row from the training data (x.train) or the test data (x.test).

Value

Returns a matrix of predictions corresponding to newdata.

Author(s)

Robert McCulloch: <robert.e.mcculloch@gmail.com>, Rodney Sparapani: <rsparapa@mcw.edu>.

References

Chipman, H., George, E., and McCulloch R. (2010) Bayesian Additive Regression Trees. *The Annals of Applied Statistics*, **4,1**, 266-298 <doi:10.1214/09-AOAS285>.

Chipman, H., George, E., and McCulloch R. (2006) Bayesian Ensemble Learning. Advances in Neural Information Processing Systems 19, Scholkopf, Platt and Hoffman, Eds., MIT Press, Cambridge, MA, 265-272.

Friedman, J.H. (1991) Multivariate adaptive regression splines. The Annals of Statistics, 19, 1–67.

See Also

wbart, mc.wbart, pwbart, mc.pwbart, mc.cores.openmp

Examples

```
##simulate data (example from Friedman MARS paper)
f = function(x){
10*sin(pi*x[,1]*x[,2]) + 20*(x[,3]-.5)^2+10*x[,4]+5*x[,5]
}
sigma = 1.0 \#y = f(x) + sigma * z, z \sim N(0,1)
n = 100
             #number of observations
set.seed(99)
x=matrix(runif(n*10),n,10) #10 variables, only first 5 matter
y=f(x)
##test BART with token run to ensure installation works
set.seed(99)
post = wbart(x,y,nskip=5,ndpost=5)
x.test = matrix(runif(500*10),500,10)
## Not run:
##run BART
set.seed(99)
post = wbart(x,y)
x.test = matrix(runif(500*10),500,10)
pred = predict(post, x.test, mu=mean(y))
plot(apply(pred, 2, mean), f(x.test))
## End(Not run)
```

pwbart

Predicting new observations with a previously fitted BART model

Description

BART is a Bayesian "sum-of-trees" model. For a numeric response y, we have $y = f(x) + \epsilon$, where $\epsilon \sim N(0, \sigma^2)$.

f is the sum of many tree models. The goal is to have very flexible inference for the uknown function f.

In the spirit of "ensemble models", each tree is constrained by a prior to be a weak learner so that it contributes a small amount to the overall fit.

Usage

116

pwbart

Arguments

x.test	Matrix of covariates to predict y for.
treedraws	<pre>\$treedraws returned from wbart or pbart.</pre>
mu	Mean to add on to y prediction.
mc.cores	Number of threads to utilize.
transposed	When running pwbart or mc.pwbart in parallel, it is more memory-efficient to transpose x.test prior to calling the internal versions of these functions.
dodraws	Whether to return the draws themselves (the default), or whether to return the mean of the draws as specified by dodraws=FALSE.
nice	Set the job niceness. The default niceness is 19: niceness goes from 0 (highest) to 19 (lowest).

Details

BART is an Bayesian MCMC method. At each MCMC interation, we produce a draw from the joint posterior $(f, \sigma)|(x, y)$ in the numeric y case and just f in the binary y case.

Thus, unlike a lot of other modelling methods in R, we do not produce a single model object from which fits and summaries may be extracted. The output consists of values $f^*(x)$ (and σ^* in the numeric case) where * denotes a particular draw. The x is either a row from the training data (x.train) or the test data (x.test).

Value

Returns a matrix of predictions corresponding to x.test.

Author(s)

Robert McCulloch: <robert.e.mcculloch@gmail.com>, Rodney Sparapani: <rsparapa@mcw.edu>.

References

Chipman, H., George, E., and McCulloch R. (2010) Bayesian Additive Regression Trees. *The Annals of Applied Statistics*, **4**,**1**, 266-298 <doi:10.1214/09-AOAS285>.

Chipman, H., George, E., and McCulloch R. (2006) Bayesian Ensemble Learning. Advances in Neural Information Processing Systems 19, Scholkopf, Platt and Hoffman, Eds., MIT Press, Cambridge, MA, 265-272.

Friedman, J.H. (1991) Multivariate adaptive regression splines. The Annals of Statistics, 19, 1-67.

See Also

wbart predict.wbart

Examples

```
##simulate data (example from Friedman MARS paper)
f = function(x)
10*sin(pi*x[,1]*x[,2]) + 20*(x[,3]-.5)^2+10*x[,4]+5*x[,5]
}
sigma = 1.0 \#y = f(x) + sigma * z, z \sim N(0,1)
n = 100
             #number of observations
set.seed(99)
x=matrix(runif(n*10),n,10) #10 variables, only first 5 matter
y=f(x)
##test BART with token run to ensure installation works
set.seed(99)
post = wbart(x,y,nskip=5,ndpost=5)
x.test = matrix(runif(500*10),500,10)
## Not run:
##run BART
set.seed(99)
post = wbart(x, y)
x.test = matrix(runif(500*10),500,10)
pred = pwbart(post$treedraws, x.test, mu=mean(y))
plot(apply(pred, 2, mean), f(x.test))
## End(Not run)
```

recur.bart

BART for recurrent events

Description

Here we have implemented a simple and direct approach to utilize BART in survival analysis that is very flexible, and is akin to discrete-time survival analysis. Following the capabilities of BART, we allow for maximum flexibility in modeling the dependence of survival times on covariates. In particular, we do not impose proportional hazards.

To elaborate, consider data in the usual form: (t_i, δ_i, x_i) where t_i is the event time, δ_i is an indicator distinguishing events ($\delta = 1$) from right-censoring ($\delta = 0$), x_i is a vector of covariates, and i = 1, ..., N indexes subjects.

We denote the K distinct event/censoring times by $0 < t_{(1)} < ... < t_{(K)} < \infty$ thus taking $t_{(j)}$ to be the j^{th} order statistic among distinct observation times and, for convenience, $t_{(0)} = 0$. Now consider event indicators y_{ij} for each subject i at each distinct time $t_{(j)}$ up to and including the subject's observation time $t_i = t_{(n_i)}$ with $n_i = \sum_j I[t_{(j)} \le t_i]$. This means $y_{ij} = 0$ if $j < n_i$ and $y_{in_i} = \delta_i$.

We then denote by p_{ij} the probability of an event at time $t_{(j)}$ conditional on no previous event. We now write the model for y_{ij} as a nonparametric probit regression of y_{ij} on the time $t_{(j)}$ and the

118

covariates x_i , and then utilize BART for binary responses. Specifically, $y_{ij} = \delta_i I[t_i = t_{(j)}]$, $j = 1, ..., n_i$; we have $p_{ij} = F(\mu_{ij})$, $\mu_{ij} = \mu_0 + f(t_{(j)}, x_i)$ where F denotes the standard normal cdf (probit link). As in the binary response case, f is the sum of many tree models.

Usage

```
recur.bart(x.train=matrix(0,0,0),
           y.train=NULL, times=NULL, delta=NULL,
           x.test=matrix(0,0,0), x.test.nogrid=FALSE,
           sparse=FALSE, theta=0, omega=1,
           a=0.5, b=1, augment=FALSE, rho=NULL,
           xinfo=matrix(0,0,0), usequants=FALSE,
           rm.const=TRUE, type='pbart',
           ntype=as.integer(
               factor(type, levels=c('wbart', 'pbart', 'lbart'))),
           k=2, power=2, base=0.95,
           offset=NULL, tau.num=c(NA, 3, 6)[ntype],
           ntree=50, numcut = 100L, ndpost=1000, nskip=250,
           keepevery=10,
           printevery = 100L,
           keeptrainfits = TRUE,
           seed=99, ## mc.recur.bart only
           mc.cores=2, ## mc.recur.bart only
           nice=19L ## mc.recur.bart only
         )
mc.recur.bart(x.train=matrix(0,0,0),
              y.train=NULL, times=NULL, delta=NULL,
              x.test=matrix(0,0,0), x.test.nogrid=FALSE,
              sparse=FALSE, theta=0, omega=1,
              a=0.5, b=1, augment=FALSE, rho=NULL,
              xinfo=matrix(0,0,0), usequants=FALSE,
              rm.const=TRUE, type='pbart',
              ntype=as.integer(
                  factor(type, levels=c('wbart', 'pbart', 'lbart'))),
              k=2, power=2, base=0.95,
              offset=NULL, tau.num=c(NA, 3, 6)[ntype],
              ntree=50, numcut = 100L, ndpost=1000, nskip=250,
              keepevery=10,
              printevery = 100L,
              keeptrainfits = TRUE,
              seed=99, ## mc.recur.bart only
```

```
mc.cores=2, ## mc.recur.bart only
nice=19L ## mc.recur.bart only
)
```

Arguments

x.train	Explanatory variables for training (in sample) data. Must be a matrix with (as usual) rows corresponding to observations and columns to variables. recur.bart will generate draws of $f(t, x)$ for each x which is a row of x.train (note that the definition of x.train is dependent on whether y.train has been specified; see below).
y.train	Binary response dependent variable for training (in sample) data. If y.train is NULL, then y.train (x.train and x.test, if specified) are gen- erated by a call to recur.pre.bart (which require that times and delta be provided: see below); otherwise, y.train (x.train and x.test, if specified) are utilized as given assuming that the data construction has already been per- formed.
times	The time of event or right-censoring. If y.train is NULL, then times (and delta) must be provided.
delta	The event indicator: 1 is an event while 0 is censored. If y.train is NULL, then delta (and times) must be provided.
x.test	Explanatory variables for test (out of sample) data. Must be a matrix and have the same structure as x.train. recur.bart will generate draws of $f(t, x)$ for each x which is a row of x.test.
x.test.nogrid	Occasionally, you do not need the entire time grid for x.test. If so, then for performance reasons, you can set this argument to TRUE.
sparse	Whether to perform variable selection based on a sparse Dirichlet prior rather than simply uniform; see Linero 2016.
theta	Set <i>theta</i> parameter; zero means random.
omega	Set omega parameter; zero means random.
а	Sparse parameter for $Beta(a,b)$ prior: $0.5 <= a <= 1$ where lower values inducing more sparsity.
b	Sparse parameter for $Beta(a, b)$ prior; typically, $b = 1$.
rho	Sparse parameter: typically $rho = p$ where p is the number of covariates under consideration.
augment	Whether data augmentation is to be performed in sparse variable selection.
xinfo	You can provide the cutpoints to BART or let BART choose them for you. To provide them, use the xinfo argument to specify a list (matrix) where the items (rows) are the covariates and the contents of the items (columns) are the cutpoints.
usequants	If usequants=FALSE, then the cutpoints in xinfo are generated uniformly; oth- erwise, if TRUE, uniform quantiles are used for the cutpoints.
rm.const	Whether or not to remove constant variables.

type	Whether to employ Albert-Chib, 'pbart', or Holmes-Held, 'lbart'.
ntype	The integer equivalent of type where 'wbart' is 1, 'pbart' is 2 and 'lbart' is 3.
k	k is the number of prior standard deviations $f(t, x)$ is away from +/-3. The bigger k is, the more conservative the fitting will be.
power	Power parameter for tree prior.
base	Base parameter for tree prior.
offset	With binary BART, the centering is $P(Y = 1 x) = F(f(x) + offset)$ where offset defaults to F^{-1}(mean(y.train)). You can use the offset parameter to over-ride these defaults.
tau.num	The numerator in the tau definition, i.e., $tau=tau.num/(k*sqrt(ntree))$.
ntree	The number of trees in the sum.
numcut	The number of possible values of c (see usequants). If a single number if given, this is used for all variables. Otherwise a vector with length equal to $ncol(x.train)$ is required, where the i^{th} element gives the number of c used for the i^{th} variable in x.train. If usequants is false, numcut equally spaced cutoffs are used covering the range of values in the corresponding column of x.train. If usequants is true, then min(numcut, the number of unique values in the corresponding columns of x.train - 1) c values are used.
ndpost	The number of posterior draws returned.
nskip	Number of MCMC iterations to be treated as burn in.
keepevery	Every keepevery draw is kept to be returned to the user.
printevery	As the MCMC runs, a message is printed every printevery draws.
keeptrainfits	Whether to keep yhat.train or not.
seed	mc.recur.bart only: seed required for reproducible MCMC.
mc.cores	mc.recur.bart only: number of cores to employ in parallel.
nice	mc.recur.bart only: set the job niceness. The default niceness is 19: niceness goes from 0 (highest) to 19 (lowest).

Value

recur.bart returns an object of type recurbart which is essentially a list. Besides the items listed below, the list has a binaryOffset component giving the value used, a times component giving the unique times, K which is the number of unique times, tx.train and tx.test, if any.

yhat.train	A matrix with ndpost rows and nrow(x.train) columns. Each row corresponds to a draw f^* from the posterior of f and each column corresponds to a row of x.train. The (i, j) value is $f^*(t, x)$ for the i^{th} kept draw of f and the j^{th} row of x.train. Burn-in is dropped.
haz.train	The hazard function, $h(t x)$, where x's are the rows of the training data.
cum.train	The cumulative hazard function, $h(t x)$, where x's are the rows of the training data.

yhat.test	Same as yhat.train but now the x's are the rows of the test data.
haz.test	The hazard function, $h(t x)$, where x's are the rows of the test data.
cum.test	The cumulative hazard function, $h(t x)$, where x's are the rows of the test data.
varcount	a matrix with ndpost rows and nrow(x.train) columns. Each row is for a draw. For each variable (corresponding to the columns), the total count of the number of times that variable is used in a tree decision rule (over all trees) is given.

Note that yhat.train and yhat.test are f(t, x) + binaryOffset. If you want draws of the probability P(Y = 1|t, x) you need to apply the normal cdf (pnorm) to these values.

Author(s)

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References

Chipman, H., George, E., and McCulloch R. (2010) Bayesian Additive Regression Trees. *The Annals of Applied Statistics*, **4**,**1**, 266-298 <doi: 10.1214/09-AOAS285>.

Friedman, J.H. (1991) Multivariate adaptive regression splines. The Annals of Statistics, 19, 1–67.

Gramacy, RB and Polson, NG (2012) Simulation-based regularized logistic regression. *Bayesian Analysis*, **7**, 567–590.

Holmes, C and Held, L (2006) Bayesian auxiliary variable models for binary and multinomial regression. *Bayesian Analysis*, **1**, 145–68.

Linero, A.R. (2018) Bayesian regression trees for high dimensional prediction and variable selection. *JASA*, **113**, 626–36.

Sparapani RA, LE Rein, SS Tarima, TA Jackson, JR Meurer (2018). Non-parametric recurrent events analysis with BART and an application to the hospital admissions of patients with diabetes. *Biostatistics*, doi:10.1093/biostatistics/kxy032

See Also

recur.pre.bart, predict.recurbart, recur.pwbart, mc.recur.pwbart

Examples

```
## load 20 percent random sample
data(xdm20.train)
data(xdm20.test)
data(ydm20.train)
##test BART with token run to ensure installation works
## with current technology even a token run will violate CRAN policy
## set.seed(99)
## post <- recur.bart(x.train=xdm20.train, y.train=ydm20.train,
## nskip=1, ndpost=1, keepevery=1)
```

```
## Not run:
```

```
recur.bart
```

```
## set.seed(99)
## post <- recur.bart(x.train=xdm20.train, y.train=ydm20.train,</pre>
##
                       keeptrainfits=TRUE)
## larger data sets can take some time so, if parallel processing
## is available, submit this statement instead
post <- mc.recur.bart(x.train=xdm20.train, y.train=ydm20.train,</pre>
                       keeptrainfits=TRUE, mc.cores=8, seed=99)
require(rpart)
require(rpart.plot)
post$yhat.train.mean <- apply(post$yhat.train, 2, mean)</pre>
dss <- rpart(post$yhat.train.mean~xdm20.train)</pre>
rpart.plot(dss)
## for the 20 percent sample, notice that the top splits
## involve cci_pvd and n
## for the full data set, notice that all splits
## involve ca, cci_pud, cci_pvd, ins270 and n
## (except one at the bottom involving a small group)
## compare patients treated with insulin (ins270=1) vs
## not treated with insulin (ins270=0)
N <- 50 ## 50 training patients and 50 validation patients
K <- post$K ## 798 unique time points</pre>
NK <- 50*K
## only testing set, i.e., remove training set
xdm20.test. <- xdm20.test[NK+1:NK, post$rm.const]</pre>
xdm20.test. <- rbind(xdm20.test., xdm20.test.)</pre>
xdm20.test.[ , 'ins270'] <- rep(0:1, each=NK)</pre>
## multiple threads will be utilized if available
pred <- predict(post, xdm20.test., mc.cores=8)</pre>
## create Friedman's partial dependence function for the
## relative intensity for ins270 by time
M <- nrow(pred$haz.test) ## number of MCMC samples</pre>
RI <- matrix(0, M, K)
for(j in 1:K) {
    h <- seq(j, NK, by=K)</pre>
    RI[ , j] <- apply(pred$haz.test[ , h+NK]/</pre>
                       pred$haz.test[ , h], 1, mean)
}
RI.lo <- apply(RI, 2, quantile, probs=0.025)</pre>
RI.mu <- apply(RI, 2, mean)</pre>
RI.hi <- apply(RI, 2, quantile, probs=0.975)</pre>
plot(post$times, RI.hi, type='l', lty=2, log='y'
     ylim=c(min(RI.lo, 1/RI.hi), max(1/RI.lo, RI.hi)),
```

recur.pre.bart

```
xlab='t', ylab='RI(t, x)',
sub='insulin(ins270=1) vs. no insulin(ins270=0)',
main='Relative intensity of hospital admissions for diabetics')
lines(post$times, RI.mu)
lines(post$times, RI.lo, lty=2)
lines(post$times, rep(1, K), col='darkgray')
## RI for insulin therapy seems fairly constant with time
mean(RI.mu)
## End(Not run)
```

recur.pre.bart Data construction for recurrent events with BART

Description

Recurrent event data contained in $(t_1, \delta_1, ..., t_k, \delta_k, x)$ must be translated to data suitable for the BART model; see recur.bart for more details.

Usage

recur.pre.bart(times, delta, x.train=NULL, tstop=NULL, last.value=TRUE)

Arguments

times	Matrix of time to event or right-censoring.
delta	Matrix of event indicators: 1 is an event while 0 is censored.
x.train	Explanatory variables for training (in sample) data. If provided, must be a matrix with (as usual) rows corresponding to observations and columns to variables.
tstop	For non-instantaneous events, this the matrix of event stop times, i.e., between times[i,j] and tstop[i,j] subject i is not in the risk set for a recurrent event. N.B. This is NOT for counting process notation.
last.value	If last.value=TRUE, then the sojourn time, v, and the number of previous events, N, are carried forward assuming that no new events occur beyond censoring. If last.value=FALSE, then these variables are coded NA for easy identification allowing replacement with the desired values.

recur.pre.bart

Value

recur.pre.bart returns a list. Besides the items listed below, the list has a times component giving the unique times and K which is the number of unique times.

y.train	A vector of binary responses.
tx.train	A matrix with the rows of the training data.
tx.test	$Generated \ from \ x. \ train \ (see \ discussion \ above \ included \ in \ the \ argument \ last. \ value).$

Author(s)

Rodney Sparapani: <rsparapa@mcw.edu>

References

Sparapani, Rein, Tarima, Jackson, Meurer (2017). Nonparametric recurrent events analysis with BART and an application to the hospital admissions of patients with diabetes. MCW Biostatistics Technical Report 64 http://www.mcw.edu/FileLibrary/Groups/Biostatistics/TechReports/TechReports5175/tr064.pdf

Xu, Daniels and Winterstein (2016). Sequential BART for imputation of missing covariates. *Bio-statistics* doi:10.1093/biostatistics/kxw009

See Also

recur.bart

Examples

```
data(bladder)
subset <- -which(bladder1$stop==0)</pre>
bladder0 <- bladder1[subset, ]</pre>
id <- unique(sort(bladder0$id))</pre>
N <- length(id)</pre>
L <- max(bladder0$enum)</pre>
times <- matrix(0, nrow=N, ncol=L)</pre>
dimnames(times)[[1]] <- paste0(id)</pre>
delta <- matrix(0, nrow=N, ncol=L)</pre>
dimnames(delta)[[1]] <- paste0(id)</pre>
x.train <- matrix(NA, nrow=N, ncol=3+2*L) ## add time-dependent cols too</pre>
dimnames(x.train)[[1]] <- paste0(id)</pre>
dimnames(x.train)[[2]] <- c('Pl', 'B6', 'Th', rep(c('number', 'size'), L))</pre>
for(i in 1:N) {
    h <- id[i]
    for(j in 1:L) {
         k <- which(bladder0$id==h & bladder0$enum==j)</pre>
```

```
if(length(k)==1) {
             times[i, j] <- bladder0$stop[k]</pre>
             delta[i, j] <- (bladder0$status[k]==1)*1</pre>
             if(j==1) {
                 x.train[i, 1] <- as.numeric(bladder0$treatment[k])==1</pre>
                 x.train[i, 2] <- as.numeric(bladder0$treatment[k])==2</pre>
                 x.train[i, 3] <- as.numeric(bladder0$treatment[k])==3</pre>
                 x.train[i, 4] <- bladder0$number[k]</pre>
                 x.train[i, 5] <- bladder0$size[k]</pre>
             }
             else if(delta[i, j]==1) {
                 if(bladder0$rtumor[k]!='.')
                      x.train[i, 2*j+2] <- as.numeric(bladder0$rtumor[k])</pre>
                 if(bladder0$rsize[k]!='.')
                      x.train[i, 2*j+3] <- as.numeric(bladder0$rsize[k])</pre>
             }
        }
    }
}
pre <- recur.pre.bart(times=times, delta=delta, x.train=x.train)</pre>
J <- nrow(pre$tx.train)</pre>
for(j in 1:J) {
    if(pre$tx.train[j, 3]>0) {
        pre$tx.train[j, 7] <- pre$tx.train[j, 7+pre$tx.train[j, 3]*2]</pre>
        pre$tx.train[j, 8] <- pre$tx.train[j, 8+pre$tx.train[j, 3]*2]</pre>
    }
}
pre$tx.train <- pre$tx.train[ , 1:8]</pre>
K <- pre$K
NK <- N*K
for(j in 1:NK) {
    if(pre$tx.test[j, 3]>0) {
        pre$tx.test[j, 7] <- pre$tx.test[j, 7+pre$tx.test[j, 3]*2]</pre>
        pre$tx.test[j, 8] <- pre$tx.test[j, 8+pre$tx.test[j, 3]*2]</pre>
    }
}
pre$tx.test <- pre$tx.test[ , 1:8]</pre>
## in bladder1 both number and size are recorded as integers
## from 1 to 8 however they are often missing for recurrences
## at baseline there are no missing and 1 is the mode of both
```

```
## at baseline there are no missing and 1 is the mode of bo
pre$tx.train[which(is.na(pre$tx.train[, 7])), 7] <- 1
pre$tx.train[which(is.na(pre$tx.train[, 8])), 8] <- 1
pre$tx.test[which(is.na(pre$tx.test[, 7])), 7] <- 1
pre$tx.test[which(is.na(pre$tx.test[, 8])), 8] <- 1</pre>
```

it is a good idea to explore more sophisticated methods

```
## such as imputing the missing data with Sequential BART
## Xu, Daniels and Winterstein. Sequential BART for imputation of missing
## covariates. Biostatistics 2016 doi: 10.1093/biostatistics/kxw009
## http://biostatistics.oxfordjournals.org/content/early/2016/03/15/biostatistics.kxw009/suppl/DC1
## https://cran.r-project.org/package=sbart
## library(sbart)
## set.seed(21)
## train <- seqBART(xx=pre$tx.train, yy=NULL, datatype=rep(0, 6),</pre>
##
                   type=0, numskip=20, burn=1000)
## coarsen the imputed data same way as observed example data
## train$imputed5[which(train$imputed5[ , 7]<1), 7] <- 1</pre>
## train$imputed5[which(train$imputed5[ , 7]>8), 7] <- 8</pre>
## train$imputed5[ , 7] <- round(train$imputed5[ , 7])</pre>
## train$imputed5[which(train$imputed5[ , 8]<1), 8] <- 1</pre>
## train$imputed5[which(train$imputed5[ , 8]>8), 8] <- 8</pre>
## train$imputed5[ , 8] <- round(train$imputed5[ , 8])</pre>
## for Friedman's partial dependence, we need to estimate the whole cohort
## at each treatment assignment (and, average over those)
pre$tx.test <- rbind(pre$tx.test, pre$tx.test, pre$tx.test)</pre>
pre$tx.test[ , 4] <- c(rep(1, NK), rep(0, 2*NK))</pre>
                                                              ## Pl
pre$tx.test[ , 5] <- c(rep(0, NK), rep(1, NK), rep(0, NK))## B6</pre>
pre$tx.test[ , 6] <- c(rep(0, 2*NK), rep(1, NK))</pre>
                                                              ## Th
## Not run:
## set.seed(99)
## post <- recur.bart(y.train=pre$y.train, x.train=pre$tx.train, x.test=pre$tx.test)</pre>
## depending on your performance, you may want to run in parallel if available
post <- mc.recur.bart(y.train=pre$y.train, x.train=pre$tx.train,</pre>
                       x.test=pre$tx.test, mc.cores=8, seed=99)
M <- nrow(post$yhat.test)</pre>
RI.B6.Pl <- matrix(0, nrow=M, ncol=K)</pre>
RI.Th.Pl <- matrix(0, nrow=M, ncol=K)</pre>
RI.Th.B6 <- matrix(0, nrow=M, ncol=K)</pre>
for(j in 1:K) {
    h \le seq(j, NK, K)
    RI.B6.Pl[ , j] <- apply(post$prob.test[ , h+NK]/</pre>
                              post$prob.test[ , h], 1, mean)
    RI.Th.Pl[ , j] <- apply(post$prob.test[ , h+2*NK]/</pre>
                              post$prob.test[ , h], 1, mean)
    RI.Th.B6[ , j] <- apply(post$prob.test[ , h+2*NK]/</pre>
                              post$prob.test[ , h+NK], 1, mean)
}
RI.B6.Pl.mu <- apply(RI.B6.Pl, 2, mean)</pre>
RI.B6.Pl.025 <- apply(RI.B6.Pl, 2, quantile, probs=0.025)
RI.B6.Pl.975 <- apply(RI.B6.Pl, 2, quantile, probs=0.975)
RI.Th.Pl.mu <- apply(RI.Th.Pl, 2, mean)</pre>
RI.Th.Pl.025 <- apply(RI.Th.Pl, 2, quantile, probs=0.025)
RI.Th.Pl.975 <- apply(RI.Th.Pl, 2, quantile, probs=0.975)</pre>
```

```
RI.Th.B6.mu <- apply(RI.Th.B6, 2, mean)</pre>
RI.Th.B6.025 <- apply(RI.Th.B6, 2, quantile, probs=0.025)</pre>
RI.Th.B6.975 <- apply(RI.Th.B6, 2, quantile, probs=0.975)</pre>
plot(post$times, RI.Th.Pl.mu, col='blue',
     log='y', main='Bladder cancer ex: Thiotepa vs. Placebo',
     type='l', ylim=c(0.1, 10), ylab='RI(t)', xlab='t (months)')
lines(post$times, RI.Th.Pl.025, col='red')
lines(post$times, RI.Th.Pl.975, col='red')
abline(h=1)
plot(post$times, RI.B6.Pl.mu, col='blue',
     log='y', main='Bladder cancer ex: Vitamin B6 vs. Placebo',
     type='l', ylim=c(0.1, 10), ylab='RI(t)', xlab='t (months)')
lines(post$times, RI.B6.Pl.025, col='red')
lines(post$times, RI.B6.Pl.975, col='red')
abline(h=1)
plot(post$times, RI.Th.B6.mu, col='blue',
     log='y', main='Bladder cancer ex: Thiotepa vs. Vitamin B6',
     type='l', ylim=c(0.1, 10), ylab='RI(t)', xlab='t (months)')
lines(post$times, RI.Th.B6.025, col='red')
lines(post$times, RI.Th.B6.975, col='red')
abline(h=1)
```

End(Not run)

rs.pbart

BART for dichotomous outcomes with parallel computation and stratified random sampling

Description

BART is a Bayesian "sum-of-trees" model.

For numeric response y, we have $y = f(x) + \epsilon$, where $\epsilon \sim N(0, \sigma^2)$.

For a binary response y, P(Y = 1|x) = F(f(x)), where F denotes the standard normal cdf (probit link).

In both cases, f is the sum of many tree models. The goal is to have very flexible inference for the uknown function f.

In the spirit of "ensemble models", each tree is constrained by a prior to be a weak learner so that it contributes a small amount to the overall fit.

Usage

```
rs.pbart(
    x.train, y.train, x.test=matrix(0.0,0,0),
    C=floor(length(y.train)/2000),
```

rs.pbart

```
k=2.0, power=2.0, base=.95,
binaryOffset=0,
ntree=50L, numcut=100L,
ndpost=1000L, nskip=100L,
keepevery=1L, printevery=100,
keeptrainfits=FALSE, transposed=FALSE,
mc.cores = 2L, nice = 19L,
seed = 99L
```

```
)
```

Arguments

y.trainDependent variable for training (in sample) data. If y is numeric a continous response model is fit (normal errors). If y is a factor (or just has values 0 and 1) then a binary response model with a probit link is fit.x.testExplanatory variables for test (out of sample) data. Should have same structure as x.train. pbart will generate draws of $f(x)$ for each x which is a row of x.test.CThe number of shards to break the data into and analyze separately.kFor binary y, k is the number of prior standard deviations $f(x)$ is away from $+/-3$. In both cases, the bigger k is, the more conservative the fitting will be.powerPower parameter for tree prior.baseBase parameter for tree prior.binaryOffsetUsed for binary y. The model is $P(Y = 1 x) = F(f(x) + binaryOffset)$. The idea is that f is shrunk towards 0, so the offset allows you to shrink towards a probability other than .5.numcutThe number of possible values of c (see usequants). If a single number if given, this is used for all variables. Otherwise a vector with length equal to ncol(x.train) is required, where the i^{th} element gives the number of c used for the i^{th} variable in x.train. If usequants is false, numcut equally spaced cutoffs are used covering the range of values in the corresponding column of x.train. If usequants is true, then min(numcut, the number of unique values in the corresponding columns of x.train - 1) c values are used.ndpostThe number of posterior draws returned.nskipNumber of MCMC iterations to be treated as burn in.	x.train	Explanatory variables for training (in sample) data. May be a matrix or a data frame, with (as usual) rows corresponding to observations and columns to variables. If a variable is a factor in a data frame, it is replaced with dummies. Note that q dummies are created if $q>2$ and one dummy is created if $q=2$, where q is the number of levels of the factor. pbart will generate draws of $f(x)$ for each x which is a row of x.train.
Should have same structure as x.train. pbart will generate draws of $f(x)$ for each x which is a row of x.test. C The number of shards to break the data into and analyze separately. k For binary y, k is the number of prior standard deviations $f(x)$ is away from +/-3. In both cases, the bigger k is, the more conservative the fitting will be. power Power parameter for tree prior. base Base parameter for tree prior. binaryOffset Used for binary y. The model is $P(Y = 1 x) = F(f(x) + binaryOffset)$. The idea is that f is shrunk towards 0, so the offset allows you to shrink towards a probability other than .5. ntree The number of trees in the sum. numcut The number of possible values of c (see usequants). If a single number if given, this is used for all variables. Otherwise a vector with length equal to ncol(x.train) is required, where the i^{th} element gives the number of c used for the i^{th} variable in x.train. If usequants is false, numcut equally spaced cutoffs are used covering the range of values in the corresponding column of x.train. If usequants is true, then min(numcut, the number of unique values in the corresponding columns of x.train - 1) c values are used. ndpost The number of posterior draws returned.	y.train	If y is numeric a continous response model is fit (normal errors). If y is a factor (or just has values 0 and 1) then a binary response model with a
CThe number of shards to break the data into and analyze separately.kFor binary y, k is the number of prior standard deviations $f(x)$ is away from $+/-3$. In both cases, the bigger k is, the more conservative the fitting will be.powerPower parameter for tree prior.baseBase parameter for tree prior.binaryOffsetUsed for binary y. The model is $P(Y = 1 x) = F(f(x) + binaryOffset)$. The idea is that f is shrunk towards 0, so the offset allows you to shrink towards a probability other than .5.ntreeThe number of possible values of c (see usequants). If a single number if given, this is used for all variables. Otherwise a vector with length equal to ncol(x.train) is required, where the i^{th} element gives the number of c used for the i^{th} variable in x.train. If usequants is false, numcut equally spaced cutoffs are used covering the range of values in the corresponding column of x.train. If usequants is true, then min(numcut, the number of unique values in the corresponding columns of x.train - 1) c values are used.ndpostThe number of posterior draws returned.	x.test	Should have same structure as x.train.
kFor binary y, k is the number of prior standard deviations $f(x)$ is away from +/-3. In both cases, the bigger k is, the more conservative the fitting will be.powerPower parameter for tree prior.baseBase parameter for tree prior.binaryOffsetUsed for binary y. The model is $P(Y = 1 x) = F(f(x) + binaryOffset)$. The idea is that f is shrunk towards 0, so the offset allows you to shrink towards a probability other than .5.ntreeThe number of trees in the sum.numcutThe number of possible values of c (see usequants). If a single number if given, this is used for all variables. Otherwise a vector with length equal to ncol(x.train) is required, where the i^{th} element gives the number of c used for the i^{th} variable in x.train. If usequants is false, numcut equally spaced cutoffs are used covering the range of values in the corresponding column of x.train. If usequants is true, then min(numcut, the number of unique values in the corresponding columns of x.train - 1) c values are used.ndpostThe number of posterior draws returned.	С	
baseBase parameter for tree prior.binaryOffsetUsed for binary y . The model is $P(Y = 1 x) = F(f(x) + binaryOffset)$. The idea is that f is shrunk towards 0, so the offset allows you to shrink towards a probability other than .5.ntreeThe number of trees in the sum.numcutThe number of possible values of c (see usequants). If a single number if given, this is used for all variables. Otherwise a vector with length equal to ncol(x.train) is required, where the i^{th} element gives the number of c used for the i^{th} variable in x.train. If usequants is false, numcut equally spaced cutoffs are used covering 	k	
binaryOffsetUsed for binary y . The model is $P(Y = 1 x) = F(f(x) + binaryOffset)$. The idea is that f is shrunk towards 0, so the offset allows you to shrink towards a probability other than .5.ntreeThe number of trees in the sum.numcutThe number of possible values of c (see usequants). If a single number if given, this is used for all variables. Otherwise a vector with length equal to ncol(x.train) is required, where the i^{th} element gives the number of c used for the i^{th} variable in x.train. If usequants is false, numcut equally spaced cutoffs are used covering the range of values in the corresponding column of x.train. If usequants is true, then min(numcut, the number of unique values in the corresponding columns of x.train - 1) c values are used.ndpostThe number of posterior draws returned.	power	Power parameter for tree prior.
The model is $P(Y = 1 x) = F(f(x) + binaryOffset)$. The idea is that f is shrunk towards 0, so the offset allows you to shrink towards a probability other than .5.ntreeThe number of trees in the sum.numcutThe number of possible values of c (see usequants). If a single number if given, this is used for all variables. Otherwise a vector with length equal to ncol(x.train) is required, where the i^{th} element gives the number of c used for the i^{th} variable in x.train. If usequants is false, numcut equally spaced cutoffs are used covering the range of values in the corresponding column of x.train. If usequants is true, then min(numcut, the number of unique values in the corresponding columns of x.train - 1) c values are used.ndpostThe number of posterior draws returned.	base	Base parameter for tree prior.
numcutThe number of possible values of c (see usequants). If a single number if given, this is used for all variables. Otherwise a vector with length equal to ncol(x.train) is required, where the i^{th} element gives the number of c used for the i^{th} variable in x.train. If usequants is false, numcut equally spaced cutoffs are used covering the range of values in the corresponding column of x.train. If usequants is true, then min(numcut, the number of unique values in the corresponding columns of x.train - 1) c values are used.ndpostThe number of posterior draws returned.	binaryOffset	The model is $P(Y = 1 x) = F(f(x) + binaryOffset)$. The idea is that f is shrunk towards 0, so the offset allows you to shrink towards
 this is used for all variables. Otherwise a vector with length equal to ncol(x.train) is required, where the <i>i</i>th element gives the number of c used for the <i>i</i>th variable in x.train. If usequants is false, numcut equally spaced cutoffs are used covering the range of values in the corresponding column of x.train. If usequants is true, then min(numcut, the number of unique values in the corresponding columns of x.train - 1) c values are used. ndpost The number of posterior draws returned. 	ntree	The number of trees in the sum.
	numcut	this is used for all variables. Otherwise a vector with length equal to $ncol(x.train)$ is required, where the i^{th} element gives the number of c used for the i^{th} variable in x.train. If usequants is false, numcut equally spaced cutoffs are used covering the range of values in the corresponding column of x.train. If usequants is true, then min(numcut, the number of unique values in the corresponding columns of
nskip Number of MCMC iterations to be treated as burn in.	ndpost	The number of posterior draws returned.
•	nskip	Number of MCMC iterations to be treated as burn in.

keepevery	Every keepevery draw is kept to be returned to the user.
printevery	As the MCMC runs, a message is printed every printevery draws.
keeptrainfits	Whether to keep yhat.train or not.
transposed	When running pbart in parallel, it is more memory-efficient to transpose x.train and x.test, if any, prior to calling mc.pbart.
seed	Setting the seed required for reproducible MCMC.
mc.cores	Number of cores to employ in parallel.
nice	Set the job niceness. The default niceness is 19: niceness goes from 0 (highest) to 19 (lowest).

Details

BART is an Bayesian MCMC method. At each MCMC interation, we produce a draw from the joint posterior $(f, \sigma)|(x, y)$ in the numeric y case and just f in the binary y case.

Thus, unlike a lot of other modelling methods in R, we do not produce a single model object from which fits and summaries may be extracted. The output consists of values $f^*(x)$ (and σ^* in the numeric case) where * denotes a particular draw. The x is either a row from the training data (x.train) or the test data (x.test).

Value

rs.pbart returns an object of type pbart which is essentially a list.

yhat.shard	Estimates generated from the individual shards rather than from the whole. This object is only useful for assessing convergence. A matrix with ndpost rows and nrow(x.train) columns. Each row corresponds to a draw f^* from the posterior of f and each column corresponds to a row of x.train. The (i, j) value is $f^*(x)$ for the i^{th} kept draw of f and the j^{th} row of x.train. Burn-in is dropped.
yhat.train	Estimates generated from the whole if keeptrainfits=TRUE. A matrix with ndpost rows and nrow(x.train) columns. Each row corresponds to a draw f^* from the posterior of f and each column corresponds to a row of x.train. The (i, j) value is $f^*(x)$ for the i^{th} kept draw of f and the j^{th} row of x.train. Burn-in is dropped.
yhat.test	Estimates generated from the whole if x.test is provided. Same as yhat.train but now the x's are the rows of the test data.
varcount	a matrix with ndpost rows and nrow(x.train) columns. Each row is for a draw. For each variable (corresponding to the columns), the total count of the number of times that variable is used in a tree decision rule (over all trees) is given.

In addition the list has a binaryOffset component giving the value used.

Note that in the binary y, case yhat.train and yhat.test are f(x) + binaryOffset. If you want draws of the probability P(Y = 1|x) you need to apply the normal cdf (pnorm) to these values.

rs.pbart

Author(s)

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References

Chipman, H., George, E., and McCulloch R. (2010) Bayesian Additive Regression Trees. *The Annals of Applied Statistics*, **4,1**, 266-298 <doi:10.1214/09-AOAS285>.

Chipman, H., George, E., and McCulloch R. (2006) Bayesian Ensemble Learning. Advances in Neural Information Processing Systems 19, Scholkopf, Platt and Hoffman, Eds., MIT Press, Cambridge, MA, 265-272.

Friedman, J.H. (1991) Multivariate adaptive regression splines. The Annals of Statistics, 19, 1-67.

See Also

mc.pbart

Examples

```
##simulate from Friedman's five-dimensional test function
##Friedman JH. Multivariate adaptive regression splines
##(with discussion and a rejoinder by the author).
##Annals of Statistics 1991; 19:1-67.
f = function(x) #only the first 5 matter
    sin(pi*x[, 1]*x[, 2]) + 2*(x[, 3]-.5)^2+x[, 4]+0.5*x[, 5]-1.5
sigma = 1.0 \#y = f(x) + sigma \times z where z \sim N(0, 1)
k = 50
             #number of covariates
thin = 25
ndpost = 2500
nskip = 100
C = 10
m = 10
n = 10000
set.seed(12)
x.train=matrix(runif(n*k), n, k)
Ey.train = f(x.train)
y.train=(Ey.train+sigma*rnorm(n)>0)*1
table(y.train)/n
x <- x.train
x4 <- seq(0, 1, length.out=m)</pre>
for(i in 1:m) {
    x[ , 4] <- x4[i]
    if(i==1) x.test <- x
    else x.test <- rbind(x.test, x)</pre>
```

```
}
## parallel::mcparallel/mccollect do not exist on windows
if(.Platform$OS.type=='unix') {
##test BART with token run to ensure installation works
    post = rs.pbart(x.train, y.train,
                C=C, mc.cores=4, keepevery=1,
                 seed=99, ndpost=1, nskip=1)
}
## Not run:
post = rs.pbart(x.train, y.train, x.test=x.test,
                C=C, mc.cores=8, keepevery=thin,
                 seed=99, ndpost=ndpost, nskip=nskip)
str(post)
par(mfrow=c(2, 2))
M <- nrow(post$yhat.test)</pre>
pred <- matrix(nrow=M, ncol=10)</pre>
for(i in 1:m) {
    h <- (i-1)*n+1:n
    pred[ , i] <- apply(pnorm(post$yhat.test[ , h]), 1, mean)</pre>
}
pred <- apply(pred, 2, mean)</pre>
plot(x4, qnorm(pred), xlab=expression(x[4]),
     ylab='partial dependence function', type='l')
i <- floor(seq(1, n, length.out=10))</pre>
j <- seq(-0.5, 0.4, length.out=10)</pre>
for(h in 1:10) {
    auto.corr <- acf(post$yhat.shard[ , i[h]], plot=FALSE)</pre>
    if(h==1) {
        max.lag <- max(auto.corr$lag[ , 1, 1])</pre>
        plot(1:max.lag+j[h], auto.corr$acf[1+(1:max.lag), 1, 1],
             type='h', xlim=c(0, max.lag+1), ylim=c(-1, 1),
             ylab='auto-correlation', xlab='lag')
    }
    else
        lines(1:max.lag+j[h], auto.corr$acf[1+(1:max.lag), 1, 1],
              type='h', col=h)
}
for(j in 1:10) {
    if(j==1)
        plot(pnorm(post$yhat.shard[ , i[j]]),
             type='l', ylim=c(0, 1),
             sub=paste0('N:', n, ', k:', k),
             ylab=expression(Phi(f(x))), xlab='m')
    else
```

132

rtgamma

```
lines(pnorm(post$yhat.shard[ , i[j]]),
              type='l', col=j)
}
geweke <- gewekediag(post$yhat.shard)</pre>
j <- -10^(log10(n)-1)
plot(geweke$z, pch='.', cex=2, ylab='z', xlab='i',
     sub=paste0('N:', n, ', k:', k),
     xlim=c(j, n), ylim=c(-5, 5))
lines(1:n, rep(-1.96, n), type='l', col=6)
lines(1:n, rep(+1.96, n), type='l', col=6)
lines(1:n, rep(-2.576, n), type='l', col=5)
lines(1:n, rep(+2.576, n), type='l', col=5)
lines(1:n, rep(-3.291, n), type='l', col=4)
lines(1:n, rep(+3.291, n), type='l', col=4)
lines(1:n, rep(-3.891, n), type='l', col=3)
lines(1:n, rep(+3.891, n), type='l', col=3)
lines(1:n, rep(-4.417, n), type='l', col=2)
lines(1:n, rep(+4.417, n), type='l', col=2)
text(c(1, 1), c(-1.96, 1.96), pos=2, cex=0.6, labels='0.95')
text(c(1, 1), c(-2.576, 2.576), pos=2, cex=0.6, labels='0.99')
text(c(1, 1), c(-3.291, 3.291), pos=2, cex=0.6, labels='0.999')
text(c(1, 1), c(-3.891, 3.891), pos=2, cex=0.6, labels='0.9999')
text(c(1, 1), c(-4.417, 4.417), pos=2, cex=0.6, labels='0.99999')
par(mfrow=c(1, 1))
##dev.copy2pdf(file='geweke.rs.pbart.pdf')
## End(Not run)
```

rtgamma

Testing truncated Gamma sampling

Description

Truncated Gamma draws are needed for the standard deviation of the random effects Gibbs conditional.

Usage

rtgamma(n, shape, rate, a)

Arguments

n	Number of samples.
shape	Sampling from a truncated Gamma where $E[x] = shape/rate$.

rtnorm

rate	This parameter is the inverse of the scale which is an alternative representation
	for the Gamma distribution.
а	The truncation point, i.e., $a < x$.

Value

Returns n truncated Gamma, i.e., Gam(shape, rate)I(a, infinity).

Author(s)

Robert McCulloch: <robert.e.mcculloch@gmail.com>, Rodney Sparapani: <rsparapa@mcw.edu> , Robert Gramacy: <rbg@vt.edu>.

References

Gentle, J. E. (2013) Random number generation and Monte Carlo methods. Springer, New York, NY.

Examples

```
set.seed(12)
rtgamma(1, 3, 1, 4)
rtgamma(1, 3, 1, 4)
a=rtgamma(10000, 10, 2, 1)
mean(a)
min(a)
```

```
rtnorm
```

Testing truncated Normal sampling

Description

Truncated Normal latents are necessary to transform a binary BART into a continuous BART.

Usage

rtnorm(n, mean, sd, tau)

Arguments

n	Number of samples.
mean	Mean.
sd	Standard deviation.
tau	Truncation point.

spectrum0ar

Value

Returns n truncated Normals, i.e., N(mean, sd)I(tau, infinity).

Author(s)

Robert McCulloch: <robert.e.mcculloch@gmail.com>,
Rodney Sparapani: <rsparapa@mcw.edu>
, Robert Gramacy: <rbg@vt.edu>.

References

Robert, C.P. (1995) Simulation of truncated normal variables. *Statistics and computing*, **5**(2), 121–125.

See Also

pbart,lbart

Examples

set.seed(12)

rtnorm(1, 0, 1, 3) rtnorm(1, 0, 1, 3)

spectrum0ar

Estimate spectral density at zero

Description

The spectral density at frequency zero is estimated by fitting an autoregressive model. spectrum0(x)/length(x) estimates the variance of mean(x).

Usage

spectrum0ar(x)

Arguments

Х

Matrix of MCMC chains: the rows are the samples and the columns are different "parameters". For BART, generally, the columns are estimates of f. For pbart, they are different subjects. For surv.bart, they are different subjects at a grid of times.

Details

The ar() function to fit an autoregressive model to the time series x. For multivariate time series, separate models are fitted for each column. The value of the spectral density at zero is then given by a well-known formula. Adapted from the spectrum0.ar function of the coda package which passes mcmc objects as arguments rather than matrices.

Value

A list with the following values

spec	The predicted value of the spectral density at frequency zero.
order	The order of the fitted model

References

Martyn Plummer, Nicky Best, Kate Cowles and Karen Vines (2006). CODA: Convergence Diagnosis and Output Analysis for MCMC, R News, vol 6, 7-11.

BW Silverman (1986). Density estimation for statistics and data analysis. Chapman and Hall, London.

See Also

gewekediag

srstepwise

Stepwise Variable Selection Procedure for survreg

Description

This stepwise variable selection procedure can be applied to obtain the best candidates for a survreg fit.

Usage

```
srstepwise(x, times, delta, sle = 0.15, sls = 0.15, dist='lognormal')
```

Arguments

х	Matrix of variables to consider.
times	The time to an event, if any.
delta	The event indicator: 1 for event, 0 for no event.
sle	The chosen significance level for entering.
sls	The chosen significance level for staying.
dist	The distribution to be used by survreg.

136

stratrs

Details

Unfortunately, no stepwise procedure exists for survreg models. Therefore, we provide this brute force method.

Value

Returns a list of indices of variables which have entered and stayed.

See Also

lung

Examples

```
names. <- names(lung)[-(2:3)]
status1 <- ifelse(lung$status==2,1,0)
X <- as.matrix(lung)[ , names.]
vars=srstepwise(X, lung$time, status1)
print(names.[vars])</pre>
```

stratrs	Perform stratified random sampling to balance outcomes
---------	--

Description

This function is used to perform stratified random sampling to balance outcomes among the shards.

Usage

stratrs(y, C=5, P=0)

Arguments

У	The binary/categorical/continuous outcome.
С	The number of shards to break the data set into.
Р	For continuous data, we break the range into P segments via the quantiles. Spec- ifying, P=20 seems to work reasonably well.

Details

To perform BART with large data sets, random sampling is employed to break the data into C shards. Each shard should be balanced with respect to the outcome. For binary/categorical outcomes, stratified random sampling is employed with this function.

surv.bart

Value

A vector is returned with each element assigned to a shard.

See Also

rs.pbart

Examples

```
set.seed(12)
x <- rbinom(25000, 1, 0.1)
a <- stratrs(x)
table(a, x)
z <- pmin(rpois(25000, 0.8), 5)
b <- stratrs(z)
table(b, z)</pre>
```

surv.bart

Survival analysis with BART

Description

Here we have implemented a simple and direct approach to utilize BART in survival analysis that is very flexible, and is akin to discrete-time survival analysis. Following the capabilities of BART, we allow for maximum flexibility in modeling the dependence of survival times on covariates. In particular, we do not impose proportional hazards.

To elaborate, consider data in the usual form: (t_i, δ_i, x_i) where t_i is the event time, δ_i is an indicator distinguishing events ($\delta = 1$) from right-censoring ($\delta = 0$), x_i is a vector of covariates, and i = 1, ..., N indexes subjects.

We denote the K distinct event/censoring times by $0 < t_{(1)} < ... < t_{(K)} < \infty$ thus taking $t_{(j)}$ to be the j^{th} order statistic among distinct observation times and, for convenience, $t_{(0)} = 0$. Now consider event indicators y_{ij} for each subject i at each distinct time $t_{(j)}$ up to and including the subject's observation time $t_i = t_{(n_i)}$ with $n_i = \sum_j I[t_{(j)} \le t_i]$. This means $y_{ij} = 0$ if $j < n_i$ and $y_{in_i} = \delta_i$.

We then denote by p_{ij} the probability of an event at time $t_{(j)}$ conditional on no previous event. We now write the model for y_{ij} as a nonparametric probit regression of y_{ij} on the time $t_{(j)}$ and the covariates x_i , and then utilize BART for binary responses. Specifically, $y_{ij} = \delta_i I[t_i = t_{(j)}]$, $j = 1, ..., n_i$; we have $p_{ij} = F(\mu_{ij})$, $\mu_{ij} = \mu_0 + f(t_{(j)}, x_i)$ where F denotes the standard normal cdf (probit link). As in the binary response case, f is the sum of many tree models.

Usage

```
surv.bart( x.train=matrix(0,0,0),
    y.train=NULL, times=NULL, delta=NULL,
    x.test=matrix(0,0,0),
```

138

```
K=NULL, events=NULL, ztimes=NULL, zdelta=NULL,
           sparse=FALSE, theta=0, omega=1,
           a=0.5, b=1, augment=FALSE, rho=NULL,
           xinfo=matrix(0,0,0), usequants=FALSE,
           rm.const=TRUE, type='pbart',
           ntype=as.integer(
               factor(type, levels=c('wbart', 'pbart', 'lbart'))),
           k=2, power=2, base=.95,
           offset=NULL, tau.num=c(NA, 3, 6)[ntype],
           ntree=50, numcut=100, ndpost=1000, nskip=250,
           keepevery = 10L,
           printevery=100L,
           id=NULL,
                       ## surv.bart only
           seed=99, ## mc.surv.bart only
           mc.cores=2, ## mc.surv.bart only
           nice=19L ## mc.surv.bart only
         )
mc.surv.bart( x.train=matrix(0,0,0),
              y.train=NULL, times=NULL, delta=NULL,
              x.test=matrix(0,0,0),
              K=NULL, events=NULL, ztimes=NULL, zdelta=NULL,
              sparse=FALSE, theta=0, omega=1,
              a=0.5, b=1, augment=FALSE, rho=NULL,
              xinfo=matrix(0,0,0), usequants=FALSE,
              rm.const=TRUE, type='pbart',
              ntype=as.integer(
                  factor(type, levels=c('wbart', 'pbart', 'lbart'))),
              k=2, power=2, base=.95,
              offset=NULL, tau.num=c(NA, 3, 6)[ntype],
              ntree=50, numcut=100, ndpost=1000, nskip=250,
              keepevery = 10L,
              printevery=100L,
              id=NULL,
                          ## surv.bart only
                          ## mc.surv.bart only
              seed=99,
              mc.cores=2, ## mc.surv.bart only
```

nice=19L ## mc.surv.bart only

)

Arguments

x.train	Explanatory variables for training (in sample) data. Must be a matrix with (as usual) rows corresponding to observations and columns to variables. surv.bart will generate draws of $f(t, x)$ for each x which is a row of x.train (note that the definition of x.train is dependent on whether y.train has been specified; see below).
y.train	Binary response dependent variable for training (in sample) data. If y.train is NULL, then y.train (x.train and x.test, if specified) are gen- erated by a call to surv.pre.bart (which require that times and delta be provided: see below); otherwise, y.train (x.train and x.test, if specified) are utilized as given assuming that the data construction has already been per- formed.
times	The time of event or right-censoring. If y.train is NULL, then times (and delta) must be provided.
delta	The event indicator: 1 is an event while 0 is censored. If y.train is NULL, then delta (and times) must be provided.
x.test	Explanatory variables for test (out of sample) data. Must be a matrix and have the same structure as x.train. surv.bart will generate draws of $f(t, x)$ for each x which is a row of x.test.
К	If provided, then coarsen times per the quantiles $1/K, 2/K,, K/K$.
events	If provided, then use for the grid of time points.
ztimes	If provided, then these columns of x.train (and x.test if any) are the times for time-dependent covariates. They will be transformed into time-dependent covariate sojourn times.
zdelta	If provided, then these columns of x.train (and x.test if any) are the delta for time-dependent covariates. They will be transformed into time-dependent covariate binary events.
sparse	Whether to perform variable selection based on a sparse Dirichlet prior rather than simply uniform; see Linero 2016.
theta	Set <i>theta</i> parameter; zero means random.
omega	Set <i>omega</i> parameter; zero means random.
а	Sparse parameter for $Beta(a,b)$ prior: $0.5 <= a <= 1$ where lower values inducing more sparsity.
b	Sparse parameter for $Beta(a, b)$ prior; typically, $b = 1$.
rho	Sparse parameter: typically $rho = p$ where p is the number of covariates under consideration.
augment	Whether data augmentation is to be performed in sparse variable selection.

surv.bart

xinfo	You can provide the cutpoints to BART or let BART choose them for you. To provide them, use the xinfo argument to specify a list (matrix) where the items (rows) are the covariates and the contents of the items (columns) are the cutpoints.
usequants	If usequants=FALSE, then the cutpoints in xinfo are generated uniformly; oth- erwise, if TRUE, uniform quantiles are used for the cutpoints.
rm.const	Whether or not to remove constant variables.
type	Whether to employ Albert-Chib, 'pbart', or Holmes-Held, 'lbart'.
ntype	The integer equivalent of type where 'wbart' is 1, 'pbart' is 2 and 'lbart' is 3.
k	k is the number of prior standard deviations $f(t, x)$ is away from +/-3. The bigger k is, the more conservative the fitting will be.
power	Power parameter for tree prior.
base	Base parameter for tree prior.
offset	With binary BART, the centering is $P(Y = 1 x) = F(f(x) + offset)$ where offset defaults to F^{-1}(mean(y.train)). You can use the offset parameter to over-ride these defaults.
tau.num	The numerator in the tau definition, i.e., tau=tau.num/(k*sqrt(ntree)).
ntree	The number of trees in the sum.
ndpost	The number of posterior draws returned.
nskip	Number of MCMC iterations to be treated as burn in.
printevery	As the MCMC runs, a message is printed every printevery draws.
keepevery	Every keepevery draw is kept to be returned to the user. A "draw" will consist of values $f^*(t, x)$ at $x = rows$ from the train(optionally) and test data, where f^* denotes the current draw of f .
numcut	The number of possible values of c (see usequants). If a single number if given, this is used for all variables. Otherwise a vector with length equal to $ncol(x.train)$ is required, where the i^{th} element gives the number of c used for the i^{th} variable in x.train. If usequants is false, numcut equally spaced cutoffs are used covering the range of values in the corresponding column of x.train. If usequants is true, then min(numcut, the number of unique values in the corresponding columns of x.train - 1) c values are used.
id	surv.bart only: unique identifier added to returned list.
seed	mc.surv.bart only: seed required for reproducible MCMC.
mc.cores	mc.surv.bart only: number of cores to employ in parallel.
nice	mc.surv.bart only: set the job niceness. The default niceness is 19: niceness goes from 0 (highest) to 19 (lowest).

Value

surv.bart returns an object of type survbart which is essentially a list. Besides the items listed below, the list has a binaryOffset component giving the value used, a times component giving the unique times, K which is the number of unique times, tx.train and tx.test, if any.

to a draw f^* from the posterior of f and each column corresponds to a row of x.train. The (i, j) value is $f^*(t, x)$ for the i^{th} kept draw of f and the j^{th} row of x.train. Burn-in is dropped. yhat.test Same as yhat.train but now the x's are the rows of the test data. surv.test The survival function, $S(t x)$, where x's are the rows of the test data. yhat.train.mean train data fits = mean of yhat.train columns. yhat.test.mean test data fits = mean of yhat.test columns. surv.test.mean mean of surv.test columns. varcount a matrix with ndpost rows and nrow(x.train) columns. Each row is for a draw		
surv.testThe survival function, $S(t x)$, where x's are the rows of the test data.yhat.train.meantrain data fits = mean of yhat.train columns.yhat.test.meantest data fits = mean of yhat.test columns.surv.test.meanmean of surv.test columns.varcounta matrix with ndpost rows and nrow(x.train) columns. Each row is for a draw For each variable (corresponding to the columns), the total count of the number	yhat.train	
<pre>yhat.train.mean train data fits = mean of yhat.train columns. yhat.test.mean surv.test.mean varcount a matrix with ndpost rows and nrow(x.train) columns. Each row is for a draw For each variable (corresponding to the columns), the total count of the number of the</pre>	yhat.test	Same as yhat.train but now the x's are the rows of the test data.
train data fits = mean of yhat.train columns.yhat.test.meantest data fits = mean of yhat.test columns.surv.test.meanmean of surv.test columns.varcounta matrix with ndpost rows and nrow(x.train) columns. Each row is for a draw For each variable (corresponding to the columns), the total count of the number	surv.test	The survival function, $S(t x)$, where x's are the rows of the test data.
<pre>yhat.test.mean test data fits = mean of yhat.test columns. surv.test.mean mean of surv.test columns. a matrix with ndpost rows and nrow(x.train) columns. Each row is for a draw For each variable (corresponding to the columns), the total count of the number </pre>	yhat.train.mear	
surv.test.mean mean of surv.test columns. varcount a matrix with ndpost rows and nrow(x.train) columns. Each row is for a draw For each variable (corresponding to the columns), the total count of the number		train data fits = mean of yhat.train columns.
varcount a matrix with ndpost rows and nrow(x.train) columns. Each row is for a draw For each variable (corresponding to the columns), the total count of the number	yhat.test.mean	test data fits = mean of yhat.test columns.
For each variable (corresponding to the columns), the total count of the number	surv.test.mean	mean of surv.test columns.
	varcount	a matrix with ndpost rows and nrow(x.train) columns. Each row is for a draw. For each variable (corresponding to the columns), the total count of the number of times that variable is used in a tree decision rule (over all trees) is given.

Note that yhat.train and yhat.test are f(t, x) + binaryOffset. If you want draws of the probability P(Y = 1|t, x) you need to apply the normal cdf (pnorm) to these values.

Author(s)

Rodney Sparapani: <rsparapa@mcw.edu>

References

Chipman, H., George, E., and McCulloch R. (2010) Bayesian Additive Regression Trees. *The Annals of Applied Statistics*, **4**,**1**, 266-298 <doi: 10.1214/09-AOAS285>.

Friedman, J.H. (1991) Multivariate adaptive regression splines. The Annals of Statistics, 19, 1–67.

Gramacy, RB and Polson, NG (2012) Simulation-based regularized logistic regression. *Bayesian Analysis*, **7**, 567–590.

Holmes, C and Held, L (2006) Bayesian auxiliary variable models for binary and multinomial regression. *Bayesian Analysis*, **1**, 145–68.

Linero, A.R. (2018) Bayesian regression trees for high dimensional prediction and variable selection. *JASA*, **113**, 626–36.

Sparapani, R., Logan, B., McCulloch, R., and Laud, P. (2016) Nonparametric survival analysis using Bayesian Additive Regression Trees (BART). *Statistics in Medicine*, **16**, 2741–53 <doi:10.1002/sim.6893>.

See Also

surv.pre.bart

Examples

load survival package for the advanced lung cancer example
data(lung)

N <- length(lung\$status)</pre>

surv.bart

```
table(lung$ph.karno, lung$pat.karno)
## if physician's KPS unavailable, then use the patient's
h <- which(is.na(lung$ph.karno))</pre>
lung$ph.karno[h] <- lung$pat.karno[h]</pre>
times <- lung$time</pre>
delta <- lung$status-1 ##lung$status: 1=censored, 2=dead
##delta: 0=censored, 1=dead
## this study reports time in days rather than weeks or months
## coarsening from days to weeks or months will reduce the computational burden
##times <- ceiling(times/30)</pre>
times <- ceiling(times/7) ## weeks</pre>
table(times)
table(delta)
## matrix of observed covariates
x.train <- cbind(lung$sex, lung$age, lung$ph.karno)</pre>
## lung$sex:
                    Male=1 Female=2
## lung$age:
                    Age in years
                    Karnofsky performance score (dead=0:normal=100:by=10)
## lung$ph.karno:
##
                    rated by physician
dimnames(x.train)[[2]] <- c('M(1):F(2)', 'age(39:82)', 'ph.karno(50:100:10)')</pre>
table(x.train[ , 1])
summary(x.train[ , 2])
table(x.train[ , 3])
##test BART with token run to ensure installation works
set.seed(99)
post <- surv.bart(x.train=x.train, times=times, delta=delta,</pre>
                  nskip=1, ndpost=1, keepevery=1)
## Not run:
## run one long MCMC chain in one process
## set.seed(99)
## post <- surv.bart(x.train=x.train, times=times, delta=delta, x.test=x.test)</pre>
## in the interest of time, consider speeding it up by parallel processing
## run "mc.cores" number of shorter MCMC chains in parallel processes
post <- mc.surv.bart(x.train=x.train, times=times, delta=delta,</pre>
                      mc.cores=8, seed=99)
pre <- surv.pre.bart(times=times, delta=delta, x.train=x.train,</pre>
                      x.test=x.train)
K <- pre$K
M <- nrow(post$yhat.train)</pre>
```

```
pre$tx.test <- rbind(pre$tx.test, pre$tx.test)</pre>
pre$tx.test[ , 2] <- c(rep(1, N*K), rep(2, N*K))</pre>
## sex pushed to col 2, since time is always in col 1
pred <- predict(post, newdata=pre$tx.test, mc.cores=8)</pre>
pd <- matrix(nrow=M, ncol=2*K)</pre>
for(j in 1:K) {
    h <- seq(j, N*K, by=K)</pre>
    pd[ , j] <- apply(pred$surv.test[ , h], 1, mean)</pre>
    pd[ , j+K] <- apply(pred$surv.test[ , h+N*K], 1, mean)</pre>
}
pd.mu <- apply(pd, 2, mean)</pre>
pd.025 <- apply(pd, 2, quantile, probs=0.025)
pd.975 <- apply(pd, 2, quantile, probs=0.975)
males <- 1:K
females <- males+K</pre>
plot(c(0, pre$times), c(1, pd.mu[males]), type='s', col='blue',
     ylim=0:1, ylab='S(t, x)', xlab='t (weeks)'
     main=paste('Advanced Lung Cancer ex. (BART::lung)'
                 "Friedman's partial dependence function"
                 'Male (blue) vs. Female (red)', sep='\n'))
lines(c(0, pre$times), c(1, pd.025[males]), col='blue', type='s', lty=2)
lines(c(0, pre$times), c(1, pd.975[males]), col='blue', type='s', lty=2)
lines(c(0, pre$times), c(1, pd.mu[females]), col='red', type='s')
lines(c(0, pre$times), c(1, pd.025[females]), col='red', type='s', lty=2)
lines(c(0, pre$times), c(1, pd.975[females]), col='red', type='s', lty=2)
```

End(Not run)

surv.pre.bart Data construction for survival analysis with BART

Description

Survival data contained in (t, δ, x) must be translated to data suitable for the BART survival analysis model; see surv.bart for more details.

Usage

```
surv.pre.bart( times, delta, x.train=NULL, x.test=NULL,
K=NULL, events=NULL, ztimes=NULL, zdelta=NULL )
```

surv.pre.bart

Arguments

times	The time of event or right-censoring.
delta	The event indicator: 1 is an event while 0 is censored.
x.train	Explanatory variables for training (in sample) data. If provided, must be a matrix with (as usual) rows corresponding to observations and columns to variables.
x.test	Explanatory variables for test (out of sample) data. If provided, must be a matrix and have the same structure as x.train.
К	If provided, then coarsen times per the quantiles $1/K, 2/K,, K/K$.
events	If provided, then use for the grid of time points.
ztimes	If provided, then these columns of x.train (and x.test if any) are the times for time-dependent covariates. They will be transformed into time-dependent covariate sojourn times.
zdelta	If provided, then these columns of x.train (and x.test if any) are the delta for time-dependent covariates. They will be transformed into time-dependent covariate binary events.

Value

surv.pre.bart returns a list. Besides the items listed below, the list has a times component giving the unique times and K which is the number of unique times.

y.train	A vector of binary responses.
tx.train	A matrix with rows consisting of time and the covariates of the training data.
tx.test	A matrix with rows consisting of time and the covariates of the test data, if any.

Author(s)

Rodney Sparapani: <rsparapa@mcw.edu>

References

Sparapani, R., Logan, B., McCulloch, R., and Laud, P. (2016) Nonparametric survival analysis using Bayesian Additive Regression Trees (BART). *Statistics in Medicine*, **16:2741-53** <doi:10.1002/sim.6893>.

See Also

surv.bart

Examples

```
## load the advanced lung cancer example
data(lung)
group <- -which(is.na(lung[ , 7])) ## remove missing row for ph.karno</pre>
times <- lung[group, 2] ##lung$time</pre>
delta <- lung[group, 3]-1 ##lung$status: 1=censored, 2=dead</pre>
                           ##delta: 0=censored, 1=dead
summary(times)
table(delta)
x.train <- as.matrix(lung[group, c(4, 5, 7)]) ## matrix of observed covariates</pre>
## lung$age: Age in years
## lung$sex:
                    Male=1 Female=2
## lung$ph.karno: Karnofsky performance score (dead=0:normal=100:by=10)
##
                    rated by physician
dimnames(x.train)[[2]] <- c('age(yr)', 'M(1):F(2)', 'ph.karno(0:100:10)')</pre>
summary(x.train[ , 1])
table(x.train[ , 2])
table(x.train[ , 3])
x.test <- matrix(nrow=84, ncol=3) ## matrix of covariate scenarios</pre>
dimnames(x.test)[[2]] <- dimnames(x.train)[[2]]</pre>
i <- 1
for(age in 5*(9:15)) for(sex in 1:2) for(ph.karno in 10*(5:10)) {
    x.test[i, ] <- c(age, sex, ph.karno)</pre>
    i <- i+1
}
pre <- surv.pre.bart(times=times, delta=delta, x.train=x.train, x.test=x.test)</pre>
str(pre)
```

transplant Liver transplant waiting list

Description

Subjects on a liver transplant waiting list from 1990-1999, and their disposition: received a transplant, died while waiting, withdrew from the list, or censored.

Usage

data("transplant")

wbart

Format

A data frame with 815 observations on the following 6 variables.

age age at addition to the waiting list sex m or f abo blood type: A, B, AB or O year year in which they entered the waiting list futime time from entry to final disposition event final disposition: censored, death, ltx or withdraw

Details

This represents the transplant experience in a particular region, over a time period in which liver transplant became much more widely recognized as a viable treatment modality. The number of liver transplants rises over the period, but the number of subjects added to the liver transplant waiting list grew much faster. Important questions addressed by the data are the change in waiting time, who waits, and whether there was an consequent increase in deaths while on the list.

Blood type is an important consideration. Donor livers from subjects with blood type O can be used by patients with A, B, AB or O blood types, whereas a donor liver from the other types will only be transplanted to a matching recipient.

Thus type O subjects on the waiting list are at a disadvantage, since the pool of competitors is larger for type O donor livers.

This data is of historical interest and provides a useful example of competing risks, but it has little relevance to current practice. Liver allocation policies have evolved and now depend directly on each individual patient's risk and need, assessments of which are regularly updated while a patient is on the waiting list. The overall organ shortage remains acute, however.

References

Kim WR, Therneau TM, Benson JT, Kremers WK, Rosen CB, Gores GJ, Dickson ER. Deaths on the liver transplant waiting list: An analysis of competing risks. Hepatology 2006 Feb; 43(2):345-51.

wbart

BART for continuous outcomes

Description

BART is a Bayesian "sum-of-trees" model. For a numeric response y, we have $y = f(x) + \epsilon$, where $\epsilon \sim N(0, \sigma^2)$.

f is the sum of many tree models. The goal is to have very flexible inference for the uknown function f.

In the spirit of "ensemble models", each tree is constrained by a prior to be a weak learner so that it contributes a small amount to the overall fit.

Usage

```
wbart(
    x.train, y.train, x.test=matrix(0.0,0,0),
    sparse=FALSE, theta=0, omega=1,
    a=0.5, b=1, augment=FALSE, rho=NULL,
    xinfo=matrix(0.0,0,0), usequants=FALSE,
    cont=FALSE, rm.const=TRUE,
    sigest=NA, sigdf=3, sigquant=.90,
    k=2.0, power=2.0, base=.95,
    sigmaf=NA, lambda=NA,
    fmean=mean(y.train), w=rep(1,length(y.train)),
    ntree=200L, numcut=100L,
    ndpost=1000L, nskip=100L, keepevery=1L,
    nkeeptrain=ndpost, nkeeptest=ndpost,
    nkeeptestmean=ndpost, nkeeptreedraws=ndpost,
    printevery=100L, transposed=FALSE
```

)

Arguments

x.train	Explanatory variables for training (in sample) data.
	May be a matrix or a data frame, with (as usual) rows corresponding to obser- vations and columns to variables.
	If a variable is a factor in a data frame, it is replaced with dummies. Note that
	q dummies are created if $q>2$ and one dummy is created if $q=2$, where q is the number of levels of the factor.
	wbart will generate draws of $f(x)$ for each x which is a row of x.train.
y.train	Continuous dependent variable for training (in sample) data.
x.test	Explanatory variables for test (out of sample) data.
	Should have same structure as x.train.
	wher twill generate draws of $f(x)$ for each x which is a row of x test.
sparse	Whether to perform variable selection based on a sparse Dirichlet prior rather than simply uniform; see Linero 2016.
theta	Set <i>theta</i> parameter; zero means random.
omega	Set omega parameter; zero means random.
а	Sparse parameter for $Beta(a, b)$ prior: $0.5 <= a <= 1$ where lower values inducing more sparsity.
b	Sparse parameter for $Beta(a, b)$ prior; typically, $b = 1$.
rho	Sparse parameter: typically $rho = p$ where p is the number of covariates under consideration.
augment	Whether data augmentation is to be performed in sparse variable selection.
xinfo	You can provide the cutpoints to BART or let BART choose them for you. To provide them, use the xinfo argument to specify a list (matrix) where the items (rows) are the covariates and the contents of the items (columns) are the cutpoints.

	If we are supported to the state in the second state in the second state is the second state in the second state is the second
usequants	If usequants=FALSE, then the cutpoints in xinfo are generated uniformly; oth- erwise, if TRUE, uniform quantiles are used for the cutpoints.
cont	Whether or not to assume all variables are continuous.
rm.const	Whether or not to remove constant variables.
sigest	The prior for the error variance (σ^2) is inverted chi-squared (the standard con- ditionally conjugate prior). The prior is specified by choosing the degrees of freedom, a rough estimate of the corresponding standard deviation and a quan- tile to put this rough estimate at. If sigest=NA then the rough estimate will be the usual least squares estimator. Otherwise the supplied value will be used.
sigdf	Degrees of freedom for error variance prior.
sigquant	The quantile of the prior that the rough estimate (see sigest) is placed at. The closer the quantile is to 1, the more aggresive the fit will be as you are putting more prior weight on error standard deviations (σ) less than the rough estimate.
k	For numeric y, k is the number of prior standard deviations $E(Y x) = f(x)$ is away from +/5. The response (y.train) is internally scaled to range from5 to .5.
	k is the number of prior standard deviations $f(x)$ is away from +/-3. The bigger k is, the more conservative the fitting will be.
power	Power parameter for tree prior.
base	Base parameter for tree prior.
sigmaf	The SD of f.
lambda	The scale of the prior for the variance.
fmean	BART operates on y.train centered by fmean.
W	Vector of weights which multiply the standard deviation.
ntree	The number of trees in the sum.
numcut	The number of possible values of c (see usequants). If a single number if given, this is used for all variables. Otherwise a vector with length equal to $ncol(x.train)$ is required, where the i^{th} element gives the number of c used for the i^{th} variable in x.train. If usequants is false, numcut equally spaced cutoffs are used covering the range of values in the corresponding column of x.train. If usequants is true, then min(numcut, the number of unique values in the corresponding columns of x.train - 1) c values are used.
ndpost	The number of posterior draws returned.
nskip	Number of MCMC iterations to be treated as burn in.
nkeeptrain	Number of MCMC iterations to be returned for train data.
nkeeptest	Number of MCMC iterations to be returned for test data.
nkeeptestmean	Number of MCMC iterations to be returned for test mean.
nkeeptreedraws	Number of MCMC iterations to be returned for tree draws.
printevery	As the MCMC runs, a message is printed every printevery draws.
keepevery	Every keepevery draw is kept to be returned to the user.
transposed	When running wbart in parallel, it is more memory-efficient to transpose x.train and x.test, if any, prior to calling mc.wbart.

Details

BART is an Bayesian MCMC method. At each MCMC interation, we produce a draw from the joint posterior $(f, \sigma)|(x, y)$ in the numeric y case.

Thus, unlike a lot of other modelling methods in R, we do not produce a single model object from which fits and summaries may be extracted. The output consists of values $f^*(x)$ (and σ^* in the numeric case) where * denotes a particular draw. The x is either a row from the training data (x.train) or the test data (x.test).

Value

wbart returns an object of type wbart which is essentially a list. In the numeric y case, the list has components:

yhat.train	A matrix with ndpost rows and nrow(x.train) columns. Each row corresponds to a draw f^* from the posterior of f and each column corresponds to a row of x.train. The (i, j) value is $f^*(x)$ for the i^{th} kept draw of f and the j^{th} row of x.train. Burn-in is dropped.
yhat.test	Same as yhat.train but now the x's are the rows of the test data.
yhat.train.mear	1
	train data fits = mean of yhat.train columns.
yhat.test.mean	test data fits = mean of yhat.test columns.
sigma	post burn in draws of sigma, length = ndpost.
first.sigma	burn-in draws of sigma.
varcount	a matrix with ndpost rows and $nrow(x.train)$ columns. Each row is for a draw. For each variable (corresponding to the columns), the total count of the number of times that variable is used in a tree decision rule (over all trees) is given.
sigest	The rough error standard deviation (σ) used in the prior.

Author(s)

Robert McCulloch: <robert.e.mcculloch@gmail.com>, Rodney Sparapani: <rsparapa@mcw.edu>.

References

Chipman, H., George, E., and McCulloch R. (2010) Bayesian Additive Regression Trees. *The Annals of Applied Statistics*, **4**,**1**, 266-298 <doi:10.1214/09-AOAS285>.

Chipman, H., George, E., and McCulloch R. (2006) Bayesian Ensemble Learning. Advances in Neural Information Processing Systems 19, Scholkopf, Platt and Hoffman, Eds., MIT Press, Cambridge, MA, 265-272.

Friedman, J.H. (1991) Multivariate adaptive regression splines. The Annals of Statistics, 19, 1-67.

Linero, A.R. (2018) Bayesian regression trees for high dimensional prediction and variable selection. *JASA*, **113**, 626–36.

xdm20.test

See Also

pbart

Examples

```
##simulate data (example from Friedman MARS paper)
f = function(x){
10*sin(pi*x[,1]*x[,2]) + 20*(x[,3]-.5)^2+10*x[,4]+5*x[,5]
}
sigma = 1.0 \ \#y = f(x) + sigma \times z, \ z \sim N(0,1)
             #number of observations
n = 100
set.seed(99)
x=matrix(runif(n*10),n,10) #10 variables, only first 5 matter
Ey = f(x)
y=Ey+sigma*rnorm(n)
lmFit = lm(y^{-}, data.frame(x, y)) #compare lm fit to BART later
##test BART with token run to ensure installation works
set.seed(99)
bartFit = wbart(x,y,nskip=5,ndpost=5)
## Not run:
##run BART
set.seed(99)
bartFit = wbart(x,y)
##compare BART fit to linear matter and truth = Ey
fitmat = cbind(y,Ey,lmFit$fitted,bartFit$yhat.train.mean)
colnames(fitmat) = c('y', 'Ey', 'lm', 'bart')
print(cor(fitmat))
## End(Not run)
```

xdm20.test

A data set used in example of recur.bart.

Description

A matrix containing a 20% random sample of the testing set for a real data example of recurrent events survival analysis. There are 100 patients in the cohort: 50 in the training set and 50 in the testing set. See the Reference below (and the References therein) for more detailed information; a brief synopsis follows.

xdm20.test contains both the training set and the testing set. There are 798 unique time points so there are 50*798=39900 rows of the training set followed by 50*798=39900 rows of the testing set. For patient's who died prior to the end of follow-up, their external factors are last value carried forward. Therefore, we can use xdm20.test to estimate the cumulative hazard for all patients for all time points.

The full data set, xdm.test, can be obtained online at http://www.mcw.edu/FileLibrary/Groups/ Biostatistics/TechReports/TechReports5175/tr064.tar. There are 488 patients in the full cohort: 235 in the training set and 253 in the testing set.

xdm. test contains both the training set and the testing set. There are 798 unique time points so there are 235*798=187530 rows of the training set followed by 253*798=201894 rows of the testing set. For patient's who died prior to the end of follow-up, their external factors are last value carried forward.

Usage

data(xdm20.test)

References

Sparapani R., Rein L., Tarima S., Jackson T., Meurer J. (2017) Nonparametric recurrent events analysis with BART and an application to the hospital admissions of patients with diabetes. *MCW Biostatistics Technical Report 64* http://www.mcw.edu/FileLibrary/Groups/Biostatistics/TechReports/TechReports5175/tr064.pdf.

See Also

xdm20.train

Examples

data(xdm20.test)
head(xdm20.test[, 1:10])

xdm20.train

A real data example for recur.bart.

Description

A matrix containing a 20% random sample of the training set for a real data example of recurrent events survival analysis. There are 100 patients in the cohort: 50 in the training set and 50 in the testing set. The full data set, xdm.train, can be obtained online at http://www.mcw.edu/FileLibrary/Groups/Biostatistics/TechReports/TechReports5175/tr064.tar. There are 488 patients in the full cohort: 235 in the training set and 253 in the testing set. See the Reference below (and the References therein) for more detailed information; a brief synopsis follows.

We explored the hospital admissions for a cohort of patients with diabetes cared for by the Froedtert and Medical College of Wisconsin health network. These patients were identified via their Electronic Health Records (EHR) which include vital signs, diagnoses, procedures, laboratory values, pharmacy orders and billing data. This human subjects research and de-identified data release was approved by the Medical College of Wisconsin and Froedtert Hospital joint Institutional Review Board. To maintain patient privacy, roughly one fourth of patients were randomly sampled for inclusion as well as other de-identification procedures.

xdm20.train

We identified likely incident diabetes mellitus type 2 patients by tabulating their first diagnosis code of primary diabetes (ICD-9 codes 250.x0 and 250.x2) in 2006 or 2007, i.e., no such codes were found for these patients prior to 2006 for as far back as each patient's records go which is variable. We restricted the population to adults aged 21 to 90 by 01/01/2008. Among the patients treated in this health system, the vast majority were racially self-identified as either white or black so our inclusion criteria is restricted to these groups. Since our interest is in patients with primary diabetes, we excluded those patients who were diagnosed with either secondary diabetes or gestational diabetes.

For this cohort, we identified every hospital admission between 01/01/2008 and 12/31/2012. For convenience, follow-up begins on 01/01/2008, rather than from each patient's actual incident diagnosis date which varied over the preceding 2 years. Following all patients concurrently allows us to temporally adapt, via our model, for seasonal/epidemic hospital admissions such as the H1N1 influenza outbreak in the US from April to June 2009.

We investigated the following risk factors: gender, race, age, insurance status (commercial, government or other), diabetes therapy (insulin, metformin and/or sulfonylurea), health care charges, relative value units (RVU), vital signs, laboratory values, comorbidity/complication diagnoses and procedures/surgeries (we will refer to vital signs and laboratory values collectively as signs; and comorbidity/complication diagnoses and procedures/surgeries collectively as conditions). In total, we considered 85 covariates of which 82 are external factors as described above and three are temporal factors: time, t, the counting process, $N_i(t-)$, and the sojourn time, $v_i(t)$. Among these potential predictors only gender, race and age are time-independent. The rest are defined as last value carried forward.

For insulin, metformin and sulfonylurea, we only had access to prescription orders (rather than prescription fills) and self-reported current status of prescription therapy during clinic office visits. Since, generally, orders are only required after every three fills, and each fill can be for up to 90 days, we define insulin, metformin and sulfonylurea as binary indicators which are one if there exists an order or current status indication within the prior 270 days; otherwise zero.

Health care charges and relative value units (RVU) are measures related to the services and procedures delivered. However, they are so closely related that recent charges/RVUs are of no practical value in this analysis. For example, just prior to a patient's hospital admission on a non-emergent basis, they often have a series of diagnostic tests and imaging. Similarly, for an emergent admission, the patient is often seen in the emergency department just prior to admission where similar services are conducted. We do not consider these charges/RVUs predictive of an admission because we are interested in identifying preventive opportunities. Therefore, we investigate charges/RVUs that are the sum total of the following moving windows of days prior to any given date: 31 to 90, 91 to 180, 181 to 300.

For many patients, some signs were not available for a given date so they were imputed; similarly, if a sign was not observed within the last 180 days, then it was imputed (except for height which never expires, weight extended to 365 days and body mass index which is a deterministic function of the two). We utilized the Sequential BART missing imputation method. However, instead of creating several imputed data sets, we imputed a new sign at each date when it was missing, i.e., in order to properly address uncertainty within one data set, a new value was imputed for each date that it was missing and never carried forward.

Conditions are binary indicators which are zero until the date of the first coding and then they are one from then on. Based on clinical rationale, we identified 26 conditions (23 comorbidities and 3 procedures/surgeries) which are potential risk factors for a hospital admission many of which are possible complications of diabetes; besides clinical merit, these conditions were chosen since they

are present in more than just a few subjects so that they may be informative. Similarly, we employed 15 general conditions which are the Charlson diagnoses and 18 general conditions from the RxRisk adult diagnoses which are defined by prescription orders. Seven conditions are a composite of diagnosis codes and prescription orders.

Usage

```
data(xdm20.train)
```

References

Sparapani R., Rein L., Tarima S., Jackson T., Meurer J. (2017) Nonparametric recurrent events analysis with BART and an application to the hospital admissions of patients with diabetes. *MCW Biostatistics Technical Report 64* http://www.mcw.edu/FileLibrary/Groups/Biostatistics/TechReports/TechReports5175/tr064.pdf.

See Also

xdm20.test

Examples

```
data(xdm20.train)
head(xdm20.train[ , 1:10])
```

ydm20.train

A data set used in example of recur.bart.

Description

Two vectors containing the training and testing set outcomes for a 20% random sample for a real data example of recurrent events survival analysis. There are 100 patients in the cohort: 50 in the training set and 50 in the testing set. See the Reference below (and the References therein) for more detailed information; a brief synopsis follows.

ydm20.train contains the training set only. ydm20.test is provided for completeness; it contains both the training set and the testing set. There are 798 unique time points so there are 50*798=39900 rows of the training set followed by 50*798=39900 rows of the testing set.

The full data sets, ydm.train and ydm.test, can be obtained online at http://www.mcw.edu/ FileLibrary/Groups/Biostatistics/TechReports/TechReports5175/tr064.tar. There are 488 patients in the full cohort: 235 in the training set and 253 in the testing set.

ydm.train contains the training set only. ydm.test contains both the training set and the testing set. There are 798 unique time points so there are 235*798=187530 rows of the training set followed by 253*798=201894 rows of the testing set.

Usage

data(ydm20.train)
data(ydm20.test)

ydm20.train

References

Sparapani R., Rein L., Tarima S., Jackson T., Meurer J. (2017) Nonparametric recurrent events analysis with BART and an application to the hospital admissions of patients with diabetes. *MCW Biostatistics Technical Report 64* http://www.mcw.edu/FileLibrary/Groups/Biostatistics/ TechReports/TechReports5175/tr064.pdf.

See Also

xdm20.train

Examples

data(ydm20.train)
data(ydm20.test)
table(ydm20.train)
table(ydm20.test)

Index

*Topic **OpenMP** mc.cores.openmp, 62 *Topic convergence diagnostics gewekediag, 42 spectrum0ar, 135 stratrs, 137 *Topic data construction crisk.pre.bart, 22 recur.pre.bart, 124 surv.pre.bart, 144 *Topic datasets ACTG175, 8 alligator, 10 arg, 12 bladder, 14 leukemia, 50 lung, 52 transplant, 146 xdm20.test, 151 xdm20.train, 152 ydm20.train, 154 *Topic multi-threading mc.cores.openmp, 62 *Topic **nonlinear** abart, 3 gbart, 32 gbmm, 37 1bart, 44 mbart, 52mbart2, 57 mc.crisk.pwbart,62 mc.crisk2.pwbart,66 mc.lbart, 69 mc.pbart,74 mc.surv.pwbart,78 mc.wbart,82 pbart.88 predict.crisk2bart,94 predict.criskbart,97

156

predict.lbart, 99 predict.mbart, 102 predict.pbart, 105 predict.recurbart, 108 predict.survbart, 111 predict.wbart, 114 pwbart, 116 rs.pbart, 128 wbart, 147 *Topic nonparametric recurrent events model recur.bart, 118 *Topic nonparametric survival model crisk.bart, 16 crisk2.bart.24 surv.bart, 138 *Topic **nonparametric** abart.3 gbart, 32 gbmm, 37 lbart, 44 mbart, 52mbart2, 57 mc.crisk.pwbart,62 mc.crisk2.pwbart,66 mc.lbart, 69 mc.pbart,74 mc.surv.pwbart,78 mc.wbart,82 pbart, 88 predict.crisk2bart,94 predict.criskbart,97 predict.lbart,99 predict.mbart, 102 predict.pbart, 105 predict.recurbart, 108 predict.survbart, 111 predict.wbart, 114 pwbart, 116

rs.pbart, 128 wbart, 147 *Topic nonproportional hazards variable selection mc.wbart.gse, 86 *Topic nonproportional hazards crisk.bart.16 crisk2.bart.24 recur.bart, 118 surv.bart, 138 *Topic package BART-package, 3 *Topic **parallel** mc.cores.openmp, 62 *Topic regression abart.3 gbart, 32 gbmm, 37 1bart, 44 mbart, 52mbart2.57 mc.crisk.pwbart,62 mc.crisk2.pwbart,66 mc.lbart, 69 mc.pbart,74 mc.surv.pwbart,78 mc.wbart,82 pbart, 88 predict.crisk2bart, 94 predict.criskbart,97 predict.lbart, 99 predict.mbart, 102 predict.pbart, 105 predict.recurbart, 108 predict.survbart, 111 predict.wbart, 114 pwbart, 116 rs.pbart, 128 wbart, 147 *Topic survival bladder, 14 *Topic tree abart, 3 gbart, 32 gbmm, 37 lbart,44 mbart, 52mbart2, 57

mc.crisk.pwbart, 62 mc.crisk2.pwbart,66 mc.lbart, 69 mc.pbart,74 mc.surv.pwbart,78 mc.wbart,82 pbart, 88 predict.crisk2bart,94 predict.criskbart,97 predict.lbart, 99 predict.mbart, 102 predict.pbart, 105 predict.recurbart, 108 predict.survbart, 111 predict.wbart, 114 pwbart, 116 rs.pbart, 128 wbart, 147 *****Topic **utilities** bartModelMatrix, 13 abart.3 ACTG175, 8 alligator, 10, 56, 61 arg, 12 BART (BART-package), 3 BART-package, 3 bartModelMatrix, 13 bladder, 14 bladder1 (bladder), 14 bladder2 (bladder), 14 cancer (lung), 52 class.ind, 14 crisk.bart, 16, 23, 29, 64, 98 crisk.pre.bart, 21, 22 crisk2.bart, 21, 24, 68, 95 draw_lambda_i, 31 gbart, 32, 56, 61 gbmm, 37 gewekediag, 42, 136 lbart, 31, 44, 73, 135 leukemia, 50 lung, 52, 137

mbart, 52, 104

INDEX

mbart2, 57, 104 mc.abart(abart), 3 mc.cores.openmp, 62, 95, 98, 101, 107, 110, 112, 115 mc.crisk.bart, 64, 98 mc.crisk.bart(crisk.bart), 16 mc.crisk.pwbart, 21, 62, 98 mc.crisk2.bart, 68, 95 mc.crisk2.bart(crisk2.bart), 24 mc.crisk2.pwbart, 29, 66, 95 mc.gbart(gbart), 32 mc.gbmm (gbmm), 37 mc.lbart, 69 mc.mbart(mbart), 52 mc.mbart2(mbart2), 57 mc.pbart, 74, 131 mc.pwbart, *115* mc.pwbart (pwbart), 116 mc.recur.bart, 110 mc.recur.bart(recur.bart), 118 mc.recur.pwbart, *110*, *122* mc.recur.pwbart (mc.surv.pwbart), 78 mc.surv.bart, 101, 107, 112 mc.surv.bart(surv.bart), 138 mc.surv.pwbart, 78, 101, 107, 112 mc.wbart, 82, 87, 115 mc.wbart.gse, 86

pbart, 36, 41, 77, 88, 135, 151
predict.crisk2bart, 29, 94
predict.criskbart, 21, 96
predict.lbart, 99
predict.mbart, 102
predict.mbart2 (predict.mbart), 102
predict.pbart, 105
predict.recurbart, 108, 122
predict.survbart, 111
predict.wbart, 114, 117
pwbart, 62, 64, 68, 80, 115, 116

recur.bart, *110*, 118, *125* recur.pre.bart, *122*, 124 recur.pwbart, *110*, *122* recur.pwbart (mc.surv.pwbart), 78 rs.pbart, 128, *138* rtgamma, 133 rtnorm, *31*, 134

spectrum0ar, *43*, 135

srstepwise, 136 stratrs, 137 surv.bart, 101, 107, 112, 138, 145 surv.pre.bart, 29, 142, 144 surv.pwbart, 101, 107, 112 surv.pwbart (mc.surv.pwbart), 78 transplant, 146 wbart, 7, 41, 48, 85, 91, 115, 117, 147 xdm20.test, 151 xdm20.test, 151 ydm20.test (ydm20.train), 154 ydm20.train, 154